

Reconstruction of Cenozoic $\delta^{11}\text{B}_{\text{sw}}$ Using A Gaussian Process

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Key Points:

- We reconstruct the temporal evolution of seawater isotope ratios of boron, strontium, lithium, and osmium over the last 65 million years
- The evolution of seawater boron isotope ratio shows similarity to the evolution of strontium, lithium and osmium isotope ratios
- Randomly drawn, smooth time series are provided for use in uncertainty propagation in calculation of palaeo pH

Abstract

The boron isotope ratio of seawater ($\delta^{11}\text{B}_{\text{sw}}$) is a parameter which must be known to reconstruct palaeo pH and CO_2 from boron isotope measurements of marine carbonates. Beyond a few million years ago, $\delta^{11}\text{B}_{\text{sw}}$ is likely to have been different to modern. Palaeo $\delta^{11}\text{B}_{\text{sw}}$ can be estimated by simultaneously constraining the vertical gradients in foraminiferal $\delta^{11}\text{B}$ ($\Delta\delta^{11}\text{B}$) and pH (ΔpH). A number of subtly different techniques have been used to estimate ΔpH in the past, all broadly based on assumptions about vertical gradients in oxygen, and/or carbon, or other carbonate system constraints. In this work we pull together existing data estimates alongside limitations on the rate of change of $\delta^{11}\text{B}_{\text{sw}}$ from modelling, and combine these into an overarching statistical framework called a Gaussian Process. The Gaussian Process technique allows us to bring together data and constraints on the rate of change in $\delta^{11}\text{B}_{\text{sw}}$ to generate random plausible evolutions of $\delta^{11}\text{B}_{\text{sw}}$. We reconstruct $\delta^{11}\text{B}_{\text{sw}}$, and by extension palaeo pH, across the last 65Myr using this novel methodology. Reconstructed $\delta^{11}\text{B}_{\text{sw}}$ is compared to other seawater isotope ratios, namely $^{87/86}\text{Sr}$, $^{187/188}\text{Os}$, and $\delta^7\text{Li}$, which we also reconstruct with Gaussian Processes. Our method provides a template for incorporation of future $\delta^{11}\text{B}_{\text{sw}}$ constraints, and a mechanism for propagation of uncertainty in $\delta^{11}\text{B}_{\text{sw}}$ into future studies.

Plain Language Summary

Boron naturally exists in two forms - ^{11}B and ^{10}B . Measuring the ratio of these two forms of the element boron within marine shells allows us to estimate how alkaline the ocean was in the past, which is related to how much carbon dioxide is in the atmosphere. Before we can do this calculation, though, we need to know some other parameters, one of which is the relative abundance of the two forms of boron in the ocean at the time (which we call $\delta^{11}\text{B}_{\text{sw}}$). Preexisting studies have estimated $\delta^{11}\text{B}_{\text{sw}}$ at particular times, and here we combine them to generate a full reconstruction across the last 65 million years, accounting for uncertainties. Our reconstruction is informed by limiting the rate at which $\delta^{11}\text{B}_{\text{sw}}$ can change, based on model simulations. We provide statistical samples which can be used in future work when calculating past ocean pH.

1 Introduction

Boron, and its two isotopes (^{10}B and ^{11}B), exist in seawater with speciation governed by acid-base equilibrium. There are four degrees of freedom in the boron isotope system, which we typically express with the following five parameters: $\delta^{11}\text{B}_4$ (the isotopic composition of borate), $\delta^{11}\text{B}_{\text{sw}}$ (the isotope composition of seawater), ε (the fractionation factor), pK_B^* (the apparent equilibrium constant for boron in solution), and pH. Knowing any four of these parameters allows us to calculate the fifth (Zeebe & Wolf-Gladrow, 2001). For a typical palaeoclimatological application, we wish to determine palaeo pH, which is done by measuring $\delta^{11}\text{B}_{\text{calcite}}$ and translating this to $\delta^{11}\text{B}_4$ (potentially requiring a species specific calibration). $\delta^{11}\text{B}_4$ is then combined with the fractionation factor (ε - known from Klochko et al. (2006); Nir et al. (2015)), the apparent equilibrium constant for boron in seawater (pK_B^* - which is estimated from temperature, pressure, and seawater composition (Dickson & Goyet, 1994)), and the boron isotope ratio of seawater ($\delta^{11}\text{B}_{\text{sw}}$). We refer the interested reader to Marschall and Foster (2018) for a full description of boron systematics in seawater, but for the purposes of this work it is sufficient to say that one of the key parameters that must be established in order to reconstruct palaeo ocean pH is $\delta^{11}\text{B}_{\text{sw}}$. Modern day seawater has a $\delta^{11}\text{B}_{\text{sw}}$ of 39.61 ± 0.04 ‰ (Foster et al., 2010) - however $\delta^{11}\text{B}_{\text{sw}}$ is very likely to have been different in the past (Lemarchand et al., 2000).

Based on assessments of the relevant input and output fluxes to the ocean, boron is thought to have a relatively long residence time in seawater of roughly 10 million years (Broecker & Peng, Tsung-Hung, 1982) - that is, the average amount of time an atom of

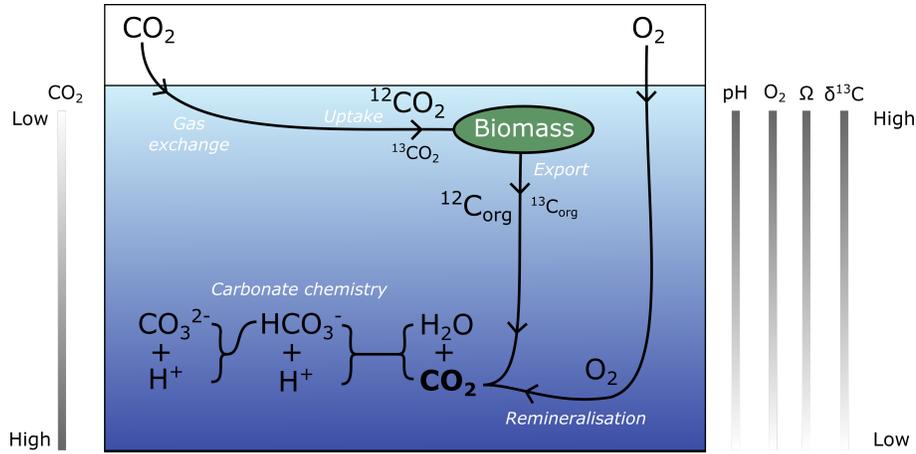


Figure 1. Schematic of the processes which cause vertical gradients in oceanic properties as harnessed in reconstructions of $\delta^{11}\text{B}_{\text{sw}}$. Oxygen and carbon dioxide concentrations are set in surface waters by the atmospheric concentrations and Henry’s Law (which is temperature dependent). Surface ocean carbon is taken up by biomass to form organic tissues, which are preferentially enriched in the lighter carbon isotope. When that biomass is exported to depth and remineralised, organic carbon is oxidised (consuming oxygen) and releasing CO_2 , which drives acidification. These processes cause correlated gradients in pH, aqueous CO_2 , aqueous O_2 , saturation state, and $\delta^{13}\text{C}$. As $\delta^{11}\text{B}_{\text{sw}}$ is a well mixed signal, differences in $\delta^{11}\text{B}_4$ between the surface and subsurface are primarily driven by the gradient in pH.

67 boron spends in the ocean. It is estimated from geochemical box modelling of the boron
 68 cycle that $\delta^{11}\text{B}_{\text{sw}}$ might have changed by up to 0.1 ‰/Myr (Lemarchand et al., 2000).
 69 This means that beyond a few million years ago, ocean $\delta^{11}\text{B}_{\text{sw}}$ might have been appre-
 70 ciably different to modern day seawater, which must be taken into account when calcu-
 71 lating palaeo pH. While halites show some promise as a direct proxy for $\delta^{11}\text{B}_{\text{sw}}$ (Paris
 72 et al., 2010), uncertainty remains about the observed variability in halite $\delta^{11}\text{B}$ recon-
 73 structions, so $\delta^{11}\text{B}_{\text{sw}}$ is currently estimated using more indirect techniques.

74 The primary technique for estimating, or placing limits on, palaeo $\delta^{11}\text{B}_{\text{sw}}$ is to ex-
 75 ploit vertical gradients in the ocean (Palmer et al., 1998; Greenop et al., 2017; Anagnostou
 76 et al., 2016; Henahan et al., 2019). This works due to the sigmoidal relationship be-
 77 tween $\delta^{11}\text{B}_4$ and pH (as shown in Figure 2). The non-linearity of this relationship makes
 78 it possible to calculate $\delta^{11}\text{B}_{\text{sw}}$ given two estimates of $\delta^{11}\text{B}_4$ and an estimate of the change
 79 in pH across this $\delta^{11}\text{B}_4$ gradient. The vertical gradient in pH (ΔpH) is correlated to the
 80 vertical gradients in carbon isotopes ($\Delta\delta^{13}\text{C}$), carbon concentration (ΔDIC), and oxy-
 81 gen concentration ($\Delta[\text{O}_2]$), linked with Apparent Oxygen Utilisation - AOU) due to their
 82 shared controlling processes (see Figure 1). Vertical gradients in all of these parameters
 83 can therefore be related to $\delta^{11}\text{B}_{\text{sw}}$.

84 The simplest option for reconstructing palaeo $\delta^{11}\text{B}_{\text{sw}}$ from measured $\delta^{11}\text{B}$ in car-
 85 bonates is to assume a constant ΔpH through time equal to modern, an approach used
 86 in Raitzsch and Hönisch (2013). By combining this with the sigmoidal relationship of
 87 $\delta^{11}\text{B}_4$ and pH, it is possible to estimate $\delta^{11}\text{B}_{\text{sw}}$ (see Figure 2). To improve upon the as-
 88 sumption of a constant ΔpH through time, one can use foraminiferal $\Delta\delta^{18}\text{O}$ and $\Delta\delta^{13}\text{C}$
 89 to guide identification of palaeo depth habitats of particular species, and to place rea-
 90 sonable limits on ΔpH (Palmer et al., 1998; Anagnostou et al., 2016; Greenop et al., 2017).
 91 For $\delta^{13}\text{C}$, this works because $\Delta\delta^{13}\text{C}$ and ΔpH are jointly controlled by subsurface rem-

92 mineralisation of organic carbon, which releases isotopically light carbon into the water
 93 and causes acidification (decreasing pH) - as illustrated in Figure 1. The rationale for
 94 such constraints is broadly justified by the difficulty of reversing the sign of the gradi-
 95 ents (which would require a fundamental change in biogeochemical dynamics), demon-
 96 strated by exploring a wide swath of model parameter space (Greenop et al., 2017) in
 97 carbon cycle models such as CYCLOPS (Hain et al., 2010), LOSCAR (Zeebe, 2012), and
 98 cGENIE (Ridgwell et al., 2007). That said, it is possible that models may not yet be ca-
 99 pable of representing the full plethora of possible carbonate chemistry states that the
 100 ocean can truly inhabit. Despite recent progress (Caves Rugenstein et al., 2019; Derry,
 101 2022) our understanding of Cenozoic carbon cycle fluxes, and their drivers, remains in-
 102 complete, as does our understanding of their relationship to oceanic properties such as
 103 DIC and pH, and by extension the vertical gradients in these ocean properties. There
 104 are circumstances which would result in the ‘normal’ relationships between these param-
 105 eters breaking down, for instance if organic carbon is predominantly respired by sulphate
 106 reducers (which would alter local alkalinity and pH). While these complications are rare,
 107 it is prudent to keep in mind their potential to impact estimates of $\delta^{11}\text{B}_{\text{sw}}$. Despite these
 108 challenges, using model predicted gradients in $\delta^{13}\text{C}$ and pH with paired planktic-benthic
 109 (or surface-subsurface) foraminiferal $\delta^{11}\text{B}$ data remains attractive, as it requires only sta-
 110 ble carbon isotope data (analyses which are routinely performed), and a model capable
 111 of providing estimates of feasible ocean profiles of $\delta^{13}\text{C}$ and pH.

112 $\delta^{11}\text{B}_{\text{sw}}$ from paired surface-deep samples can also be refined by estimation of AOU
 113 (Anagnostou et al., 2016). Surface ocean water oxygen saturation is mainly controlled
 114 by temperature (which is already a requirement for the $\delta^{11}\text{B}$ to pH calculation) and it
 115 is assumed based on modern observations that samples from deeper dwelling planktic
 116 foraminifera can not have inhabited anoxic waters (Hull et al., 2011). Similar to pH and
 117 $\delta^{13}\text{C}$, the vertical gradient in oxygen concentration is primarily a function of how much
 118 remineralisation of organic carbon has occurred (see Figure 1). Remineralisation adds
 119 CO_2 to the water, increasing the DIC concentration. A Redfield Ratio can be used to
 120 convert constraints on ΔO_2 to ΔDIC , however the impact on ΔpH is complicated by the
 121 buffering influence of alkalinity. The calculation therefore requires that we know (or as-
 122 sume) a second carbonate system parameter (in addition to pH) to make ΔDIC calcu-
 123 lable. This is not a major imposition, as quantification of palaeo CO_2 from boron isotope
 124 derived pH already requires assumption or knowledge of a second carbonate system
 125 parameter. Such an estimate may itself be derived from the same type of carbon
 126 cycle models used to estimate $\Delta\delta^{13}\text{C}$ and ΔpH . Carbon cycle models have been used
 127 to provide an estimate of saturation state for specific sites or times in the past, or to pro-
 128 vide estimates of alkalinity (Anagnostou et al., 2016; Henehan et al., 2019), which simul-
 129 taneously informs $\delta^{11}\text{B}_{\text{sw}}$, and palaeo CO_2 reconstructed from boron isotope derived pH.

130 The requirement of a second carbonate system parameter to predict palaeo CO_2
 131 from boron isotope derived pH presents a challenge due to various limitations in carbon-
 132 ate system reconstructions. For instance, although alkenone carbon isotopes can be used
 133 to reconstruct surface water CO_2 (Stoll et al., 2019; Zhang et al., 2020), the pairing of
 134 pH and CO_2 to determine the carbonate system tends to lead to large uncertainties due
 135 to their close covariance (J. W. B. Rae, 2018). While boron/calcium ratios show promis-
 136 ing relationships with carbonate system parameters (including DIC, ΔCO_3^{2-} , and HCO_3^-
 137 (Yu & Elderfield, 2007; Haynes et al., 2017; Sosdian et al., 2020)), there is still some de-
 138 bate as to which of these parameters is most faithfully recorded, and Cenozoic-scale records
 139 remain fragmentary. Current approaches tend to centre on assumptions linked to the sat-
 140 uration state for calcite (denoted Ω_{calcite}). Saturation state can not have been too low,
 141 or carbonate would not have been preserved, nor can it have been too high, or abiotic
 142 carbonate would have precipitated. The precise limits on reasonable values of near-surface
 143 seawater Ω_{calcite} are somewhat subjective and are both context and site dependent, but
 144 a reasonable broad range is from 1 to 10. In some circumstances, such as when produc-
 145 ing estimates for the subtropical surface ocean or targeting background Cenozoic climates,

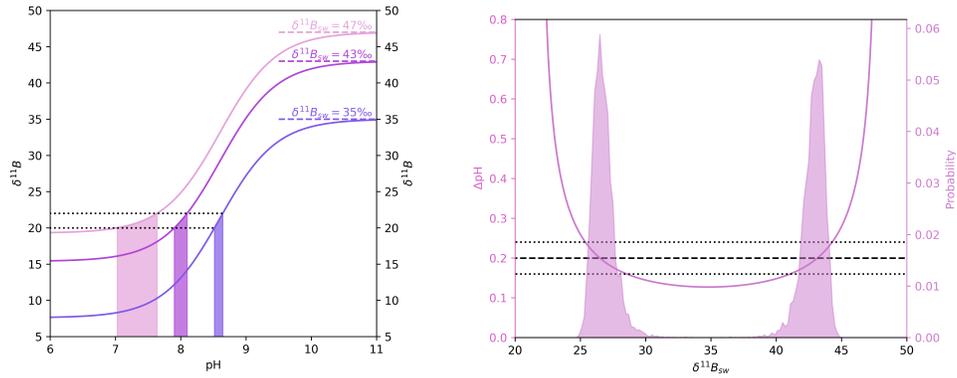


Figure 2. The left panel shows a graph of pH vs $\delta^{11}\text{B}_4$ for three different $\delta^{11}\text{B}_{\text{sw}}$'s (indicated by pink shades). A hypothetical 2‰ excursion from 22‰ to 20‰ is depicted by the black dotted lines. The equivalent pH change for the same excursion at variable $\delta^{11}\text{B}_{\text{sw}}$ is displayed in the shaded region. Note this curve is symmetrical about the value of pK_B^* (roughly 8.6 for standard modern open ocean conditions).

The right panel shows (for the same 22‰ to 20‰ excursion as shown in the left panel) ΔpH as a function of $\delta^{11}\text{B}_{\text{sw}}$ (pink line). A hypothetical constraint on ΔpH of 0.2 ± 0.04 (at 2σ) is shown by the black dashed lines, with uncertainty in the black dotted lines. Where this hypothetical constraint intersects with the pink line gives the region of possible $\delta^{11}\text{B}_{\text{sw}}$'s. We illustrate that a Monte Carlo approach, which samples possible ΔpH from the hypothetical constraint to give probability distributions (shown in pink shaded regions) for $\delta^{11}\text{B}_{\text{sw}}$, aligns with the emplaced constraint. Due to the symmetry of the curves shown in the left panel, there are often two $\delta^{11}\text{B}_{\text{sw}}$'s compatible with a ΔpH constraint. Typically the lower window is rejected as it would resolve to an unreasonably low pH.

146 one can be more prescriptive - using a one or two unit range around the modern aver-
 147 age surface ocean saturation state of 6 (Ridgwell & Zeebe, 2005; Anagnostou et al., 2016;
 148 Boudreau et al., 2019). We note, however, that this assumption may not be valid dur-
 149 ing transient periods of acidification (e.g. PETM (Penman et al., 2014)) or alkalinity im-
 150 balance (e.g. early Danian (Henehan et al., 2019)). Crucially, quantification of carbon-
 151 ate system conditions using the saturation state approach depend on quantification of
 152 $[\text{Ca}^{2+}]_{\text{sw}}$, which is used in combination with the saturation state assumption to derive
 153 $[\text{CO}_3^{2-}]$. For a given assumption or constraint on saturation state, any change in $[\text{Ca}^{2+}]_{\text{sw}}$
 154 thus translates almost linearly into a change in $[\text{CO}_3^{2-}]$, meaning that accurately quan-
 155 tifying the concentration of $[\text{Ca}^{2+}]_{\text{sw}}$, and its uncertainty, is of paramount importance
 156 to saturation state based constraints on the past ocean carbonate system.

157 Overall, it is therefore necessary to balance a number of requirements when recon-
 158 structing $\delta^{11}\text{B}_{\text{sw}}$. The estimated $\delta^{11}\text{B}_{\text{sw}}$ must produce a reasonable: ΔpH , $\Delta\delta^{13}\text{C}$, sat-
 159 uration state and AOU. Finding the space in which all these parameters are viable al-
 160 lows quantification of $\delta^{11}\text{B}_{\text{sw}}$ with attendant uncertainty. The boron isotope proxy is for-
 161 tunate however, in that almost all data and assumptions required to estimate $\delta^{11}\text{B}_{\text{sw}}$ are
 162 already a part of the $\delta^{11}\text{B}_4$ to CO_2 calculation.

163 Most previous applications of the techniques described above have focused on in-
 164 dividual time slices of the Cenozoic (as described in Section 2 and Table 1). By combin-
 165 ing each of these individual studies, we are able to reach a critical mass of information,
 166 allowing us to produce an estimate for how $\delta^{11}\text{B}_{\text{sw}}$ evolved throughout the Cenozoic. Our
 167 study represents an advance compared to two particularly relevant previous works that
 168 provided Cenozoic timescale estimates of $\delta^{11}\text{B}_{\text{sw}}$. Raitzsch and Hönisch (2013) predicted
 169 Cenozoic $\delta^{11}\text{B}_{\text{sw}}$ by assuming a constant ΔpH and a linear trend in deep ocean pH, mean-
 170 ing reconstructions of pH using this $\delta^{11}\text{B}_{\text{sw}}$ are only able to reconstruct the initial as-
 171 sumption (J. W. B. Rae, 2018) (further impacts of which are discussed in Section 5.3).
 172 Rae et al. (2021) compiled and reanalysed marine palaeo CO_2 proxy data (including
 173 boron isotopes), and therefore required a curve for $\delta^{11}\text{B}_{\text{sw}}$. However, generation of a Ceno-
 174 zoic $\delta^{11}\text{B}_{\text{sw}}$ curve was not the primary focus of that study and the authors noted the need
 175 to improve interpolation and constrain uncertainty. Here we provide a more robust es-
 176 timate of the evolution of $\delta^{11}\text{B}_{\text{sw}}$ through time by bringing existing and updated $\delta^{11}\text{B}_{\text{sw}}$
 177 constraints together into a statistical framework called a Gaussian Process. The Gaus-
 178 sian Process is able to integrate both the expected smoothness of the $\delta^{11}\text{B}_{\text{sw}}$ signal from
 179 modelling work and various forms of constraint from the available data.

180 2 Data

181 Data constraints on $\delta^{11}\text{B}_{\text{sw}}$ are varied. Some previous works presented central es-
 182 timates of $\delta^{11}\text{B}_{\text{sw}}$ (Gutjahr et al., 2017; Henehan et al., 2019, 2020), while another pro-
 183 vided lower or upper limits on $\delta^{11}\text{B}_{\text{sw}}$ (Anagnostou et al., 2016), and another provided
 184 full probability distributions for possible values of $\delta^{11}\text{B}_{\text{sw}}$ (Greenop et al., 2017). Two
 185 of those studies reconstructed $\delta^{11}\text{B}_{\text{sw}}$ for a particular event (or short timeslice) (Henehan
 186 et al., 2019; Gutjahr et al., 2017), and two reconstructed $\delta^{11}\text{B}_{\text{sw}}$ over a wider time win-
 187 dow, within which $\delta^{11}\text{B}_{\text{sw}}$ might have evolved (Anagnostou et al., 2016; Greenop et al.,
 188 2017). Here we use $\delta^{11}\text{B}_{\text{sw}}$ estimates from Greenop et al. (2017) exactly as presented in
 189 the original study. The original published estimate from Henehan et al. (2019), however,
 190 is based on carbonate system calculations whose equilibrium constants use fitting pa-
 191 rameters from the supplementary tables of (Hain et al., 2015). These tables have since
 192 been found to contain inaccuracies, and so here we update carbonate system calculations,
 193 and hence $\delta^{11}\text{B}_{\text{sw}}$ constraints, based on corrected equilibrium constants packaged with
 194 Raitzsch et al. (2022). Updated carbonate system calculations and CO_2 estimates for
 195 this time are provided in the Supplementary Materials, and are plotted in Henehan and
 196 Witts (2023). Anagnostou et al. (2016) is updated by modifying the calculation of vital
 197 effects to account for changing seawater chemistry. With these recalculations, Henehan

Age	Central Estimate	95% interval	Form	Source
0.0	39.61	0.04	Gaussian	Foster et al. (2010)
0.68	39.69	4.28	Non-Gaussian	Greenop et al. (2017)
1.14	38.55	3.74	Non-Gaussian	Greenop et al. (2017)
1.16	41.60	3.27	Non-Gaussian	Greenop et al. (2017)
1.45	40.51	2.00	Non-Gaussian	Greenop et al. (2017)
2.27	41.57	1.66	Non-Gaussian	Greenop et al. (2017)
2.87	39.82	2.05	Non-Gaussian	Greenop et al. (2017)
5.37	40.38	2.78	Non-Gaussian	Greenop et al. (2017)
8.67	42.30	1.88	Non-Gaussian	Greenop et al. (2017)
9.33	40.22	2.28	Non-Gaussian	Greenop et al. (2017)
10.14	36.35	5.98	Non-Gaussian	Greenop et al. (2017)
11.62	40.34	2.05	Non-Gaussian	Greenop et al. (2017)
12.27	35.69	5.99	Non-Gaussian	Greenop et al. (2017)
12.80	37.47	2.53	Non-Gaussian	Greenop et al. (2017)
13.53	36.43	5.89	Non-Gaussian	Greenop et al. (2017)
16.39	36.49	5.76	Non-Gaussian	Greenop et al. (2017)
17.69	37.00	5.66	Non-Gaussian	Greenop et al. (2017)
19.00	41.10	1.95	Non-Gaussian	Greenop et al. (2017)
19.67	40.44	1.93	Non-Gaussian	Greenop et al. (2017)
22.62	39.41	4.47	Non-Gaussian	Greenop et al. (2017)
22.98	34.65	6.10	Non-Gaussian	Greenop et al. (2017)
23.08	39.11	3.50	Non-Gaussian	Greenop et al. (2017)
37.00	37.63	2.36	Non-Gaussian	Anagnostou et al. (2016)*
44.40	38.51	0.75	Non-Gaussian	Anagnostou et al. (2016)*
45.60	37.81	1.18	Non-Gaussian	Anagnostou et al. (2016)*
53.00	38.49	0.70	Non-Gaussian	Anagnostou et al. (2016)*
55.80	38.94	0.41	Gaussian	Gutjahr et al. (2017)
66.04	39.30	0.50	Uniform	Henehan et al. (2019)*

Table 1. Table of data constraints with representative central values and standard deviations as an indicator of uncertainty. * symbol indicates the values has been updated from the original publication for this work.

198 et al. (2019)’s $\delta^{11}\text{B}_{\text{sw}}$ estimate is updated from the originally published value of 39.05
 199 - 39.85 ‰ to 39.05 - 39.55 ‰, while estimates from Anagnostou et al. (2016) are inte-
 200 grated as full probability distributions instead of the lower/upper limits presented in the
 201 original study (see Table 1 and Supplement S1).

202 To supplement these existing $\delta^{11}\text{B}_{\text{sw}}$ constraints, we take planktic $\delta^{11}\text{B}_4$ as pre-
 203 sented in Rae et al. (2021), based on original studies by Anagnostou et al. (2016, 2020);
 204 Badger et al. (2013); Chalk et al. (2017); de la Vega et al. (2020); Dyez et al. (2018); Fos-
 205 ter (2008); Foster et al. (2012); Greenop et al. (2014, 2017, 2019); Gutjahr et al. (2017);
 206 Harper et al. (2020); Henehan et al. (2019, 2020); Hönisch et al. (2009); Lemarchand et
 207 al. (2000); Martínez-Botí et al. (2015); Paris et al. (2010); Pearson et al. (2009); Pen-
 208 man et al. (2014); Raitzsch and Hönisch (2013); Sosdian et al. (2018), to calculate a range
 209 of valid $\delta^{11}\text{B}_{\text{sw}}$ by exploiting the sigmoidal shape of the relationship between pH and $\delta^{11}\text{B}_4$
 210 (as seen in Figure 2). The maximum offset between $\delta^{11}\text{B}_4$ and $\delta^{11}\text{B}_{\text{sw}}$ is seen at low pH,
 211 and is described by the fractionation factor ε (or α). For any given estimate of $\delta^{11}\text{B}_4$,
 212 the minimum valid $\delta^{11}\text{B}_{\text{sw}}$ is equal to $\delta^{11}\text{B}_4$, and the maximum $\delta^{11}\text{B}_{\text{sw}}$ can be calculated
 213 by combination with the fractionation factor. We first bin data into 1 Myr intervals, then
 214 take the maximum measured $\delta^{11}\text{B}_4$ as the lower limit for $\delta^{11}\text{B}_{\text{sw}}$, and use the minimum

215 measured $\delta^{11}\text{B}_4$ to calculate the maximum $\delta^{11}\text{B}_{\text{sw}}$. Uncertainty in measured $\delta^{11}\text{B}_{\text{foram}}$
 216 is propagated to uncertainty in the possible $\delta^{11}\text{B}_{\text{sw}}$, and the upper 99% quantile is used
 217 to estimate the maximum permissible $\delta^{11}\text{B}_{\text{sw}}$. As described, lower limits can be calcu-
 218 lated using this method, however these values are so low as to be uninformative across
 219 the Cenozoic. Upper limits created using this method are shown in Figure 3.

220 In this work we therefore have four potential categories of constraint: constraints
 221 where the uncertainty is well represented by a Gaussian distribution (Gaussian constraints),
 222 constraints where the uncertainty is not well represented by a Gaussian distribution (non
 223 Gaussian constraints), lower and upper limits, and limitations on the rate of change in
 224 $\delta^{11}\text{B}_{\text{sw}}$ from modelling.

225 3 Methods

226 Having assembled the data described in Section 2, we reconstruct $\delta^{11}\text{B}_{\text{sw}}$ using a
 227 Gaussian Process (GP). The Gaussian Process is a statistical technique which allows us
 228 to generate smooth time series conditioned to match data constraints (for a fuller, more
 229 rigorous description of the Gaussian Process - see Supplement S1). In the case of $\delta^{11}\text{B}_{\text{sw}}$,
 230 we have an expectation of smoothness from the work of Lemarchand et al. (2000), which
 231 we combine with data constraints as described in Section 2 and shown in Figure 3. The
 232 Gaussian Process works by using a kernel function, which encodes structure into the re-
 233 construction, and hyperparameters which tune the behaviour. Uncorrelated Gaussian
 234 noise is transformed into autocorrelated values with the covariance structure prescribed
 235 by the kernel function and hyperparameters. Here we use the squared exponential ker-
 236 nel (also known as the Radial Basis Function), which expresses that nearby points are
 237 more likely to be similar to each other than distant points. There are two controlling hy-
 238 perparameters - one expresses the length scale over which there is significant correlation,
 239 which is related to the expected rate of change in a signal. The other parameter is the
 240 noise scale - which manifests as how much uncertainty is expected at a time where no
 241 data constraints are available. The Gaussian Process can be used to generate random
 242 smooth lines with the prescribed characteristics even in the absence of data constraints,
 243 however data can be incorporated by adapting the covariance structure such that the
 244 statistical samples it generates will go through datapoints where permitted by the cho-
 245 sen hyperparameters. Uncertainty in data constraints can be incorporated directly into
 246 the Gaussian Process if uncertainty in the estimates is Gaussian in nature, and other types
 247 of constraint can be incorporated by adapting the approach.

248 The Gaussian Process is able to provide a number of equally likely, independent,
 249 stochastic time series, which are useful in reconstructing time series of palaeo data with
 250 an estimate of the uncertainty. Each obeys the smoothness constraint encapsulated by
 251 the kernel, while simultaneously attempting to match any available data. The result is
 252 that where a data constraint with low uncertainty is available, time series will be strongly
 253 influenced to go through this datapoint. Where data are sparse, or data constraints are
 254 uncertain, statistical replicates diverge to represent increasing uncertainty (see Supple-
 255 ment S1 for a demonstration of this behaviour). Because each sample drawn from the
 256 Gaussian process is independent and equally likely, we can straightforwardly apply fil-
 257 ters to reject any sample that has undesirable properties. As mentioned above, data con-
 258 straints where uncertainties can be well represented by a Gaussian distribution can be
 259 directly assimilated into the Gaussian Process. Here we also wish to enforce three other
 260 types of constraint, lower/upper limitations on $\delta^{11}\text{B}_{\text{sw}}$, limitations on the rate of change
 261 in $\delta^{11}\text{B}_{\text{sw}}$, and data constraints with a non Gaussian uncertainty structure. Limitations
 262 (either on the value of $\delta^{11}\text{B}_{\text{sw}}$ or the rate of change in $\delta^{11}\text{B}_{\text{sw}}$) are relatively straight-
 263 forward to enforce - we can compare each Gaussian Process sample to the limitation and
 264 simply reject those which are outside the established limits. Non-Gaussian constraints
 265 are slightly more difficult to integrate, but can also be done within a rejection framework
 266 by approximating each non-Gaussian constraint with a Gaussian distribution. Here we

do this by creating Gaussian constraints with the same mean as their non-Gaussian counterpart, but with higher standard deviation. Samples can then be strategically rejected to tweak the Gaussian Process such that it has effectively sampled from non-Gaussian constraints (the mechanics of this type of rejection sampling are clarified in Supplement S1).

One difficulty of rejection sampling, however, is dealing with simultaneous but mutually exclusive data constraints. Gaussian distributions are nonzero across their domain, meaning no value (however unlikely) is truly impossible. The nature of the non-Gaussian constraints in this work though, suggests that at any given time some $\delta^{11}\text{B}_{\text{sw}}$ values are impossible to reconcile with the data estimates. Given multiple constraints of this type, in close proximity to one another, it becomes exceedingly unlikely to draw samples from the Gaussian Process which have the requisite smoothness and pass through the possible region of every datapoint. We overcome this difficulty by giving each non-Gaussian constraint the possibility of being an outlier value. In summary, Gaussian Process samples are not always rejected completely where in disagreement with data, but the probability of acceptance is highest where in agreement with the data constraints, and lower (but non zero) further from the data constraints.

We reconstruct $\delta^{11}\text{B}_{\text{sw}}$ by conditioning a Gaussian Process on the few available central estimates of $\delta^{11}\text{B}_{\text{sw}}$ (shown in Table 1). Additional data constraints are integrated by filtering the generated statistical samples (as described above and in Supplement S1). Any samples which fall outside the lower or upper limits are rejected, and some samples are rejected to adjust the Gaussian Process such that it appropriately incorporates non Gaussian constraints. We use hyperparameters of 2 ‰ noise scale, and 10 Myr length scale. The Gaussian Process does not enforce a specific rate of change, but the chosen noise scale and length scale give an approximation of the rate of change, in this case roughly equivalent to a 0.2 ‰/Myr rate of change, which is on the faster end of agreement with the residence time and maximum rate of change from box modelling of the geochemical cycle of boron (Lemarchand et al., 2000). Lemarchand et al. (2000) suggest an upper limit to the rate of change of $\delta^{11}\text{B}_{\text{sw}}$ of 0.1 ‰/Myr. This estimate is based on modern day fluxes, so we allow greater uncertainty in the past when the boron fluxes in and out of the ocean may have been different, increasing the permissible maximum rate of change linearly to 0.7 ‰/Myr at 70 Ma (discussed further in Section 5.2). Output samples are filtered such that those with a rate of change greater than the values described above are rejected. This, alongside the rejection strategy used to integrate non-Gaussian constraints, leaves a subset of the originally generated samples. Approximately 10 in each 10,000 are accepted, and we run the algorithm until 10,000 samples have been accepted.

4 Results

Our reconstruction of $\delta^{11}\text{B}_{\text{sw}}$ suggests rather muted change across the Cenozoic relative to the change in $\delta^{11}\text{B}_4$. $\delta^{11}\text{B}_4$ has changed by roughly 8 ‰, and we find that $\delta^{11}\text{B}_{\text{sw}}$ has been responsible for a perhaps 2 ‰ of that change, leaving a 6 ‰ change driven predominantly by pH. The pattern of change of $\delta^{11}\text{B}_{\text{sw}}$ is non-linear, with a decline of roughly 1 ‰ from the early to mid Cenozoic, followed by an increase of approximately 1 ‰ from 30 Ma to 10 Ma, and a relatively stable value between those time periods and from 10 Ma until the present day. Our reconstruction generally matches the evolution curve used by Rae et al. (2021), except in the interval between 20 Ma and 10 Ma. Within this interval both curves are guided predominantly by the data from Greenop et al. (2017), but Rae et al. (2021) used Greenop et al. (2017)'s binned values whereas our approach uses the probability distribution of each individual estimate. Our Gaussian Process methodology favours the higher $\delta^{11}\text{B}$ values in this interval due to their lower reported uncertainty (relative to the lower $\delta^{11}\text{B}_{\text{sw}}$ estimates from Greenop et al. (2017)). This results in an overall higher estimate of $\delta^{11}\text{B}_{\text{sw}}$ during the Miocene, and implies pH was potentially lower than previously calculated at this time. However, we note the uncertainties

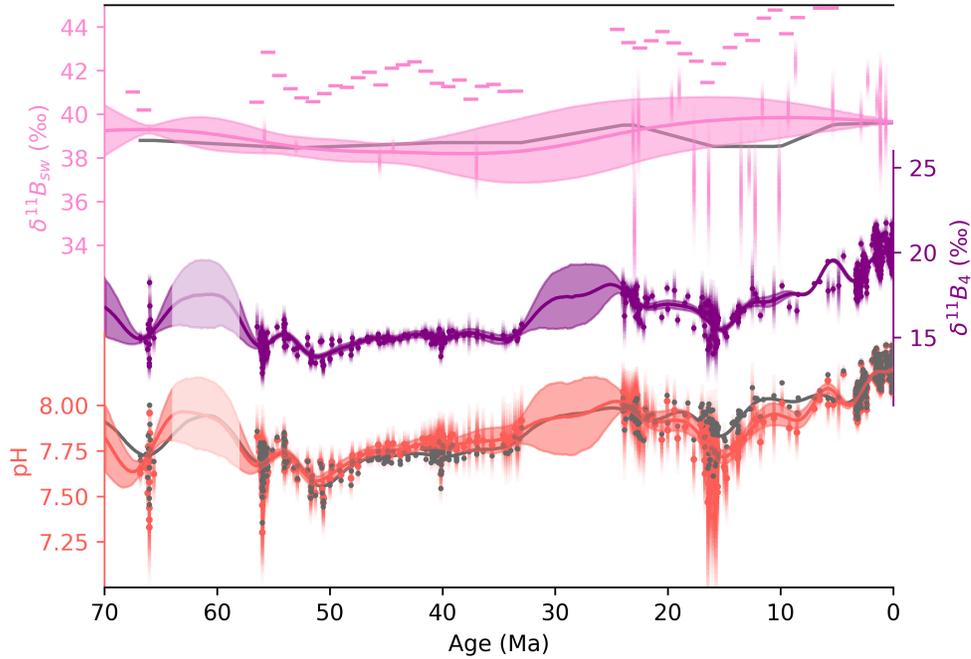


Figure 3. Our reconstruction of $\delta^{11}\text{B}_{\text{sw}}$ is shown pink, with a central line depicting the median, and a window representing the 95 % confidence interval. Central data constraints are shown by vertical pink bars representative of 95 % confidence intervals, and upper limits are shown by horizontal pink bars. The grey line depicts $\delta^{11}\text{B}_{\text{sw}}$ reconstructed by Rae et al. (2021) for comparison. $\delta^{11}\text{B}_4$ datapoints from Rae et al. (2021) are shown as purple dots (interpolated in the purple shaded region using a Gaussian Process), which are converted to pH using our $\delta^{11}\text{B}_{\text{sw}}$ (red points, line, and shaded region) and the $\delta^{11}\text{B}_{\text{sw}}$ from Rae et al. (2021) (grey points and line) for comparison. We note that our Gaussian Process interpolation of $\delta^{11}\text{B}_4$ (and therefore also pH) has difficulty during large data gaps. In particular during the Palaeogene (which we have faded out), the large data gap is bounded by events with rapid changes in $\delta^{11}\text{B}_4$, and our reconstruction would be tempered by filling in this region with $\delta^{11}\text{B}_4$ data.

319 in both our reconstruction and the individual $\delta^{11}\text{B}_{\text{sw}}$ constraints are high in the Neo-
 320 gene, and that some of the data constraints suggest rates of change in $\delta^{11}\text{B}_{\text{sw}}$ exceed-
 321 ing those compatible with geochemical box model predictions (as discussed further in
 322 Section 5.2). Uncertainty on $\delta^{11}\text{B}_{\text{sw}}$ is also particularly high in data gaps where $\delta^{11}\text{B}_4$
 323 has yet to be measured. In particular we note a large window during the Oligocene within
 324 which no boron isotope data has yet been published, and which correspondingly has high
 325 uncertainty in $\delta^{11}\text{B}_{\text{sw}}$.

326 We provide illustrative curves for $\delta^{11}\text{B}_4$ and pH (see Figure 3) by using a Gaus-
 327 sian Process to interpolate $\delta^{11}\text{B}_4$, then combining this with our predicted $\delta^{11}\text{B}_{\text{sw}}$ and
 328 other ancillary parameters as in Rae et al. (2021). The Gaussian Process used to recon-
 329 struct $\delta^{11}\text{B}_4$ uses a length scale of 2 Myr to target relatively long term changes in pH,
 330 rather than individual palaeoclimatic events.

331 The pattern of change we find in $\delta^{11}\text{B}_{\text{sw}}$ is very similar to temporal trends in a num-
 332 ber of other related biogeochemical signals, such as oceanic $^{87/86}\text{Sr}$, $^{187/188}\text{Os}$, and $\delta^7\text{Li}$.
 333 Here we take published $^{87/86}\text{Sr}$ and $\delta^7\text{Li}$ from Misra and Froelich (2012), and compile a
 334 new record of $^{187/188}\text{Os}$ from Josso et al. (2019); Klemm et al. (2005); Oxburgh (1998);
 335 Oxburgh et al. (2007); Paquay et al. (2008, 2014); Pegram and Turekian (1999); Peucker-
 336 Ehrenbrink and Ravizza (2000, 2020); van der Ploeg et al. (2018); Ravizza (1993); Rav-
 337 izza and Turekian (1992); Ravizza and Peucker-Ehrenbrink (2003); Ravizza et al. (2001);
 338 Reusch et al. (1998); Robinson et al. (2009). For each signal, we assume that data con-
 339 straints have Gaussian uncertainty (with magnitude given with original estimates, ex-
 340 cept in the case of $^{87/86}\text{Sr}$ where an illustrative uncertainty is used), which allows us to
 341 perform a straightforward Gaussian Process reconstruction, with the residence time of
 342 each element informing the length scale used ($^{87/86}\text{Sr}$ - 5.1 Myr (Broecker & Peng, Tsung-
 343 Hung, 1982), $\delta^7\text{Li}$ - 2.8 Myr (Stoffynegli & Mackenzie, 1984), $^{187/188}\text{Os}$ - 1 Myr). Inter-
 344 polated data products for both $^{87/86}\text{Sr}$ and $\delta^7\text{Li}$ have been previously published (for in-
 345 stance in Misra and Froelich (2012)), but to our knowledge this is the first interpolated
 346 data product available for $^{187/188}\text{Os}$. There remains uncertainty in the residence time of
 347 osmium, but it is thought to be extremely short relative to the other signals shown here
 348 (all estimates are $<100\text{kyr}$ - see e.g. Oxburgh (2001)). We use a length scale of 1 Myr
 349 in the reconstruction to balance the available data density against the short residence
 350 time. Overall, our reconstructions use a more sophisticated fitting strategy than previ-
 351 ous incarnations, which is guided primarily by the data and integrates information on
 352 residence time of each element. This allows us to provide a robust quantification of the
 353 uncertainty in each signal, within the limitations of currently available data density.

354 Each of the seawater isotope signals we examine, like $\delta^{11}\text{B}_{\text{sw}}$, shows a long term
 355 increase over the Cenozoic. Oceanic strontium isotopes appear to show most similarity
 356 with our reconstructed $\delta^{11}\text{B}_{\text{sw}}$, while we note resemblance between the evolutions of pH,
 357 lithium isotopes, and osmium isotopes (as shown in Figure 4). We are able to provide
 358 an extremely narrow uncertainty window on our $^{87/86}\text{Sr}$ reconstruction due to strontium's
 359 long residence time and relatively high data density (and data quality) over the Ceno-
 360 zoic. By contrast, $^{187/188}\text{Os}$ which has greater data density and comparable scale of un-
 361 certainty in datapoints, has more uncertainty in our reconstruction. This is due to os-
 362 mium's extremely short residence time, and persists despite us using an artificially long
 363 length scale to reconstruct this signal. $\delta^7\text{Li}$ by contrast has quite large uncertainties, due
 364 in large part to the uncertainty in the individual data constraints. We are unable to re-
 365 construct the rapid shift in $\delta^7\text{Li}$ at the K-Pg boundary, which occurs faster than the mod-
 366 ern day residence time of lithium (see Section 5.2 for further discussion). Despite these
 367 challenges we believe reconstruction of these signals benefits from the Gaussian Process
 368 approach, in that uncertainties on our reconstruction are more representative, and the
 369 timescale of change in each signal aligns more closely to our expectations based on their
 370 residence times.

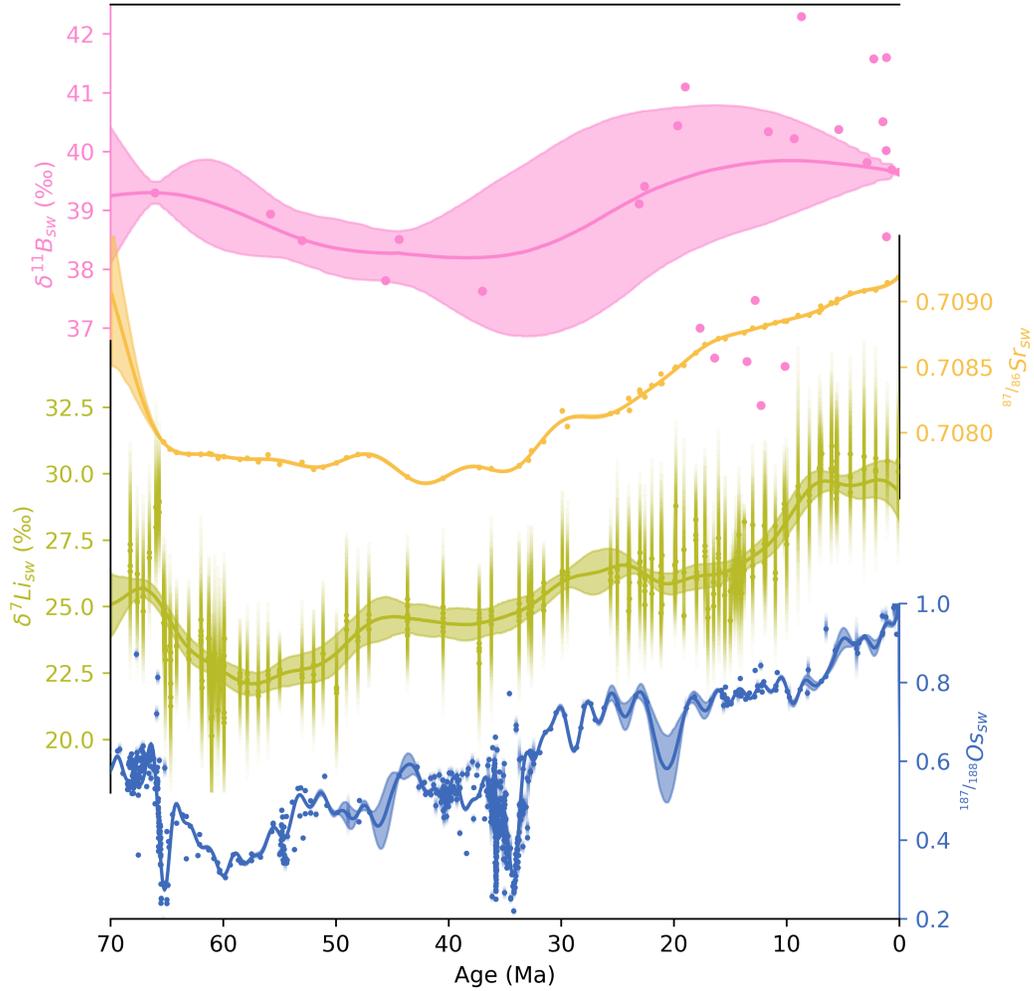


Figure 4. Our reconstruction of $\delta^{11}\text{B}_{\text{sw}}$ is shown pink, with a central line depicting the median, and a window representing the 95 % confidence interval. Data constraints are shown by the pink dots (here displayed without uncertainty for clearer comparison of signal trends). Other related geochemical signals $\delta^7\text{Li}$, $^{87/86}\text{Sr}$, and $^{187/188}\text{Os}$ are shown in yellow, green, and blue respectively after Misra and Froelich (2012). Data constraining $^{87/86}\text{Sr}$ and $\delta^7\text{Li}$ is sourced from Misra and Froelich (2012), while data constraining $^{187/188}\text{Os}$ is compiled from a number of sources (listed in the main text). We interpolate each of these signals with Gaussian Process with hyperparameters guided by the residence time of each signal.

5 Discussion

5.1 Decomposition of $\delta^{11}\text{B}_4$

$\delta^{11}\text{B}_4$ is an integrated signal, combining the effects of $\delta^{11}\text{B}_{\text{sw}}$, pH, pK_B^* , and ε . Of these, only a few are time-variable ($\delta^{11}\text{B}_{\text{sw}}$, pH, and some of the factors which influence pK_B^* - temperature, and seawater elemental composition). The sensitivity of $\delta^{11}\text{B}_4$ to these factors is such that only changes in $\delta^{11}\text{B}_{\text{sw}}$ or pH would be of sufficient magnitude to drive the observed 8 ‰ change in $\delta^{11}\text{B}_4$ across the Cenozoic, though temperature could have a non-negligible impact. To first order we might therefore simplify the $\delta^{11}\text{B}_4$ record into two components, $\delta^{11}\text{B}_{\text{sw}}$ and pH. Any change in $\delta^{11}\text{B}_4$ not explained by changes in $\delta^{11}\text{B}_{\text{sw}}$ must be the result of pH, and vice versa. Given the observed 8 ‰ change in $\delta^{11}\text{B}_4$, and our reconstructed 2 ‰ change in $\delta^{11}\text{B}_{\text{sw}}$, this suggests roughly 6 ‰ of change has been driven by changing pH. That is roughly equivalent to an increase in pH of 0.4 units across the Cenozoic, or a decrease in hydrogen ion availability by 60%. By comparison, anthropogenic CO_2 release has driven a surface ocean pH change of roughly 0.15 units, equivalent to a 41% increase in hydrogen ion availability (Findlay et al., 2022) relative to preindustrial conditions. Relative to their respective initial conditions, the anthropogenic surface ocean $[\text{H}^+]$ perturbation is therefore approximately two thirds the magnitude of long term change seen within the last 65 million years.

5.2 $\delta^{11}\text{B}_{\text{sw}}$ Rate of Change

A key feature of the Gaussian Process methodology used here is the ability to draw smooth potential evolutions of $\delta^{11}\text{B}_{\text{sw}}$, which we augment by filtering samples to reject those with an unfeasibly high temporal gradient. The feasibility of the rate of change in $\delta^{11}\text{B}_{\text{sw}}$ (and the hyperparameters which tune the Gaussian Process smoothness) are primarily based on the geochemical box modelling work of Lemarchand et al. (2000). Lemarchand et al. (2000) suggest that the likely maximum rate of change in $\delta^{11}\text{B}_{\text{sw}}$ is 0.1 ‰/Myr. We acknowledge that this is based on modern fluxes – fluxes which are not exceptionally well constrained (Park & Schlesinger, 2002) – so (as described in Section 3) we allow increasing maximum rates of change further back into the past - up to 0.7 ‰/Myr at 70 Ma. We choose the value of 0.7 ‰/Myr at 70 Ma because it allows us to enforce a rate limit near 0.1 ‰/Myr when we are most sure of that value (close to modern), without enforcing a strong limit earlier in the Cenozoic when we are much less certain about the residence time of boron and potential rate of change in $\delta^{11}\text{B}_{\text{sw}}$. 0.7 ‰/Myr is large enough that it does not result in rejection of potential evolutions in the earlier half of the Cenozoic, meaning the influence of the rate of change limit is mostly constrained to the rejection of samples as a result of their temporal gradient during the Neogene.

Suggestions of a higher rate of change in $\delta^{11}\text{B}_{\text{sw}}$ than previously recognised are present in the dataset of Greenop et al. (2017). The surface-deep $\delta^{11}\text{B}_4$ pairs of Greenop et al. (2017) (as described in Section 2) appear to record a bimodal distribution, with some indicating $\delta^{11}\text{B}_{\text{sw}}$ similar to modern, and others (mostly in the middle Miocene climatic optimum) suggesting $\delta^{11}\text{B}_{\text{sw}}$ roughly 2 ‰ lower. These would appear to suggest oscillations in $\delta^{11}\text{B}_{\text{sw}}$ more rapid than would be consistent with a rate of change of 0.1 ‰/Myr. We find that in order to match these data constraints, our Gaussian Process would need to have a length scale of approximately 3 Myr (which is very close to Park and Schlesinger (2002)'s estimate of the residence time of boron at 3.3Myr). Instead, we draw evolutions consistent with the rate of change suggested by (Lemarchand et al., 2000) - which requires that we give each non-Gaussian constraint (shown in Table 1) the possibility of being an outlier. The Gaussian Process then forges a path roughly through the centre of these constraints, drawn slightly high by the purportedly lower uncertainties in the higher $\delta^{11}\text{B}_{\text{sw}}$ estimates.

In summary, we proceed here under the existing paradigm of a long residence time for boron in seawater, and a slow rate of change in $\delta^{11}\text{B}_{\text{sw}}$. However, we acknowledge

the possibility that the rate of change in $\delta^{11}\text{B}_{\text{sw}}$ is faster than currently appreciated, and look to further modelling efforts and an improved understanding of the boron cycle to guide future interpretation of the data collated here. Faster rates of change may be explored with the algorithm presented here, but this increases the requirement for higher resolution data constraining $\delta^{11}\text{B}_{\text{sw}}$. Indeed our work underscores the value of, and need for more, data-derived $\delta^{11}\text{B}_{\text{sw}}$ constraints outside of individual palaeoclimatic events.

5.3 Comparison to $^{87/86}\text{Sr}$, $^{187/188}\text{Os}$, and $\delta^7\text{Li}_{\text{sw}}$

Figure 4 shows that there is a broad scale similarity between the temporal evolution of $\delta^{11}\text{B}$, $\delta^7\text{Li}$, $^{87/86}\text{Sr}$ and $^{187/188}\text{Os}$. In particular though, we observe greater similarity between $\delta^{11}\text{B}_{\text{sw}}$ and $^{87/86}\text{Sr}$, and also between pH, $\delta^7\text{Li}$ and $^{187/188}\text{Os}$. The similarity between $^{87/86}\text{Sr}$ and $\delta^{11}\text{B}_{\text{sw}}$ is present in the overall shape of both signals, and in both showing an inflection point at approximately the same time, around 35Ma. However we note that $^{87/86}\text{Sr}$ has been increasing continuously since 40 Ma, while our reconstruction of $\delta^{11}\text{B}_{\text{sw}}$ begins to decline at approximately 10 Ma. Given $^{87/86}\text{Sr}$ and $\delta^{11}\text{B}_{\text{sw}}$ share many controls (such as weathering and hydrothermal influx), it is not surprising that their signals share some similarities.

We note an excellent correspondence between $\delta^{11}\text{B}_4$ and $\delta^7\text{Li}$ (shown in Figures 3 and 4, or together in Figure S1), in agreement with previous findings (Raitzsch & Hönisch, 2013; Greenop et al., 2017) as well as similarity between $\delta^{11}\text{B}_4$ and $^{187/188}\text{Os}$. Previously the correspondence between $\delta^{11}\text{B}_4$ and $\delta^7\text{Li}$ has been attributed to the overlap in drivers of $\delta^{11}\text{B}_{\text{sw}}$ and $\delta^7\text{Li}$. Under the two component model described in Section 5.1, we propose that similarity of $\delta^{11}\text{B}_4$ and $\delta^7\text{Li}$ could either be due to a relationship between $\delta^7\text{Li}$ and $\delta^{11}\text{B}_{\text{sw}}$ (as previously suggested by Raitzsch and Hönisch (2013)), or due to a relationship between $\delta^7\text{Li}$ and pH, or a combination of both. $\delta^{11}\text{B}_{\text{sw}}$ and $\delta^7\text{Li}$ share drivers, as do pH and $\delta^7\text{Li}$, which are linked to weathering, clay formation, and seafloor spreading. These confounding factors make it difficult to ascribe this correlation to either the $\delta^{11}\text{B}_{\text{sw}}$ or pH signals unambiguously (see Figure S1). If pH is prescribed to change slowly and linearly (as in Raitzsch and Hönisch (2013)), then, by necessity, $\delta^{11}\text{B}_{\text{sw}}$ will reflect $\delta^{11}\text{B}_4$ - requiring relatively rapid fluctuations in $\delta^{11}\text{B}_{\text{sw}}$. However, as discussed in Section 5.2, we proceed here under the assumption that the rate of change in $\delta^{11}\text{B}_{\text{sw}}$ is as calculated in Lemarchand et al. (2000), removing the possibility of fast changes in $\delta^{11}\text{B}_{\text{sw}}$, and necessitating that $\delta^{11}\text{B}_4$ and pH are tightly correlated. Therefore here, it is pH and $\delta^7\text{Li}$ which have similar trajectories across the Cenozoic.

Notwithstanding the broad scale correlation between $\delta^7\text{Li}$ and $\delta^{11}\text{B}_4$, we note an interesting divergence between these signals at the K-Pg boundary. At this time, there is a large excursion in $\delta^7\text{Li}$ of approximately 5 ‰ in scale (almost as large as all the change which occurs during the rest of the Cenozoic). This excursion occurs at the same time as a large excursion in $^{187/188}\text{Os}$. While there is also a large perturbation in foraminiferal boron isotopes at approximately this time (Henehan et al., 2019), the temporal agreement is poor, and the nature of the two signals is different. $\delta^{11}\text{B}_4$ undergoes an excursion but rapidly recovers to near pre-perturbation levels, whereas $\delta^7\text{Li}$ values stay low for the next ~ 15 million years. This indicates that the drivers of pH and $\delta^7\text{Li}$ can be decoupled. However, the recorded change in $\delta^7\text{Li}$ at the K-Pg is extremely rapid, faster even than the modern residence time of lithium in seawater (approximately 1.2 Myr (Misra & Froelich, 2012)). It seems equally plausible that there is alternative, non-seawater, driver of foraminiferal $\delta^7\text{Li}$ at this time. If this alternative control is linked to the carbonate system (as suggested by Vigier et al. (2015); Roberts et al. (2018)), similar effects could conceivably be influencing the correlation between $\delta^{11}\text{B}_4$ and $\delta^7\text{Li}$ more broadly during the Cenozoic. At present, however, studies disagree as to the nature of carbonate system control on foraminiferal $\delta^7\text{Li}$ (Vigier et al., 2015; Roberts et al., 2018).

5.4 Palaeo pH and CO₂

pH is linked to the ocean carbonate system, with a particularly close relationship to atmospheric CO₂ concentrations (Hain et al., 2018). The maximum offset between central estimates of the long term trajectory of the Cenozoic pH reconstruction of Rae et al. (2021) and our pH (shown in Figure 3) occurs during the Miocene (at approximately 12 Ma) and is 0.15 units in scale. All other factors being equal, a fall in pH of 0.15 units would suggest an increase in atmospheric CO₂ concentration of roughly 50%. Naïvely scaling Miocene CO₂ estimates from Rae et al. (2021) results in CO₂ concentrations of approximately 750 ppm after the Miocene Climatic Optimum (MCO). During the MCO, the offset between our predicted pH and previous work is slightly smaller, which would suggest (again, assuming all other factors are equal) an increase in atmospheric CO₂ of 45% relative to Rae et al. (2021). These suggestions of increased CO₂ relative to previous work come with the important caveat that, as mentioned above, the constraints on $\delta^{11}\text{B}_{\text{sw}}$ in this interval are highly variable, perhaps suggesting additional complicating factors which make $\delta^{11}\text{B}_{\text{sw}}$ difficult to estimate at this time. Our reconstruction of $\delta^{11}\text{B}_{\text{sw}}$ (and consequently pH) has high overall uncertainties during the Neogene to reflect this. We encourage future work to provide additional constraints in this interval and across the Cenozoic.

Secondly, uncertainties remain in estimates of the second carbonate system parameter in the Miocene and throughout the Cenozoic. The difference in estimated CO₂ from this work and Rae et al. (2021) may be partially or wholly ameliorated by changing our expectations of the second carbonate system parameter. In this case, the suggested higher atmospheric CO₂ could be averted by a reduction in DIC relative to previous estimates - or the reality could lie somewhere in between, with atmospheric CO₂ concentration mildly elevated compared to previous reconstructions, and DIC mildly lowered. Understanding of possible ocean DIC at this time is mostly derived from carbon cycle box models, supplemented by suggestions from the B/Ca proxy (Sosdian et al., 2018). The range in DIC estimates is from roughly 1200 $\mu\text{mol}/\text{kg}$ to 2500 $\mu\text{mol}/\text{kg}$, meaning we are unable to disambiguate whether this record is truly indicative of higher CO₂ concentrations at this time, or lower DIC concentrations, or a combination of both.

6 Benefits of the Gaussian Process Approach

The Gaussian Process methodology allows us to integrate data constraints with limitations on the rate of change in $\delta^{11}\text{B}_{\text{sw}}$ from modelling, and (as described in Section 3) by tweaking the standard approach we are able to incorporate constraints with non-Gaussian uncertainty structures. Uncertainty in the reconstruction itself behaves intuitively, such that the spread in the reconstruction is guided by uncertainties in the data where available, and grows larger with increasing separation from data constraints. The shape of the reconstruction is not specified *a priori*, as would be the case with parametric fits. Instead, the reconstruction can take on almost any shape as guided by the data constraints and chosen hyperparameters, allowing us to model arbitrary shapes in the evolution of $\delta^{11}\text{B}_{\text{sw}}$ - and the other isotope systems reconstructed here (Figure 4).

While the standard Gaussian process (constrained by data with Gaussian uncertainties) can directly predict the mean and variance of the signal being reconstructed, our approach is reliant on drawing samples from the Gaussian Process and then filtering them to adjust the posterior prediction. Once this process is complete we have 10,000 possible time series which are plausible evolutions in $\delta^{11}\text{B}_{\text{sw}}$ over the last 65 Myr. The 10,000 possible evolutions can be summarised by their mean, median, and/or 95% confidence interval, but retaining each of the possibilities makes it possible to propagate uncertainties into future data products. For instance, uncertainty in palaeo pH can be propagated by using a Monte Carlo approach whereby each of these evolutions is sampled alongside other required parameters to provide 10,000 possible evolutions of pH. Keep-

523 ing each possible evolution maintains the embedded covariance structure, meaning that
 524 it is possible to calculate derivative properties (such as the change in $\delta^{11}\text{B}_{\text{sw}}$ or pH be-
 525 tween one time and another), which would not be possible to do from metrics such as
 526 the mean and standard deviation. This is particularly beneficial in the context of recon-
 527 structing the palaeo carbonate system as trends in parameters are often more robust than
 528 their absolute value. For instance, for short time windows (relative to the residence time
 529 of boron), although we may not know the absolute value of $\delta^{11}\text{B}_{\text{sw}}$, we believe that it
 530 can not have changed substantially. Combining the $\delta^{11}\text{B}_{\text{sw}}$ statistical samples generated
 531 here with a Monte Carlo approach allows uncertainty to be propagated in such a way
 532 as to explore the full range of absolute values for $\delta^{11}\text{B}_{\text{sw}}$ while each sample preserves a
 533 reasonable $\Delta\delta^{11}\text{B}_{\text{sw}}$ (see Tierney et al. (2022) for an example of how an analogous ap-
 534 proach was used to constrain change in atmospheric CO_2 concentration). As the 10,000
 535 possible evolutions of $\delta^{11}\text{B}_{\text{sw}}$ that we provide are considered equally likely, it also allows
 536 further filtering. For instance if looking at a particular time period, or new information
 537 comes to light, which means we are able to be more certain about the rate of change in
 538 $\delta^{11}\text{B}_{\text{sw}}$, then the samples provided here can be refiltered to enforce the more restrictive
 539 condition - though naturally this will result in a decreased number of valid samples and
 540 weakened statistical power.

541 In summary, we believe the Gaussian Process approach provides benefits both in
 542 being able to provide a holistic representation of our understanding of $\delta^{11}\text{B}_{\text{sw}}$ from data
 543 and modelling, but also in terms of producing results which make facilitate more sophis-
 544 ticated forms of onward uncertainty propagation.

545 7 Limitations

546 The Gaussian Process methodology used in this work has many properties that make
 547 it ideal for geochemical data interpolation, but also has a few caveats. The first is that
 548 input data constraints are expected to be Gaussian distributions. As discussed above and
 549 in Supplement S1, we adjust the standard Gaussian Process methodology by using a re-
 550 jection sampling strategy to incorporate other types of constraint.

551 The second limitation of the Gaussian Process is more fundamental. The two hy-
 552 perparameters which tune the fit describe the length scale and noise scale, as described
 553 above (Section 3). Here, we use the residence time of each element as the length scale
 554 of the Gaussian Process, however those concepts are not identical. In particular, as most
 555 signals we are reconstructing here are isotope ratios, the concept of elemental residence
 556 time is not necessarily directly applicable. Nonetheless, we believe that using the re-
 557 sidence time as a guide for the rate of change in these signals is an improvement over us-
 558 ing parametric methods, or non-parametric methods with arbitrary smoothing param-
 559 eters. In particular, for $\delta^{11}\text{B}_{\text{sw}}$, we are not strongly reliant on the assumption that the
 560 Gaussian Process length scale is equivalent to the residence time because Lemarchand
 561 et al. (2000) provide a direct rate of change estimate which we use as a constraint. Given
 562 a residence time for boron of 10 Myr, and a rate of change of $\delta^{11}\text{B}_{\text{sw}}$ of 0.1 ‰/Myr, this
 563 implies a noise scale of 1 ‰. However, 1 ‰ is a small range for uncertainty where there
 564 are no data constraints. Increasing the noise scale results in rates of change incompat-
 565 ible with rate of change presented in Lemarchand et al. (2000) unless the length scale
 566 is commensurately increased - however this is then inconsistent with our understanding
 567 of the residence time of boron in seawater. Our solution to this is to use values which
 568 permit slightly faster changes than suggested by Lemarchand et al. (2000) - a length scale
 569 of 10 Myr, but a noise scale of 2 ‰, then filtering out results which are incompatibly
 570 fast.

571 Using the Gaussian Process with the methodology described here is highly com-
 572 putationally intensive. Each generated sample has only a small change of being accepted,
 573 and it is necessary to try tens of millions of possibilities to achieve 10,000 viable statis-

574 tical samples. It is inherent in the rejection sampling methodology to be inefficient in
 575 this way, and the more criteria that are used (or the more restrictive those criteria are)
 576 the less efficient this method becomes. In future, we may look to alternative statistical
 577 techniques to increase our efficiency and allow us to explore a greater range of possibil-
 578 ities, in particular with respect to gradient limitations and signal smoothness.

579 Our reconstruction of $\delta^{11}\text{B}_{\text{sw}}$ is also limited by our understanding of past ocean
 580 conditions. As discussed in Section 1, most constraints on $\delta^{11}\text{B}_{\text{sw}}$ are at some level de-
 581 pendent on models. Typically, a wide range of model conditions were used to predict ver-
 582 tical gradients in $\delta^{13}\text{C}$ and pH, and an even wider range was used in uncertainty propa-
 583 gation to calculate these estimates (see for instance, Greenop et al. (2017)). Nonethe-
 584 less, it would be remiss not to acknowledge that models are a simplification of reality,
 585 meaning it is possible that ocean occupied a different mode in the past where the ver-
 586 tical gradients in $\delta^{13}\text{C}$ and pH were decoupled or otherwise difficult to predict. Over-
 587 all, the data constraints in this work are contingent upon carbon cycle model simulations
 588 producing realistic ranges for the $\delta^{13}\text{C}$ vs pH gradient, and the validity of assumptions
 589 which determine AOU, while our reconstruction itself is dependent on these data and
 590 the rate of change determined from modelling of the boron cycle.

591 8 Conclusions

592 We provide Cenozoic reconstructions of $\delta^{11}\text{B}_{\text{sw}}$ by collating existing data constraints
 593 and integrating these into a Gaussian Process based statistical approach. This allows us
 594 to bring together varying types of constraint (including central estimates, lower and up-
 595 per limits, and other forms of distribution) while rigorously propagating uncertainties.
 596 Our results suggest that $\delta^{11}\text{B}_{\text{sw}}$ was slightly higher than previously thought during the
 597 Miocene, but are generally in agreement with previous estimates of $\delta^{11}\text{B}_{\text{sw}}$ during the
 598 remainder of the Cenozoic. Generally speaking, uncertainties on $\delta^{11}\text{B}_{\text{sw}}$ are approximately
 599 1 ‰, apart from during the Neogene where large uncertainties on data constraints prop-
 600 agate to large uncertainties in our reconstruction. Our higher estimated $\delta^{11}\text{B}_{\text{sw}}$ is indica-
 601 tive of lower Miocene pH than previously thought, though we acknowledge high uncer-
 602 tainties during this time.

603 We see an notable correspondence between $\delta^{11}\text{B}_4$ and $\delta^7\text{Li}$, something which has
 604 previously been used to infer that $\delta^{11}\text{B}_{\text{sw}}$ likely followed a similar trajectory to $\delta^7\text{Li}$ (Raitzsch
 605 & Hönisch, 2013). However the evolution of $\delta^{11}\text{B}_{\text{sw}}$ constrained here shows that the ma-
 606 jority of the Cenozoic change in $\delta^{11}\text{B}_4$ was driven by pH, indicating that links between
 607 the controls on pH and $\delta^7\text{Li}$ are perhaps the more important control on the similar tra-
 608 jectories of $\delta^{11}\text{B}_4$ and $\delta^7\text{Li}$.

609 Uncertainties in our reconstruction are largest where boron isotope data are sparse,
 610 such as during the Oligocene, or where datapoints are in disagreement with one another,
 611 such as during the Neogene, and we encourage the generation of future records to tar-
 612 get these intervals. Looking forward, it would undoubtedly be helpful to find more di-
 613 rect proxies for $\delta^{11}\text{B}_{\text{sw}}$, and to improve constraints on the various models which guide
 614 both the data constraints, and limits on the rate of change in $\delta^{11}\text{B}_{\text{sw}}$. However, using
 615 this method we are able to constrain $\delta^{11}\text{B}_{\text{sw}}$ to a range of ± 1 ‰ across most of the Ceno-
 616 zoic, improving current estimates. Results from this study can be used to propagate un-
 617 certainties in $\delta^{11}\text{B}_{\text{sw}}$ into future reconstructions of palaeo pH from boron isotopes and,
 618 by extension, palaeo CO_2 . We provide both the metrics which describe our reconstruc-
 619 tion of $\delta^{11}\text{B}_{\text{sw}}$ (the median, and 95% confidence interval), but also provide 10,000 sta-
 620 tistical samples of possible evolutions of $\delta^{11}\text{B}_{\text{sw}}$. Uncertainty in $\delta^{11}\text{B}_{\text{sw}}$ can then be prop-
 621 agated into future data products using a Monte Carlo approach as described in Section 6.
 622 In addition we provide analogous information for all signals reconstructed here using the
 623 Gaussian Process ($\delta^{11}\text{B}_4$, pH, $^{87/86}\text{Sr}$, $^{187/188}\text{Os}$, and $\delta^7\text{Li}$).

9 Open Research

9.1 Data Availability

All code used in and produced by this project is stored within our GitHub Repository: <https://github.com/St-Andrews-Isotope-Geochemistry/d11Bsw-Gaussian-Process> and a final version will be archived on Zenodo on publication. Data files associated with this project are currently privately shared at the following link: <https://figshare.com/s/043a054532aea2348125>, and by the time of publication will be permanently and publically archived. Three data files are provided which include:

- Data output for $\delta^{11}\text{B}_{\text{sw}}$ in the form of a .xlsx file, which contains both summary metrics and all 10,000 time series realisations.
- Original data, metrics summary of the reconstruction, and 10,000 individual statistical samples for $^{87/86}\text{Sr}$, $^{187/188}\text{Os}$, and $\delta^7\text{Li}$ in a .xlsx file.
- Metrics summary of the reconstruction, and individual statistical samples for $\delta^{11}\text{B}_4$ and pH in a .xlsx file.

Two forms of output for $\delta^{11}\text{B}_{\text{sw}}$ are given, because while the median and 95% confidence interval give a sense of reasonable values and allow easy plotting, they are unable to convey the covariance embedded in each Gaussian Process sample. Thus for uncertainty propagation in future calculations, we recommend using the time series contained within the .xlsx file. This methodology allows propagation of both uncertainties in $\delta^{11}\text{B}_{\text{sw}}$ and also the rate of change of $\delta^{11}\text{B}_{\text{sw}}$ as described in Section 6.

9.2 Software Availability

Software used in the project is written in Python, and is available on our GitHub repository during peer review: <https://github.com/St-Andrews-Isotope-Geochemistry/d11Bsw-Gaussian-Process>, and will be permanently archived on Zenodo on publication. It uses a software package we've written to perform the statistical calculations, in particular representing distributions, drawing samples, and performing the Gaussian Process interpolation. Scripts to perform the calculation, analyse the output, and display the results are also included.

References

- Anagnostou, E., John, E. H., Babila, T. L., Sexton, P. F., Ridgwell, A., Lunt, D. J., ... Foster, G. L. (2020, September). Proxy evidence for state-dependence of climate sensitivity in the Eocene greenhouse. *Nature Communications*, *11*(1), 4436. doi: 10.1038/s41467-020-17887-x
- Anagnostou, E., John, E. H., Edgar, K. M., Foster, G. L., Ridgwell, A., Inglis, G. N., ... Pearson, P. N. (2016, May). Changing atmospheric CO₂ concentration was the primary driver of early Cenozoic climate. *Nature*, *533*(7603), 380–384. doi: 10.1038/nature17423
- Badger, M. P. S., Lear, C. H., Pancost, R. D., Foster, G. L., Bailey, T. R., Leng, M. J., & Abels, H. A. (2013). CO₂ drawdown following the middle Miocene expansion of the Antarctic Ice Sheet. *Paleoceanography*, *28*(1), 42–53. doi: 10.1002/palo.20015
- Boudreau, B. P., Middelburg, J. J., Shuijs, A., & van der Ploeg, R. (2019, April). Secular variations in the carbonate chemistry of the oceans over the Cenozoic. *Earth and Planetary Science Letters*, *512*, 194–206. doi: 10.1016/j.epsl.2019.02.004
- Broecker, W. S., & Peng, Tsung-Hung. (1982). *Tracers in the Sea*. Lamont-Doherty Geological Observatory, Columbia University.
- Caves Rugenstein, J. K., Ibarra, D. E., & von Blanckenburg, F. (2019, July). Neo-

- 672 gene cooling driven by land surface reactivity rather than increased weathering
673 fluxes. *Nature*, *571*(7763), 99–102. doi: 10.1038/s41586-019-1332-y
- 674 Chalk, T. B., Hain, M. P., Foster, G. L., Rohling, E. J., Sexton, P. F., Badger,
675 M. P. S., . . . Wilson, P. A. (2017, December). Causes of ice age intensification
676 across the Mid-Pleistocene Transition. *Proceedings of the National Academy of*
677 *Sciences*, *114*(50), 13114–13119. doi: 10.1073/pnas.1702143114
- 678 de la Vega, E., Chalk, T. B., Wilson, P. A., Bysani, R. P., & Foster, G. L. (2020,
679 July). Atmospheric CO₂ during the Mid-Piacenzian Warm Period and the M2
680 glaciation. *Scientific Reports*, *10*(1), 11002. doi: 10.1038/s41598-020-67154-8
- 681 Derry, L. A. (2022, November). Carbonate weathering, CO₂ redistribution, and
682 Neogene CCD and pCO₂ evolution. *Earth and Planetary Science Letters*, *597*,
683 117801. doi: 10.1016/j.epsl.2022.117801
- 684 Dickson, A., & Goyet, C. (1994). Handbook of methods for the analysis of the vari-
685 ous parameters of the carbon dioxide system in sea water; version 2. In *DOE*.
- 686 Dyez, K. A., Hönisch, B., & Schmidt, G. A. (2018). Early Pleistocene Obliquity-
687 Scale pCO₂ Variability at 1.5 Million Years Ago. *Paleoceanography and Paleo-*
688 *climatology*, *33*(11), 1270–1291. doi: 10.1029/2018PA003349
- 689 Findlay, H., Artioli, Y., Birchenough, S., Hartman, S., Leon, P., & Stiasny, M.
690 (2022). Ocean acidification around the UK and Ireland. *MCCIP Rolling*
691 *Evidence Updates*, 24 pages. doi: 10.14465/2022.REU03.OAC
- 692 Foster, G. L. (2008, July). Seawater pH, pCO₂ and [CO₂-3] variations in the
693 Caribbean Sea over the last 130 kyr: A boron isotope and B/Ca study of
694 planktic foraminifera. *Earth and Planetary Science Letters*, *271*(1), 254–266.
695 doi: 10.1016/j.epsl.2008.04.015
- 696 Foster, G. L., Lear, C. H., & Rae, J. W. B. (2012, August). The evolution of pCO₂,
697 ice volume and climate during the middle Miocene. *Earth and Planetary Sci-*
698 *ence Letters*, *341–344*, 243–254. doi: 10.1016/j.epsl.2012.06.007
- 699 Foster, G. L., Pogge von Strandmann, P. a. E., & Rae, J. W. B. (2010). Boron
700 and magnesium isotopic composition of seawater. *Geochemistry, Geophysics,*
701 *Geosystems*, *11*(8). doi: 10.1029/2010GC003201
- 702 Greenop, R., Foster, G. L., Wilson, P. A., & Lear, C. H. (2014). Middle Miocene cli-
703 mate instability associated with high-amplitude CO₂ variability. *Paleoceanog-*
704 *raphy*, *29*(9), 845–853. doi: 10.1002/2014PA002653
- 705 Greenop, R., Hain, M. P., Sosdian, S. M., Oliver, K. I. C., Goodwin, P., Chalk,
706 T. B., . . . Foster, G. L. (2017, February). A record of Neogene seawater $\delta^{11}\text{B}$
707 reconstructed from paired $\delta^{11}\text{B}$ analyses on benthic and planktic foraminifera.
708 *Climate of the Past*, *13*(2), 149–170. doi: 10.5194/cp-13-149-2017
- 709 Greenop, R., Sosdian, S. M., Henahan, M. J., Wilson, P. A., Lear, C. H., & Foster,
710 G. L. (2019). Orbital Forcing, Ice Volume, and CO₂ Across the Oligocene-
711 Miocene Transition. *Paleoceanography and Paleoclimatology*, *34*(3), 316–328.
712 doi: 10.1029/2018PA003420
- 713 Gutjahr, M., Ridgwell, A., Sexton, P. F., Anagnostou, E., Pearson, P. N., Pälike,
714 H., . . . Foster, G. L. (2017, August). Very large release of mostly volcanic
715 carbon during the Palaeocene–Eocene Thermal Maximum. *Nature*, *548*(7669),
716 573–577. doi: 10.1038/nature23646
- 717 Hain, M. P., Foster, G. L., & Chalk, T. (2018, October). Robust Constraints on
718 Past CO₂ Climate Forcing From the Boron Isotope Proxy. *Paleoceanography*
719 *and Paleoclimatology*, *33*(10), 1099–1115. doi: 10.1029/2018PA003362
- 720 Hain, M. P., Sigman, D. M., & Haug, G. H. (2010). Carbon dioxide effects of
721 Antarctic stratification, North Atlantic Intermediate Water formation, and
722 subantarctic nutrient drawdown during the last ice age: Diagnosis and syn-
723 thesis in a geochemical box model. *Global Biogeochemical Cycles*, *24*(4). doi:
724 10.1029/2010GB003790
- 725 Hain, M. P., Sigman, D. M., Higgins, J. A., & Haug, G. H. (2015). The effects of
726 secular calcium and magnesium concentration changes on the thermodynam-

- 727 ics of seawater acid/base chemistry: Implications for Eocene and Cretaceous
 728 ocean carbon chemistry and buffering. *Global Biogeochemical Cycles*, 29(5),
 729 517–533. doi: 10.1002/2014GB004986
- 730 Harper, D. T., Hönisch, B., Zeebe, R. E., Shaffer, G., Haynes, L. L., Thomas, E., &
 731 Zachos, J. C. (2020). The Magnitude of Surface Ocean Acidification and Car-
 732 bon Release During Eocene Thermal Maximum 2 (ETM-2) and the Paleocene-
 733 Eocene Thermal Maximum (PETM). *Paleoceanography and Paleoclimatology*,
 734 35(2), e2019PA003699. doi: 10.1029/2019PA003699
- 735 Haynes, L. L., Hönisch, B., Dyez, K. A., Holland, K., Rosenthal, Y., Fish, C. R.,
 736 ... Rae, J. W. B. (2017). Calibration of the B/Ca proxy in the planktic
 737 foraminifer *Orbulina universa* to Paleocene seawater conditions. *Paleoceanogra-*
 738 *phy*, 32(6), 580–599. doi: 10.1002/2016PA003069
- 739 Henehan, M. J., Edgar, K. M., Foster, G. L., Penman, D. E., Hull, P. M., Greenop,
 740 R., ... Pearson, P. N. (2020). Revisiting the Middle Eocene Climatic Op-
 741 timum “Carbon Cycle Conundrum” With New Estimates of Atmospheric
 742 pCO₂ From Boron Isotopes. *Paleoceanography and Paleoclimatology*, 35(6),
 743 e2019PA003713. doi: 10.1029/2019PA003713
- 744 Henehan, M. J., Ridgwell, A., Thomas, E., Zhang, S., Alegret, L., Schmidt, D. N.,
 745 ... Hull, P. M. (2019, November). Rapid ocean acidification and protracted
 746 Earth system recovery followed the end-Cretaceous Chicxulub impact. *Pro-*
 747 *ceedings of the National Academy of Sciences*, 116(45), 22500–22504. doi:
 748 10.1073/pnas.1905989116
- 749 Henehan, M. J., & Witts, J. D. (2023, May). Continental flood basalts do not
 750 drive later Phanerozoic extinctions. *Proceedings of the National Academy of*
 751 *Sciences*, 120(21), e2303700120. doi: 10.1073/pnas.2303700120
- 752 Hönisch, B., Hemming, N. G., Archer, D., Siddall, M., & McManus, J. F. (2009).
 753 Atmospheric Carbon Dioxide Concentration across the Mid-Pleistocene Transi-
 754 tion. *Science*, 324(5934), 1551–1554.
- 755 Hull, P. M., Osborn, K. J., Norris, R. D., & Robison, B. H. (2011). Seasonality
 756 and depth distribution of a mesopelagic foraminifer, *Hastigerinella digitata*, in
 757 Monterey Bay, California. *Limnology and Oceanography*, 56(2), 562–576. doi:
 758 10.4319/lo.2011.56.2.0562
- 759 Josso, P., Parkinson, I., Horstwood, M., Lusty, P., Chenery, S., & Murton, B. (2019,
 760 May). Improving confidence in ferromanganese crust age models: A compos-
 761 ite geochemical approach. *Chemical Geology*, 513, 108–119. doi: 10.1016/j
 762 .chemgeo.2019.03.003
- 763 Klemm, V., Levasseur, S., Frank, M., Hein, J. R., & Halliday, A. N. (2005, Septem-
 764 ber). Osmium isotope stratigraphy of a marine ferromanganese crust. *Earth*
 765 *and Planetary Science Letters*, 238(1), 42–48. doi: 10.1016/j.epsl.2005.07.016
- 766 Klochko, K., Kaufman, A. J., Yao, W., Byrne, R. H., & Tossell, J. A. (2006,
 767 August). Experimental measurement of boron isotope fractionation in
 768 seawater. *Earth and Planetary Science Letters*, 248(1), 276–285. doi:
 769 10.1016/j.epsl.2006.05.034
- 770 Lemarchand, D., Gaillardet, J., Lewin, É., & Allègre, C. J. (2000, December). The
 771 influence of rivers on marine boron isotopes and implications for reconstructing
 772 past ocean pH. *Nature*, 408(6815), 951–954. doi: 10.1038/35050058
- 773 Marschall, H., & Foster, G. (Eds.). (2018). *Boron Isotopes*. Cham: Springer Interna-
 774 tional Publishing. doi: 10.1007/978-3-319-64666-4
- 775 Martínez-Botí, M. A., Foster, G. L., Chalk, T. B., Rohling, E. J., Sexton, P. F.,
 776 Lunt, D. J., ... Schmidt, D. N. (2015, February). Plio-Pleistocene climate
 777 sensitivity evaluated using high-resolution CO₂ records. *Nature*, 518(7537),
 778 49–54. doi: 10.1038/nature14145
- 779 Misra, S., & Froelich, P. N. (2012, February). Lithium Isotope History of Ceno-
 780 zoic Seawater: Changes in Silicate Weathering and Reverse Weathering. *Sci-*
 781 *ence*, 335(6070), 818–823. doi: 10.1126/science.1214697

- 822 Nir, O., Vengosh, A., Harkness, J. S., Dwyer, G. S., & Lahav, O. (2015, March).
823 Direct measurement of the boron isotope fractionation factor: Reducing the
824 uncertainty in reconstructing ocean paleo-pH. *Earth and Planetary Science*
825 *Letters*, *414*, 1–5. doi: 10.1016/j.epsl.2015.01.006
- 826 Oxburgh, R. (1998, June). Variations in the osmium isotope composition of sea wa-
827 ter over the past 200,000 years. *Earth and Planetary Science Letters*, *159*(3),
828 183–191. doi: 10.1016/S0012-821X(98)00057-0
- 829 Oxburgh, R. (2001). Residence time of osmium in the oceans. *Geochemistry, Geo-*
830 *physics, Geosystems*, *2*(6). doi: 10.1029/2000GC000104
- 831 Oxburgh, R., Pierson-Wickmann, A.-C., Reisberg, L., & Hemming, S. (2007, Novem-
832 ber). Climate-correlated variations in seawater 187Os/188Os over the past
833 200,000 yr: Evidence from the Cariaco Basin, Venezuela. *Earth and Planetary*
834 *Science Letters*, *263*(3), 246–258. doi: 10.1016/j.epsl.2007.08.033
- 835 Palmer, M. R., Pearson, P. N., & Cobb, S. J. (1998, November). Reconstructing
836 Past Ocean pH-Depth Profiles. *Science*, *282*(5393), 1468–1471. doi: 10.1126/
837 science.282.5393.1468
- 838 Paquay, F. S., Ravizza, G., & Coccioni, R. (2014, November). The influence of ex-
839 traterrestrial material on the late Eocene marine Os isotope record. *Geochim-*
840 *ica et Cosmochimica Acta*, *144*, 238–257. doi: 10.1016/j.gca.2014.08.024
- 841 Paquay, F. S., Ravizza, G. E., Dalai, T. K., & Peucker-Ehrenbrink, B. (2008, April).
842 Determining Chondritic Impactor Size from the Marine Osmium Isotope
843 Record. *Science*, *320*(5873), 214–218. doi: 10.1126/science.1152860
- 844 Paris, G., Gaillardet, J., & Louvat, P. (2010, November). Geological evolution of
845 seawater boron isotopic composition recorded in evaporites. *Geology*, *38*(11),
846 1035–1038. doi: 10.1130/G31321.1
- 847 Park, H., & Schlesinger, W. H. (2002). Global biogeochemical cycle of boron. *Global*
848 *Biogeochemical Cycles*, *16*(4), 20-1-20-11. doi: 10.1029/2001GB001766
- 849 Pearson, P. N., Foster, G. L., & Wade, B. S. (2009, October). Atmospheric carbon
850 dioxide through the Eocene–Oligocene climate transition. *Nature*, *461*(7267),
851 1110–1113. doi: 10.1038/nature08447
- 852 Pegram, W. J., & Turekian, K. K. (1999, December). The osmium isotopic compo-
853 sition change of Cenozoic sea water as inferred from a deep-sea core corrected
854 for meteoritic contributions. *Geochimica et Cosmochimica Acta*, *63*(23), 4053–
855 4058. doi: 10.1016/S0016-7037(99)00308-7
- 856 Penman, D. E., Hönisch, B., Zeebe, R. E., Thomas, E., & Zachos, J. C. (2014).
857 Rapid and sustained surface ocean acidification during the Paleocene-
858 Eocene Thermal Maximum. *Paleoceanography*, *29*(5), 357–369. doi:
859 10.1002/2014PA002621
- 860 Peucker-Ehrenbrink, B., & Ravizza, G. (2000, June). The effects of sampling
861 artifacts on cosmic dust flux estimates: A reevaluation of nonvolatile trac-
862 ers (Os, Ir). *Geochimica et Cosmochimica Acta*, *64*(11), 1965–1970. doi:
863 10.1016/S0016-7037(99)00429-9
- 864 Peucker-Ehrenbrink, B., & Ravizza, G. E. (2020, January). Chapter 8 - Osmium
865 Isotope Stratigraphy. In F. M. Gradstein, J. G. Ogg, M. D. Schmitz, &
866 G. M. Ogg (Eds.), *Geologic Time Scale 2020* (pp. 239–257). Elsevier. doi:
867 10.1016/B978-0-12-824360-2.00008-5
- 868 Rae, Zhang, Y. G., Liu, X., Foster, G. L., Stoll, H. M., & Whiteford, R. D. (2021,
869 May). Atmospheric CO₂ over the Past 66 Million Years from Marine Archives.
870 *Annual Review of Earth and Planetary Sciences*, *49*(1), 609–641. doi: 10.1146/
871 annurev-earth-082420-063026
- 872 Rae, J. W. B. (2018). Boron Isotopes in Foraminifera: Systematics, Biomineralisa-
873 tion, and CO₂ Reconstruction. In H. Marschall & G. Foster (Eds.), *Boron Iso-*
874 *topes: The Fifth Element* (pp. 107–143). Cham: Springer International Pub-
875 lishing. doi: 10.1007/978-3-319-64666-4_5
- 876 Raitzsch, M., Hain, M., Henehan, M., & Gattuso, J.-P. (2022, January). *Seacarb* -

- 837 *seacarb extension for deep-time carbonate system calculations*. Zenodo. doi: 10
838 .5281/zenodo.5909811
- 839 Raitzsch, M., & Hönisch, B. (2013, May). Cenozoic boron isotope variations in ben-
840 thic foraminifers. *Geology*, *41*(5), 591–594. doi: 10.1130/G34031.1
- 841 Ravizza, G. (1993, July). Variations of the 187Os/186Os ratio of seawater
842 over the past 28 million years as inferred from metalliferous carbonates.
843 *Earth and Planetary Science Letters*, *118*(1), 335–348. doi: 10.1016/
844 0012-821X(93)90177-B
- 845 Ravizza, G., Norris, R. N., Blusztajn, J., & Aubry, M. P. (2001). An osmium isotope
846 excursion associated with the Late Paleocene thermal maximum: Evidence
847 of intensified chemical weathering. *Paleoceanography*, *16*(2), 155–163. doi:
848 10.1029/2000PA000541
- 849 Ravizza, G., & Peucker-Ehrenbrink, B. (2003, May). The marine 187Os/188Os
850 record of the Eocene–Oligocene transition: The interplay of weathering and
851 glaciation. *Earth and Planetary Science Letters*, *210*(1), 151–165. doi:
852 10.1016/S0012-821X(03)00137-7
- 853 Ravizza, G., & Turekian, K. K. (1992, May). The osmium isotopic composition
854 of organic-rich marine sediments. *Earth and Planetary Science Letters*, *110*(1),
855 1–6. doi: 10.1016/0012-821X(92)90034-S
- 856 Reusch, D. N., Ravizza, G., Maasch, K. A., & Wright, J. D. (1998, July). Miocene
857 seawater 187Os/188Os ratios inferred from metalliferous carbonates. *Earth and*
858 *Planetary Science Letters*, *160*(1), 163–178. doi: 10.1016/S0012-821X(98)00082
859 -X
- 860 Ridgwell, A., Hargreaves, J. C., Edwards, N. R., Annan, J. D., Lenton, T. M.,
861 Marsh, R., ... Watson, A. (2007, January). Marine geochemical data as-
862 similation in an efficient Earth System Model of global biogeochemical cycling.
863 *Biogeosciences*, *4*(1), 87–104. doi: 10.5194/bg-4-87-2007
- 864 Ridgwell, A., & Zeebe, R. (2005, June). The role of the global carbonate cycle in
865 the regulation and evolution of the Earth system. *Earth and Planetary Science*
866 *Letters*, *234*(3–4), 299–315. doi: 10.1016/j.epsl.2005.03.006
- 867 Roberts, J., Kaczmarek, K., Langer, G., Skinner, L. C., Bijma, J., Bradbury, H.,
868 ... Misra, S. (2018, September). Lithium isotopic composition of benthic
869 foraminifera: A new proxy for paleo-pH reconstruction. *Geochimica et Cos-*
870 *mochimica Acta*, *236*, 336–350. doi: 10.1016/j.gca.2018.02.038
- 871 Robinson, N., Ravizza, G., Coccioni, R., Peucker-Ehrenbrink, B., & Norris, R. (2009,
872 May). A high-resolution marine 187Os/188Os record for the late Maas-
873 trichtian: Distinguishing the chemical fingerprints of Deccan volcanism and
874 the KP impact event. *Earth and Planetary Science Letters*, *281*(3), 159–168.
875 doi: 10.1016/j.epsl.2009.02.019
- 876 Sosdian, S. M., Babila, T. L., Greenop, R., Foster, G. L., & Lear, C. H. (2020, Jan-
877 uary). Ocean Carbon Storage across the middle Miocene: A new interpretation
878 for the Monterey Event. *Nature Communications*, *11*(1), 134. doi: 10.1038/
879 s41467-019-13792-0
- 880 Sosdian, S. M., Greenop, R., Hain, M. P., Foster, G. L., Pearson, P. N., & Lear,
881 C. H. (2018, September). Constraining the evolution of Neogene ocean carbon-
882 ate chemistry using the boron isotope pH proxy. *Earth and Planetary Science*
883 *Letters*, *498*, 362–376. doi: 10.1016/j.epsl.2018.06.017
- 884 Stoffynegli, P., & Mackenzie, F. T. (1984, April). Mass balance of dissolved lithium
885 in the oceans. *Geochimica et Cosmochimica Acta*, *48*(4), 859–872. doi: 10
886 .1016/0016-7037(84)90107-8
- 887 Stoll, H. M., Guitian, J., Hernandez-Almeida, I., Mejia, L. M., Phelps, S., Polissar,
888 P., ... Ziveri, P. (2019, March). Upregulation of phytoplankton carbon con-
889 centrating mechanisms during low CO₂ glacial periods and implications for
890 the phytoplankton pCO₂ proxy. *Quaternary Science Reviews*, *208*, 1–20. doi:
891 10.1016/j.quascirev.2019.01.012

- 892 Tierney, J. E., Zhu, J., Li, M., Ridgwell, A., Hakim, G. J., Poulsen, C. J., ... Kump,
893 L. R. (2022, October). Spatial patterns of climate change across the Pale-
894 ocene–Eocene Thermal Maximum. *Proceedings of the National Academy of*
895 *Sciences*, 119(42), e2205326119. doi: 10.1073/pnas.2205326119
- 896 van der Ploeg, R., Selby, D., Cramwinckel, M. J., Li, Y., Bohaty, S. M., Middelburg,
897 J. J., & Sluijs, A. (2018, July). Middle Eocene greenhouse warming facilitated
898 by diminished weathering feedback. *Nature Communications*, 9(1), 2877. doi:
899 10.1038/s41467-018-05104-9
- 900 Vigier, N., Rollion-Bard, C., Levenson, Y., & Erez, J. (2015, January). Lithium
901 isotopes in foraminifera shells as a novel proxy for the ocean dissolved in-
902 organic carbon (DIC). *Comptes Rendus Geoscience*, 347(1), 43–51. doi:
903 10.1016/j.crte.2014.12.001
- 904 Yu, J., & Elderfield, H. (2007, June). Benthic foraminiferal B/Ca ratios reflect deep
905 water carbonate saturation state. *Earth and Planetary Science Letters*, 258(1),
906 73–86. doi: 10.1016/j.epsl.2007.03.025
- 907 Zeebe, R. E. (2012, January). LOSCAR: Long-term Ocean-atmosphere-Sediment
908 Carbon cycle Reservoir Model v2.0.4. *Geoscientific Model Development*, 5(1),
909 149–166. doi: 10.5194/gmd-5-149-2012
- 910 Zeebe, R. E., & Wolf-Gladrow, D. A. (2001). *CO₂ in seawater: Equilibrium, kinet-*
911 *ics, isotopes* (No. 65). Amsterdam ; New York: Elsevier.
- 912 Zhang, Y. G., Henderiks, J., & Liu, X. (2020, July). Refining the alkenone-pCO₂
913 method II: Towards resolving the physiological parameter ‘b’. *Geochimica et*
914 *Cosmochimica Acta*, 281, 118–134. doi: 10.1016/j.gca.2020.05.002

Figure 1.

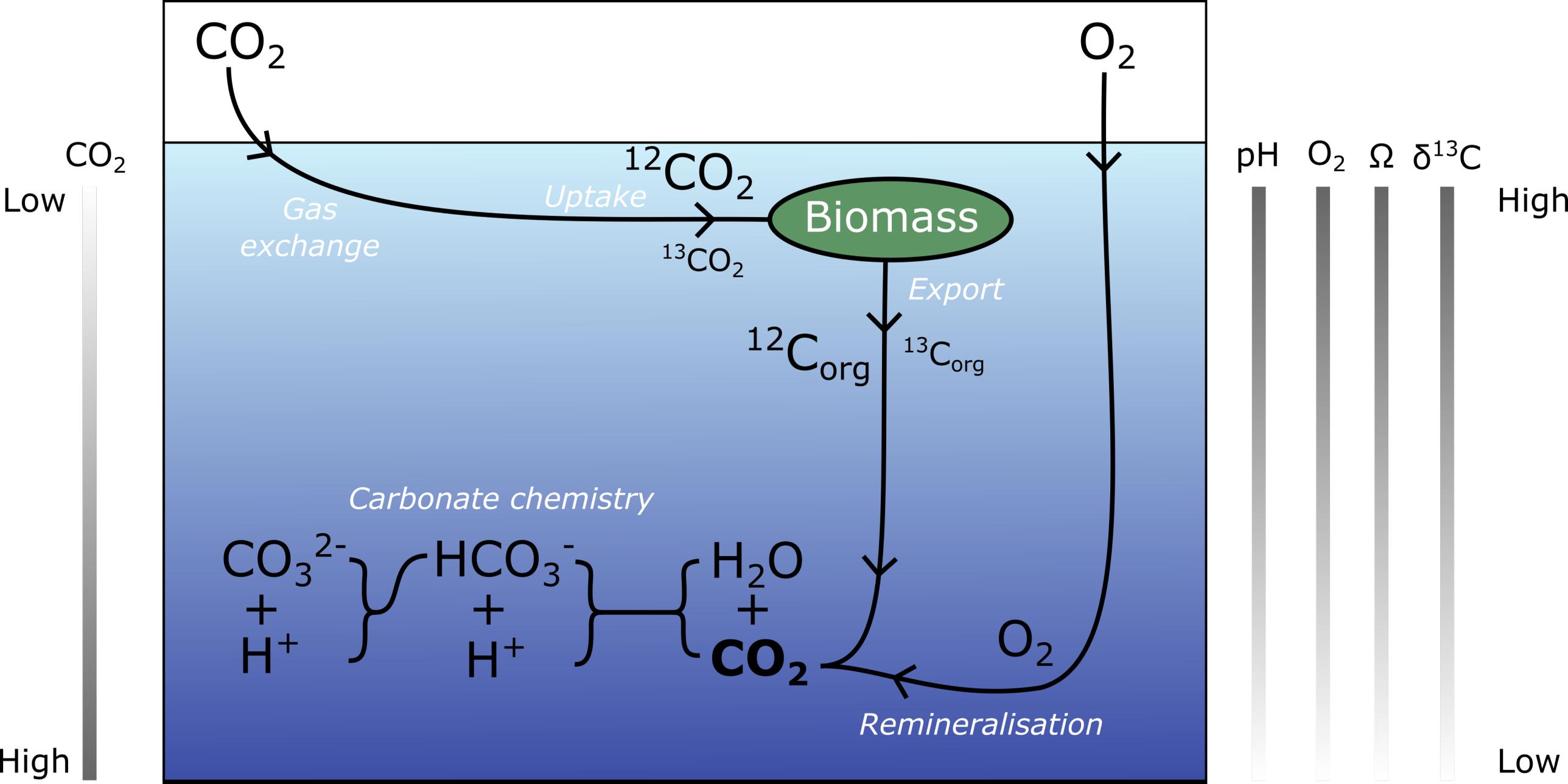


Figure 2a.

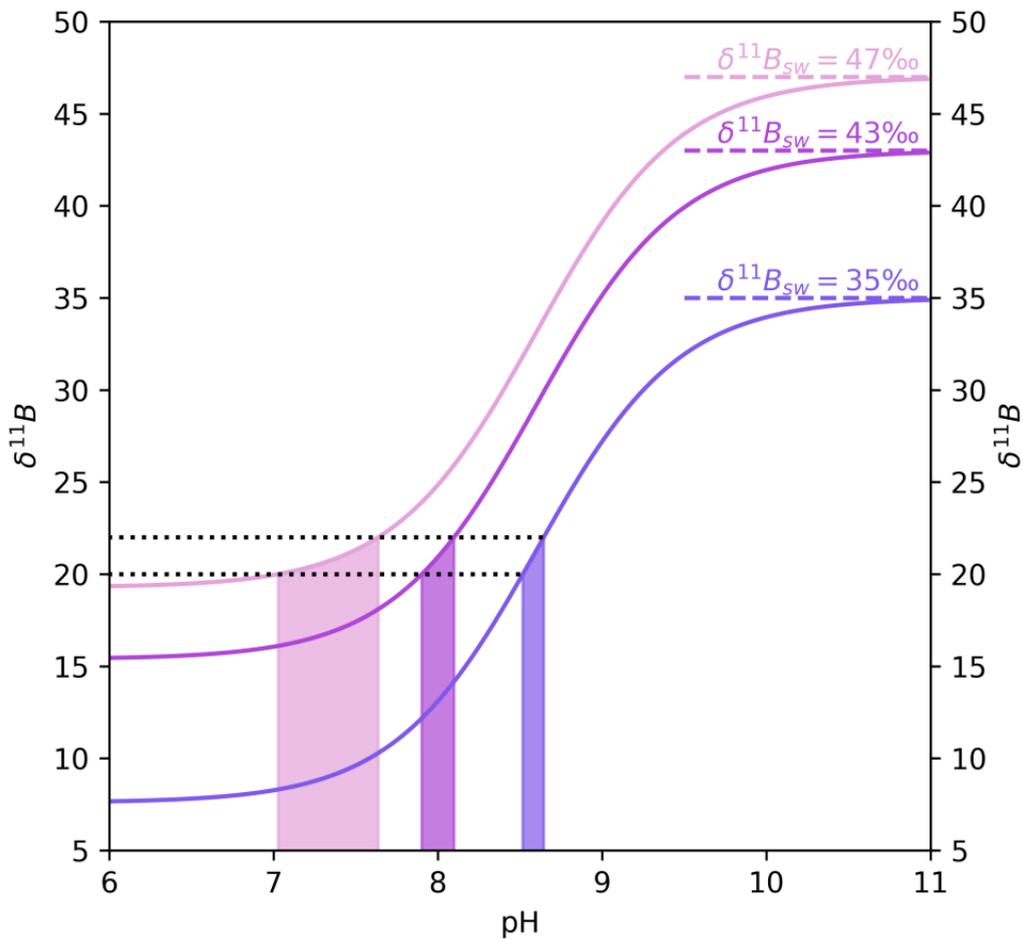


Figure 2b.

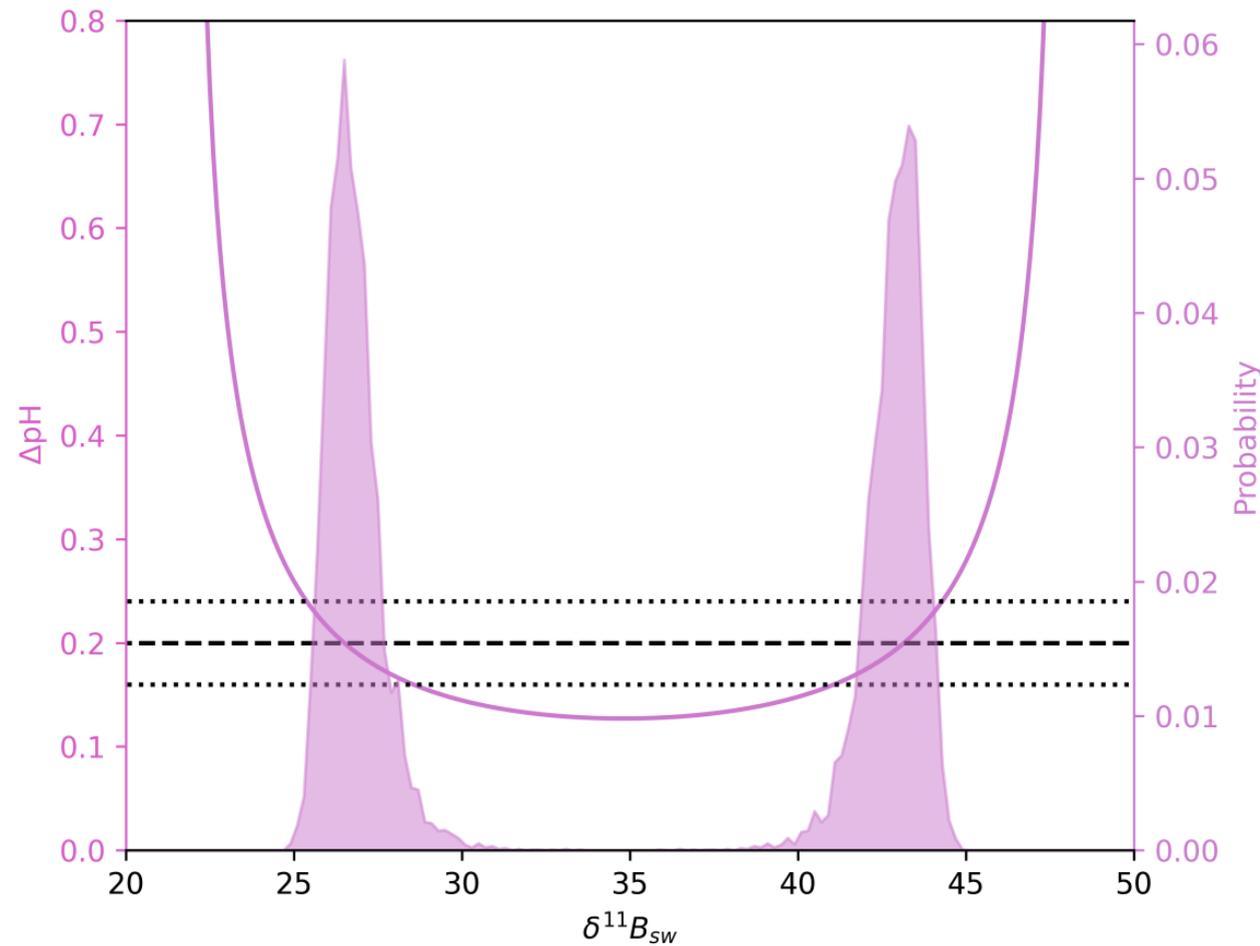


Figure 3.

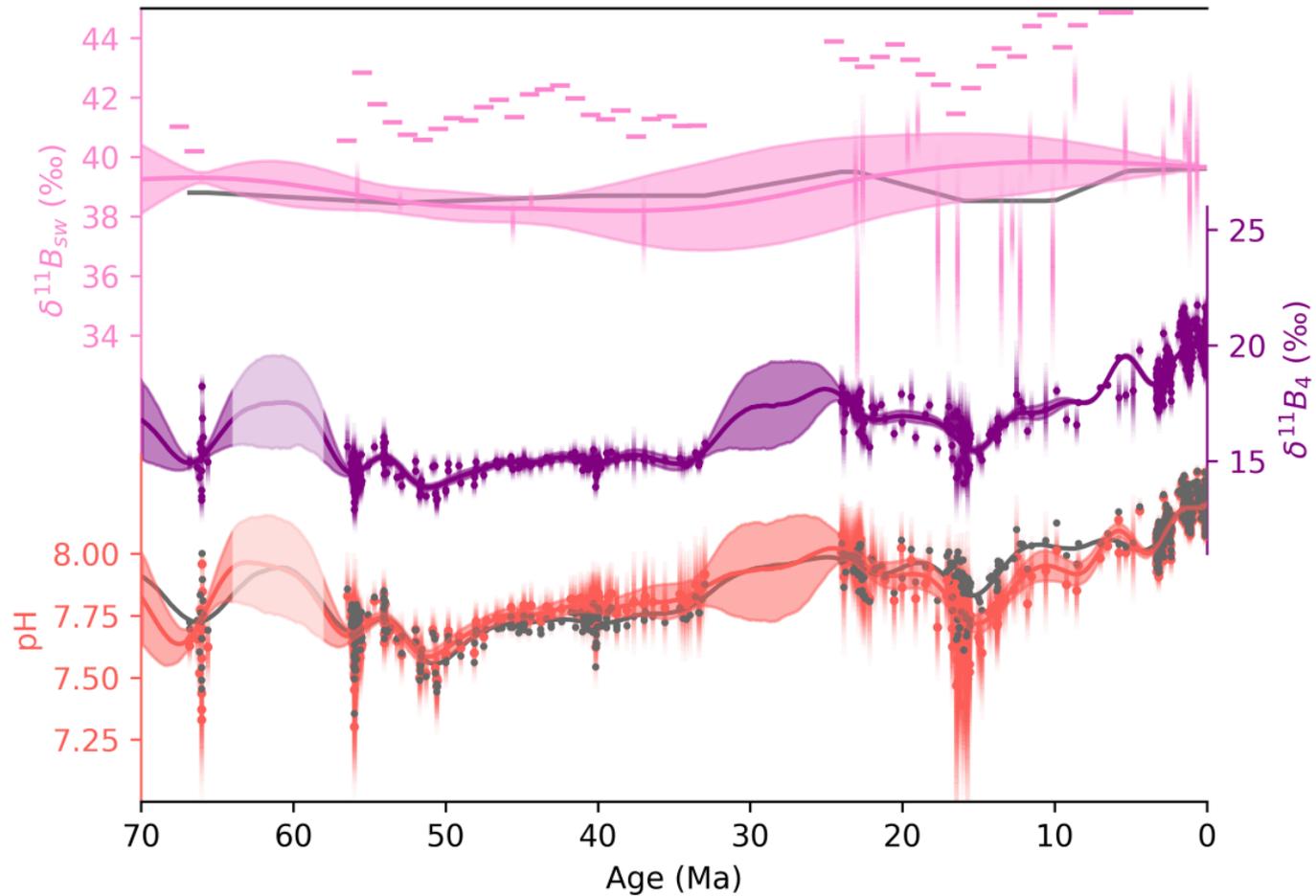


Figure 4.

