

Strong-motion Broadband Displacements from Collocated Ocean-bottom Pressure Gauges and Seismometers

Ayumu Mizutani^{1,2}, Diego Melgar², and Kiyoshi Yomogida¹

¹Department of Earth and Planetary Sciences, Faculty of Sciences, Hokkaido University,
Sapporo, Japan.

²Department of Earth Sciences, University of Oregon, Eugene, Oregon, U.S.A.

Corresponding author: A. Mizutani (mizutaniayumumail@gmail.com)

Key Points:

- Propose a new method to estimate the near-fault displacement waveform associated with an offshore earthquake.
- The method utilizes the collocated strong-motion seismometer and ocean-bottom pressure gauge.
- The obtained displacement waveforms improved the finite fault model.

Abstract

Dense and broad-coverage ocean-bottom observation networks enable us to obtain near-fault displacement records associated with an offshore earthquake. However, simple integration of ocean-bottom strong-motion acceleration records leads to physically unrealistic displacement records. Here we propose a new method using a Kalman filter to estimate coseismic displacement waveforms using the collocated ocean-bottom seismometers and pressure gauges. First, we evaluate our method using synthetic records and then apply it to an offshore Mw 6.0 event that generated a small tsunami. In both the synthetic and real cases, our method successfully estimates reasonable displacement waveforms. Additionally, we show that the computed waveforms improve the results of the finite fault modeling process. In other words, the proposed method will be useful for estimating the details of the rupture mechanism of offshore earthquakes as a complement to onshore observations.

Plain language summary

Ocean-bottom observations enable us to obtain near-fault displacement records associated with an offshore earthquake. However, simple integration of ocean-bottom acceleration records leads to physically unrealistic displacement records. Here we propose a new method to estimate offshore coseismic displacement waveforms. First, we evaluate our method using synthetic records and then apply it to an offshore earthquake that generated a small tsunami. In both cases, our method successfully estimates reasonable displacements. Additionally, we show that the computed waveforms improve the results of the earthquake source modeling process. In other words, the proposed method will be useful for estimating the details of the rupture mechanism of offshore earthquakes as a complement to onshore observations.

39

40 **1 Introduction**

41 Recently, real-time ocean-bottom seismometer networks have been deployed at active tectonic
42 margins for the dual purpose of both basic research and real-time monitoring (e.g., S-net and
43 DONET in Japan, NEPTUNE in Canada, and OOI in the US; Aoi et al., 2020; Barnes & Team,
44 2007; Trowbridge et al., 2019). These networks enable us to obtain near-fault records associated
45 with an offshore earthquake. When coseismic deformation is large enough, tsunamis occur due
46 to such events and can damage coastal areas. Coseismic displacement records at near-fault
47 stations are thus important because they have the potential to help in evaluating the earthquake
48 source and its resulting tsunami quickly – this can improve the performance of early warning
49 systems. In addition, they can be useful in estimating the details of the rupture mechanism of
50 offshore earthquakes as a complement to onshore observations.

51 The ocean-bottom record has complicated noise sources for seismic recordings of any
52 kind (e.g., Hilmo & Wilcock, 2020; Webb, 1998), more so than in the onshore environment.
53 Ideally, we seek to obtain a displacement waveform through the double integrations of an
54 acceleration or “strong motion” record. However, even in the simpler situation of onshore
55 recordings, simple integration leads to unphysical results due to “baseline offsets” which are
56 small shifts in the records (Iwan et al., 1985). Many schemes have been proposed to remove the
57 drifts in onshore strong-motion records (e.g., Boore, 2001; Wu & Wu, 2007; Wang et al., 2011).
58 These can often succeed in baseline correction, but their convergence is not always guaranteed,
59 and even more worrying, even if they do converge it is not always the case that they converge to
60 the right final static offset (Boore et al., 2002). Additionally, baseline correction is difficult to
61 apply in real-time settings. Alternatively, Bock et al. (2011) applied a Kalman filter approach to

the records of the collocated high-rate Global Navigation Satellite System (HR-GNSS) and seismometer sites, and succeeded in estimating the displacement waveform. Lately, many papers expanded on the use of the Kalman filter approach with onshore records (e.g., Geng et al., 2013; Melgar et al., 2013; Niu & Xu, 2014; Tu et al., 2014; Zang et al., 2019).

In this study, we propose a new method to estimate the coseismic displacement waveforms from offshore strong-motion records. We base the approach on the general philosophy of Bock et al. (2011): using the Kalman filter and combining the strong-motion record with the collocated ocean-bottom pressure gauge (OBPG) records. However, we have added challenges in the offshore environment, since a coseismic OBPG record contains not only seafloor displacements but also seafloor accelerations, ocean acoustic waves, and tsunamis (Saito, 2013), we cannot use the same Kalman filter formulation employed for onshore records. Section 2 explains the innovation of the Kalman filter approach proposed in this study. Then we apply it to synthetic data (Section 3) and real data for an M_w 6.0 earthquake recorded offshore in the Nankai, Japan region (Section 4). Finally, in Section 5, the estimated displacement waveforms are evaluated through the finite fault modeling.

Note that our method focuses only on vertical displacement because OBPGs are only sensitive to physical phenomena that can be leveraged to calculate vertical displacement. Unless otherwise described all the variables in the later sections are the vertical component.

2 Kalman filter implementation

The Kalman filter is an optimal estimation method based on the state-space representation of a dynamic system (Kalman, 1960). It consists of the combination of two different models: (1) the dynamic model which captures the physics of the processes involved and describes the time

84 evolution of the states, and (2) the observation model which establishes the relationship between
 85 measurements and the states. The models used in this study are expressed as:

$$\frac{d}{dt} \begin{bmatrix} d \\ v \\ \Omega \\ \eta \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} d \\ v \\ \Omega \\ \eta \end{bmatrix} + \begin{bmatrix} 0 & 0 \\ 1 & 0 \\ 0 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} a \\ \dot{h} \end{bmatrix} + \begin{bmatrix} 0 \\ \varepsilon^a \\ \varepsilon^\Omega \\ \varepsilon^{\dot{h}} \end{bmatrix}, \#(1)$$

$$\begin{bmatrix} h \\ \tilde{\eta} \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} d \\ v \\ \Omega \\ \eta \end{bmatrix} + \begin{bmatrix} \varepsilon^h \\ \varepsilon^{\tilde{\eta}} \end{bmatrix}, \#(2)$$

86 where d , v , η , and Ω are the displacement, velocity, tsunami height, and DC offset of
 87 acceleration. The variables of ε are the properties of noise in estimation. The DC offset is
 88 defined by the difference in baselines between the observed acceleration a^{obs} and the true
 89 acceleration a^{true} : $\Omega = a^{obs} + \varepsilon^a - a^{true}$ (Melgar et al., 2013). The vector $[d \ v \ \Omega \ \eta]^T$ is
 90 thus the state vector, the output or result of the Kalman filter estimator. In this study, we use the
 91 water-depth fluctuation $h = \eta - d$ and estimated tsunami height $\tilde{\eta}$ as the observation (Eq. 2).
 92 Note that \dot{h} in Eq. 1 is the time derivative of h ; h and $\tilde{\eta}$ are independently estimated by any
 93 methods other than the Kalman filter as we'll discuss soon. The noise properties of each variable,
 94 ε , are considered to be the Gaussian with zero mean and a standard deviation, i.e., $\varepsilon \sim N(0, \sigma)$,
 95 and independent of each other.

96 Because Eqs. 1 and 2 are for continuous time series, an extra step in the derivation is
 97 needed to discretize them (Lewis et al., 2008):

$$\begin{bmatrix} d_{t+1} \\ v_{t+1} \\ \Omega_{t+1} \\ \eta_{t+1} \end{bmatrix} = \begin{bmatrix} 1 & \Delta t & -\frac{\Delta t^2}{2} & 0 \\ 0 & 1 & -\Delta t & 0 \\ 0 & 0 & 1 & 0 \\ 0 & \Delta t & -\frac{\Delta t^2}{2} & 1 \end{bmatrix} \begin{bmatrix} d_t \\ v_t \\ \Omega_t \\ \eta_t \end{bmatrix} + \begin{bmatrix} \frac{\Delta t^2}{2} & 0 \\ \Delta t & 0 \\ 0 & 0 \\ \frac{\Delta t^2}{2} & \Delta t \end{bmatrix} \begin{bmatrix} a_t \\ \dot{h}_t \end{bmatrix} + q_t, \#(3)$$

$$\begin{bmatrix} h_t \\ \tilde{\eta}_t \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} d_t \\ v_t \\ \Omega_t \\ \eta_t \end{bmatrix} + r_t, \#(4)$$

98 where Δt is the time interval of the dynamic model (0.01 sec in our case, which is the sample
 99 rate of the ocean bottom accelerometer); q_t and r_t are the Gaussian noise such as $q_t \sim N(0, \mathbf{Q}_t)$
 100 and $r_t \sim N(0, \mathbf{R}_t)$, respectively. The covariance matrices, \mathbf{Q}_t and \mathbf{R}_t , are written as:

$$\mathbf{Q}_t = \begin{bmatrix} 0 & \sigma_t^a \Delta t^2 / 2 & 0 & 0 \\ \sigma_t^a \Delta t^2 / 2 & \sigma_t^a \Delta t & -\sigma_t^\Omega \Delta t^2 / 2 & \sigma_t^a \Delta t^2 / 2 \\ 0 & -\sigma_t^\Omega \Delta t^2 / 2 & \sigma_t^\Omega \Delta t & 0 \\ 0 & \sigma_t^a \Delta t^2 / 2 & 0 & \sigma_t^h \Delta t \end{bmatrix}, \#(5)$$

$$\mathbf{R}_t = \begin{bmatrix} \sigma_t^h / \Delta \tau & 0 \\ 0 & \sigma_t^{\tilde{\eta}} / \Delta \tau \end{bmatrix}, \#(6)$$

101 where $\Delta \tau$ is the time interval of the observation model (1 sec in our case, which is the sample
 102 rate of h and $\tilde{\eta}$). If Δt and $\Delta \tau$ are equal, Eqs. 3 and 4 are applied at every time step. If not, Eq. 4
 103 is only applied when a measurement, $[h_t \quad \tilde{\eta}_t]^T$, is available or every $\Delta \tau$. Note that as in Bock et
 104 al. (2011), we apply not only the Kalman filter but also the Kalman smoother which is applied
 105 backwards in time.

106 Before applying the Kalman filter, we need to obtain h and $\tilde{\eta}$ independently of the
 107 ongoing estimation. In this study, they are estimated by the method proposed by Mizutani et al.
 108 (2020), extracting the tsunami and displacement components from the coseismic OBPG records

on a real-time basis, and the tsunami source model estimated by the tsunami waveform inversion using time-derivative waveform (Kubota et al., 2018), respectively (Fig. 1). When calculating $\tilde{\eta}$, we assume that the tsunami occurs instantaneously, or, put another way that the rise time for the deformation of the seafloor and sea surface can be negligible. The tsunami inversion is regularized using spatial smoothing. The weight factor, or the strength of regularization, is determined based on the trade-off curve between the variance reduction (VR) and the model variance. The details of the inversion methods and the trade-off curves are given in Text S1 and Fig. S1.

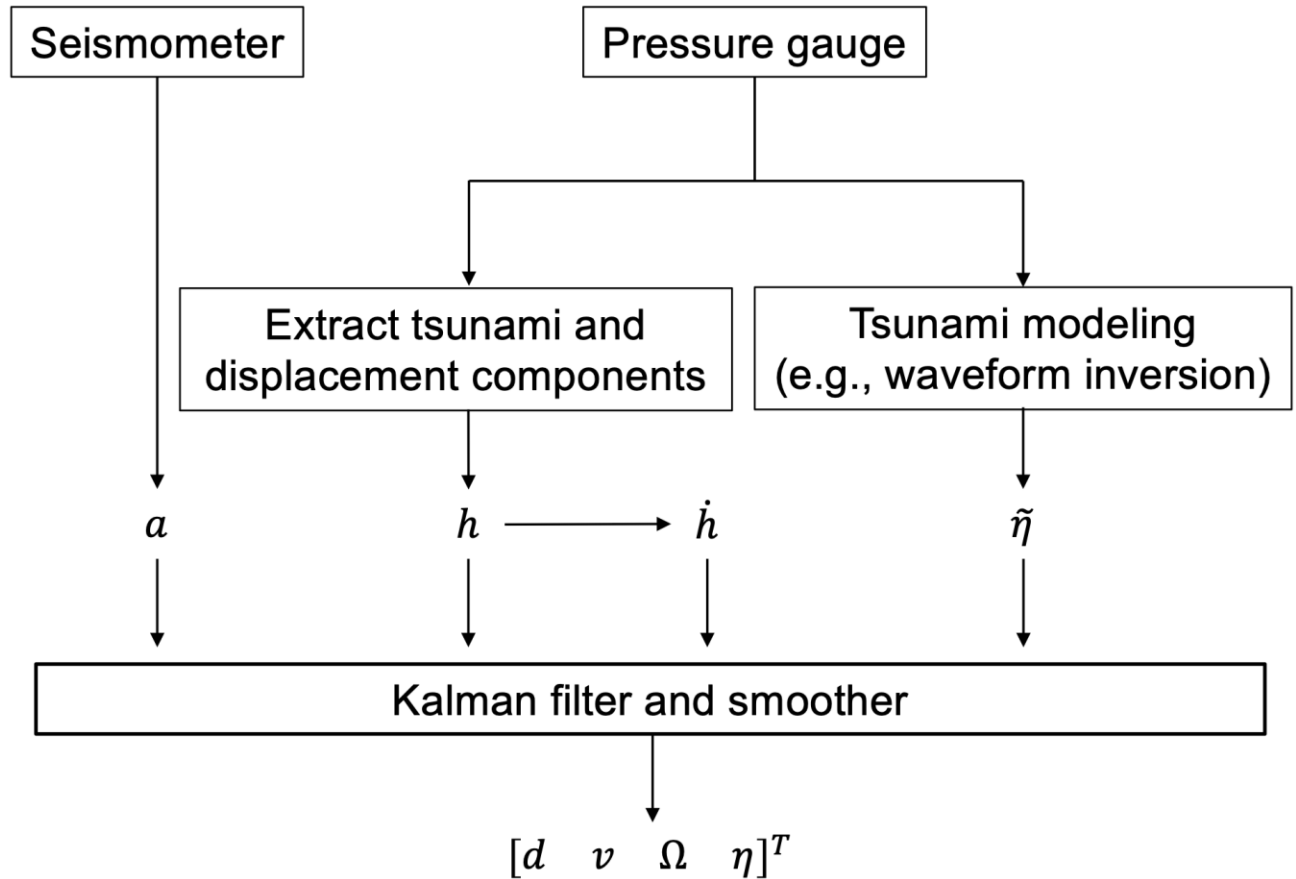


Figure 1. The schematic flow of the proposed method.

The covariance matrices, \mathbf{Q}_t and \mathbf{R}_t , or the variances of each variable, σ_t , are important tuning parameters of the Kalman filter. We propose them to be automatically calculated from the records by moving time windows. For the strong-motion records, σ_t^a is the moving variance of a and σ_t^Ω is the absolute value of the moving average of a ; the 5-sec window is used in both cases. Since h_t is estimated as the difference between two filtered records with a moving taper window (Mizutani et al., 2020, Section 5.1), σ_t^h is the sum of the variance of filtered records with the range of the taper's flat part (48 sec). Using σ_t^h , $\sigma_t^{\tilde{h}}$ is calculated as $(\sigma_t^h + \sigma_{t-1}^h)/\Delta t$. Finally, $\sigma_t^{\tilde{\eta}}$ is defined as the diagonal elements of $\mathbf{G}_{\text{forward}} \mathbf{G}_{\text{inv}}^{-1} [\text{cov } \mathbf{p}] [\mathbf{G}_{\text{forward}} \mathbf{G}_{\text{inv}}^{-1}]^T$, where \mathbf{G}_{inv} and $\mathbf{G}_{\text{forward}}$ are the kernel matrices used in the waveform inversion and forward calculation; $[\text{cov } \mathbf{p}]$ is the covariance matrix of the data used in the inversion, that is, the diagonal matrix whose elements are $(\sigma_t^p + \sigma_{t-1}^p)/\Delta \tau$, where σ_t^p is the moving variance of the data with a time window of 60 sec. Note that we do not use σ_t^p but $(\sigma_t^p + \sigma_{t-1}^p)/\Delta \tau$ because the waveform inversion of Kubota et al. (2018) uses time-derivative waveforms.

3 Synthetic test

In this section, we confirm the validity of our method and assumptions with synthetic records. Based on the methodology of Saito & Tsushima (2016), the records were obtained using opensource software for simulating seismic wave propagation, OpenSWPC (Maeda et al., 2017), and tsunami propagation, GeoClaw (Clawpack Development Team, 2022; Mandli et al., 2016). First, the seafloor acceleration, velocity, displacement, and stress change were calculated by OpenSWPC, and then, GeoClaw calculated the tsunami caused by the seafloor movement under the non-linear long-wave approximation.

A two-layer velocity model was used for the synthetic test: a water layer with P wave speed of 1.5 km and density of 1.0 kg/m^3 ; a homogeneous sea-bottom layer with P and S wave speed of 7 and 4 km/s and density of 2.7 kg/m^3 . The thickness of each layer was 4 and 400 km, and the horizontal dimensions of the model domain were $200 \times 200 \text{ km}$. The domain was divided into 0.5 and 1 km cells in the horizontal and vertical direction, respectively, and the time interval was 0.02 sec. The source was represented as a point source whose parameters were as follows: the moment magnitude was 7.0; the strike, dip, and rake were 0° , 45° , and 90° (a pure reverse fault); the depth was 10 km; and the rise time was 7.5 sec. We set this source at the center of the model domain (Fig. 2a).

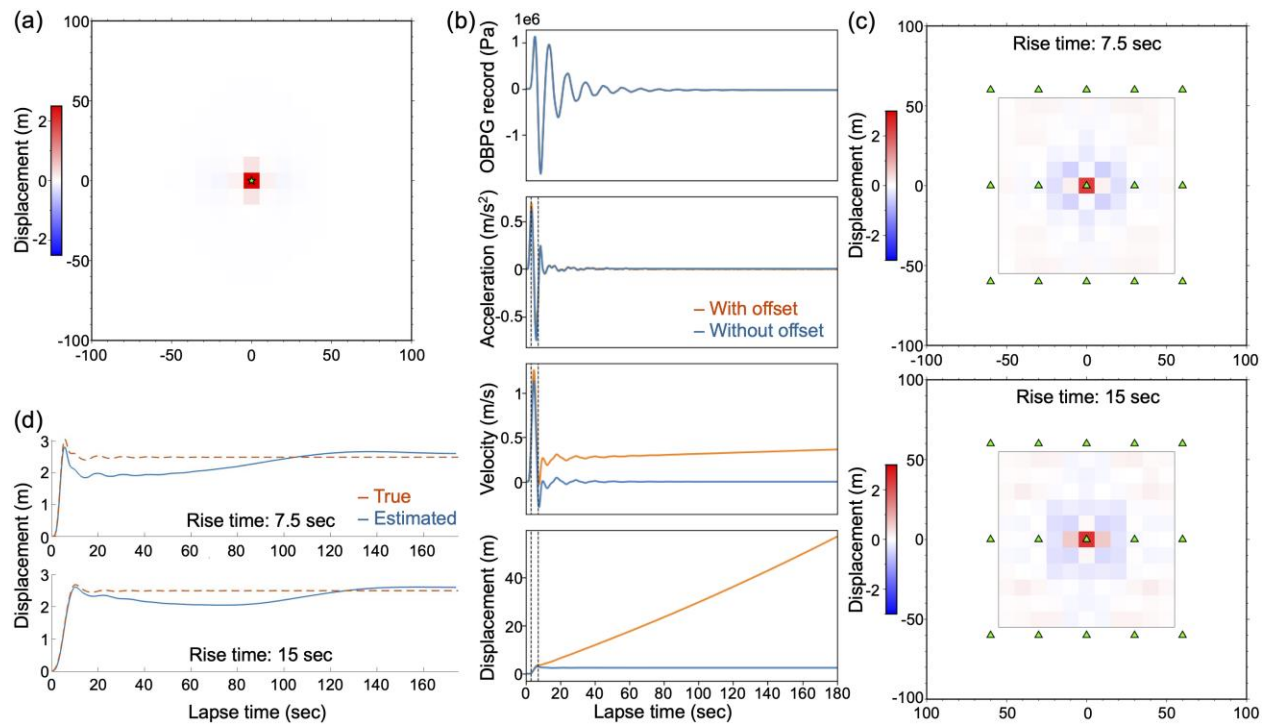


Figure 2. (a) Sea-bottom residual displacement in the synthetic test. The Green star represents the source location. (b) Synthetic records of ocean-bottom pressure, acceleration, velocity, and displacement at the station directly above the source. The blue lines are the records without noise. The orange line in the acceleration is with the baseline shift, and the lines in the

displacement and velocity are integrated from it. The black dashed line represents the strong motion duration causing the baseline shift. (c) The result of tsunami waveform inversion for $\tilde{\eta}$ with the rise time of 7.5 sec (top) and 15 sec (bottom). The green triangles and black rectangle represent the stations and target region. (d) Estimated result of the Kalman filter (blue) and true waveform (orange) with the rise time of 7.5 sec (top) and 15 sec (bottom).

Fig. 2b shows the synthetic records directly above the source. The OBPG record had a large amplitude due to the ocean acoustic waves and sea-bottom acceleration. In acceleration records, we added the baseline offset based on the model of Iwan et al. (1985), i.e., strong ground motion causes an offset, and after that, a minor offset still remains. We defined the strong motion for the baseline shift as over 0.5 m/s^2 , following Iwan et al. (1985). The offsets during and after the strong motion were 0.07 and 0.0007 m/s^2 , which were visually adjusted. Although the baseline shifts slightly affected the acceleration record, they significantly altered the velocity and displacement records. Note that we applied the Kalman filter to the record at this station; others were used only for the tsunami inversion.

The estimated tsunami source model for $\tilde{\eta}$ and the outcoming results of the Kalman filter are shown in Figs. 2c and 2d, respectively. Although the input acceleration was contaminated by the noise, the displacement waveform estimated by our method agreed with the “true” one.

When calculating $\tilde{\eta}$, our method assumes that a tsunami occurs instantaneously. To investigate the effect of the rise time, we conducted the same synthetic test with twice the rise time (15 sec). In this case, the threshold for the baseline shifts in the acceleration was defined as 0.1 m/s^2 . The resultant waveforms also agreed with the true one, particularly in the dynamic part of the displacement waveform (Fig. 2d). Since the seafloor and sea surface move simultaneously, it is difficult for the OBPG to observe any dynamic displacement components, that is, this

agreement comes from the acceleration record. In other words, the method proposed in this study successfully combined the information of the collocated OBPG and strong-motion seismometer.

4 Application to real data

We used the records of Dense Oceanfloor Network system for Earthquakes and Tsunamis (DONET; Aoi et al., 2020), which is deployed off the coast of Kii Peninsula, Japan (Fig 3a). Each station of this network consists of an ocean-bottom seismometer and an OBPG. On 1 April 2016, an Mw 6.0 event occurred inside this network (e.g., Araki et al., 2017; Takemura et al., 2018). The OBPGs clearly observed the pressure change originated from the tsunami, and strong-motion accelerometer records observed significant shaking (the peak ground acceleration (PGA) was over 0.5 m/s^2 at near-fault stations) and contained clear baseline shifts (Kubota et al., 2018; Mizutani et al., 2020; Wallace et al., 2016). For the preprocessing of the acceleration data, we removed the pre-earthquake offset in the records by taking the mean of the record 10 sec before the earthquake. For the OBPG data, the ocean tide component and the offset were removed by the theoretical tide model (Matsumoto et al., 2000) and the mean of the 30 min of the pre-event record.

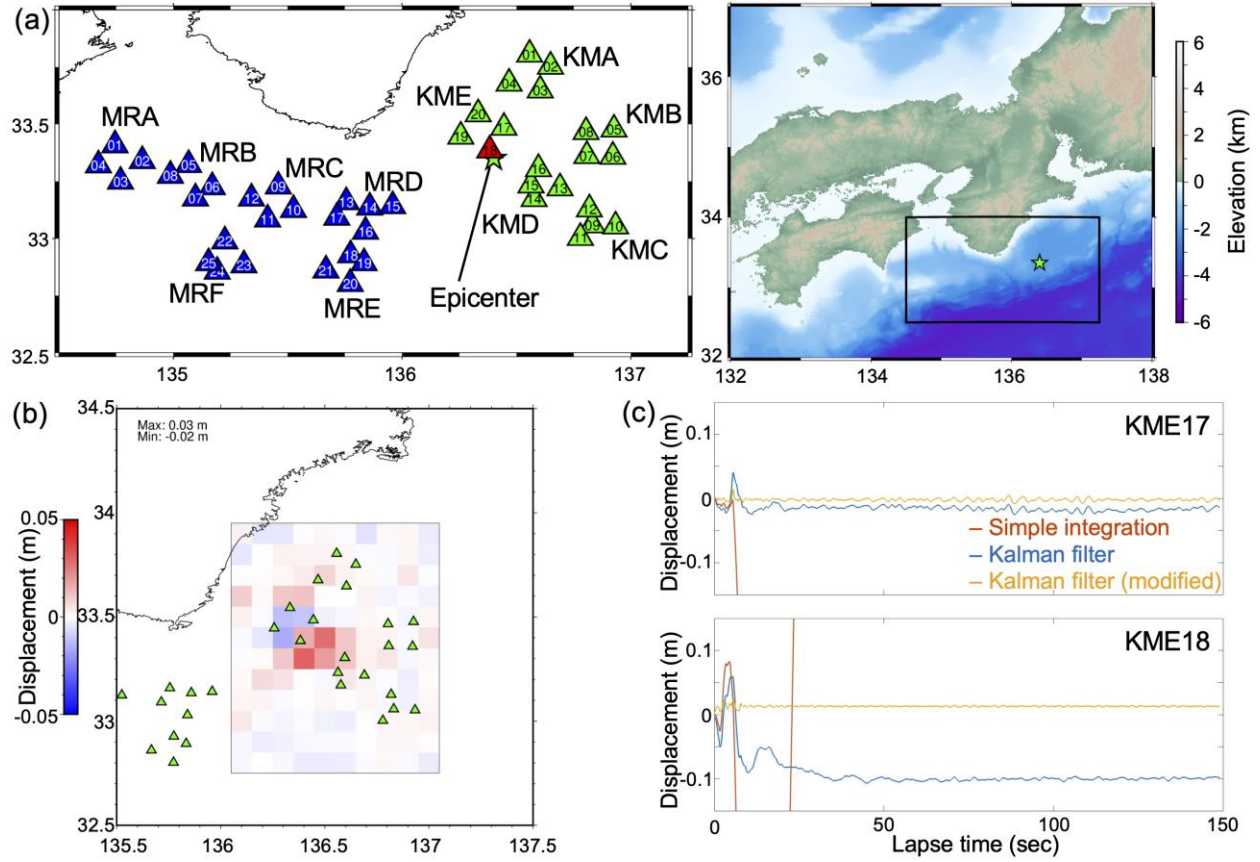


Figure 3. (a) *DONET* stations used in this study. The blue, red, and green triangles are the stations used only for the tsunami source inversion, only for the Kalman filter, and for both, respectively. Sets of three characters represent the subarrays of *DONET*. The green star is the epicenter estimated by Wallace *et al.* (2016). The black rectangle in the right panel represents the area of the left panel. (b) Tsunami source model for $\tilde{\eta}$ estimated by the tsunami waveform inversion. (c) Displacement waveforms at stations KME17 and KME18 estimated with h of Mizutani *et al.* (2020) (blue) and with h by the tsunami source inversion (yellow). The Orange lines are the displacements simply integrated from the acceleration record.

When conducting the tsunami source inversion for $\tilde{\eta}$, we calculated Green's functions with the GEBCO_2023 bathymetry (GEBCO, 2023) with grid intervals of 0.02° from unit sources which were set each 0.1° . Note that we excluded station KME18, the closest station to

the source, from the tsunami source inversion as well as Kubota et al. (2018), although applied the Kalman filter to its record. The resultant model is shown in Fig. 3b.

Fig.3c shows the displacement waveforms at stations KME18 and KME17, the second closest station to the source (the results of other stations are shown in Fig. S2). As with the synthetic test (Section 3), we succeeded in obtaining stable displacement waveforms. We, however, must pay attention to the residual displacement or DC component of the waveforms. For example, the waveform at KME18 indicated a subsidence of about 10 cm. The same signal was observed in the OBPG record, which previous studies considered as a false signal (Kubota et al., 2018; Wallace et al., 2016). Since our method estimates the displacement via h from OBPG records (Eq. 4), the residual displacement was affected by such an unphysical offset in OBPG records.

To avoid this problem, we changed a method to estimate h in Eq. 4. We now estimate h from the same model for $\tilde{\eta}$, and the variance σ_t^h was also calculated in the same scheme as $\tilde{\eta}$. Note that this alternative method was applied only to the stations whose OBPG records might have been contaminated by unphysical offsets: KMA03, KME17, and KME18, as suggested by Kubota et al. (2018). The displacement waveforms obtained from this method were also stable (yellow lines in Fig 3c) and the unphysical offsets could be removed. The residual displacements agreed with the one by the tsunami source inversion.

5 Finite fault estimation

To evaluate the utility of the displacement waveforms from Section 4, we next conducted a finite fault inversion and compared the resultant model with the one obtained from the inversion of tsunami records. We solved this linear inverse problem by the non-negative least square method

(Lawson & Hanson, 1995) with spatial smoothing (Text S1 and Fig. S1). Green's functions were calculated by OpenSWPC and GeoClaw. In the seismic waveform calculation, we used the 3-D velocity structure model by Koketsu et al. (2012) with grid intervals of 0.25 km and a time step of 0.01 sec. In the tsunami case, we used the same model in Section 4, i.e., GEBCO_2023 bathymetry with 0.02° interval.

The number of subfaults used was 81, each with a subfault size of 5×5 km and a rise time of 3 sec. Here, we estimated only the slip amount at each subfault; the other fault parameters were fixed as the values of Wallace et al. (2016): the strike, dip, and rake were 215°, 5°, and 95°; the center of the fault model was at 33.385°N and 136.434°E, and at 9.8 km below the seafloor. We set the rupture speed to 2.1 km/s, 80 % of the S wave speed in this region (Kamei et al., 2012; Wallace et al., 2016).

Fig. 4a shows the result of the inversion using the displacement waveforms. To investigate estimation errors, we conducted a bootstrap method with 200 samples where we randomly selected stations at each iteration (Chernick, 2007). The M_w calculated from this model was 5.9 and the VR was 68.7%. From the standard deviation of the bootstrap (right panel in Fig. 4a), a large slip patch beside the epicenter reflects the actual fault slip, while small one close to station KME20 is perhaps an estimation error. This result is consistent with the aftershock distribution detected by Japan Meteorological Agency (JMA) and the result from the tsunami-only inversion (the M_w and VR were 5.9 and 59%; Fig. 4b). We therefore conclude that the displacement waveforms estimated in Section 4 can be used reliably for studying offshore sources.

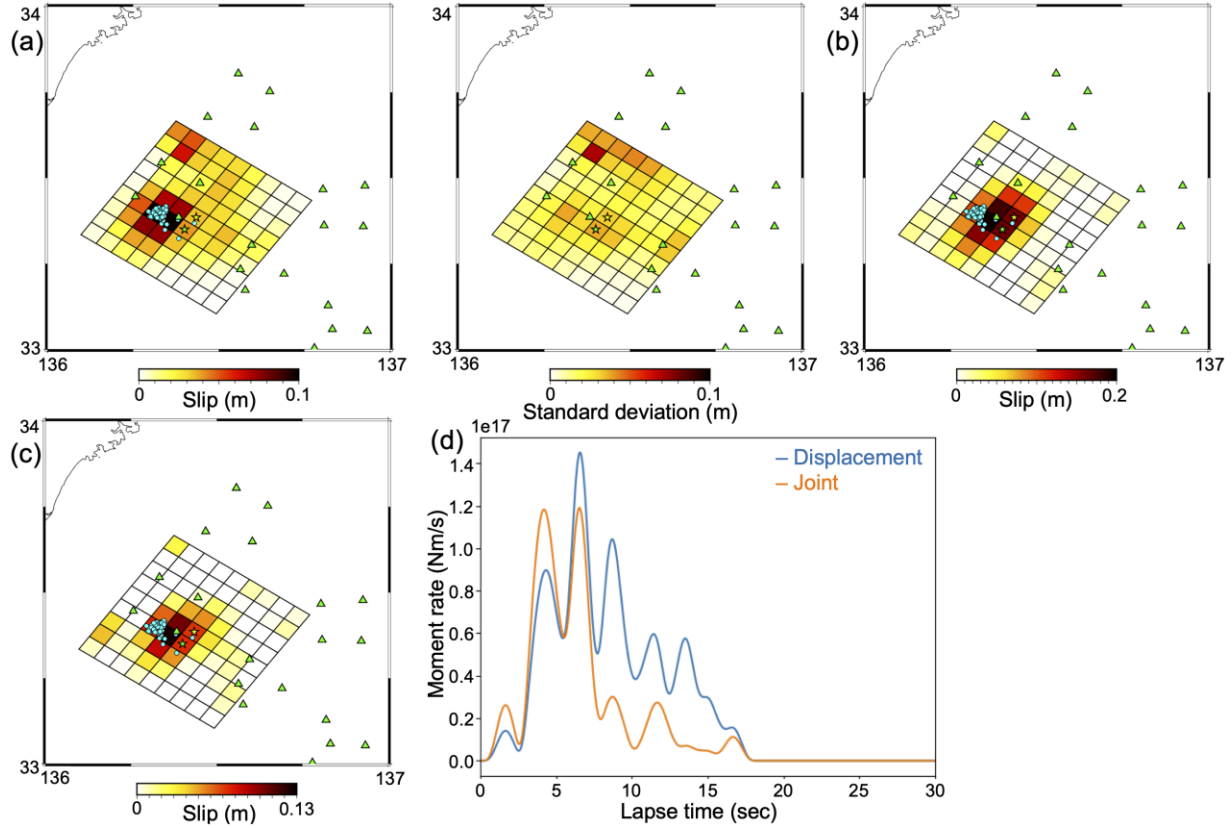


Figure 4. (a) Slips of the finite fault model (left) and their standard deviations (right) by the bootstrap method with displacement waveforms. The green triangles and blue circles represent DONET stations and aftershocks larger than magnitude 1 detected by JMA, which occurred within two days after the main shock. The green and yellow stars are the epicenter and the fault location estimated by Wallace *et al.* (2016). (b)(c) Same as (a) except that by the tsunami waveform inversion and by the joint inversion with the displacement and tsunami waveforms. (d) The blue and orange lines represent the source time functions calculated by the models of (a) and (c).

6 Discussion

To combine displacement and tsunami data, we conducted an additional joint inversion (Text S1 and Fig. S1). The obtained fault model is shown in Fig. 4c. The VR were 57.1% and 44.1% for

the displacement and tsunami; the estimated moment magnitude was 5.8. The model indicated that the slip propagated from the epicenter to the downdip direction. Compared to the model from the displacement waveforms only, the fault slip concentrated only around the epicenter. Its extent was also narrower than the model only using the tsunami.

Using the seismic records enables us to calculate the source time function (Fig. 4d). It indicated that a large rupture occurred at 3 sec after the origin time, and lasted 5 sec. The shorter duration compared to the one by the model using the displacement only reflects the slip distribution smaller than that.

Wallace et al. (2016) suggested that the aftershocks associated with this event occurred due to the afterslip immediately following the main shock because their fault model was separated from the aftershock cluster. Our model, on the other hand, agrees with the aftershock distribution and indicates that the aftershocks were caused directly by the main shock, that is, the afterslip may not be necessary for the aftershocks.

The aftershock distribution in Fig. 4 concentrates on the west of the slip. This is because JMA detected the earthquake location using only onshore stations. Araki et al. (2017) found slow-slip events after this earthquake located in the area between stations KME17 and KME18, different from the afterslip proposed by Wallace et al. (2016), which cover the north region of our fault model (Araki et al., 2017, Fig. 2b). In other words, our fault model can explain the aftershock distribution associated with this event sequence very well.

7 Conclusion

We proposed a new method to estimate the coseismic displacement waveform from collocated ocean-bottom strong-motion accelerometers and OBPBs. Through the synthetic test and the

application to real data, we confirmed the displacement waveforms estimated by this method to be reliable.

On the other hand, at some stations close to the epicenter, the resultant waveform had a relatively large offset due to unphysical DC components in OBPG records. At present, we cannot remove such an offset automatically because it is difficult to model this offset, that is, cannot be included simply in the Kalman filter estimation. Although several studies investigated unphysical drifts in OBPG records, they focused on the static records (Chadwick et al., 2006; Hino et al., 2022). Clarifying the characteristics of coseismic OBPG records will improve the Kalman filter approach to ocean-bottom records.

The finite fault model that jointly inverted from both the displacement and tsunami waveforms showed improvements compared to the models estimated independently. In other words, the displacement waveform by our method can help us to reveal the details of the rupture process of offshore earthquakes.

Acknowledgments

The records of DONET used in this study were provided by the NIED. This work benefitted from access to the University of Oregon high performance computing cluster, Talapas. This work was partially supported by JSPS KAKENHI grant number 22J10212.

Open Research

DONET records (NIED, 2019) can be downloaded from the NIED website
 (<https://www.hinet.bosai.go.jp/?LANG=en>, for strong-motion records;
<https://www.seafloor.bosai.go.jp>, for pressure records) with data request and permission. The
 codes of OpenSWPC and GeoClaw are freely available from GitHub
 (<https://tktmyd.github.io/OpenSWPC/> and <https://github.com/clawpack>).

References

- Aoi, S., Asano, Y., Kunugi, T., Kimura, T., Uehira, K., Takahashi, N., Ueda, H., Shiomi, K.,
 Matsumoto, T., & Fujiwara, H. (2020). MOWLAS: NIED observation network for earthquake,
 tsunami and volcano. *Earth, Planets and Space*, 72(1), 126. [https://doi.org/10.1186/s40623-020-](https://doi.org/10.1186/s40623-020-01250-x)
 01250-x
- Araki, E., Saffer, D. M., Kopf, A. J., Wallace, L. M., Kimura, T., Machida, Y., Ide, S., Davis, E.,
 & IODP EXPEDITION 365 SHIPBOARD SCIENTISTS. (2017). Recurring and triggered slow-
 slip events near the trench at the Nankai Trough subduction megathrust. *Science*, 356(6343),
 1157–1160. <https://doi.org/10.1126/science.aan3120>
- Barnes, C. R., & Team, N. C. (2007). Building the World’s First Regional Cabled Ocean
 Observatory (NEPTUNE): Realities, Challenges and Opportunities. *OCEANS 2007*, 1–8.
<https://doi.org/10.1109/OCEANS.2007.4449319>
- Bock, Y., Melgar, D., & Crowell, B. W. (2011). Real-Time Strong-Motion Broadband
 Displacements from Collocated GPS and Accelerometers. *Bulletin of the Seismological Society*
of America, 101(6), 2904–2925. <https://doi.org/10.1785/0120110007>

Boore, D. M. (2001). Effect of baseline corrections on displacements and response spectra for several recordings of the 1999 Chi-Chi, Taiwan, earthquake. *Bulletin of the Seismological Society of America*, 91(5), 1199–1211.

Boore, D. M., Stephens, C. D., & Joyner, W. B. (2002). Comments on Baseline Correction of Digital Strong-Motion Data: Examples from the 1999 Hector Mine, California, Earthquake. *Bulletin of the Seismological Society of America*, 92(4), 1543–1560.

<https://doi.org/10.1785/0120000926>

Chadwick, W., Noonan, S., Zumberge, M., Embley, R., & Fox, C. (2006). Vertical deformation monitoring at Axial Seamount since its 1998 eruption using deep-sea pressure sensors. *Journal of Volcanology and Geothermal Research*, 150, 313–327.

Chernick, M. (2007). *Bootstrap Methods: A Guide for Practitioners and Researchers*. Wiley.

Clawpack Development Team. (2022). *Clawpack software*.

<https://doi.org/10.5281/zenodo.7026045>

GEBCO. (2023). *The General Bathymetric Chart of the Oceans* [dataset].

<https://doi.org/10.5285/f98b053b-0cbc-6c23-e053-6c86abc0af7b>

Geng, J., Bock, Y., Melgar, D., Crowell, B. W., & Haase, J. S. (2013). A new seismogeodetic approach applied to GPS and accelerometer observations of the 2012 Brawley seismic swarm: Implications for earthquake early warning. *Geochemistry, Geophysics, Geosystems*, 14(7), 2124–2142. <https://doi.org/10.1002/ggge.20144>

- 342 Hilmo, R., & Wilcock, W. S. D. (2020). Physical Sources of High-Frequency Seismic Noise on
 343 Cascadia Initiative Ocean Bottom Seismometers. *Geochemistry, Geophysics, Geosystems*,
 344 *21*(10), e2020GC009085. <https://doi.org/10.1029/2020GC009085>
- 345 Hino, R., Kubota, T., Chikasada, N. Y., Ohta, Y., & Otsuka, H. (2022). Assessment of S-net
 346 seafloor pressure data quality in view of seafloor geodesy. *Progress in Earth and Planetary*
 347 *Science*, *9*(1), 73. <https://doi.org/10.1186/s40645-022-00526-y>
- 348 Iwan, W. D., Moser, M. A., & Peng, C.-Y. (1985). Some observations on strong-motion
 349 earthquake measurement using a digital accelerograph. *Bulletin of the Seismological Society of*
 350 *America*, *75*(5), 1225–1246.
- 351 Kalman, R. E. (1960). A New Approach to Linear Filtering and Prediction Problems. *Journal of*
 352 *Basic Engineering*, *82*(1), 35–45. <https://doi.org/10.1115/1.3662552>
- 353 Kamei, R., Pratt, R. G., & Tsuji, T. (2012). Waveform tomography imaging of a megasplay fault
 354 system in the seismogenic Nankai subduction zone. *Earth and Planetary Science Letters*, *317*–
 355 *318*, 343–353. <https://doi.org/10.1016/j.epsl.2011.10.042>
- 356 Koketsu, K., Miyake, H., & Suzuki, H. (2012). *Japan Integrated Velocity Structure Model*
 357 *Version 1*. The 15th World Conference on Earthquake Engineering, Lisboa.
 358 https://www.iitk.ac.in/nicee/wcee/article/WCEE2012_1773.pdf
- 359 Kubota, T., Suzuki, W., Nakamura, T., Chikasada, N. Y., Aoi, S., Takahashi, N., & Hino, R.
 360 (2018). Tsunami source inversion using time-derivative waveform of offshore pressure records
 361 to reduce effects of non-tsunami components. *Geophysical Journal International*, *215*(2), 1200–
 362 1214. <https://doi.org/10.1093/gji/ggy345>

Lawson, C., & Hanson, R. (1995). *Solving least squares problems*. Society for Industrial and Applied Mathematics.

Lewis, F., Xie, L., & Popa, D. (2008). *Optimal and Robust Estimation: With an Introduction to Stochastic Control Theory* (2nd ed.). CRC Press.

Maeda, T., Takemura, S., & Furumura, T. (2017). OpenSWPC: An open-source integrated parallel simulation code for modeling seismic wave propagation in 3D heterogeneous viscoelastic media. *Earth, Planets and Space*, 69(1), 102. <https://doi.org/10.1186/s40623-017-0687-2>

Mandli, K. T., Ahmadi, A. J., Berger, M., Calhoun, D., George, D. L., Hadjimichael, Y., Ketcheson, D. I., Lemoine, G. I., & LeVeque, R. J. (2016). Clawpack: Building an open source ecosystem for solving hyperbolic PDEs. *PeerJ Computer Science*, 2, e68. <https://doi.org/10.7717/peerj-cs.68>

Matsumoto, K., Takanezawa, T., & Ooe, M. (2000). Ocean tide models developed by assimilating TOPEX/POSEIDON altimeter data into hydrodynamical model: A global model and a regional model around Japan. *Journal of Oceanography*, 56(5), 567–581.

Melgar, D., Bock, Y., Sanchez, D., & Crowell, B. W. (2013). On robust and reliable automated baseline corrections for strong motion seismology. *Journal of Geophysical Research: Solid Earth*, 118(3), 1177–1187. <https://doi.org/10.1002/jgrb.50135>

Mizutani, A., Yomogida, K., & Tanioka, Y. (2020). Early Tsunami Detection With Near-Fault Ocean-Bottom Pressure Gauge Records Based on the Comparison With Seismic Data. *Journal of Geophysical Research: Oceans*, 125(9), e2020JC016275. <https://doi.org/10.1029/2020JC016275>

- 384 National Research Institute for Earth Science and Disaster Resilience (NIED). (2019). *NIED*
 385 *DONET*. <https://doi.org/10.17598/nied.0008>
- 386 Niu, J., & Xu, C. (2014). Real-Time Assessment of the Broadband Coseismic Deformation of the
 387 2011 Tohoku-Oki Earthquake Using an Adaptive Kalman Filter. *Seismological Research Letters*,
 388 85(4), 836–843. <https://doi.org/10.1785/0220130178>
- 389 Saito, T. (2013). Dynamic tsunami generation due to sea-bottom deformation: Analytical
 390 representation based on linear potential theory. *Earth, Planets and Space*, 65(12), 1411–1423.
- 391 Saito, T., & Tsushima, H. (2016). Synthesizing ocean bottom pressure records including seismic
 392 wave and tsunami contributions: Toward realistic tests of monitoring systems. *Journal of*
 393 *Geophysical Research: Solid Earth*, 121(11), 8175–8195. <https://doi.org/10.1002/2016JB013195>
- 394 Takemura, S., Kimura, T., Saito, T., Kubo, H., & Shiomi, K. (2018). Moment tensor inversion of
 395 the 2016 southeast offshore Mie earthquake in the Tonankai region using a three-dimensional
 396 velocity structure model: Effects of the accretionary prism and subducting oceanic plate. *Earth,*
 397 *Planets and Space*, 70(1), 50. <https://doi.org/10.1186/s40623-018-0819-3>
- 398 Trowbridge, J., Weller, R., Kelley, D., Dever, E., Plueddemann, A., Barth, J. A., & Kawka, O.
 399 (2019). The Ocean Observatories Initiative. *Frontiers in Marine Science*, 6.
 400 <https://www.frontiersin.org/articles/10.3389/fmars.2019.00074>
- 401 Tu, R., Wang, R., Walter, T. R., & Diao, F. (2014). Adaptive recognition and correction of
 402 baseline shifts from collocated GPS and accelerometer using two phases Kalman filter. *Advances*
 403 *in Space Research*, 54(9), 1924–1932. <https://doi.org/10.1016/j.asr.2014.07.008>

- Wallace, L. M., Araki, E., Saffer, D., Wang, X., Roesner, A., Kopf, A., Nakanishi, A., Power, W., Kobayashi, R., & Kinoshita, C. (2016). Near-field observations of an offshore Mw 6.0 earthquake from an integrated seafloor and subseafloor monitoring network at the Nankai trough, southwest Japan. *Journal of Geophysical Research: Solid Earth*, 121(11), 8338–8351.
- Wang, R., Schurr, B., Milkereit, C., Shao, Z., & Jin, M. (2011). An Improved Automatic Scheme for Empirical Baseline Correction of Digital Strong-Motion Records. *Bulletin of the Seismological Society of America*, 101(5), 2029–2044. <https://doi.org/10.1785/0120110039>
- Webb, S. C. (1998). Broadband seismology and noise under the ocean. *Reviews of Geophysics*, 36(1), 105–142. <https://doi.org/10.1029/97RG02287>
- Wu, Y.-M., & Wu, C.-F. (2007). Approximate recovery of coseismic deformation from Taiwan strong-motion records. *Journal of Seismology*, 11(2), 159–170.
- Zang, J., Xu, C., Chen, G., Wen, Q., & Fan, S. (2019). Real-time coseismic deformations from adaptively tight integration of high-rate GNSS and strong motion records. *Geophysical Journal International*, 219(3), 1757–1772. <https://doi.org/10.1093/gji/ggz397>