

1 Supporting Information for

2 **Link between crustal thickness and Moho transition zone at 9°N East Pacific Rise**

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### 19 **Text S1. Finite-difference waveform modelling**

20 The modelled seismic data are calculated by solving 2-D elastic wave equation using a  
21 temporal 2<sup>nd</sup>-order and spatial 4<sup>th</sup>-order staggered-grid finite-difference scheme [Levander,  
22 1988]. To avoid numerical dispersion, we used 57.5 m and 28.75 m grid spacings, respectively,  
23 in the modelling of 3-5 Hz and 3-10 Hz data. These settings ensure five grid points are sampled  
24 by the shortest wavelength (wavelength in the water column), satisfying the dispersion  
25 condition [Levander, 1988]. Time steps of 4 ms and 2 ms were used in the modelling of 3-5 Hz  
26 and 3-10 Hz data, respectively, to keep the waveform modelling stable. An absorbing boundary  
27 condition [Clayton and Engquist, 1977] was used to attenuate the reflections from model  
28 boundaries.

29

### 30 **Text S2. Source wavelet**

31 An accurate source wavelet is critical for the success of FWI because the errors in seismic  
32 waveform difference due to an inaccurate source wavelet will be directly mapped into the  
33 velocity model. In this study, we estimated the source wavelet by stacking the near-offset water  
34 arrivals. The source wavelets are estimated separately for OBSs and OBHs. Here we detailed  
35 the workflow of source estimate for OBHs, and that for OBSs is the same except using OBS  
36 dataset. We extracted four near-offset traces from each OBH dataset after predictive gapped  
37 deconvolution and aligned these traces to the same starting time (0.05 s). The signals after 0.6  
38 s were muted to mitigate the influence of seismic multiples and later reflections. These traces  
39 show high similarity in waveform of direct water arrivals (Figure S3A). We stacked the aligned  
40 traces (Figure S3B) and filtered the stacked signal (Figure S3C) using the same band-pass  
41 filters (3-5 Hz or 3-10 Hz) as applied to seismic data in FWI. The starting time of the source  
42 wavelet is determined by performing finite-difference waveform modelling and comparing the  
43 modelled and observed near-offset water wave. Figure S3C shows the source wavelets for  
44 OBSs (dashed curves) and OBHs (solid curves). Precise amplitude of the source wavelet is not  
45 needed because we normalized the seismic traces in the trace normalized FWI and the whole  
46 seismic gather in the true amplitude FWI (see text below). The good match between the  
47 modelled and observed near-offset direct water arrivals for OBH and OBS data (Figure S4)  
48 indicates that the estimated source wavelets are sufficiently accurate for performing FWI.

49

### 50 **Text S3. Starting models**

51 The water velocity is set to 1.5 km/s and is not updated in the FWI. The starting crustal P-wave  
52 velocity model is obtained from a ray-based travel time tomography of Pg and PmP arrivals

53 [Canales *et al.*, 2003]. The starting mantle P-wave velocity is expanded from a one-  
 54 dimensional velocity profile hanging from the seafloor, where the mantle velocity increases  
 55 linearly from 7.9 to 8.2 km/s within 5 km depth range. We smoothed the velocity around the  
 56 tomographically constrained Moho to avoid a sharp boundary between the crust and mantle.  
 57 The starting P-wave velocity model is shown in Figure S5. The starting S-wave velocity and  
 58 density are calculated from P-wave velocity using the empirical relations given in [Brocher,  
 59 2005]. The S-wave velocity and density are not updated in the FWI.

60

#### 61 **Text S4. FWI**

62 We used a 2-D time domain elastic FWI developed originally by Shipp and Singh [2002] for  
 63 marine streamer data with constant shot and receiver spacings and modified the code to  
 64 accommodate seismic data recorded by ocean bottom instruments with arbitrary geometry in  
 65 2-D space. Starting from an initial estimate of velocity of the subsurface, the elastic FWI  
 66 iteratively updates the velocity model by reducing the misfit between the observed and  
 67 modelled seismic data

$$68 \quad m_{n+1} = m_n + \alpha_n g_n, \quad (1)$$

69 where  $m$  is the model parameter,  $\alpha$  is a step length,  $g$  is the gradient of the misfit function  
 70 [Shipp and Singh, 2002] and  $n$  is the iteration number. In this study, we only inverted the P-  
 71 wave velocity of the subsurface. A constant step-length of 30 m/s was used in all iterations.

72

73 We simultaneously inverted the pressure data recorded by OBHs and the vertical component  
 74 data of OBSs. The conventional elastic FWI directly compares the least-squared difference  
 75 between the modelled and observed waveforms [Shipp and Singh, 2002; Tarantola, 1986].  
 76 Because the magnitude of amplitudes of the OBH and OBS data are very different, direct  
 77 comparison of waveforms leads to unbalanced contributions to the gradient for OBH and OBS  
 78 data. To solve this problem, two FWI approaches comparing normalised seismic data were used  
 79 in this study.

80

81 We performed the trace normalized FWI of Tao *et al.* [2017] in the first stage. In this FWI  
 82 approach, each trace of the observed and modelled data is normalised by its  $L_2$ -norm, and the  
 83 misfit function is defined as the least-squared difference between the modelled and observed  
 84 seismic data after trace-by-trace normalisation

$$85 \quad J_1 = \sum_i^{N_s} \sum_j^{N_r} \left\| \frac{d_{i,j}}{\|d_{i,j}\|} - \frac{u_{i,j}}{\|u_{i,j}\|} \right\|^2, \quad (2)$$

86 where  $d$  and  $u$  represent the observed and modelled seismic data,  $N_s$  is the number of seismic  
 87 gathers and  $N_r$  is the number of traces within each seismic gather, and  $\| \cdot \|$  represents the  $L_2$   
 88 norm. From Equation (2), we can see that the trace normalised FWI is insensitive to the  
 89 amplitude of the seismic data [Tao et al., 2017]. Furthermore, the trace-normalised FWI is  
 90 capable of inverting triplicated waveforms [Tao et al., 2017], which in our case are the PmP  
 91 arrivals. However, this method ignores the amplitude variation with offset (AVO) effect and  
 92 mainly compares the phase information in seismic data, leading to reduced resolution than  
 93 conventional FWI [Liu et al., 2016]. The seismic residual of the trace normalised FWI is

$$94 \quad R_{i,j} = \frac{1}{\|d_{i,j}\| \|u_{i,j}\|} \left( \frac{\int d_{i,j,t} \cdot u_{i,j,t} dt}{\|d_{i,j}\| \|u_{i,j}\|} u_{i,j} - d_{i,j} \right), \quad (3)$$

96

97 where  $\int dt$  represents the integration over time and  $\cdot$  is the multiplication operator.

98

99 To ensure the inversion convergence to the global minimum, we applied the multi-scale  
 100 inversion strategy of *Bunks et al.* [1995] in the trace normalised FWI. We first inverted the  
 101 seismic data between 3 and 5 Hz, and then this inverted velocity model was used as a starting  
 102 model for the inversion of 3-10 Hz data. We also applied the multi-stage inversion strategy of  
 103 *Shipp and Singh* [2002] for each frequency-band, where the near-offset (<20 km) data are  
 104 inverted first and we increased the offset by 20 km every 7 iterations.

105

106 Taking the inverted model of the trace normalised FWI as starting model, we further performed  
 107 30 iterations of true amplitude FWI for 3-10 Hz data in the second stage. In the true amplitude,  
 108 each seismic gather is normalised by the  $L_2$ -norm of the whole seismic gather, which scales the  
 109 amplitude of OBH and OBS data to similar magnitude. The misfit function of the shot-  
 110 normalised FWI is defined as the least-squared difference between the modelled and observed  
 111 data after normalisation

112

$$113 \quad J_2 = \sum_i^{N_s} \left\| \frac{d_i}{\|d_i\|} - \frac{u_i}{\|u_i\|} \right\|^2. \quad (4)$$

114

115 This FWI approach compares both the amplitude and the phase information, which can further  
 116 refine the velocity of the subsurface. The seismic residual is defined as follows

$$117 \quad r_{i,j} = \frac{1}{\|d_i\| \|u_i\|} \left( \frac{\int d_{i,j,t} \cdot u_{i,j,t} dt dr}{\|d_i\| \|u_i\|} u_{i,j} - d_{i,j} \right), \quad (5)$$

118

119 where  $\int dt dr$  represents the integration over time and trace and  $j$  is the index of trace. The  
120 multi-offset inversion strategy of *Shipp and Singh* [2002] is not used in the second stage  
121 because no cycle skipping between modelled and observed data is observed after the trace-  
122 normalised FWI.

123

124 The gradient ( $g$ ) in the FWI is computed by zero-lag cross-correlating the source generated  
125 forward-propagated wavefield and the adjoint source generated wavefield by back projecting  
126 the seismic residuals [*Shipp and Singh, 2002*]. We muted the gradient in the water column to  
127 avoid updating the velocity of water and we tapered the gradient within 115 m distance from  
128 OBHs and OBSs. A conjugate-gradient method [*Scales, 1987*] was used to speed up the  
129 convergence. The conjugate gradient was multiplied by square root of depth to partially account  
130 for spherical divergence [*Krebs et al., 2009*], except for the last twenty iterations of the second  
131 stage where the conjugate gradient was multiplied by square of depth to further enhance the  
132 energy around and below the MTZ. To suppress the artifacts introduced by the sparse  
133 distribution of ocean bottom instruments, we applied a 2-D wavenumber domain low-passed  
134 filter [*Jian et al., 2021*] to the velocity gradient. The low-passed filter is defined as

135 
$$\left| \frac{k_x}{k_{cx}} \right| + \left| \frac{k_z}{k_{cz}} \right| = 1, \quad (6)$$

136 where  $k_x$  and  $k_z$  are the wavenumbers along horizontal distance and depth.  $k_{cx}$  and  $k_{cz}$  are the  
137 cut-off wavenumbers of the 2-D low-passed filter.  $k_{cx}$  is set as the inverse of the minimum  
138 distance (8 km) between two neighbouring ocean bottom instruments ( $k_{cx} = 0.125 \text{ km}^{-1}$ ). We  
139 set  $k_{cz}$  as the maximum resolvable wavenumber ( $k_{z \text{ max}}$ ) of FWI, which is defined as follows  
140 [*Brenders and Pratt, 2007*]

141 
$$k_{cz} = k_{z \text{ max}} = \frac{2\pi f}{v}, \quad (7)$$

142 where  $f$  is the frequency and  $v$  is the background velocity. In this study, we used velocity  $v =$   
143 6.5 km/s and the frequency  $f$  of 5 and 10 Hz to determine  $k_{cz}$  in FWI of 3-5 and 3-10 Hz data,  
144 respectively.

145

#### 146 **Text S5. Checkerboard test**

147 We performed checkerboard tests to assess the resolution of the FWI result. The checkerboard  
148 input models are designed by adding 2-D sinusoidal anomalies into the crust and mantle of the  
149 FWI model. The maximum velocity perturbation is  $\pm 5\%$ , which is the same as that used in the  
150 travel time tomography study from *Canales et al.* [2003]. We tested velocity anomalies with

151 size of  $0.5 \times 10$  km (horizontal  $\times$  vertical),  $0.5 \times 8$  km,  $0.3 \times 8$  km and  $0.5 \times 5$  km (Figure  
152 S7-10A). Synthetic seismic data are modelled by performing the finite-difference modelling  
153 using the estimated source wavelets of 3-10 Hz and the same source-receiver geometry as that  
154 of the field data. We inverted these synthetic seismic data using the same inversion parameters  
155 and time window as that for the FWI of the field data, starting from the final model of FWI  
156 using field data. We only performed the second stage of true amplitude FWI in the  
157 checkerboard tests, because no obvious cycle-skipping is observed. The results show that  
158 velocity anomalies of  $0.5 \times 10$  km and  $0.5 \times 8$  km size are completely recovered between 10  
159 and 80 km horizontal distances (Figure S7B and S8B) and the velocity anomalies of  $0.3 \times 8$   
160 km size are recovered with locally reduced recovery in the mid-crust (Figure S9B). In contrast,  
161 the velocity anomalies of  $0.5 \times 5$  km size are not recovered (Figure S10B). Therefore, the  
162 minimum resolution is  $\sim 8$  km in the horizontal direction and  $\sim 0.3$  km in the depth direction,  
163 and therefore, we only interpret anomalies larger than these values.

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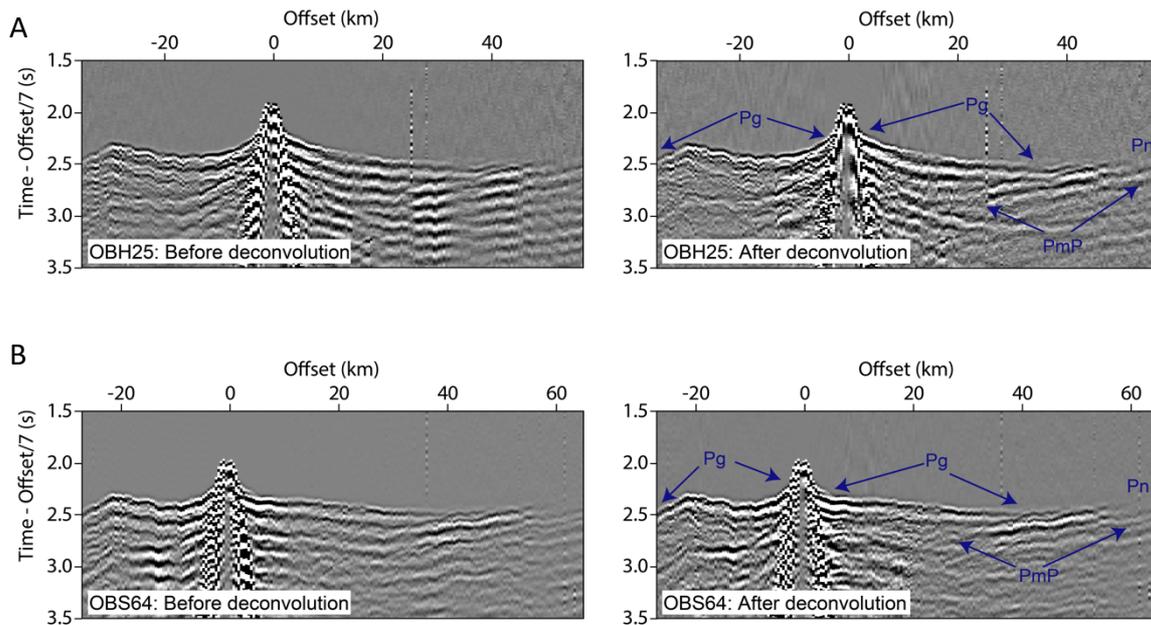
#### 165 **Text S6. Synthetic tests for the recovery of MTZ**

166 We performed synthetic tests (Figure S11-S17) to assess the resolvability of the FWI method  
167 for a thick or thin MTZ, following the approach proposed in *Jian et al.* [2021]. A MTZ with  
168 velocity increasing linearly from 7.0 km/s to 7.85 km/s with depth is inserted in the final  
169 inverted model from FWI of OBS data. The thickness of MTZ is 0.5, 1.0, 1.5, 2.0, 2.5, 3.0 and  
170 3.5 km in these tests (Figure S11-S17(A)), respectively. These designed models (hereafter  
171 referred to as ‘synthetic true model’) were used to generate synthetic seismic data by  
172 performing finite-difference modelling using the estimated source wavelets of 3-10 Hz and the  
173 same source-receiver geometry as that of the field data. We designed a starting model (Figure  
174 S11-S17(B)) for synthetic tests by smoothing the velocity below the top of the MTZ within the  
175 synthetic true model. The lateral width of the smoothing window is 8.0 km and the vertical  
176 width is twice of the thickness of the inserted MTZ. This is to ensure the starting model is  
177 smooth but doesn’t lead to cycle-skipping. We only performed the inversion of 3-10 Hz data in  
178 the second stages of the FWI workflow. The same inversion parameters as those for FWI of  
179 field data were used in the synthetic tests. The final inverted models and comparisons of some  
180 1-D velocity profiles are shown in Figure S11-S17(C). The difference between the synthetic  
181 true and starting models is shown in Figure S11-S17(D) and that between the synthetic true  
182 and inverted models is shown in Figure S11-S17(E). For the 0.5 km thick MTZ, the velocity  
183 of the MTZ is partially recovered between 10 and 80 km horizontal distance (Figure S11). In  
184 contrast, the velocity of the inserted MTZ between 10 and 80 km horizontal distance is almost

185 completely recovered when the MTZ is 1.0-3.5 km thick ([Figure S12-S17](#)). The recovery of  
186 the MTZ at 10-25 km horizontal distance is slightly worse than that to the further north, likely  
187 due to sparser instruments deployed in this region.

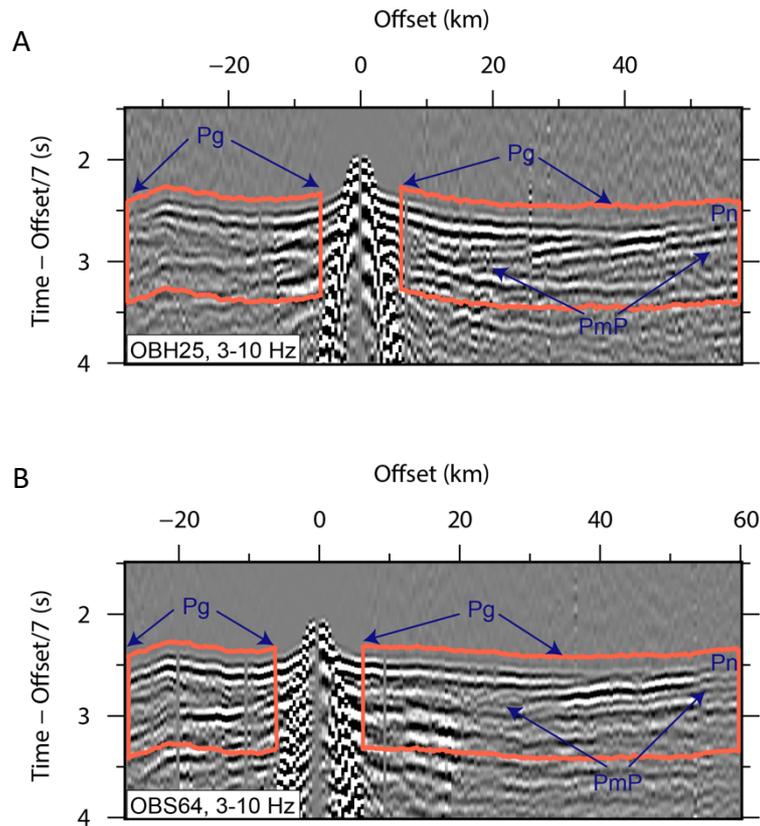
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**Figure S1. Comparisons of seismic data before (left column) and after (right column) predictive gapped deconvolution. (A) for OBH25 and (B) for OBS64. The travel time of seismic data is reduced using a reduction velocity of 7.0 km/s. The seismic bubble pulses are suppressed after the predictive gapped deconvolution, and the crustal refractions (Pg), the Moho reflections (PmP) and the mantle refractions (Pn) are clearer.**



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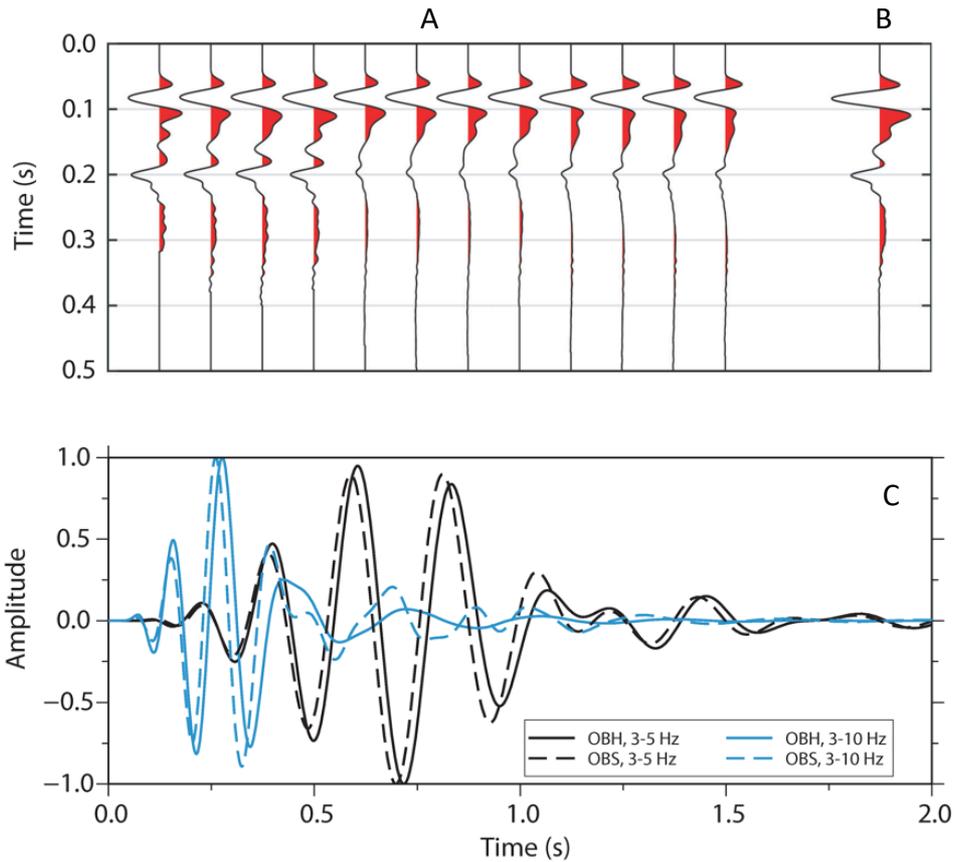
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201 **Figure S2. Time window overlapping on seismic plot.** (A) for OBH25 and (B) for OBS64.

202 The oranges boxes show the 1.0 s-wide time window used in the FWI of 3-10 Hz data. The

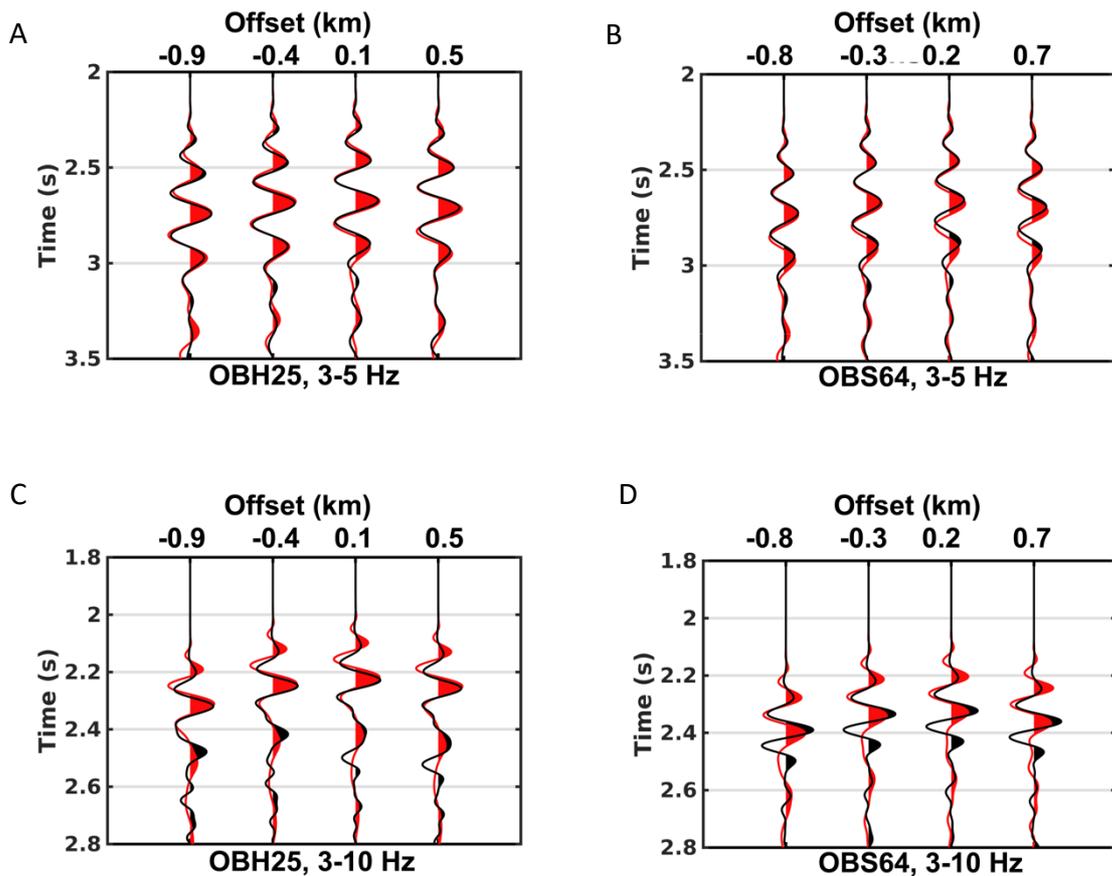
203 waveforms of the Pg, PmP and Pn arrivals are included in the time window. The travel time of

204 seismic data is reduced using a reduction velocity of 7.0 km/s.



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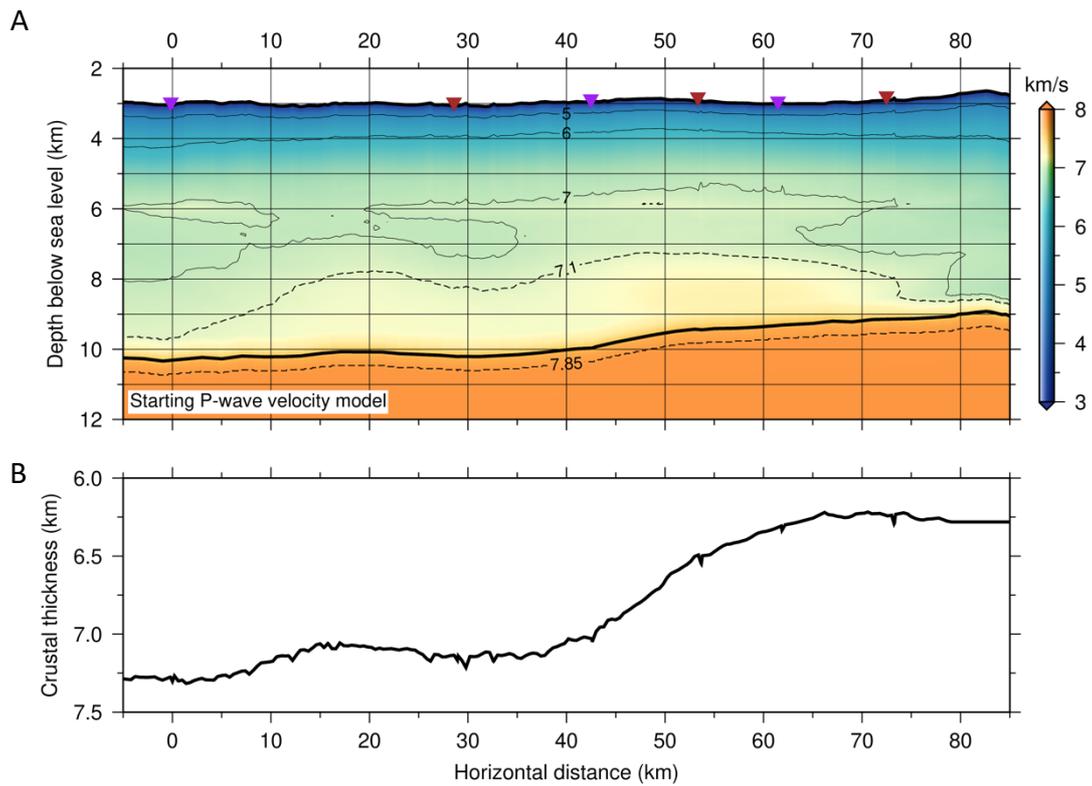
**Figure S3.** (A) Aligned seismic traces showing the near-offset direct water wave extracted from OBH gathers after filtering between 3-30 Hz. (B) Stack of traces in A. (C) The black and blue solid curves show the source wavelets for modelling of OBH data obtained by filtering the stacked signal in b to 3-5 Hz and 3-10 Hz, respectively. The black and blue dashed curves are the source wavelets for modelling of 3-5 and 3-10 Hz OBS data, respectively.



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229 **Figure S4. Comparisons of synthetic (in black) and observed (in red) near-offset water**  
 230 **wave for OBH25 (A,C) and OBS64 (B,D).** The synthetic data shown in A,B and C,D are  
 231 modelled using the tomographic model using the 3-5 and 3-10 Hz source wavelets, respectively.  
 232 The source wavelets are shown in Supplementary Fig. 4C. Correspondingly, the observed data  
 233 are filtered to 3-5 Hz in A,B and to 3-10 Hz in C,D, respectively. The good match between the  
 234 synthetic and observed data demonstrates the estimated source wavelets in Supplementary Fig.  
 235 4C are accurate enough for performing FWI.

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242 **Figure S5.** (A) Starting P-wave velocity model for FWI. The thick black curve is the

243 tomographic Moho from *Canales et al.* [2003]. The brown and purple triangles show the

244 locations of OBHs and OBSs, respectively. (B) Variation of crustal thickness obtained from

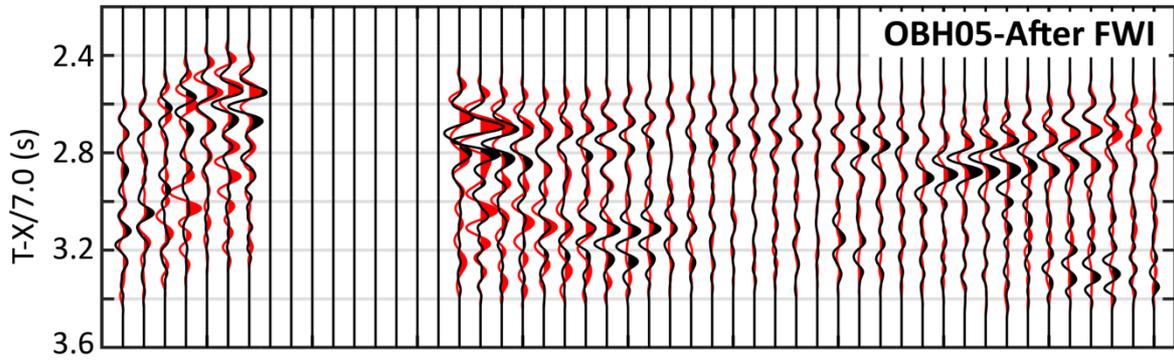
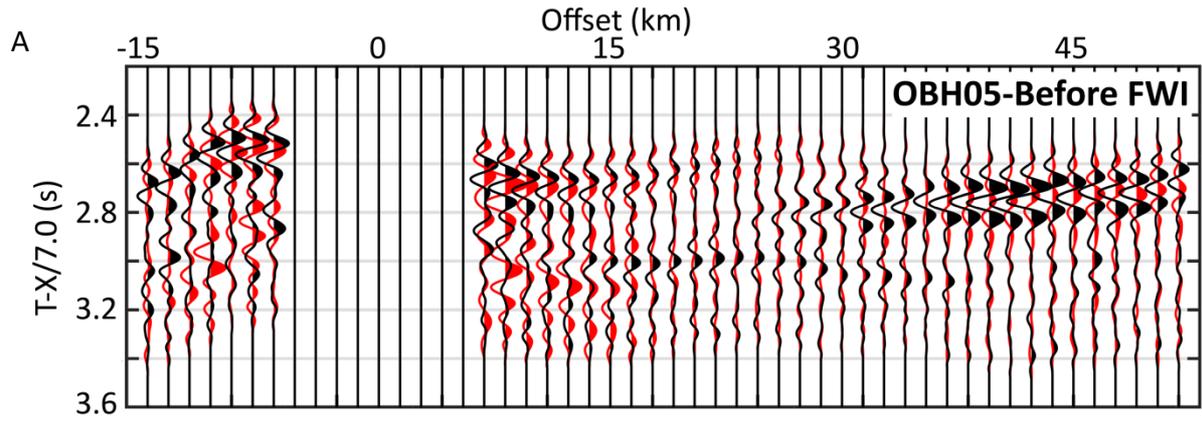
245 travel time tomography [*Canales et al.*, 2003].

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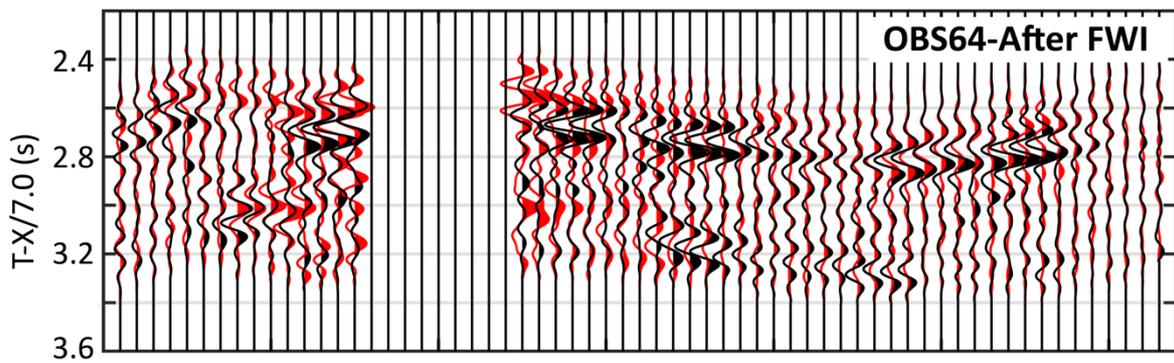
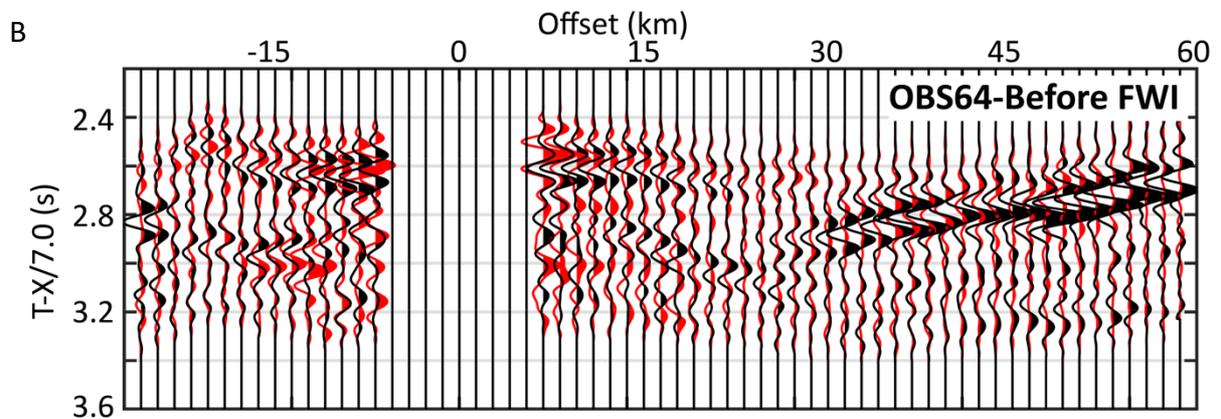
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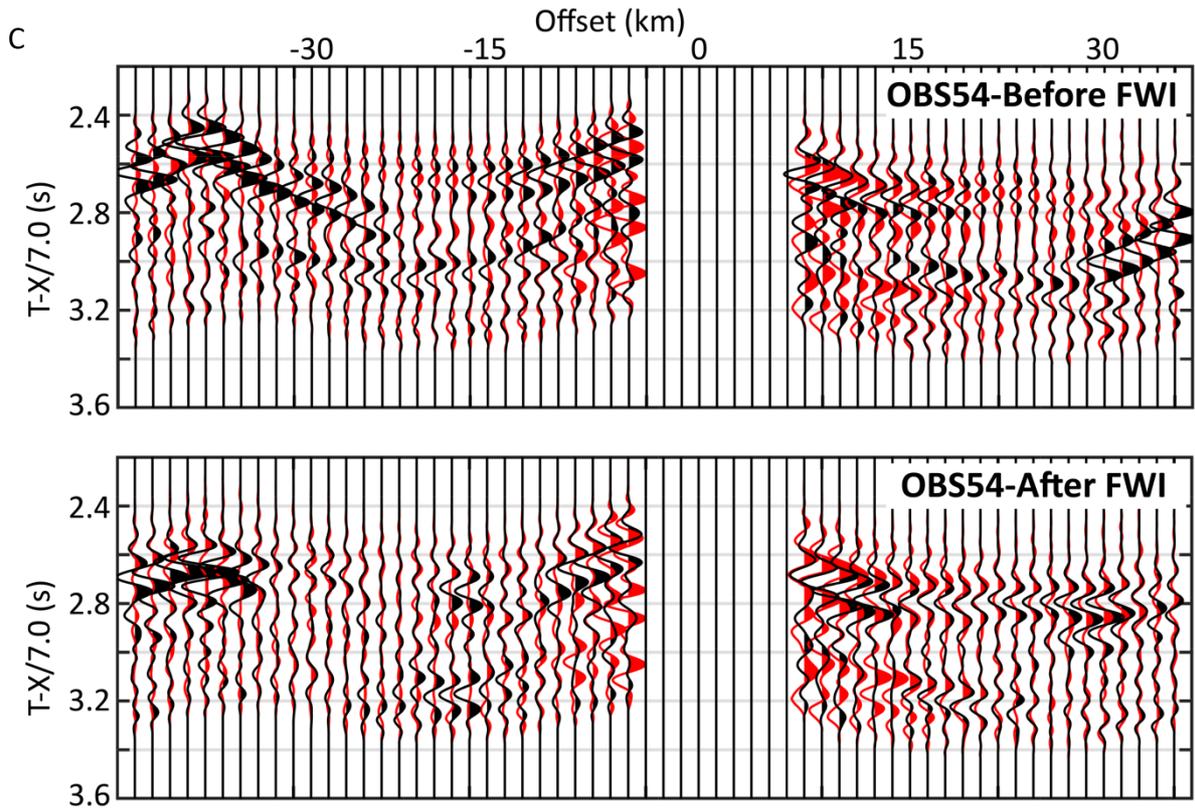
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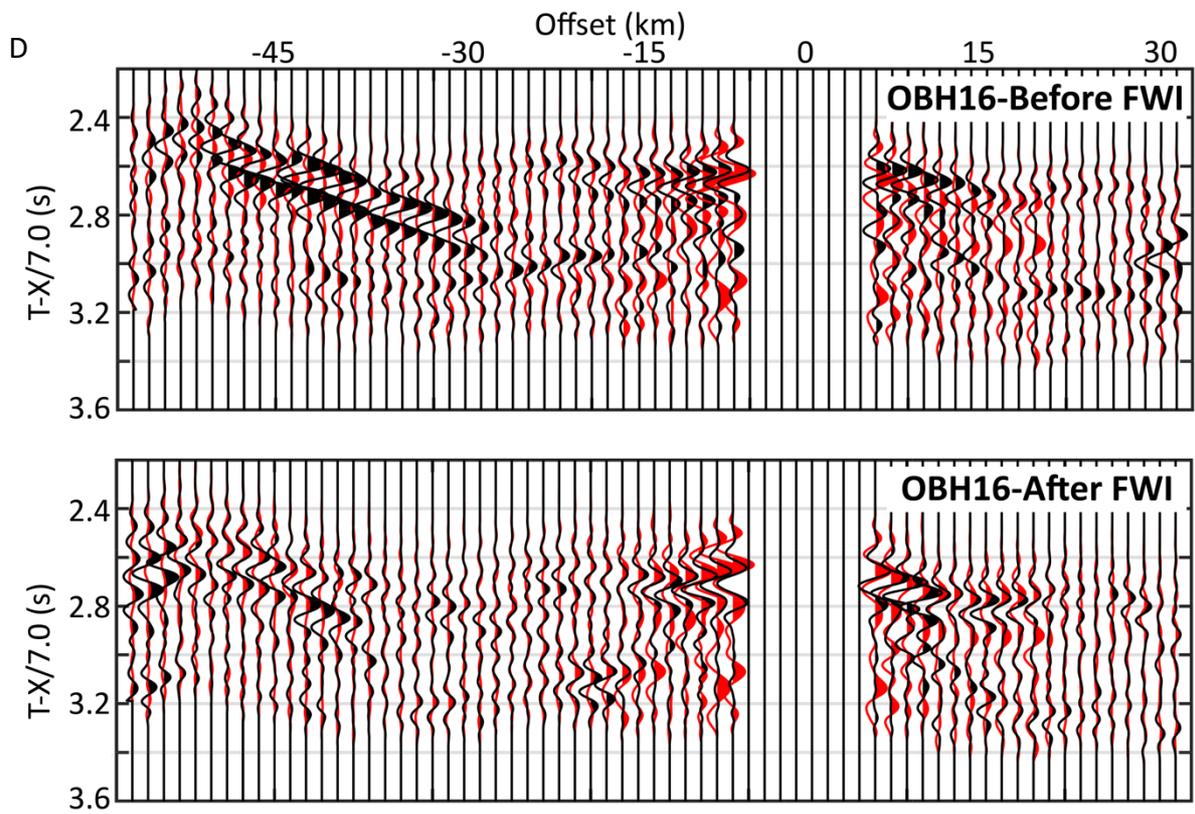
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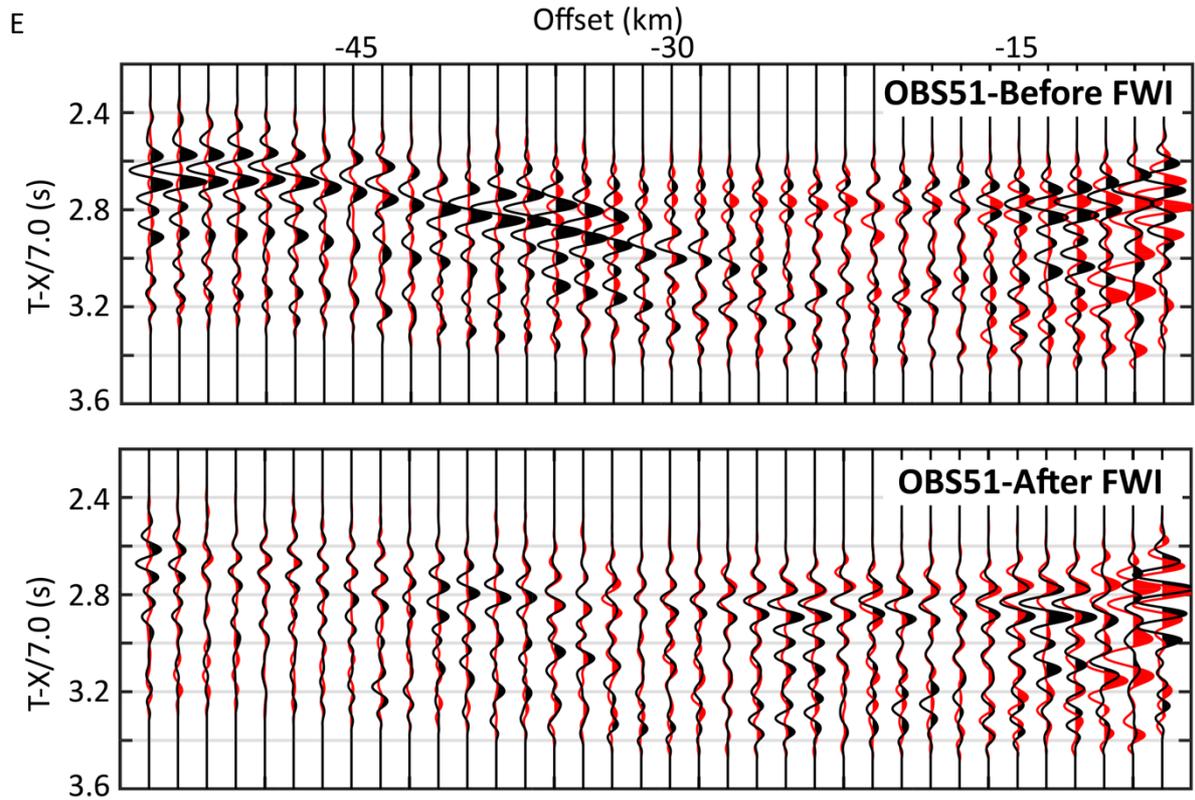
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262 **Figure S6. Comparisons of modelled (in black) and observed (in red) seismic data (3-10**

263 **Hz) before and after full waveform inversion (FWI).** Travel time (T) of seismic data is

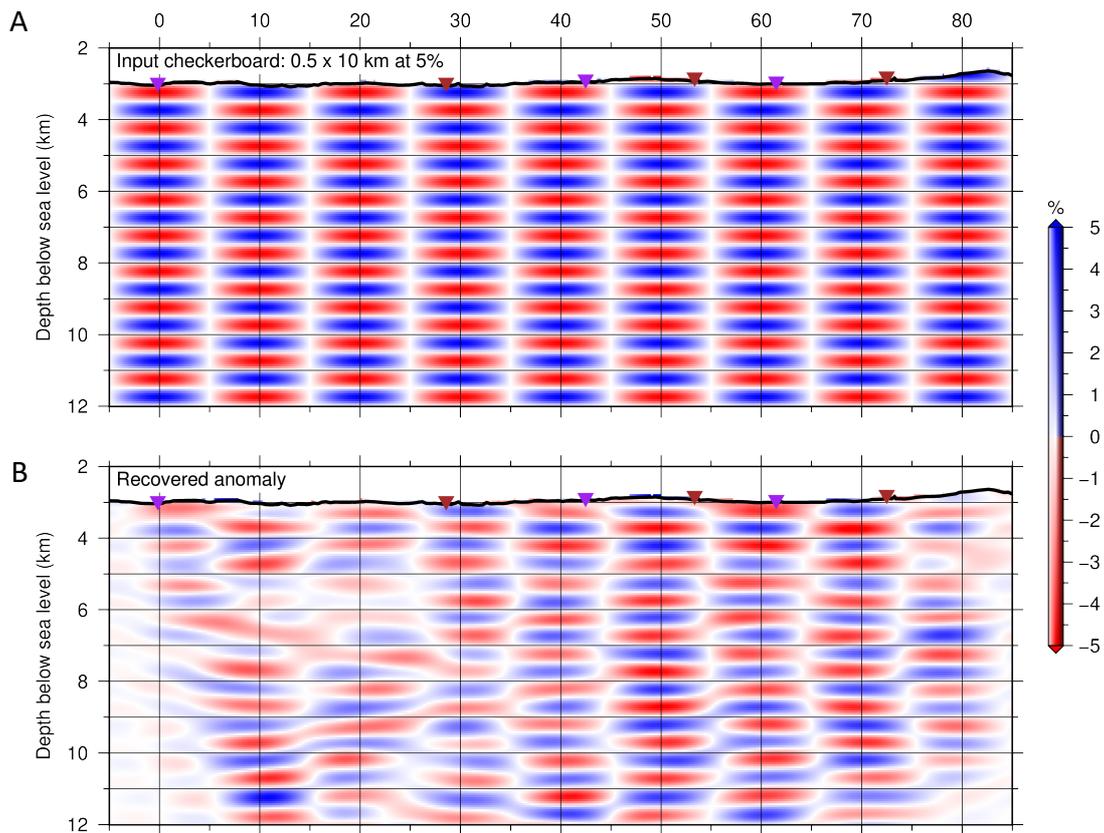
264 reduced using a reduction velocity of 7.0 km/s. For better visibility, a scalar weighting factor

265  $(1+0.1 \times X)$  was multiplied for each trace to enhance the amplitude at large offsets, where X is

266 offset. (A) OBH05; (B) OBS64; (C) OBS54; (D) OBH16; (E) OBS51.

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272 **Figure S7. Checkerboard test using  $0.5 \times 10$  km (vertical  $\times$  horizontal) checkerboard**

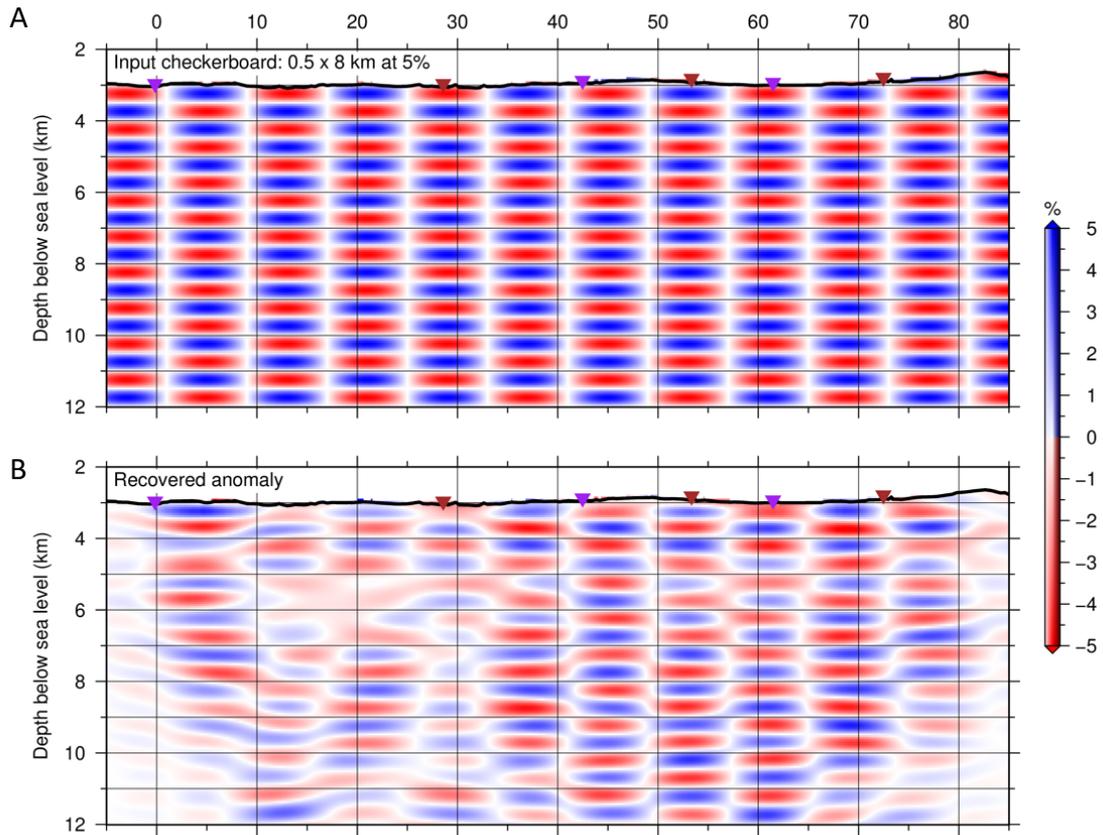
273 **pattern.** Panels (A) and (B) show the input checkerboard pattern and the recovered anomaly,

274 respectively. The maximum velocity perturbation is 5%. The brown and purple triangles show

275 the locations of OBHs and OBSs, respectively.

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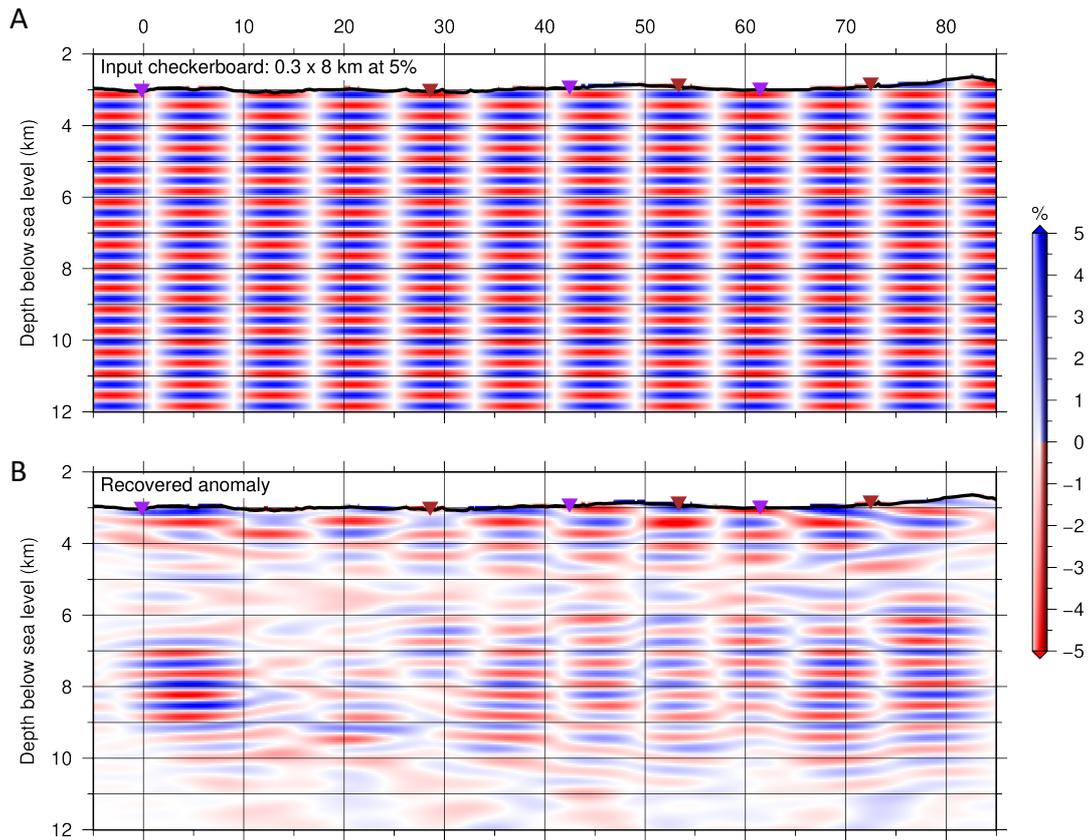


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280 **Figure S8. Checkerboard test using  $0.5 \times 8$  km (vertical  $\times$  horizontal) checkerboard**  
 281 **pattern.** Panels (A) and (B) show the input checkerboard pattern and the recovered anomaly,  
 282 respectively. The maximum velocity perturbation is 5%. The brown and purple triangles show  
 283 the locations of OBHs and OBSs, respectively.

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289 **Figure S9. Checkerboard test using  $0.3 \times 8$  km (vertical  $\times$  horizontal) checkerboard**

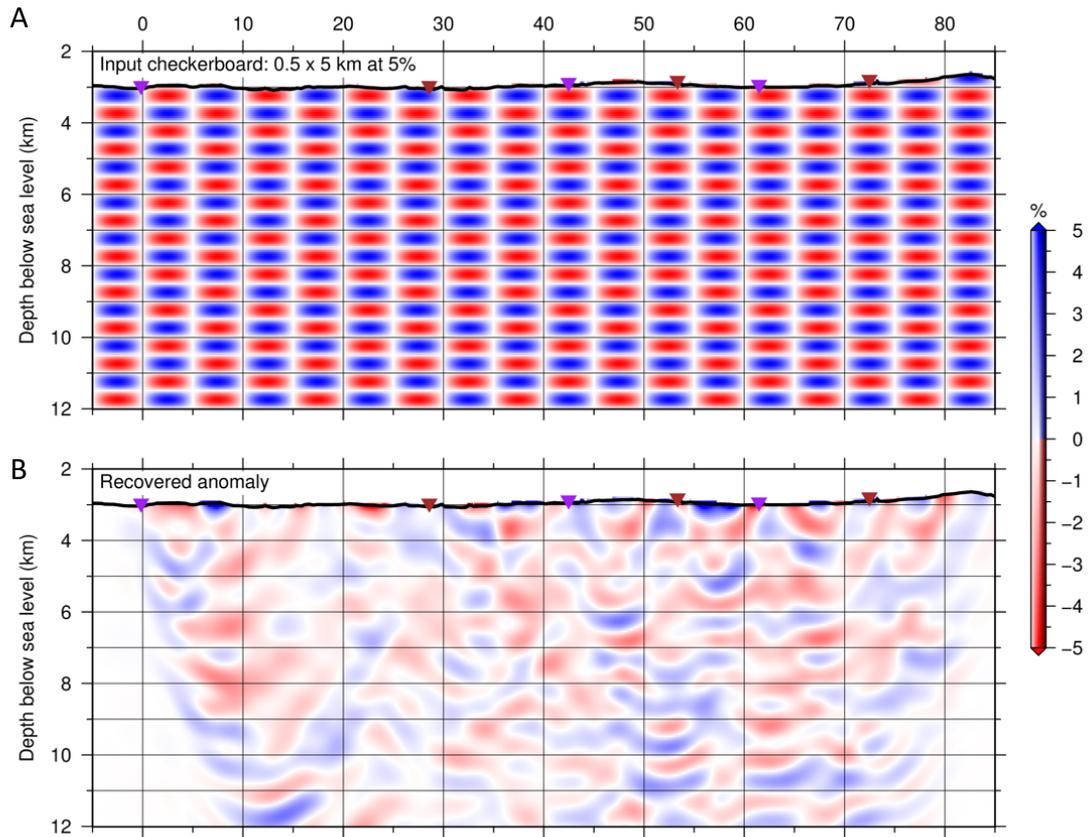
290 **pattern.** Panels (A) and (B) show the input checkerboard pattern and the recovered anomaly,

291 respectively. The maximum velocity perturbation is 5%. The brown and purple triangles show

292 the locations of OBHs and OBSs, respectively.

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297 **Figure S10. Checkerboard test using  $0.5 \times 5$  km (vertical  $\times$  horizontal) checkerboard**

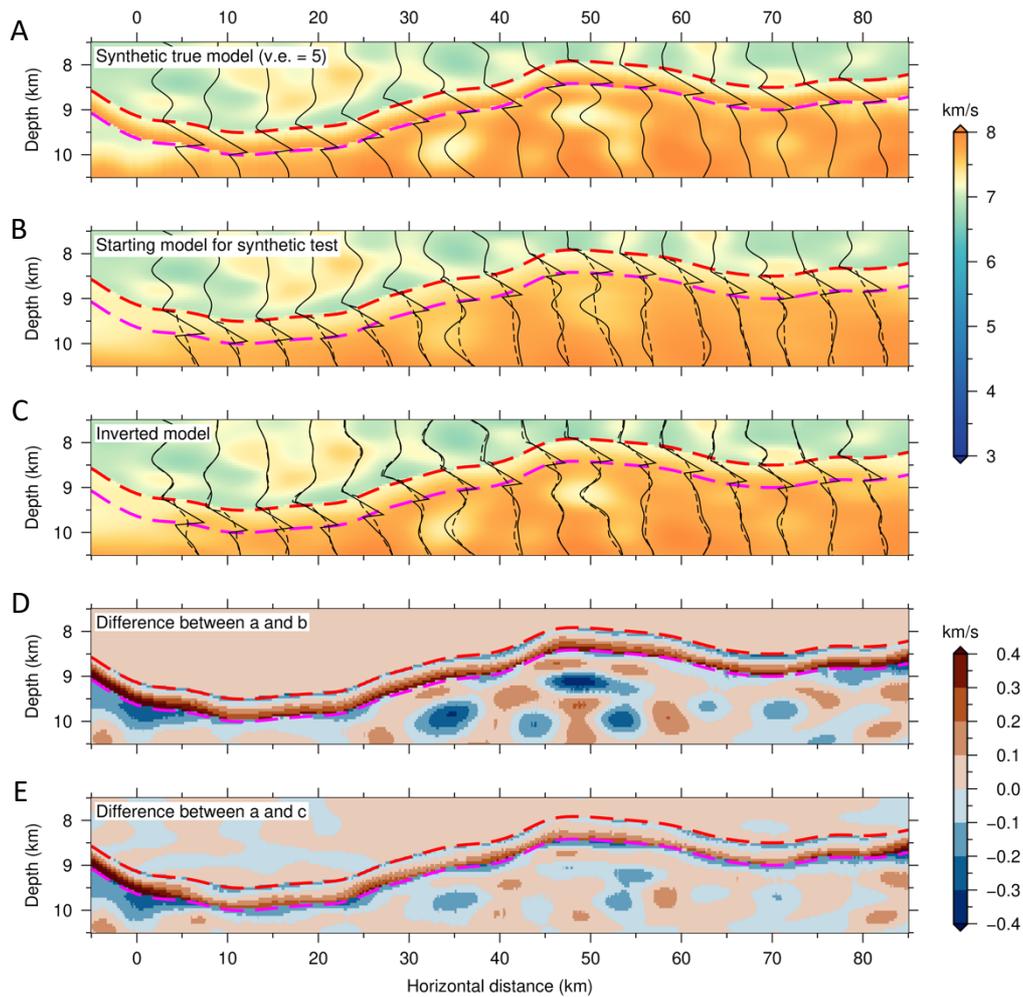
298 **pattern.** Panels (A) and (B) show the input checkerboard pattern and the recovered anomaly,

299 respectively. The maximum velocity perturbation is 5%. The brown and purple triangles show

300 the locations of OBHs and OBSs, respectively.

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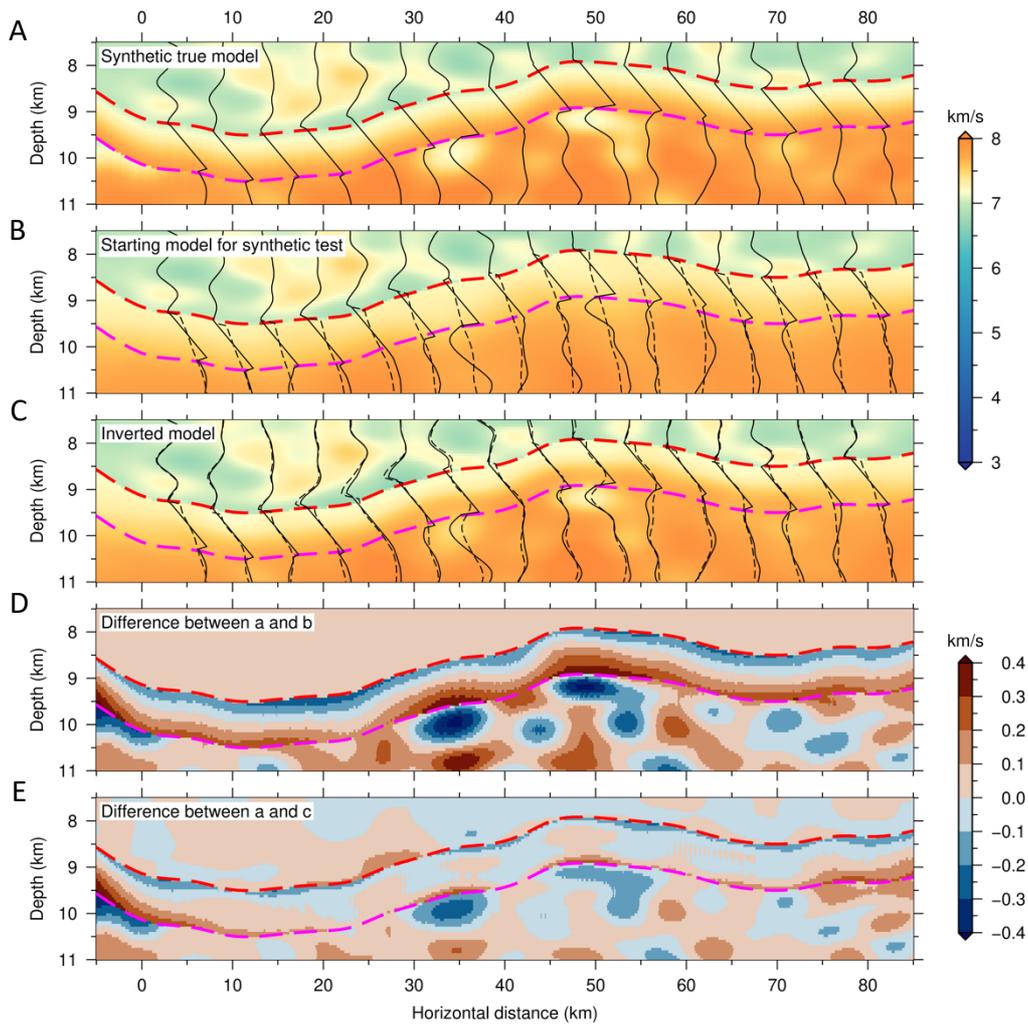


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305 **Figure S11. Synthetic test for the recovery of a 0.5 km thick Moho transition zone (MTZ).**

306 (A) True model for synthetic modelling which is modified by inserting a 0.5 km thick MTZ  
 307 into the final model of full waveform inversion (FWI) of field data. Only the portion of the  
 308 model around the MTZ is shown. The velocity of the inserted MTZ increases linearly with  
 309 depth from 7.0 to 7.85 km/s. The 1-D profiles show vertical velocity profiles every 5 km  
 310 between 5 and 80 km horizontal distance. (B) Starting model for synthetic test. The 1-D profiles  
 311 compare the synthetic true (solid curves) and starting (dashed curves) velocities every 5 km  
 312 between 5 and 80 km horizontal distance. (C) Inverted model from FWI. The 1-D profiles  
 313 compare the synthetic true (solid curves) and inverted (dashed curves) velocities every 5 km  
 314 between 5 and 80 km horizontal distance. (D) Difference between the synthetic true model (A)  
 315 and the starting model (B). (E) Difference between the synthetic true model (A) and the  
 316 inverted model (C). The red and magenta curves in A-E represent the top and bottom of the  
 317 inserted 0.5 km thick MTZ, respectively.

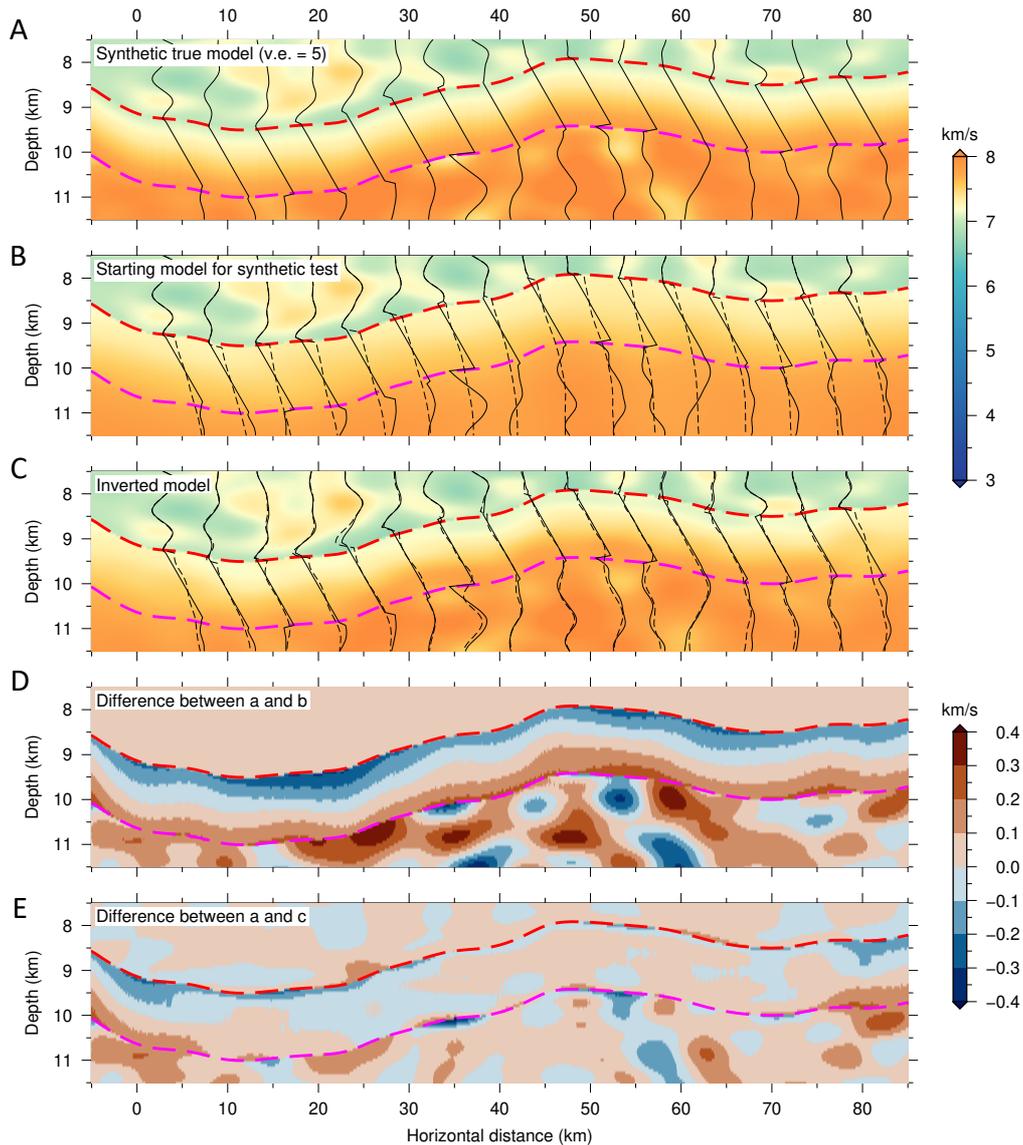
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319 **Figure S12. Synthetic test for the recovery of a 1.0 km thick Moho transition zone (MTZ).**

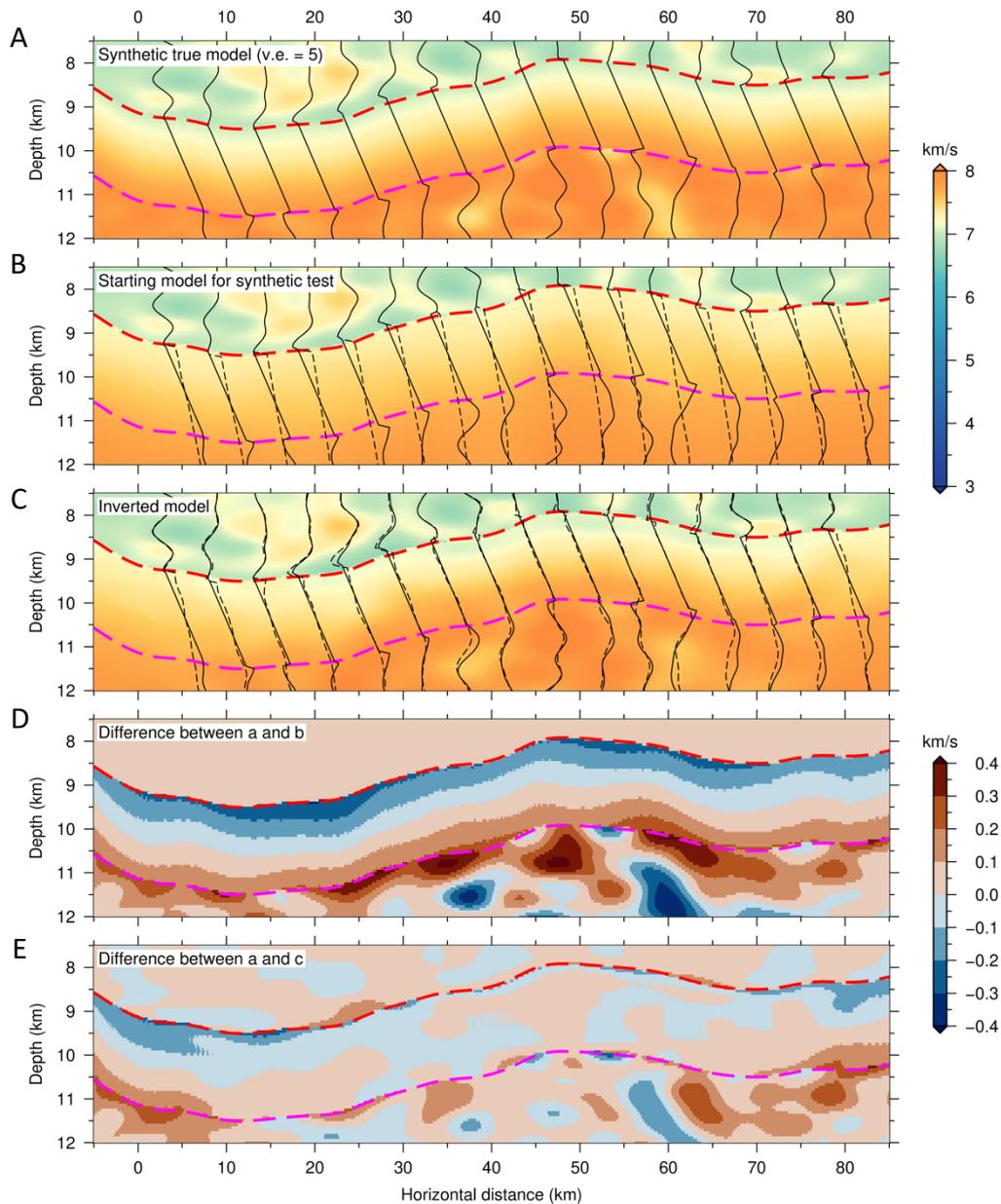
320 (A) True model for synthetic modelling which is modified by inserting a 1.0 km thick MTZ  
 321 into the final model of full waveform inversion (FWI) of field data. Only the portion of the  
 322 model around the MTZ is shown. The velocity of the inserted MTZ increases linearly with  
 323 depth from 7.0 to 7.85 km/s. The 1-D profiles show vertical velocity profiles every 5 km  
 324 between 5 and 80 km horizontal distance. (B) Starting model for synthetic test. The 1-D profiles  
 325 compare the synthetic true (solid curves) and starting (dashed curves) velocities every 5 km  
 326 between 5 and 80 km horizontal distance. (C) Inverted model from FWI. The 1-D profiles  
 327 compare the synthetic true (solid curves) and inverted (dashed curves) velocities every 5 km  
 328 between 5 and 80 km horizontal distance. (D) Difference between the synthetic true model (A)  
 329 and the starting model (B). (E) Difference between the synthetic true model (A) and the  
 330 inverted model (C). The red and magenta curves in A-E represent the top and bottom of the  
 331 inserted 1.0 km thick MTZ, respectively.  
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 335 **Figure S13. Synthetic test for the recovery of a 1.5 km thick Moho transition zone (MTZ).**  
 336 (A) True model for synthetic modelling which is modified by inserting a 1.5 km thick MTZ  
 337 into the final model of full waveform inversion (FWI) of field data. Only the portion of the  
 338 model around the MTZ is shown. The velocity of the inserted MTZ increases linearly with  
 339 depth from 7.0 to 7.85 km/s. The 1-D profiles show vertical velocity profiles every 5 km  
 340 between 5 and 80 km horizontal distance. (B) Starting model for synthetic test. The 1-D profiles  
 341 compare the synthetic true (solid curves) and starting (dashed curves) velocities every 5 km  
 342 between 5 and 80 km horizontal distance. (C) Inverted model from FWI. The 1-D profiles  
 343 compare the synthetic true (solid curves) and inverted (dashed curves) velocities every 5 km  
 344 between 5 and 80 km horizontal distance. (D) Difference between the synthetic true model (A)  
 345 and the starting model (B). e: Difference between the synthetic true model (A) and the inverted

346 model (C). The red and magenta curves in A-E represent the top and bottom of the inserted 1.5  
347 km thick MTZ, respectively.  
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351 **Figure S14. Synthetic test for the recovery of a 2.0 km thick Moho transition zone (MTZ).**

352 (A) True model for synthetic modelling which is modified by inserting a 2.0 km thick MTZ

353 into the final model of full waveform inversion (FWI) of field data. Only the portion of the

354 model around the MTZ is shown. The velocity of the inserted MTZ increases linearly with

355 depth from 7.0 to 7.85 km/s. The 1-D profiles show vertical velocity profiles every 5 km

356 between 5 and 80 km horizontal distance. (B) Starting model for synthetic test. The 1-D profiles

357 compare the synthetic true (solid curves) and starting (dashed curves) velocities every 5 km

358 between 5 and 80 km horizontal distance. (C) Inverted model from FWI. The 1-D profiles

359 compare the synthetic true (solid curves) and inverted (dashed curves) velocities every 5 km

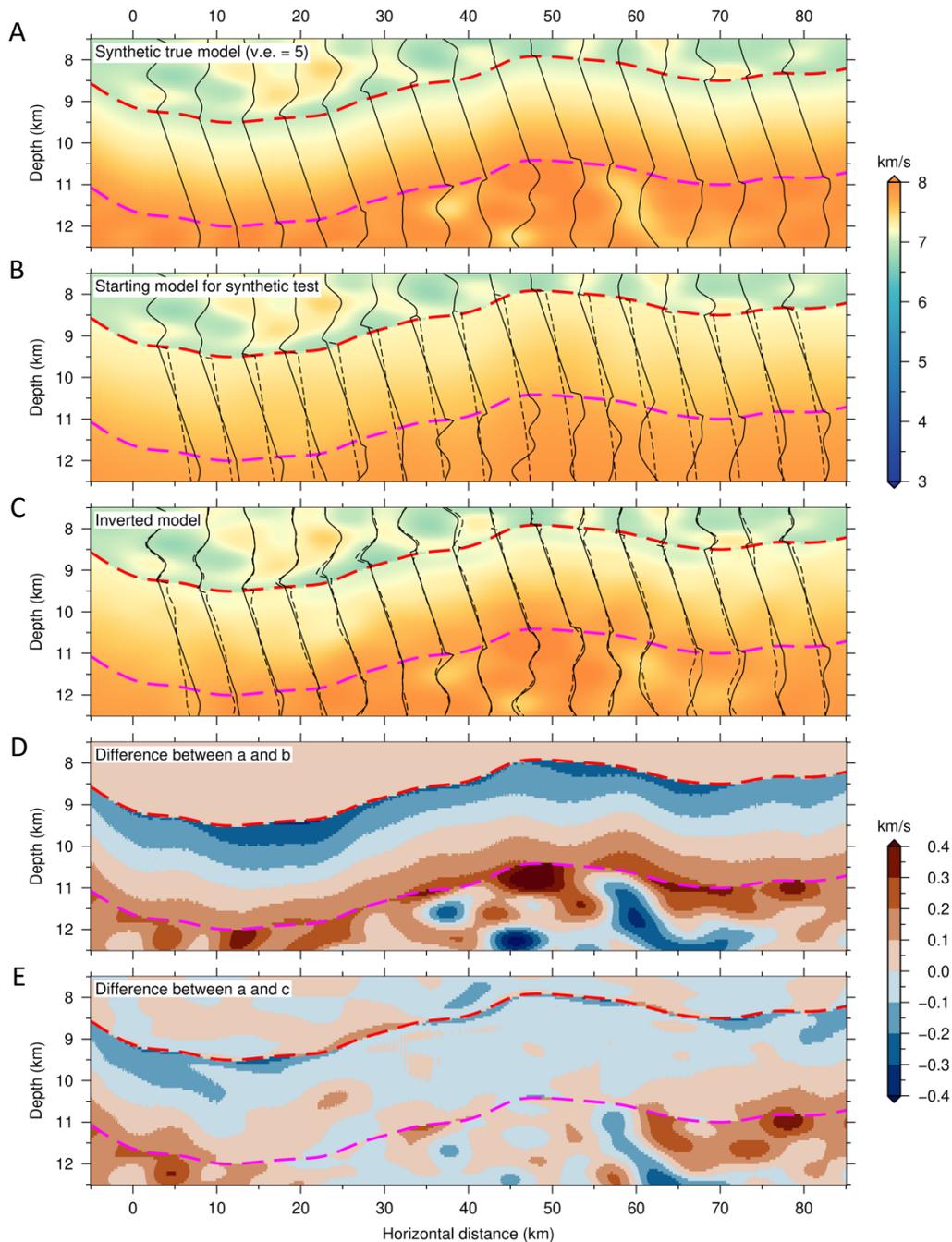
360 between 5 and 80 km horizontal distance. (D) Difference between the synthetic true model (A)

361 and the starting model (B). (E) Difference between the synthetic true model (A) and the  
362 inverted model (C). The red and magenta curves in A-E represent the top and bottom of the  
363 inserted 2.0 km thick MTZ, respectively.

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368 **Figure S15. Synthetic test for the recovery of a 2.5 km thick Moho transition zone (MTZ).**

369 (A) True model for synthetic modelling which is modified by inserting a 2.5 km thick MTZ  
 370 into the final model of full waveform inversion (FWI) of field data. Only the portion of the  
 371 model around the MTZ is shown. The velocity of the inserted MTZ increases linearly with  
 372 depth from 7.0 to 7.85 km/s. The 1-D profiles show vertical velocity profiles every 5 km  
 373 between 5 and 80 km horizontal distance. (B) Starting model for synthetic test. The 1-D profiles  
 374 compare the synthetic true (solid curves) and starting (dashed curves) velocities every 5 km  
 375 between 5 and 80 km horizontal distance. (C) Inverted model from FWI. The 1-D profiles

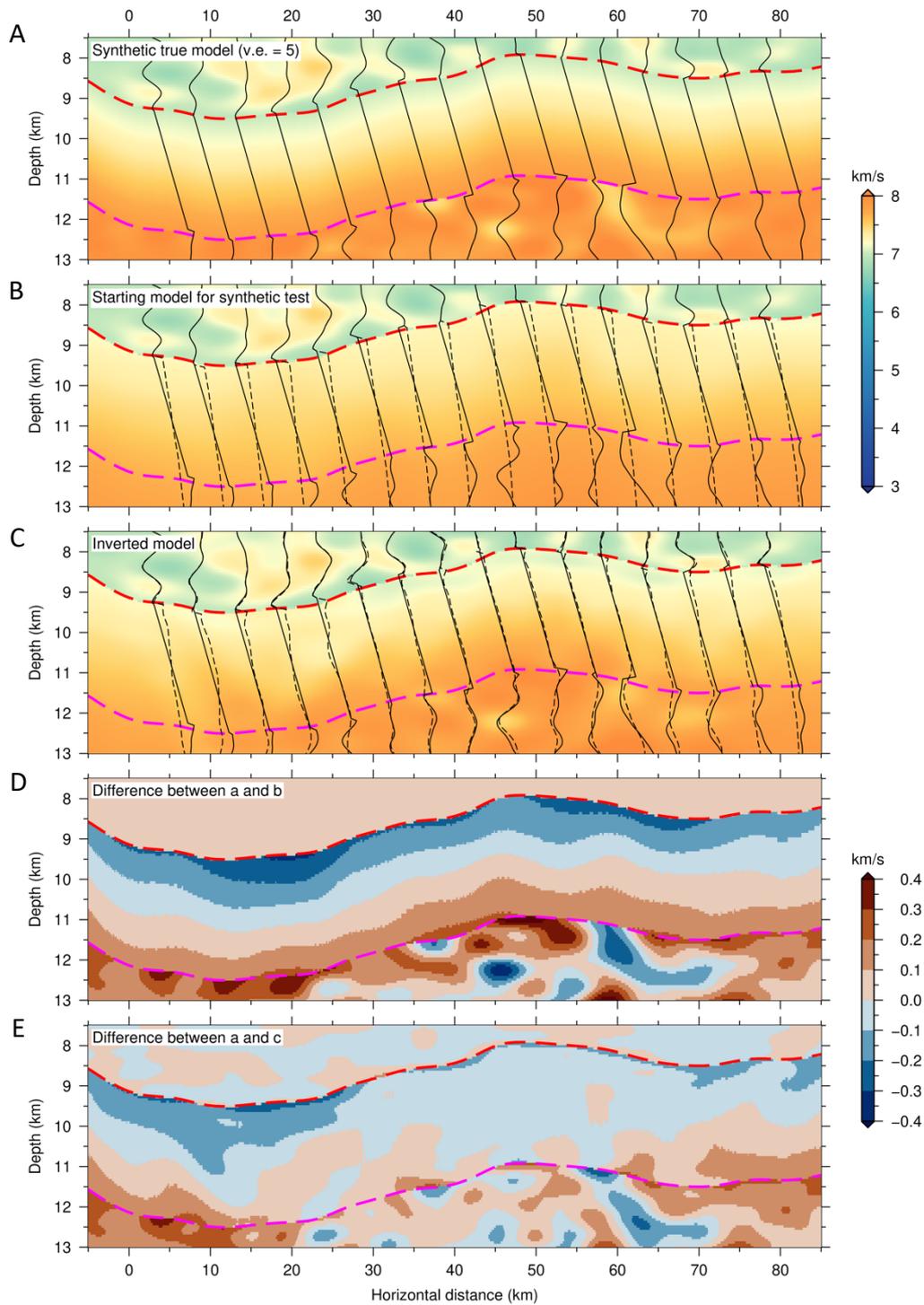
376 compare the synthetic true (solid curves) and inverted (dashed curves) velocities every 5 km  
377 between 5 and 80 km horizontal distance. (D) Difference between the synthetic true model (A)  
378 and the starting model (B). (E) Difference between the synthetic true model (A) and the  
379 inverted model (C). The red and magenta curves in A-E represent the top and bottom of the  
380 inserted 2.5 km thick MTZ, respectively.

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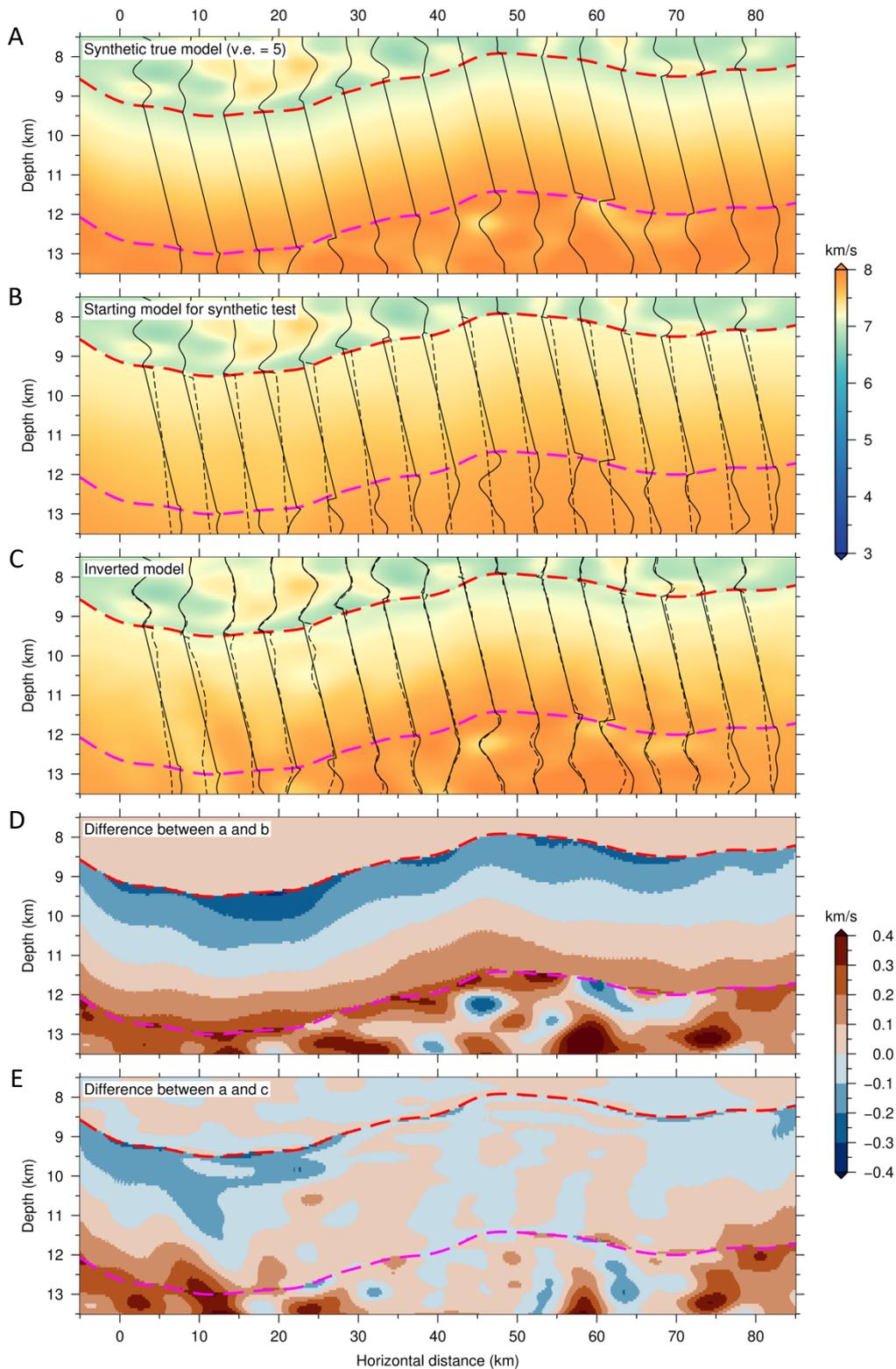
386 **Figure S16: Synthetic test for the recovery of a 3.0 km thick Moho transition zone (MTZ).**

387 (A) True model for synthetic modelling which is modified by inserting a 3.0 km thick MTZ  
 388 into the final model of full waveform inversion (FWI) of field data. Only the portion of the  
 389 model around the MTZ is shown. The velocity of the inserted MTZ increases linearly with  
 390 depth from 7.0 to 7.85 km/s. The 1-D profiles show vertical velocity profiles every 5 km  
 391 between 5 and 80 km horizontal distance. (B) Starting model for synthetic test. The 1-D profiles

392 compare the synthetic true (solid curves) and starting (dashed curves) velocities every 5 km  
393 between 5 and 80 km horizontal distance. (C) Inverted model from FWI. The 1-D profiles  
394 compare the synthetic true (solid curves) and inverted (dashed curves) velocities every 5 km  
395 between 5 and 80 km horizontal distance. (D) Difference between the synthetic true model (A)  
396 and the starting model (B). (E) Difference between the synthetic true model (A) and the  
397 inverted model (C). The red and magenta curves in A-E represent the top and bottom of the  
398 inserted 3.0 km thick MTZ, respectively.

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402 **Figure S17. Synthetic test for the recovery of a 3.5 km thick Moho transition zone (MTZ).**

403 (A) True model for synthetic modelling which is modified by inserting a 3.5 km thick MTZ  
 404 into the final model of full waveform inversion (FWI) of field data. Only the portion of the  
 405 model around the MTZ is shown. The velocity of the inserted MTZ increases linearly with

406 depth from 7.0 to 7.85 km/s. The 1-D profiles show vertical velocity profiles every 5 km  
407 between 5 and 80 km horizontal distance. (B) Starting model for synthetic test. The 1-D profiles  
408 compare the synthetic true (solid curves) and starting (dashed curves) velocities every 5 km  
409 between 5 and 80 km horizontal distance. (C) Inverted model from FWI. The 1-D profiles  
410 compare the synthetic true (solid curves) and inverted (dashed curves) velocities every 5 km  
411 between 5 and 80 km horizontal distance. (D) Difference between the synthetic true model (A)  
412 and the starting model (B). (E) Difference between the synthetic true model (A) and the  
413 inverted model (C). The red and magenta curves in a-e represent the top and bottom of the  
414 inserted 3.5 km thick MTZ, respectively.  
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