Evaluating Radio Occultation (RO) Constellation Designs Using Observing System Simulation Experiments (OSSEs) for Ionospheric Specification

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Key Points:

- OSSE study assessing hypothetical RO constellations, the first to comprehensively account for forecast model and Abel inversion errors.
- The RO constellation with low- and high-inclination orbits at 520 km altitude performs the best with the highest observation counts.
- Uncharacterized Abel inversion errors and poorly retrieved low plasma density limit assimilation impact on the equatorial ionosphere.

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Abstract

Low Earth orbit (LEO) radio occultation (RO) constellations can provide global electron density profiles (EDPs) to better specify and forecast the ionosphere-thermosphere (I-T) system. To inform future RO constellation design, this study uses comprehensive Observing System Simulation Experiments (OSSEs) to assess the ionospheric specification impact of assimilating synthetic EDPs into a coupled I-T model. These OSSEs use 10 different sets of RO constellation configurations containing 6 or 12 LEO satellites with base orbit parameter combinations of 520 km or 800 km altitude, and 24 degrees or 72 degrees inclination. The OSSEs are performed using the Ensemble Adjustment Kalman Filter implemented in the Data Assimilation Research Testbed and the Thermosphere-Ionosphere-Electrodynamics General Circulation Model (TIEGCM). A different I-T model is used for the nature run, the Whole Atmosphere Model-Ionosphere Plasmasphere Electrodynamics (WAM-IPE), to simulate the period of interest is the St. Patrick's Day storm on March 13-18, 2015. Errors from models and EDP retrieval are realistically accounted for in this study through distinct I-T models and by retrieving synthetic EDPs through an extension Abel inversion algorithm. OSSE assessment, using multiple metrics, finds that greater EDP spatial coverage leading to improved specification at altitudes 300 km and above, with the 520 km altitude constellations performing best due to yielding the highest observation counts. A potential performance limit is suggested with two 6-satellite constellations. Lastly, close examination of Abel inversion error impacts highlights major EDP limitations at altitudes below 200 km and dayside equatorial regions with large horizontal gradients and low electron density magnitudes.

Plain Language Summary

The upper atmosphere, the region above 100 km altitude, is strongly influenced by space weather events that can negatively impact ground and space-based technologies. These technologies include communication and navigation systems impacted by radio wave propagation through high altitudes plasma, a region called the ionosphere. Developing observing systems that provide global monitoring of the ionosphere is a critical need for understanding and forecasting space weather changes, such as radio occultations (RO) that provide plasma observations using global positioning radio signals. In this study, we evaluate these hypothetical RO observing systems in simulated experiments using data assimilation, an approach that integrates synthetic observations into a physics-based model. We find that increased observational coverage corresponds to better estimated plasma states, and that lower orbit altitude constellations yield higher observation counts. This study comprehensively incorporates model and observation errors to more realistically represent real-world conditions. One limitation of RO data is highlighted in regions near the equator and at lower altitudes (below 250 km) where there is a breakdown in assumptions for observation retrieval. This study illustrates the clear operational benefits of these plasma observations, informing the future observing system design and aiding their use for space weather forecasting.

1 Introduction

Monitoring the near-Earth space environmental conditions for space weather nowcasting and forecasting is increasingly pertinent to maintaining critical ground and space-based technological systems. One such critical impact is ionospheric plasma disturbances affecting navigational systems via the propagation of radio waves for Global Navigation Satellite Systems (GNSS) and very low frequency signals, along with other communication systems utilizing high frequency and ultra high frequency radio signals. The peak heights and magnitudes of plasma density affects whether radio signals are reflected or absorbed, the index of refraction that bends these signals, and small-scale plasma density irregularities can cause radio signals to scatter or scintillate. These space weather

effects on radio signals can be characterized using parameters, such as the F-region peak electron density, N_mF_2, and its height, h_mF_2, the total electron content (TEC), the rate of change of TEC index (ROTI), and the S_4 index. Geomagnetic storms can induce considerable variations and disturbances of the near-Earth plasma environments, stressing our radio-based systems as indicated by dramatic changes in ROTI and S_4 index (Moreno et al., 2011). As underscored by the Promoting Research and Observations of Space Weather to Improve the Forecasting of Tomorrow (PROSWIFT) Act in 2020 (Lugaz, 2020) and space weather gap analysis findings (Vourlidas et al., 2023), continuing and developing new ionospheric observing systems, as well as their integration into forecast models with the help of data assimilation (DA), is essential for advancing space weather now-casting and forecasting capabilities. Moreover, the Weather Research and Innovation Forecasting Act of 2017 specifically mandates the National Oceanic and Atmospheric Association (NOAA) to perform Observing System Simulation Experiments (OSSEs), wherein DA frameworks are used to quantitatively assess hypothetical observing systems for their relative value and benefit.

GNSS constellations are designed for global positioning, enabling radio occultation (RO) observations with global coverage of the ionosphere. Currently available GNSS constellations include GPS, GLONASS, Galileo, and BeiDou. The development and operation of RO satellite constellations have considerably grown over recent decades, providing real-time observations for ionospheric space weather prediction, climatological study, and insight into ionospheric physics. In addition to their well-recognized and valuable role as an observing system for ionospheric plasma density, recent DA studies (Matsuo & Hsu, 2021; Dietrich et al., 2022) suggest their utility as a global monitoring system of thermospheric mass density. Earth-based RO constellations began in 1995 with the launch of MicroLab-1 Global Positioning System/Meteorology (GPS/MET) (Hajj & Romans, 1998; Kursinski et al., 1997), and was succeeded in 2006 by the FORMOSAT-3/COSMIC (F3/C) (Anthes et al., 2008) and its follow-on mission FORMOSAT-7/COSMIC-2 (F7/C2) (Yue, Schreiner, Pedatella, et al., 2014; Fong et al., 2019) in 2019. F3/C consisted of a 6-satellite low Earth orbit (LEO) constellation, orbiting in separate orbital planes, each at 72° latitude and 800 km altitude. RO observations counts of F3/C were doubled with the launch of the more recent F7/C2, a 6-satellite constellation in a similar orbit configuration at 24° inclination and 550 km altitude. Commercial RO sources has additionally grown to include satellites and constellations in near polar orbit (e.g., Angling et al., 2021), promoting their use within DA experiments quantifying their benefit, i.e., RO Modeling EXperiment (ROMEX) (Anthes et al., 2023).

RO soundings have provided a wealth of ionospheric information to produce 3-dimensional, global observations of the ionosphere. During an RO sounding, the slant TEC is measured along the radio signal's limb sounding geometry connecting the GNSS satellite and the observing LEO satellite. Electron density profiles (EDPs) are consequently retrieved from these slant TEC observations at the ray tangent point locations through Abel inversion, with this inversion relying on a spherical symmetry assumption. RO EDPs are highly accurate observations of the ionosphere's F-region, generally around 300-400 km altitude, especially for F_2 region parameters N_mF_2 and h_mF_2 (Cherniak et al., 2021; Yue et al., 2010; Lei et al., 2007). Relatively large errors can exist for low altitudes, i.e., the E-region below 200 km altitude (Kelley et al., 2009). Large RO EDP errors are also reported where there are breakdowns in the spherical symmetry assumption such as near equatorial latitudes (Tsai et al., 2001; Tsai & Tsai, 2004) and beneath the crests of the equatorial ionization anomaly (EIA), peaking at 200% (Liu et al., 2010; Yue et al., 2010). Recent algorithm improvements have been made to the Abel inversion retrieval, aided by prior ionosphere information (e.g., Yue et al., 2013; Pedatella et al., 2015; Chou et al., 2017; Lin et al., 2020; Tulasi Ram et al., 2016), or using a bottom-up retrieval for the D- and E-regions (Wu, 2018).

OSSEs have been used to quantitatively evaluate the value of RO observations (e.g., Yue, Schreiner, Kuo, et al., 2014; Lee et al., 2013; Hsu et al., 2018; He et al., 2019; Lin et al., 2015, 2017; Scherliess et al., 2004; Pedatella et al., 2020; Forsythe et al., 2021). Within an OSSE, synthetic data are generated from a nature run model simulation (that serves as a truth model) and then assimilated into a biased forecast model to assess improvement. Yue, Schreiner, Kuo, et al. (2014) performed an OSSE study prior to the launch of F7/C2, assessing the multiple planned RO EDPs from F7/C2 using NeQuick model as the nature run and assimilating EDPs into the empirical ionospheric model IRI. Lee et al. (2013) assimilated synthetic F7/C2 EDPs into a coupled ionosphere-thermosphere (I-T) physics-based model, and saw global improvements in electron density states over previous F3/C EDPs. Further to realistically assess the value of observing systems, it is crucial to quantify observation errors for DA. In particular, RO EDP assimilation can be negatively impacted by Abel retrieval errors if not properly characterized, with most recent RO error quantification performed in Yue et al. (2010); Liu et al. (2010). Even though OSSEs have been proven to be useful for mission planning and in informing the most effective constellations designs, previous OSSE work has yet to account for both forecast model errors and Abel retrieval errors in a comprehensive manner. For example, the tropospheric weather forecasting community has been investing considerable efforts to design standard and fair nature runs for OSSE studies (e.g., Masutani et al., 2007; Andersson & Masutani, 2010; Errico et al., 2013; Hoffman & Atlas, 2016). These standardized nature runs use state-of-the-art numerical model simulations that climatologically match the real atmosphere and contain realistic differences from the forecast model.

This study aims to evaluate the value of different RO constellation designs by quantifying the ionospheric specification impact of assimilating EDP observations into a coupled I-T model. We do this by adopting a comprehensive OSSE approach that overcomes the limitations of past RO EDP OSSE studies. The nature run is performed using the Whole Atmosphere Model-Ionosphere Plasmasphere Electrodynamics (WAM-IPE) (Akmaev, 2011; Maruyama et al., 2016), and the forecast coupled I-T model used in the DA framework is the Thermosphere Ionosphere Electrodynamics General Circulation Model (TIEGCM) developed by the National Center for Atmospheric Research (NCAR) (Qian et al., 2014; Richmond et al., 1992). Here, synthetic EDPs are retrieved from the WAM-IPE nature run simulation through an extensive Abel inversion procedure combined with simulated RO limb sounding geometries between the GNSS and hypothetical RO constellations. This Abel inversion procedure is built on the operational procedure used for the COSMIC-2 EDP data product. Synthetic EDP observations used in this study therefore include realistic Abel inversion errors, that cannot be represented by directly sampling electron density from the nature run at RO tangent points. We run a widely-used ensemble DA framework developed by NCAR's Data Assimilation Research Testbed (DART) (Anderson et al., 2009) with TIEGCM, denoted as DART-TIEGCM. The Ensemble Adjustment Kalman Filter (EAKF) is used (Anderson, 2001). The OSSEs are run for a popularly studied event, the week of the March 2015 St. Patrick's day storm. A total of ten OSSEs are performed for the different permutations of the four base virtual LEO constellation configurations. To address what constellation design is "best", evaluated across different ionospheric regions, the results from these OSSEs are compared using various metrics including key ionospheric parameters of TEC, N_mF_2 and h_mF_2, as well as the three-dimensional plasma density structure.

In the following sections, Section 2 provides details for the EDP Abel retrieval and its errors as well as the OSSE design. Section 3 provides the OSSE results, including assimilation impact, a relative OSSE ranking metric and a potential limit to observation impact. Section 4 contains general discussion assessing observation impact from DART-TIEGCM and Abel inversion errors, along with future work. Finally, Section 5 provides the conclusions.

2 Methods

2.1 Data Assimilation: DART-TIEGCM

In this study, we employ an ensemble-based approach, specifically the EAKF as developed and implemented by DART (Anderson, 2001; Anderson et al., 2009). In ensemble DA, states and their uncertainties are represented with ensembles in an Monte Carlo approach tailored for high-dimensional state estimation. The typical cycle of the EAKF consists of two steps: (1) the forecast step that propagates model states with the full non-linear model dynamics and (2) the analysis step that optimally updates states using observation information. The forecast step produces a forecast, or prior state, that is used in the analysis step to produce an analysis estimate, or posterior. The DA cycle continues, feeding the posterior into the next forecast step. In the EAKF, each observation has a spatially localised impact on model states determined by ensemble covariance information. This covariance information determines the statistical relationship between an observation and nearby surrounding model states, and is dynamically estimated from model ensembles that reflect nonlinear dynamics and physics.

We use the TIEGCM v2.0 developed by NCAR as the forecast model, solving a self-consistent solution of first-principle equations of the I-T system and producing the three-dimensional, time-varying field of the thermosphere and ionosphere states. The 5° resolution version of TIEGCM is used, with 29 pressure levels with half scale-height resolution that spans from $\sim$ 97 km to $\sim$ 500 km altitudes, depending on the solar conditions. External forcing in TIEGCM is specified through solar ultraviolet irradiance parameterized with respect to a daily value of the F10.7 index (F10.7), and lower boundary tides through the Global Scale Wave Model (GSWM). The magnetospheric forcing is specified by the empirical Heelis convection model and an empirical auroral model.

2.2 Nature Run (Truth) Model: WAM-IPE

The nature run simulation, which serves as the truth model, is achieved with a free-run of the I-T coupled physics-based model WAM-IPE developed by NOAA. There are a number of differences in how the I-T physics and dynamics are solved between TIEGCM and WAM-IPE. It is expected that these differences manifest as forecast model biases and likely widen during the storm-period. WAM is a spectral whole atmosphere model, containing 150 pressures levels that solves neutral states from the surface up to 400$-$600 km altitudes, output at 1° horizontal resolution. IPE solves plasma state physics along flux tubes in the semi-Lagrangian reference frame, extending up into the plasmasphere encompassing 90 km to 10,000 km altitudes. In contrast, TIEGCM solves both neutral and plasma states in the Euler reference frame, approximating the O^+ flux at the upper boundary, and using lower boundary tide conditions specified by GSWM. In WAM-IPE, solar irradiance is also parameterized using daily F10.7 but magnetospheric forcing is specified by an empirical Weimer convection model driven by solar wind states at 1-minute cadence. These model differences are expected to introduce distinctive ionosphere biases partly corrected by assimilation of EDP observations.

2.3 Virtual Constellations

For this study, we use four base virtual LEO constellation configurations, derived from the F3/C and F7/C2 constellations, to design ten different sets of hypothetical RO constellation configurations. Each base constellation consists of six satellites with the same inclination and altitude and at separate orbital planes. We simulate RO events between GPS and GLONASS and LEO satellite constellations in a similar mode of operation used by F7/C2. The base constellation parameters are as follows: (i) a 520 km altitude and 24° inclination constellation (similar to F7/C2), (ii) a 520 km altitude and 72° inclination constellation, (iii) a 800 km altitude and 24° inclination constellation, and

(iv) a 800 km altitude and 72° inclination constellation (similar to F3/C). All ten OSSE combinations of one or two base virtual constellations are detailed in Table 1. Each OSSE is referenced according to a short-hand notation, with the first two digits referencing the constellation altitude, and the second two digits referencing the constellation inclination. For instance, OSSE 1, with the short-hand notation 5024, is performed using the LEO constellation of satellites at 520 km altitude and 24° inclination.

Within each OSSE, we assimilate EDPs from 160 km to 500 km altitude at 10 km vertical sampling intervals to update the DART state vector containing electron density, e^-, and atomic oxygen ion, O^+. Gaussian uncorrelated noises are assigned to each electron density using the variances determined from the EDP uncertainty quantification process detailed in Section 2.3.2. The RO tangent point locations for each of these base constellations for a full day of observations is shown in Figure 1 to illustrate their respective coverage. As expected, the low-inclination constellations provide only low- and mid-latitude observations, while the high-inclination constellations provide observations in all latitude regions, at the cost of less dense spatial coverage.

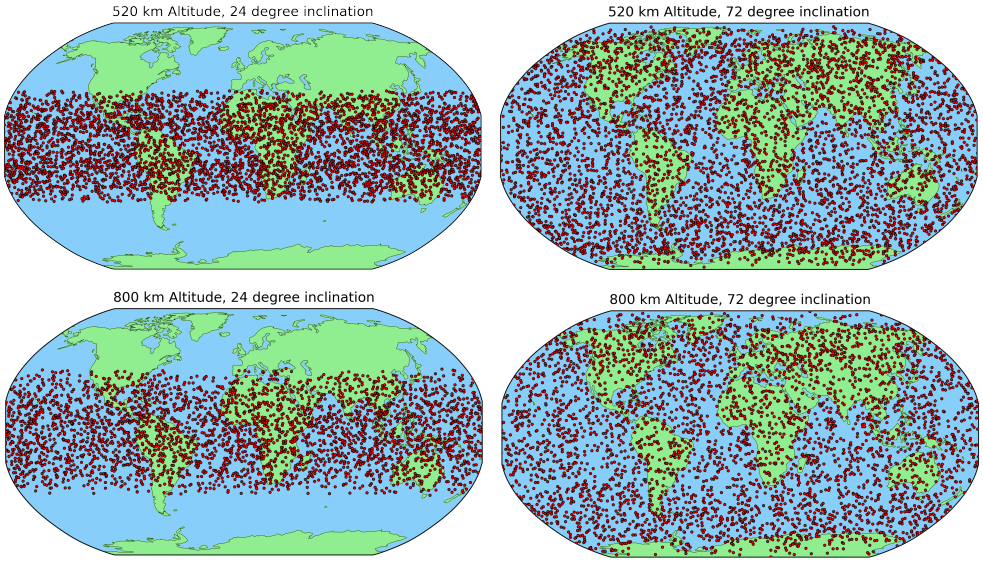

Figure 1. The RO observation tangent points shown for the full day of March 13th at 300 km altitude. Shown for the four base virtual LEO constellation configurations.

2.3.1 Synthetic EDP Retrieval Using RO Simulation and Abel Inversion

Synthetic RO EDPs are generated from the WAM-IPE nature run simulation with the typical EDP retrieval processes, as detailed in Hajj and Romans (1998); Schreiner et al. (1999). Specifically, we use the Abel inversion algorithm adapted from the operational data product procedure used to generate ionPrf files from F3/C and F7/C2. The sounding paths from GNSS satellites to LEO RO satellites are used to generate the synthetic slant TEC profiles. For a typical RO sounding there is an occultation side and an auxiliary side, where the auxiliary side passes through both the upper ionosphere and plasmasphere and the occultation side passes through the ionosphere, atmosphere and plasmasphere. Here, WAM-IPE's ionosphere extension provides plasmasphere information. The resulting calibrated slant TEC profile comes from subtracting the auxiliary side TEC profile from the occultation side TEC profile and contains only the impact of the ionosphere. The synthetic EDPs are then retrieved by applying Abel inversion to these

Table 1. List of 10 OSSEs for different base LEO satellite constellation designs. For shorthand notation, the first two digits reference the constellation altitude and the last two digits reference the constellation inclination.

Experiment Name	LEO Constellations	Short-Hand Notation
OSSE 1	520 km alt, 24° inc	5024
OSSE 2	520 km alt, 72° inc	5072
OSSE 3	800 km alt, 24° inc	8024
OSSE 4	800 km alt, 72° inc	8072
OSSE 5	520 km alt, 24° inc & 800 km alt, 72° inc	5024 & 8072
OSSE 6	520 km alt, 24° inc & 520 km alt, 72° inc	5024 & 5072
OSSE 7	520 km alt, 24° inc & 800 km alt, 24° inc	5024 & 8024
OSSE 8	800 km alt, 24° inc & 800 km alt, 72° inc	8024 & 8072
OSSE 9	520 km alt, 72° inc & 800 km alt, 72° inc	5072 & 8072
OSSE 10	520 km alt, 72° inc & 800 km alt, 24° inc	5072 & 8024

synthetic calibrated slant TEC profiles. The synthetic EDP data retrieved in this study thus contain the same systemic error as real ionPrf data products, ensuring the OSSE results more closely reflect reality.

2.3.2 Uncertainty Quantification of Synthetic EDPs

To determine observation uncertainties necessary for DA, the EDP errors due to Abel inversion are quantified. Observation errors are calculated using the difference between synthetic EDPs and the modeled electron density distribution from the WAM-IPE nature run. Sample standard deviations are computed after binning difference data with respect to the following parameters: day of year, constellation inclination, altitude, magnetic latitude, and solar local time. Four solar local time (LT) bins are used: LTs $4-10$, LTs $10-16$, LTs $16-22$, and LTs $22-4$. LEO constellation altitude was found to have a negligible effect on errors. Similar studies with EDP observations have used percentage errors over local time, altitude, and magnetic latitude (Lee et al., 2013; Liu et al., 2010; Yue et al., 2010), while we quantify errors using standard deviation. Standard deviations are computed from EDP samples within ± 5 km for a given altitude, and within $\pm 5°$ for a given latitude. An example of the calculated EDP uncertainties for March 13th at 300 km is shown in Figure 2. Notable features is the distinct difference in the error magnitude for the four solar local time bins and the impact that constellation inclination has on error magnitudes for the LT $16-22$ in the equatorial latitudes. Over these local times, there are highly variable spatial features such as the EIA and the prereversal enhancement. The pronounced dependence on constellation inclinations can also be due to smaller low-latitude observation counts for the high inclination orbit (shown in Supporting Information (SI) Figure S1).

The Abel retrieval errors are furthermore characterized for N_mF_2, h_mF_2 and over multiple EDP altitudes as shown in Figure 3. For N_mF_2, we see peak errors of 85% near the south Atlantic anomaly (SAA), while the global error average is 18%, with structures following Earth's magnetic field lines. As expected, we see very small errors for h_mF_2 with percentage errors peaking at 17% and averaging 4%. As for altitude variations of errors, we see substantial errors at 200 km altitude, which is considerably higher than past studies wherein they peak approximately at 200% (Liu et al., 2010; Yue et al., 2010). Errors are smaller at 300 km, with peaks along the magnetic and near the SAA. Outside these two regions, errors are below 40%, with a median error of 25%. For 400 and 500 km altitudes, we see increasingly smaller errors, with a peak error near the SAA and

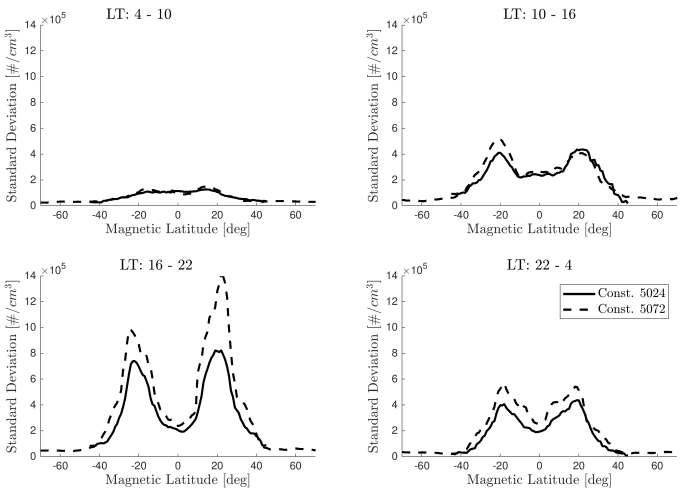

Figure 2. Standard deviations attributed to EDP observations. Shown for two constellations, 5024 and 5072, at 300 km altitude on March 13th. Standard deviations are computed from the difference between synthetic EDPs and plasma density from the WAM-IPE nature run simulation after binning data with respect to day of year, constellation inclination, altitude, magnetic latitude, and solar local time.

a global average of 17%. There are some spurious high errors seen at high latitudes where there are low observation counts. It is noted these errors are highly dependent on solar LT, with two example local time cases shown in SI Figures S2 and S3.

These large errors seen in Figure 3 come primarily from break-downs of the spherical symmetry assumption used in Abel inversion. The break-downs of this assimilation are expected to impact regions with large horizontal gradients in electron density distribution, such as near and below the magnetic equator and EIA. The impact is less acute with increasing altitude. These errors are well-captured within uncertainty calculations considered in this study. An additional source of RO errors are from on-board GNSS receivers as well as receiver errors, but these errors are not considered in this study.

2.4 Experiment Set-up

The OSSE period is the St. Patrick's day storm of March 2015, with observed solar and geomagnetic indices and solar wind states shown for this period in Figure 4. The OSSE is broken into two periods, the preceding quiet period and storm-time. The quiet period begins at UT00 on March 13th and ends at UT23 on March 16th. Localization is done using the Gaspari-Cohn (GC) function (Gaspari & Cohn, 1999) with a GC radius of 0.2 radians ($\sim$ 1300 km) without vertical localization, so observations have impact on all pressure levels. We do not use ensemble inflation. As the upper atmosphere is strongly influenced by external forcing, we perturb solar irradiance with the F10.7 index and geomagnetic indices driven with the Heelis model for ensemble initialization with 90 members. These perturbations are normally distributed and kept constant through the quiet period. The sampled F10.7 indices are sampled from $d_{F10.7} \sim \mathcal{N}(120, 4^2)$ and Heelis input is defined through the hemispheric power, $d_{HP} \sim \mathcal{N}(22, 4^2)$ and the cross-tail potential $d_\Phi \sim \mathcal{N}(46, 8^2)$. Ensembles are run through a 7-day spin-up period to reach a steady-state for the start of the OSSE. For the storm period, magnetospheric drivers have updated samples, sampling from $d_{HP} \sim \mathcal{N}(115, 10^2)$ and $d_\Phi \sim \mathcal{N}(135, 20^2)$ with the same quiet period F10.7 samples.

Additional quality control is necessary for DA with observation flags and rejection to avoid assimilating poor quality observations. We reject observations for three reasons: negative values, outside an outlier threshold, and a failed forward operator, with rejection rates shown in Figure 5a. Negative values are the most common reason for rejection, notably at low altitudes where observation quality is worst. Between $10-50\%$ of

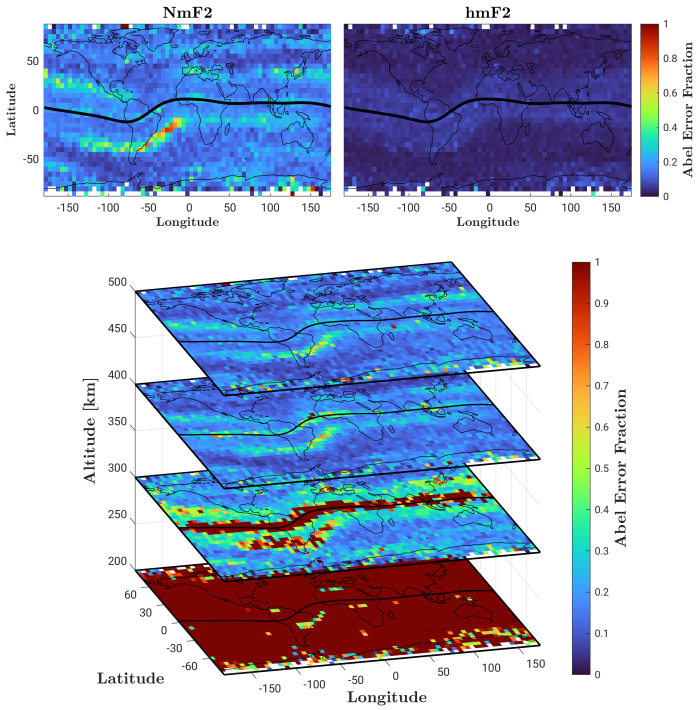

Figure 3. Binned average fractional error due to Abel retrieval, across all local times. Shown for N_mF_2, h_mF_2 and at each EDP altitude. Black line indicates the magnetic equator. Blank regions are due to lack of observation coverage.

observations are rejected between 160 − 250 km altitude, with rejection rates considerably improving at higher altitudes. We reject very far off observations using a 10 standard deviation threshold. For OSSE observation counts shown in Figure 5b, 520 km altitude constellations show greater observation counts than the 800 km altitude constellations.

3 OSSE Results

3.1 OSSE Ionospheric Results

First highlighting the quiet period, we show the impact of the first analysis step at UT01 on March 13th in Figure 6, for 300 km altitude. In the top row is the WAM-IPE nature run, where synthetic observations are derived, and the no-assimilation control (identical to the prior here), for electron densities at 300 km altitude. In the middle row are the posterior electron densities for OSSEs 1-4, each containing a single constellation. A first notable bias between WAM-IPE and TIEGCM control is the EIA, where WAM-IPE produces higher magnitudes and sharper horizontal gradients. High electron densities additionally extend into the night-side for WAM-IPE. In contrast, TIEGCM has a less prominent EIA peak and smoother spatial gradients, stretching for longer length scales, and has EIA peaks westward of WAM-IPE's. Comparing electron density magnitudes between TIEGCM and WAM-IPE, TIEGCM under-represents electron densities on the day-side and over-represents electron densities on the night-side. Assessing the posterior electron density states, seen in the middle row of Figure 6, the analysis step is as expected positively impacting posterior states, such as in increasing the EIA magnitude and better replicating the extension of higher electron density magnitudes into

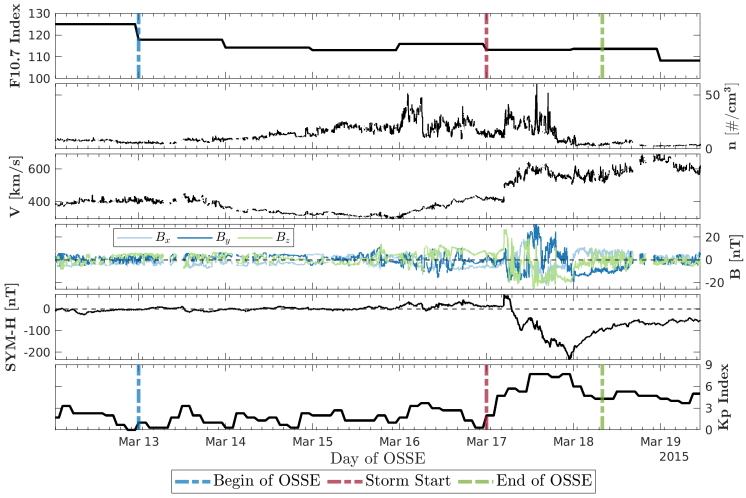

Figure 4. Solar (F10.7), solar wind conditions, and geomagnetic indices (Kp and Sym-H) for the week event. Solar wind states include plasma density, n, flow speed, V, and three magnetic field components, B. Vertical lines denote the OSSE quiet and storm periods.

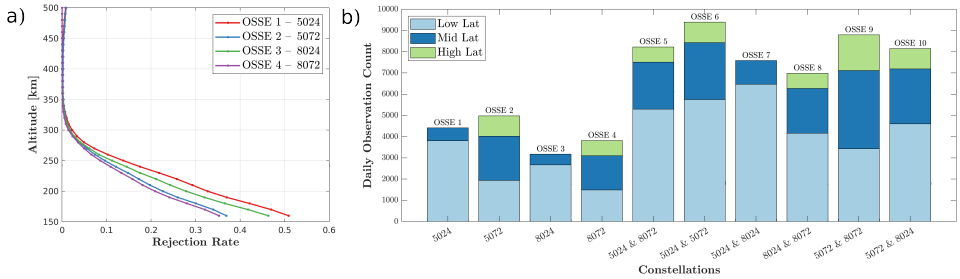

Figure 5. a) Shows the observation rejection rate as a function of altitude. b) Shows the daily EDP observation count for each OSSE constellation configuration, separated by latitude region.

the low-latitude night side. For high inclination constellations 5072 and 8072, electron density magnitudes are noticeably reduced in the night side high-latitudes.

Illustrating the performance of the analysis update is shown in the bottom row of Figure 6. The analysis bias improvement is defined as

$$\textbf{Bias Improve} = |\bar{\boldsymbol{x}}^{prior} - \boldsymbol{x}^{NR}| - |\bar{\boldsymbol{x}}^{post} - \boldsymbol{x}^{NR}| \tag{1}$$

where $|\boldsymbol{x}|$ is the element-wise absolute value of mean OSSE state vectors $\bar{\boldsymbol{x}}^{prior}, \bar{\boldsymbol{x}}^{post} \in \mathbb{R}^n$ and nature run state vector $\boldsymbol{x}^{NR} \in \mathbb{R}^n$. Bias improvement is shown in the bottom row of Figure 6, where blue regions indicate improved electron density biases and red regions indicated worsened biases. For state grid point comparisons between the two models, we down-sample WAM-IPE and interpolate as needed to TIEGCM's 5° grid resolution. At locations where WAM-IPE shows large electron density magnitudes, biases overall improve when observations are available. This is most evident for constellations 5024 and 8024 at peak EIA magnitudes. In red regions directly off WAM-IPE's EIA, we see the analysis step worsen biases. Generally, there are red worsen regions where there is a large gradient in WAM-IPE electron densities. More discussion of these worsening regions is addressed in Section 4, and is largely explained by Abel retrieval errors and improper background covariance. A similar figure for the storm period is shown in SI Figure S4.

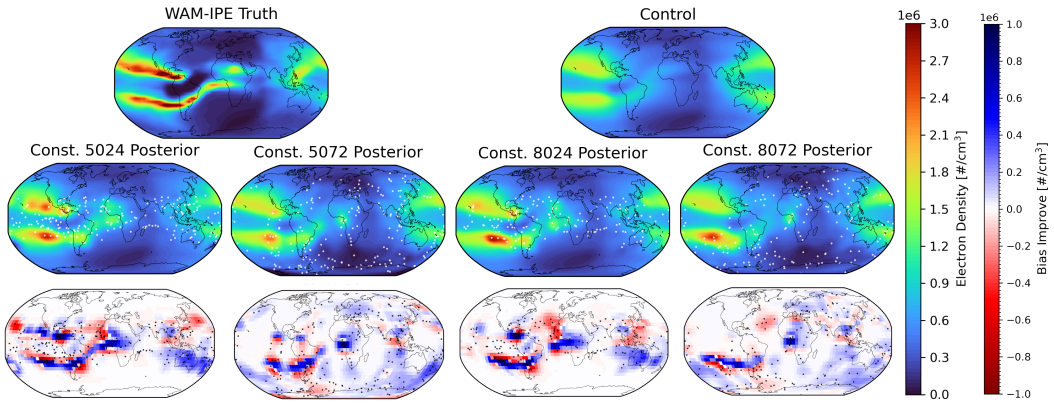

Figure 6. Electron density shown for the nature run, control, and OSSEs 1-4 posteriors at 300 km altitude at UT01 on March 13th, the first analysis step. The middle row shows posterior states, where white points are the assimilated tangent-point observations at 300 km altitude. Bias improvement, shown on bottom row, is illustrated with blue regions providing improvement and red regions worsening.

As the primary metric to assess OSSE performance, we use the root mean-square error (RMSE) defined as

$$\text{RMSE} = \sqrt{\frac{\sum_{j=1}^{N} \left(x_j^{NR} - \overline{x}_j^{exp}\right)^2}{N}} \tag{2}$$

where x_j^{NR} is the jth WAM-IPE state, $\overline{x}_j^{exp}$ is the jth ensemble mean OSSE state, and N is the total number of states. As RMSE is a magnitude dependent quantity, we separate results into three latitudes regions, where low latitude is between $-30°$ and $+30°$, middle latitude is between $-30°$ and $-60°$ as well as $30°$ and $+60°$, and high latitude is below $-60°$ and above $60°$. We show results for N_mF_2, h_mF_2, TEC, and altitude electron densities. We compare relative posterior RMSE performance against a no-assimilation control.

The N_mF_2 RMSE for all ten OSSEs is shown in Figure 7 for both quiet and storm periods. At high latitudes, the best performance is seen from OSSE 9 including constellations 5072 & 8072, the constellations with the most high-latitude coverage. As expected, OSSEs 1, 3 and 7 have no high-latitude coverage resulting in negligible impact on high-latitude errors. At low latitudes, OSSE 7, containing constellations 5024 & 8024, performs the best with the highest coverage of observations. Additionally, OSSEs 3 and 4 containing only constellations 5072 & 8072 have the least improvement in errors. At mid-latitudes, the OSSEs containing just constellations 5024 or 8024 have the worst performance, OSSEs 1,3 and 7. High inclination OSSEs show consistent improvement in N_mF_2 RMSE at low-latitudes and in high-latitudes.

The N_mF_2 posterior RMSEs for the storm period are also shown in Figure 7. As with the quiet period at low- and high-latitudes, there is a consistent improvement in RMSE over the control for the storm period, with more observation coverage of a region providing better performance. OSSE 7 with constellations 5024 & 8024 performs the best at low latitudes, and OSSE 9 with constellations 5072 & 8072 performs the best at high latitudes. It is also noted that the control RMSE increases for the storm-period due to increasing model biases between TIEGCM and WAM-IPE.

Further RMSE time-series plots are available in the SI Figures S5-S10. The TEC RMSE time series is shown in SI Figure S5, showing very similar performance to N_mF_2

RMSEs. h_mF_2 RMSEs are additionally shown in Supporting Plots S6. For h_mF_2, we see only slight impact to posterior RMSEs as compared with the no-assimilation control. This negligible performance is primarily attributed to a lack of state spread in h_mF_2, as we expect h_mF_2 observation quality to be very high, see Figure 3. Additional figures, including RMSE at each altitude (200, 300, 400 and 500 km) are available in the SI Figures S7, S8, S9 and S10. Altitude RMSEs show similar performance results as the N_mF_2 RMSEs with the exception of 200 km altitude.

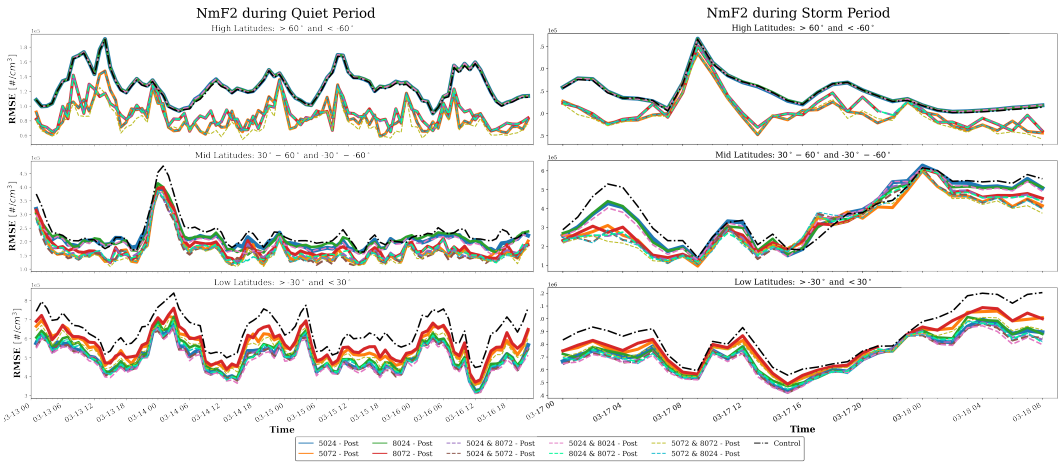

Figure 7. The N_mF_2 RMSE for each OSSE throughout the quiet period (left) and storm period (right). Solid lines indicate single constellation OSSEs and dashed lines indicate two constellation OSSEs. Performance is assessed compared to a no-assimilation control in the dashed black curve.

Observation comparisons at 200 km and 400 km altitude are shown in Figure 8, created through collecting all quiet-period observations at a given altitude. Here, IPE electron density states at EDP observation tangent points are shown against the Abel retrieval, TIEGCM prior and TIEGCM posterior, and separated by latitude region. Each plot is a density map of the observations in each range, normalized by the respective max binned observation count, shown in units of 10^5 cm^{-3}. The goodness of fit to the line $x = y$, R^2, and the number of observations, N, are provided for each sub-figure. For 400 km altitude, there is quite good agreement among the IPE states and Abel retrievals. TIEGCM prior biases are most noticeable at the low latitudes and for the 400 km altitudes there is consistent improvement in posterior agreement and R^2. Posterior states at 400 km perform best at the high latitudes and worst at low latitudes, likely due to EIA biases. We see all Abel retrieval values of R^2 greater than or equal to 0.78. Observation comparisons for 300 and 500 km altitudes are shown in SI Figure S11 and show similar results to 400 km altitude.

In the left sub-figure of Figure 8 for 200 km altitude, we see very different results. For all latitude regions, the Abel retrieval and TIEGCM prior and posterior are all severely underbiased to IPE nature run electron densities. Still, we do see improvement in agreement for posterior states at the middle and high latitudes, while the 200 km low latitudes show worsening error. The low and middle latitudes priors have surprising good R^2 values, due to many states being very low magnitude (not very visible on this plot axis scale), while the Abel retrieval at low latitudes has a negative R^2 value.

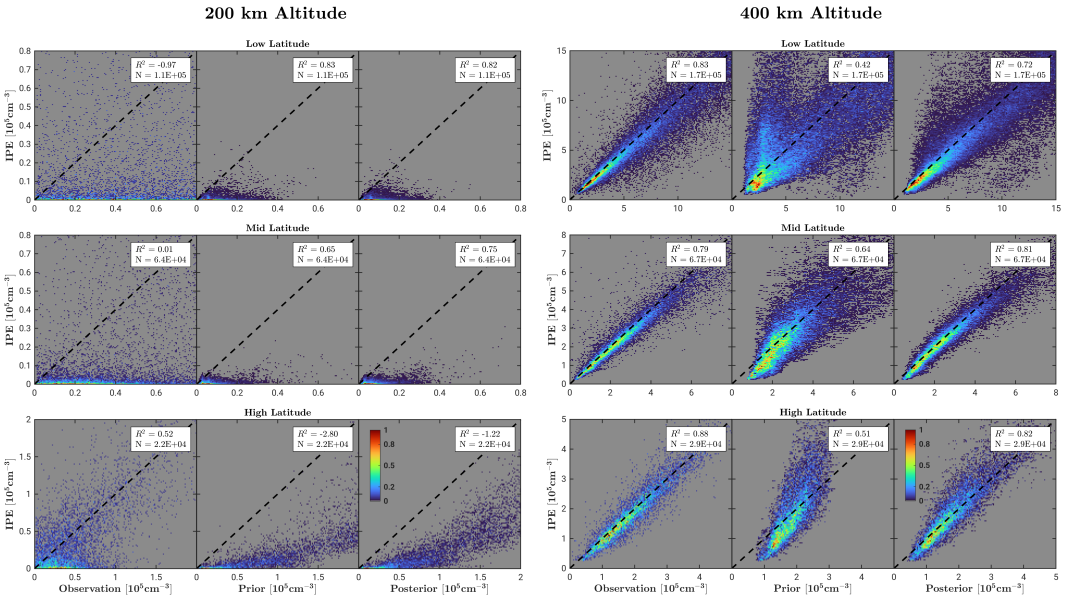

Figure 8. Comparison of electron density observations at given altitudes (200 and 400 km), with the nature run IPE state shown against the Abel retrieval, TIEGCM prior and TIEGCM posterior states. Density heat maps are shown, with counts normalized by the max bin count for that subplot. Units are all in $10^5 cm^{-3}$.

3.2 Ranking Metric

To further quantify relative OSSE performance, we devise a simple high-level ranking metric. Using the time series of RMSEs calculated for N_mF_2, h_mF_2, TEC and altitude electron densities, each OSSE is ranked for each hour. The ten OSSEs are ordered and ranked according to each OSSE's RMSE, 1 through 10, with 1 having the lowest error (best performance) and 10 having the highest error (worst performance). Averaging hourly OSSE ranks over the whole experiment period then gives the ranking metric.

The vertically integrated TEC ranking metric is shown in Figure 9 for the three latitude bins and globally, for both the quiet and storm periods. Table cells are color-coated with deep green indicating the best performance (close to 1) and deep red indicating worst performance (close to 10). For low latitudes, OSSE 7 (5024 & 8024) performs the best with the highest coverage of low latitudes. For high latitudes, OSSE 9 (5072 & 8072) performs the best with the highest coverage in that respective region. OSSEs that mix high and low inclination constellations, OSSE 5, 6, 8 and 10, generally do well across the board. OSSE performances are similar for quiet and storm conditions as most quiet and storm rankings are within a rank of 1. For global rankings, these typically reflect performance at the low and mid-latitudes, where the largest electron density magnitudes are present and thus dominate RMSEs. Additional ranking metric tables are available for NmF2, hmF2 and electron density at altitudes 200, 300, 400 and 500 km in SI Figures S12, S13 and S14. It is noted that TEC, NmF2 and 300-500 km altitude ranking values all indicated similar results.

To explain ranking metrics performance, we collect all the rankings for the quiet period at 200, 300, 400 and 500 km electron density altitudes (SI Figure S12) and plot them against their daily average observation count, shown in Figure 10. The left subfigure shows results collected for altitudes 300, 400 and 500 km, and the right shows rank-

		Low Lat	*Mid Lat*	*High Lat*	*Global*	*Low Lat*	*Mid Lat*	*High Lat*	*Global*
Experiment Name	**Constellations**	**Quiet**				**Storm**			
OSSE 1	5024	4.98	9.31	8.8	5.85	5.7	8.42	8.58	6.79
OSSE 2	5072	9.09	5.37	3.97	9.03	7.97	4.09	3.06	7.09
OSSE 3	8024	6.8	9.28	8.96	7.24	5.82	6.94	9.06	6.48
OSSE 4	8072	9.91	6.9	4.27	9.91	9.67	5.18	4.55	9.03
OSSE 5	5024 & 8072	3.6	4	4.84	3.05	4.91	6.3	5.42	4.88
OSSE 6	5024 & 5072	2.27	2.55	4.37	1.64	3.09	4.7	3.85	2.76
OSSE 7	5024 & 8024	1.34	7.71	8.93	2.79	2.21	7.82	8.73	4.42
OSSE 8	8024 & 8072	5.43	4.53	4.55	4.93	4.85	5.15	5.48	4.82
OSSE 9	5072 & 8072	7.83	2.31	2.19	7.43	7.33	2.82	2.45	5.94
OSSE 10	5072 & 8024	3.77	2.81	4.13	3.13	3.45	3.58	3.82	2.79

Figure 9. OSSE ranking metric for TEC. Rankings are averaged over the quiet period defined from March 13th UT01 to March 16th UT022 and averaged over the storm period defined from March 17th UT00 to March 18th UT08. Values close to 1 indicate the best performance and values close to 10 indicate the worst performance.

437 ings for 200 km, also splitting for low, mid and high latitudes. Very simply, where we
438 have more observation, we see better OSSE performance with lower metric ranks as shown
439 with a strong negative correlation. This finding holds for all regions except for one: 200
440 km altitude at low latitudes. These values are reflected in SI Figure S12 where worsen-
441 ing ranking is seen for 200 km in OSSEs, as well as in Figure 8 at 200 km with little agree-
442 ment between IPE states and Abel retrieved EDPs. Regardless, we still do see improve-
443 ment in the ranking metric at 200 km altitudes for mid- and high-latitudes, same as all
444 other regions improving performance with greater observation coverage.

445 A couple of additional results are as follows. First, we see more observations from
446 the 520 km altitude constellations than the 800 km altitude constellations, and this di-
447 rectly corresponds to better ranking metrics for these OSSEs. With this, it is arguable
448 that OSSE 6 with 5024 & 5072 is the best performing OSSE (as reflected in the global
449 ranking metric in Figure 9). We see constellation 8024 have 27% less profiles than con-
450 stellation 5024; we see constellation 8072 have 24% less profiles than constellation 5072.
451 The differences is likely explained by the shorter orbit period of the 520 km altitude con-
452 stellations, enabling more limb passes and RO events. Secondly, OSSE 9 with 5072 &
453 8072 performs poorly for low latitude observations, as one might expect; however from
454 Figure 5, OSSE 9 performs worse than OSSEs 1 (5024) and 3 (8024) with comparable
455 low-latitude coverage. This worse performance can potentially be explained by larger ob-
456 servation errors that the high inclination constellations show at low-latitudes, as illus-
457 trated most evidently in the bottom left panel of Figure 2. Thus a combination of a low-
458 and high-inclination constellation provides the best global coverage.

459 ### 3.3 Observation Performance Limit

460 An additional question raised when designing an observing system and adding more
461 observations: what is the potential performance limit? We define a "performance limit"
462 as the point when assimilating more observations plateaus improving OSSE errors. To
463 address this question with available OSSE results, we compute the RMSE for all grid
464 points for the low-, mid- and high-latitude regions of each OSSE, as well as for the con-

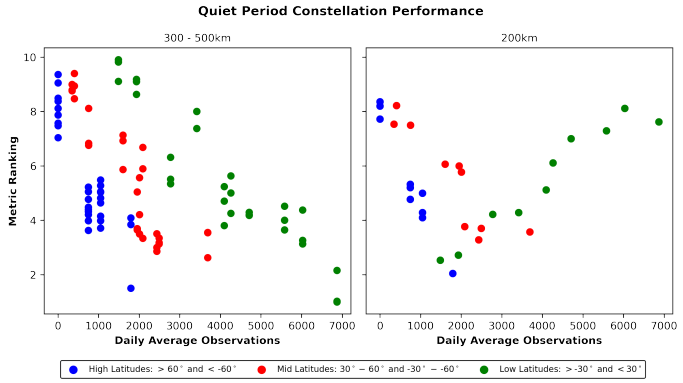

Figure 10. The relationship between the latitude observation counts shown in Figure 5b and the ranking metrics in SI Figure S12. Again noting that 1 indicates the best ranking and 10 indicates the worst ranking. All show a negative correlation (improvement with more observations) with the exception of 200 km at low latitudes

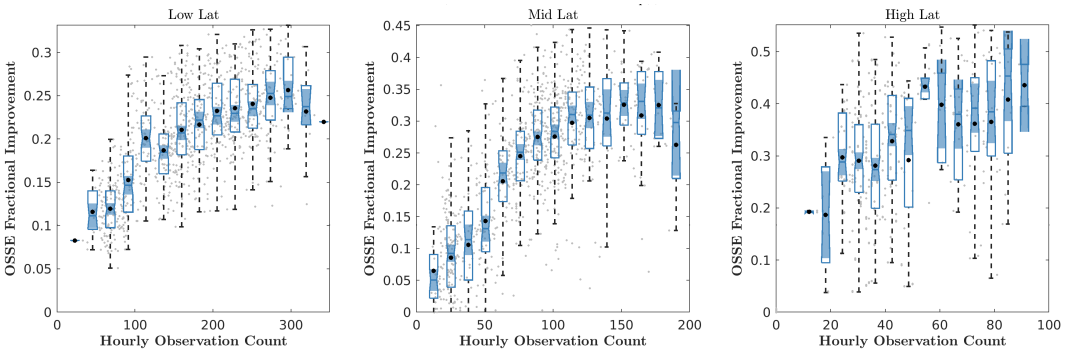

Figure 11. OSSE N_mF_2 RMSE fractional improvement over the control as a function of observation count, defined in Equation 3. Calculated for the entire N_mF_2 grid RMSE within each latitude band. Mean improvement (black dots) and notched box plots are averaged over count bins of all samples (grey dots). Non-overlapping shaded regions indicate the significant difference between medians (5% confidence).

trol. We then define the OSSE fractional improvement over the control as

$$\text{Fractional Improvement} = \frac{\text{RMSE}_{cntrl} - \text{RMSE}_{exp}}{\text{RMSE}_{cntrl}} \tag{3}$$

This is done for every hour of the OSSE and all ten OSSEs. Next binning over hourly observation counts we show the mean and notched box plot for the N_mF_2 RMSEs in Figure 11. For the low- and mid-latitudes, there is a steady improvement in performance with more observations and a visible leveling off, as the improvement is no longer statistically significant at the peak observation counts. It is noted for the end points of each latitude region, shaded regions have very small or very large spread due to a limited number of samples. For high latitudes, the results are more noisy as we have less samples due having only two constellations with high-latitude coverage. We see a positive trend in the high-latitude fractional improvement that does not appear to plateau. Results for TEC show very similar results to N_mF_2 (SI Figure S15), and h_mF_2 fractional improvement are less consistent (SI Figure S16). Further study is needed to investigate the cause of this performance limit, such as due to observation errors, background covariance, localization and other DA parameters, model errors, model resolution, or observation spatial density.

4 Discussion

Returning to the initial question we first posed as to what constellation configuration is best: it depends. Simply put, with more observation coverage in a given region, we gain better ionosphere specification, with a combination of a low- and high-inclination constellation providing the best global coverage. Therefore, designing an RO constellation observing system depends on what regions we desire to study or monitor.

Fully simulating the Abel inversion retrieval for EDP observations allows us to evaluate the impact of Abel inversion errors within a DA framework, as compared with studies such as Hsu et al. (2014); Lee et al. (2013) that only perturbed using Gaussian errors. Previously documented Abel inversion errors are evident, notably at the low latitudes and low altitudes (Tsai et al., 2001), and their resulting in poor analysis updates. Abel inversion particularly has trouble reproducing the low electron densities in "plasma caves" beneath the EIA crests (Liu et al., 2010; Yue et al., 2010), as this is the one the one region (200 km, low latitude) we see the DA have negative impact on electron density states. These were also expected from Figure 3 where there are considerably high Abel retrieval errors. Nevertheless, we do see positive impact for 200 km altitudes at the mid and high latitudes. Additionally as we move to higher altitudes, we see observations consistently provide positive data impact.

OSSE results suggest this region of very low electron densities is likely an inherent limitation of RO and the Abel inversion technique. As we move to lower altitudes, the radio signal passes becoming increasing longer, comprising more of the ionosphere and yielding larger slant TEC observations. The Abel retrieved EDPs cannot the resolve IPE's low electron densities using large TEC observations, especially if the spherical symmetry assumption is increasingly broken, adding increasingly more observation noise. We also see many negative observations in this region, reducing data available for assimilation. Therefore we see RO EDPs to not be useful for ionospheric specification in this low latitude, low altitude region, supporting the conclusions of Lee et al. (2012).

To detail poor EDP performance, we highlight two assimilated profiles shown in Figure 12. We focus on the worsening regions of constellation 5024 from Figure 6. We show the WAM-IPE nature run, Abel retrieval, and the TIEGCM prior and posterior at profile locations.

One source of poor analysis updates come from DART-TIEGCM, exhibited by profile (a) of Figure 12. At this location, there is good agreement between the Abel retrieved EDP (and its assigned 1 standard deviation (std) uncertainty) and the IPE nature run. This observation point is within EIA peak electron density, and as the EAKF locally updates states using the ensemble background covariance, an over-correction is performed for grid points off IPE's EIA structure. The regional impact of this observation is shown in the bottom plot of Figure 12, including the nature run IPE state at 300 km, TIEGCM's background electron density correlation and the observation increment. TIEGCM shows high background correlations extending beyond IPE's sharper electron density gradient, and the update is very much defined by the isotropic GC localization. This poor update underscore the importance of having a good background covariance, and is a necessary filter feature for global specification. Many studies have been devoted to improving the local update impact, either through improved background covariance or through localization (e.g., Lin et al., 2015; Hsu et al., 2018; Forsythe et al., 2020; Zhang et al., 2023).

Another source of poor analysis updates, one very much a focus of this study, come from Abel inversion errors, shown at point (b) of Figure 12. At this location, the prior EDP has fine agreement with IPE; however, the Abel inverted EDP is considerably more biased, and we see worse posterior error. This profile deviates from the typical Chapman function, instead showing a double peak structure in both the EDP observation and IPE RO tangent points. A view of this profile and the IPE states are shown in SI Fig-

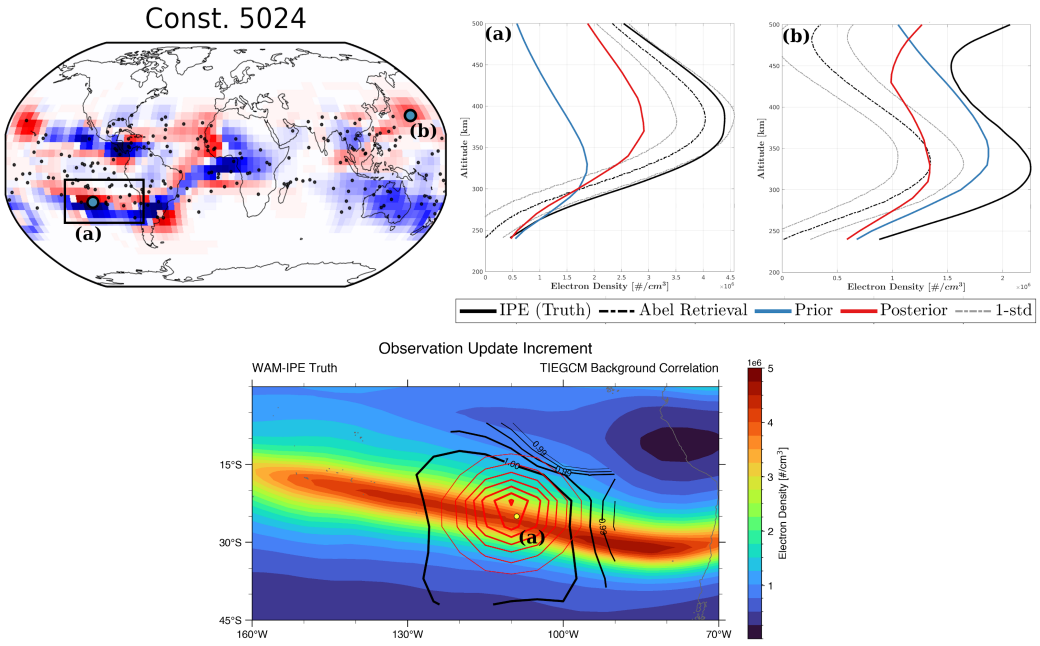

Figure 12. Highlighting two EDPs introducing poor analysis updates. Shown using first analysis step of constellation 5024 (same as in Figure 6). EDP (a) highlights poor background covariance, EDP (b) highlights large Abel inversion error. Bottom contour plot shows the IPE electron density at 300 km, and the observation increment (red) and TIEGCM background correlation (black).

ure S17, where the tangent points' quasi-vertical profile at high altitudes includes higher magnitude electron densities. Ideally, this observation profile should be flagged for quality control and not assimilated, or alternatively the observation uncertainty should be considerably increased to more sufficiently account for the Abel inversion error.

It is noted as a caveat that the devised ranking metrics only provides a big-picture view of the relative OSSE results. These rankings do not indicate the magnitude of the relative OSSE performance, and should be viewed in conjunction with the RMSE time series plots to gain a full perspective. Regardless, conclusions from these rankings generally support the findings from the RMSE time-series. Additionally assessing errors through RMSE and with parameters TEC and N_mF_2 can simplify the global impression of ionosphere specification. These metrics are decidedly magnitude dependent, sometimes representing only the highest magnitude locations, e.g., the EIA or F_2 peak. The altitude profile of the electron density can be very important for space weather influences, making ionospheric specification a three-dimensional problem needing to be address through multiple metrics.

We focus in this study on the relative performance of all OSSEs, and the filter performed well enough for assessment. Filter features such as tuned localization, implementing inflation, and better ensemble initialization with more realistic geomagnetic forcing would all help to improve data impact of the synthetic EDPs. One evident source of poor impact is with the lack of h_mF_2 spread in TIEGCM, as previously noted in Lee et al. (2012), that causes h_mF_2 improvement to be considerably less than expected given their low errors.

Another large restriction in filter performance was achieving sustained RMSE improvement from using a coupled I-T model due to plasma states have limited memory in the system. Non-updated neutral states in TIEGCM quickly rebound posterior plasma states back to control states in the forecast step, showing only a 1-2 hour system memory. Previous studies have shown plasma forecasting only on the order of hours with ionosphere assimilation in coupled I-T models (Jee et al., 2007; Chartier et al., 2013). Neutral states have a longer forecasting memory (Chartier et al., 2013), and specifying neutral states such as oxygen composition have been shown to greatly improve plasma forecasting (Hsu et al., 2014). This would help the system to retain plasma RMSE improvements when forecasting and see greater OSSE performance. Another possibility not included in this study is the potential to estimate neutral states using the EDP observations, and has been shown to have positive impact for composition, neutral temperature, and neutral winds (Matsuo & Hsu, 2021; Dietrich et al., 2022).

Accounting for realistic Abel inversion and forecast model errors in this study underscores the need for more complete EDP error quantification and observation quality control. There still remains work needed to fully quantify Abel inversion errors, and quantify their impacts from breakdowns in the spherical symmetry assumption. In this study there are two main error sources included in these OSSEs: errors from Abel inversion and errors within the DART-TIEGCM DA framework, and it is challenging to fully deconvolve these two error sources. Future OSSE work could apply the same OSSE setup while also running equivalent OSSEs with synthetic EDPs directly sampled at WAM-IPE locations, enabling direct comparisons of error impacts and more complete quantification of Abel inversion errors. Abel error fitting over altitude, magnetic latitude and local time, as in Yue et al. (2010); Liu et al. (2010), was shown to not be sufficient in some cases. Additional error analysis capturing exactly how the spherical symmetry assumption is being broken is needed by analyzing the radio ray paths taken through the ionosphere. Better quantification of these Abel errors should improve DA performance in negatively impacted regions, and provide means for better observation quality control. Further, more advanced Abel inversion algorithms have improved low altitude observations errors and improved their DA impact (e.g., Pedatella et al., 2015; Wu, 2018; Chou et al., 2017; Tulasi Ram et al., 2016) and were not included in this study.

5 Conclusions

To inform future RO constellation mission planning and design, this study uses a comprehensive OSSE approach to evaluate the ionospheric specification impact of assimilating RO EDPs into a coupled I-T model. We perform ten OSSE configurations to evaluate four base hypothetical RO constellations. These RO constellations are modeled after F3/C and F7/C2, at either 24° or 72° inclination and at either 520 or 800 km altitude orbits. Each OSSE's relative performance is evaluated through multiple metrics during the St. Patrick's Day storm on March 13-18, 2015, including quiet and storm-time conditions, by using the DART-TIEGCM and a nature run simulation provided by WAM-IPE. This study is the first ionospheric OSSE study to comprehensively and realistically account for forecast model and observation errors by using a distinct nature run simulation and forecast model, as well as retrieving synthetic EDP observations from the WAM-IPE nature run with an extensive Abel inversion procedure.

Overall, better spatial coverage of EDP observations from a given RO constellation design corresponds to a better OSSE performance. For low-inclination constellations with greater low-latitude coverage, the best performance is obtained for the low latitude ionosphere, and likewise for high-inclination constellations the best performance is achieved for the high latitude ionosphere. The increased spatial coverage of EDPs directly corresponding to improved results is best reflected in a ranking metric, with higher observation counts seen for the 520 km altitude constellations, arguably making OSSE 6 (5024 & 5072) the best performing OSSE. This combination of a low- and high-inclination con-

stellation additionally provides the best global coverage. Consistent posterior improvement is seen at all latitudes for altitudes 300 to 500 km, demonstrating evident benefits to EDP assimilation. A performance limit is also conceivably illustrated for two 6-satellite constellations, and further study is needed to uncover its causes and validity.

Another notable finding is the limitations of RO EDP data impact on the dayside equatorial region at low altitudes. DA impact in this region is negatively impacted by worsening Abel inversion errors due to both breakdowns in the spherical symmetry as well as RO's inherent shortcoming in accurately retrieving very low, low altitude plasma densities. Additional large retrieval errors are seen when vertical plasma density structures deviate from the typical Chapman function, such as double peaked EDPs.

Ultimately, RO EDPs offer a unique, three-dimensional global ionospheric perspective advantageous for global ionospheric specification. While Abel retrieval and uncertainty quantification may still be improved, as considered in the discussion, RO EDPs offer clear operational space weather benefits for the upper atmosphere. Further assessment of space weather observing systems using comprehensive OSSE studies will considerably enhance future observation integration into DA systems, as well as greatly aid in future constellation design.

Open Research Section

Software tools used for the work are all publicly available. The Whole Atmosphere Model Ionosphere Plasmasphere Electrodynamics (WAM-IPE) software was developed by the NOAA Space Weather Prediction Center and available from `https://github.com/NOAA-SWPC`. The Data Assimilation Research Testbed (DART) software was developed by the National Center for Atmospheric Research (NCAR) Computational and Information Systems Lab and available from `http://dart.ucar.edu`. The Thermosphere Ionosphere Electrodynamics General Circulation Model (TIEGCM) software was developed by the NCAR High Altitude Observatory and available from `http://www.hao.ucar.edu/modeling/tgcm/tie.php`. Abel inversion algorithm code was developed by the COSMIC Data Analysis and Archive Center (CDAAC) and available from `https://cdaac-www.cosmic.ucar.edu/`.

The Observing System Simulation Experiment data used for the experiment ensembles, control, and nature runs used in this study are available at `https://osf.io/em7fk/?view_only=309c10ed65d34ea8920ca1281d570a76` via `https://doi.org/10.17605/OSF.IO/EM7FK` with open source access.

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