

Clouds and radiatively induced circulations

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In the atmosphere, there is an intimate relationship between clouds, atmospheric radiative cooling/heating, and radiatively induced circulations at various temporal and spatial scales. This coupling remains not well understood, which contributes to limiting our ability to model and predict clouds and climate accurately.

Cloud liquid and ice particles interact with both shortwave (SW) and longwave (LW) radiation, leading to cloud radiative effect (CRE). The CRE includes perturbations of the radiative fluxes at the top of the atmosphere (TOA) and the surface, as well as perturbations of the radiative cooling profile within the atmosphere. The effect of clouds that results in atmospheric radiative heating or cooling that is distinct from the clear-sky radiative cooling profile will be termed the CRE on atmospheric heating, or CRE-AH. The CRE-AH can significantly modify the horizontal and vertical gradients of the diabatic heating profile, inducing circulations at various scales in the atmosphere. In turn, circulations govern cloud formation and evolution processes and therefore the properties and distribution of clouds.

This chapter explores advances in research of the coupling between clouds and radiatively induced circulations and identify the paths forward. The chapter is organized into three sections. Section 1 discusses the relationship between clouds and tropospheric diabatic circulations in which condensate and precipitation are produced. Section 2 focuses on low clouds and shallow radiatively induced circulations in the boundary layer and lower free troposphere. Section 3 focuses on tropical high clouds and the circulations induced by the CRE-AH in these clouds. All the radiatively induced circulations discussed in the three sections are illustrated in Fig. 1.

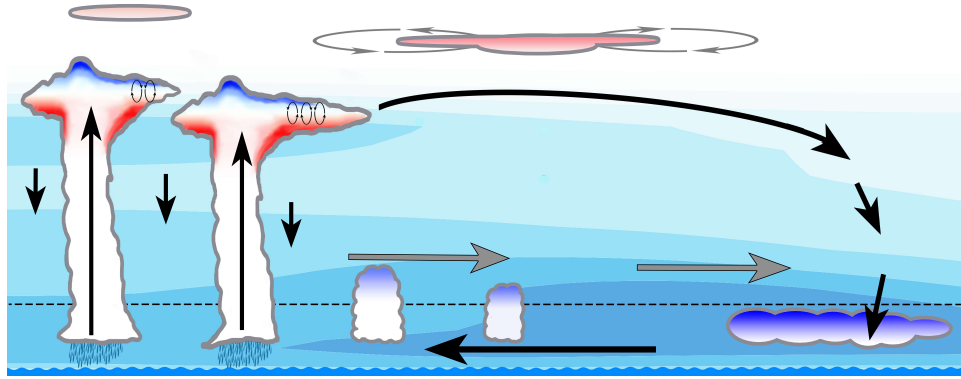


Figure 1: Illustration of the radiatively induced circulations discussed in this chapter, including tropospheric diabatic circulations (thick, black arrows, see Section 1), large-scale shallow circulations (thick, black arrows in the boundary layer and thick, grey arrows in the lower free troposphere, see Section 2), mesoscale circulations of tropical high clouds (thin, grey arrows, see Section 3), and small-scale convective motions within the anvils (thin, black arrows, see Section 3). The thin, dashed line marks the top of the boundary layer, which is located at altitudes of about 1–2 km. The background shading represents the clear-sky radiative cooling. The shading within the clouds indicates the CRE-AH. Blue indicates radiative cooling and red indicates radiative heating.

1 Clouds and tropospheric diabatic circulations

The relationship between clouds and tropospheric diabatic circulations is two-way. On the one hand, clouds are formed in the atmosphere as water vapor condenses within the moist, convective branch of these diabatic circulations. On the other hand, the perturbation in the diabatic heating profile due to the CRE-AH can feed back on to weaken or strengthen the circulations in which clouds form and evolve. In this section, we will review progresses in our understanding of this coupling, particularly in the context of the tropospheric diabatic circulations that underlie the atmospheric water cycle.

Following directly from the fact that cloud condensates are produced within the atmospheric water cycle, understanding of cloud behaviors may be obtained by studying the atmospheric water cycle. As a metric of the strength of the atmospheric water cycle, let us use the rate of condensation of water vapor in the atmosphere, i.e. the rate (in $\text{kg kg}^{-1} \text{s}^{-1}$) at which water vapor is transformed into condensate at a given location in the atmosphere. The condensation rate by itself does not dictate the percentage of condensates that remain in the atmosphere as clouds rather than falling to the surface as precipitation. But, if we assume that the percentage of cloud condensates (out of the total condensates) does not change under small perturbations of the climate, we will be able to obtain a first-order constraint on clouds based on the constraint on the condensation rate.

To formulate a constraint on the condensation rate—hereafter denoted by m_{cond} , we consider the moisture budget in the atmosphere following Schneider et al. (2010). In the free troposphere, a balanced water vapor budget in steady state is maintained between condensation and vertical advection of water vapor, i.e.

$$[m_{\text{cond}}] = -[\omega \partial_p q], \quad (1)$$

where ω is the pressure velocity, p is pressure, and q is the specific humidity. The notation $[\cdot]$ indicates that the variable between the brackets is averaged horizontally over a sufficiently large domain for which horizontal advection of water vapor into/out of the domain can be neglected. The entire globe and the tropics are examples of such a domain. Equation (1) however applies only to the free troposphere; in the boundary layer, the source of moisture that results from surface evaporation must be considered. Below, we will first focus on the free troposphere and then touch upon the complications of the boundary layer toward the end of the section.

69 In a moist convecting atmosphere, vertical advection of water vapor is
 70 upward and mostly carried out by moist convection. The updrafts inside
 71 moist convective regions are saturated with water vapor above the lifted
 72 condensation level (LCL). Thus,

$$[m_{\text{cond}}] \sim -[\omega_{\uparrow} \partial_p q_{\text{sat}}]_{\text{conv}} \sim -[\omega_{\uparrow}]_{\text{conv}} [\partial_p q_{\text{sat}}]_{\text{conv}} \quad (2)$$

73 above the LCL (c.f. Eq. 5 in Schneider et al., 2010). Here q_{sat} is the satura-
 74 tion specific humidity, ω_{\uparrow} is the upward component of the pressure velocity,
 75 and $[\cdot]_{\text{conv}}$ indicates that the variable between the square brackets is averaged
 76 over moist convective regions within the domain only.

77 Over this domain, an overturning diabatic circulation can be constructed
 78 as consisting of a moist ascending branch in which latent heat is released
 79 as water vapor condenses forming condensates and precipitation (see the
 80 upward arrows in the deep convective clouds in Fig. 1) and a dry descending
 81 branch regulated by radiative cooling (see the downward arrows in clear air
 82 in Fig. 1). A nice illustration of such an overturning diabatic circulation
 83 is Fig. 10.3 in Wallace and Hobbs (2006). Following Yano et al. (2002),
 84 Zelinka and Hartmann (2010), Bony et al. (2016), Dinh and Fueglistaler
 85 (2017, 2019), we seek to estimate the convective mass flux $[\omega_{\uparrow}]_{\text{conv}}$ as

$$[\omega_{\uparrow}]_{\text{conv}} \sim -[\omega_{\text{rad}}], \quad (3)$$

86 where

$$[\omega_{\text{rad}}] \sim \frac{[Q_{\text{rad}}]}{[\sigma]} \quad (4)$$

87 is the radiative subsidence mass flux, Q_{rad} is the radiative cooling rate,
 88 σ is the static stability, and T is atmospheric temperature. Furthermore,
 89 by assuming that the saturation specific humidity within moist convective
 90 regions scales with the domain average profile ($[\partial_p q_{\text{sat}}]_{\text{conv}} \sim [\partial_p q_{\text{sat}}]$), we
 91 obtain

$$[m_{\text{cond}}] \sim \frac{[\partial_p q_{\text{sat}}]}{[\sigma]} [Q_{\text{rad}}]. \quad (5)$$

92 Equation (5) indicates that the condensation rate depends on the radiative
 93 cooling rate as well as the factor

$$[f] = \frac{[\partial_p q_{\text{sat}}]}{[\sigma]}, \quad (6)$$

94 which is a function of atmospheric temperature. The atmospheric water
 95 cycle can be considered as driven by atmospheric radiative cooling, but

processes that affect the vertical profile of temperature can affect the condensation rate and potentially clouds as well.

The linkage between tropospheric diabatic circulations and clouds as outlined above has been used to explain how clouds would change following an increase in atmospheric CO₂ concentration and subsequent global warming. The responses of the water cycle and clouds to the radiative forcing from CO₂ increase consist of two components (Dinh and Fueglistaler, 2017): (i) rapid adjustment (Gregory et al., 2004) which occurs in the atmosphere independently of surface temperature changes and (ii) a slower response that follows surface warming. Climate models consistently predict that global precipitation and cloud water decrease during rapid atmospheric adjustment (see Dinh and Fueglistaler, 2019 and references therein). Dinh and Fueglistaler (2019) explained that the weakening of the atmospheric water cycle and decrease in cloud water are driven by the decrease in atmospheric radiative cooling, a direct result of the CO₂ increase. Atmospheric radiative cooling decreases because the added CO₂ enhances the total atmospheric absorption of the LW radiation emitted by the surface. On the other hand, the slow response following surface warming shows increases in tropical rain rate and high cloud water content (Larson and Hartmann, 2003). These changes under warming are driven by an increase in atmospheric radiative cooling, which is largely associated with increased water vapor and increased emission of LW radiation by water vapor at higher atmospheric temperatures. Further research is needed to confirm whether the increase in cloud water holds globally and to investigate the differences in the responses of tropical and extra-tropical clouds to warming.

The radiative cooling constraint on tropospheric diabatic circulations has been shown useful in evaluating the radiative climate feedback of tropical high clouds. Given that the convective mass flux is constrained by the radiative cooling ($[Q_{\text{rad}}]$) following Eqs. (3) and (4), it can be expected that tropical convection and convective anvil clouds detrains near the level in the upper troposphere where $[Q_{\text{rad}}]$ decreases rapidly with height. For the Earth’s atmosphere, $[Q_{\text{rad}}]$ is governed to a large extent by water vapor, whose vertical profile and radiative effect depend strongly on atmospheric temperature. Hartmann and Larson (2002) therefore proposed that the atmospheric temperature at which the LW radiative emission and atmospheric radiative cooling by water vapor become inefficient remains the same regardless of surface temperature. It follows that the temperature at the detrainment level and therefore the emission temperature of tropical anvil clouds remain constant as the surface warms; the clouds absorb more upwelling LW radiation from a warming surface and atmosphere below but emit the same

136 amount of LW radiation. This “fixed anvil temperature” (FAT) hypothesis
137 therefore implies a positive climate feedback of tropical anvil clouds.

138 The original FAT hypothesis does not account for the increased static
139 stability ($[\sigma]$) at the level where $[Q_{\text{rad}}]$ decreases rapidly with height. In a
140 follow-up work, Zelinka and Hartmann (2010) calculated the convergence
141 profile of tropical tropospheric diabatic circulations from the vertical gra-
142 dient of $[\omega_{\text{rad}}]$ using the clear-sky $[Q_{\text{rad}}]$ profile (see Eq. 4). They found
143 that the peak of the convergence profile shifts upward as the surface warms,
144 consistently with the upward shift of the clear-sky $[Q_{\text{rad}}]$. However, the
145 peak convergence level warms slightly and correspondingly the anvil cloud
146 temperature increases slightly as the static stability at this level increases.
147 These findings confirm that the climate feedback of tropical anvil clouds is
148 positive but of a smaller magnitude than that suggested by the original FAT
149 hypothesis.

150 Using the same argument, Bony et al. (2016) proposed that tropical anvil
151 cloud cover is expected to shrink under warming. As the climate warms, the
152 anvil clouds rise to remain at approximately the same temperature follow-
153 ing the FAT hypothesis. As the clouds rise they are embedded in a more
154 stable atmosphere. The increased stability decreases the radiatively driven
155 mass flux (see Eq. 4) and the convective outflow, leading to a reduction of
156 the anvil cloud fraction. This stability effect has been confirmed based on
157 interannual variations of anvil cloud fraction (Saint-Lu et al., 2020) in data
158 from the Cloud-Aerosol Lidar and Infrared Pathfinder Satellite Observations
159 (CALIPSO).

160 The original FAT hypothesis was developed for the tropics only, but the
161 same general behavior of atmospheric radiative cooling, which is dominated
162 by water vapor, also holds in the extra-tropics (Thompson et al., 2017). The
163 pressure level in the upper troposphere at which the clear-sky atmospheric
164 radiative cooling profile decreases rapidly with height thus defines the top
165 of the troposphere and cloud-top temperature throughout the globe. This
166 is a strong constraint that can be used to infer cloud top height and how it
167 changes under warming.

168 Much of the discussions above have focused on the aspect of the
169 circulation–cloud coupling which concerns how the atmospheric water cy-
170 cle governs large-scale cloudiness. Let us now address the second aspect of
171 this coupling which concerns how the CRE-AH—through its impact on at-
172 mospheric radiative cooling—feeds back on diabatic circulations. Referring
173 again to Eq. (5), we see that the CRE-AH can affect the condensation rate
174 and therefore precipitation either by directly modifying the radiative cool-
175 ing profile or by indirectly modifying the temperature profile through the

radiative cooling perturbation. The temperature profile governs both the vertical gradient of the saturation specific humidity and the static stability in the atmosphere, which are the numerator and denominator of the factor $[f]$ defined in Eq. (6).

A number of studies using numerical simulations have shown that the CRE-AH plays an important role in determining the mean tropical circulation (Slingo and Slingo, 1988, 1991, Bergman and Hendon, 2000, Tian and Ramanathan, 2003) as well as the general circulation of the atmosphere and global precipitation (Randall et al., 1989, Li et al., 2015). Averaged over the tropics and/or globally, the CRE-AH produces radiative heating in the free troposphere, correspondingly a reduction in the all-sky radiative cooling rate (see e.g. Fig. 4 in Li et al., 2015). If this were the only effect of the CRE-AH, we would expect that precipitation decreases—particularly in the tropics where the reduction in the radiative cooling rate by the CRE-AH is largest. However, in all of the aforementioned studies but Li et al. (2015), it was found on the contrary that the CRE-AH enhances precipitation. Randall et al. (1989) found that the CRE-AH results in a warmer and deeper troposphere. When integrated over a warmer and deeper troposphere, the $[\partial_p q_{\text{sat}}]$ term in Eq. (5) increases significantly. An enhancement in precipitation thus occurs despite reduced radiative cooling.

Given that the role of the CRE-AH on diabatic circulations remains inconclusive, it would be worthwhile to re-examine this topic in future studies. For future analysis, the impact of the CRE-AH on precipitation can be evaluated more accurately by accounting for all of the three terms $[Q_{\text{rad}}]$, $[\partial_p q_{\text{sat}}]$, and $[\sigma]$ in Eq. (5). Above we have touched upon the impacts of the CRE-AH on $[Q_{\text{rad}}]$ and $[\partial_p q_{\text{sat}}]$, but the CRE-AH also affects $[\sigma]$ —both locally by modifying the vertical profile of temperature in cloudy air and remotely by modifying the meridional temperature gradient. As shown in Li et al. (2015), the difference in the CRE-AH between the tropics and the extra-tropics leads to a meridional temperature gradient that affects the meridional transport of energy by the eddies. The transport of energy by the eddies in turn affects the static stability in the extra-tropics.

The discussions so far have been limited to clouds in the free troposphere above the boundary layer. Strictly speaking, the scaling argument used previously for the free troposphere (see Eqs. 1–6) does not apply to the boundary layer because (i) the source of moisture that results from surface evaporation must be added to the moisture budget balance in Eq. (1) for the boundary layer and (ii) the updrafts in the boundary layer below the LCL are not saturated. Nevertheless, in the upper boundary layer, the impact of clouds on large-scale diabatic circulations can be qualitatively understood

216 from the radiative cooling constraint. In the upper boundary layer (around
 217 750–850 hPa), the CRE-AH is dominated by the LW emission by cloud
 218 hydrometeors, leading to enhanced radiative cooling there (Haynes et al.,
 219 2013). This effect is apparent in the prevalent marine stratocumulus in the
 220 subtropics and higher latitudes (Wood, 2012). The CRE-AH of boundary
 221 layer clouds thus strengthens the overturning diabatic circulations, resulting
 222 in an increase in the globally averaged precipitation (Fermepin and Bony,
 223 2014). For other issues regarding the coupling between radiatively induced
 224 circulations and low clouds, the readers are referred to Section 2 below.

225 In summary, notable progress in our understanding of the coupling be-
 226 tween circulations and clouds has been made in the last few decades. In
 227 particular, constraints on how clouds change under climate change have
 228 been obtained based on basic understanding of tropospheric diabatic cir-
 229 culations. These constraints on cloud properties (vertical and horizontal
 230 distributions, water content, and coverage) will enable improved, accurate
 231 evaluation of the impacts of the CRE on the Earth’s energy budget and the
 232 climate feedback of clouds on global warming. However, existing studies
 233 have not settled on the roles of the CRE-AH on circulations and precipi-
 234 tation. This leaves significant opportunities for future studies. Progress is
 235 anticipated to occur rapidly within the next decade given the advancement
 236 in model development and increasing availability of global and long-term
 237 observational data of clouds (such as CALIPSO).

238 2 Low clouds and shallow circulations

239 Shallow circulations are characterized by a convergence/divergence in the
 240 boundary layer and a compensating flow in the lower free troposphere. The
 241 ascending branch of these circulations is generally located in the warm,
 242 convective regions and the descending branch in the cooler, less convective
 243 regions because of the pressure gradients created by the temperature anom-
 244 lies. Boundary layer convergence occurs in the warm, convective regions and
 245 divergence in the cool, non-convective regions (see the horizontal black arrow
 246 near the bottom of Fig. 1), with opposite patterns just above the boundary
 247 layer (see the horizontal grey arrows in Fig. 1). Shallow circulations appear
 248 in numerical model simulations at both mesoscale and large scales and have
 249 been observed in the tropics at large scales. In this section, we will first
 250 explain the mechanism that gives rise to such circulations. Second, we will
 251 review how these circulations influence the spatial organization of convec-
 252 tion. Lastly, we will review the instances of observed shallow circulations

253 and their influence on the large-scale tropical climatology.

254 **2.1 Mechanism of shallow circulations**

255 In non-convective regions, the boundary layer experiences radiative cooling
 256 at its top, mostly through LW radiation. This cooling results from both low
 257 clouds and clear-sky processes. Indeed, the boundary layer is significantly
 258 moister, and therefore absorbs and re-emits more LW radiation than the
 259 free troposphere above. A large part of the LW radiation emitted upward
 260 at the top of the boundary layer is not absorbed by the free troposphere
 261 and hence escapes to space, allowing the boundary layer top to cool. Cloud
 262 hydrometeors also absorb and emit infrared radiation very efficiently, so low
 263 clouds experience strong radiative cooling at their tops as well. This cooling
 264 is particularly intense in the case of stratocumulus clouds (Wood, 2012,
 265 Bellon and Geoffroy, 2016, Bellon and Bony, 2020). Mixing by turbulence
 266 redistributes the cooling from the top of the boundary layer downward.
 267 Vertical turbulent mixing is very efficient in a well-mixed boundary layer
 268 but a little less so in a shallow convective boundary layer.

269 The radiative cooling in the boundary layer can give rise to shallow
 270 circulations. In the hydrostatic approximation,

$$\frac{\partial \Phi}{\partial p} = -\frac{1}{\rho} \approx -\frac{R_a T}{p} \quad (7)$$

271 with Φ the geopotential, ρ the density, T the temperature, p the pressure,
 272 and R_a the specific gas constant of air. This means that the vertical increase
 273 of the geopotential through the boundary layer is smaller in radiatively
 274 cooled regions than in others. The baroclinic component of this pattern
 275 corresponds to the geopotential near the surface being larger in radiatively
 276 cooled regions than in others, and the geopotential at the top of the bound-
 277 ary layer being smaller in these cooled regions than in others. The associated
 278 geopotential gradient forces a circulation that includes outflow of air from
 279 the cooled regions in the boundary layer and inflow of air toward the cooled
 280 regions just above the boundary layer. This mechanism has been illustrated
 281 and validated by Large Eddy Simulation experiments and conceptual models
 282 (Naumann et al., 2017, 2019).

283 **2.2 Shallow circulations and aggregation of convection**

284 Shallow circulations differ from troposphere-deep circulations particularly in
 285 terms of the transport of moist static energy (MSE) $h = c_p T + \Phi + L_v q$, with

286 c_p the specific heat capacity of air at constant pressure, L_v the latent heat
 287 of vaporization, and q the specific humidity. Shallow circulations transport
 288 MSE up-gradient and therefore increase the contrast in MSE between the
 289 convective and dry regions, while deep circulations transport MSE down-
 290 gradient and reduce such contrast.

291 The difference in the direction of transport of MSE between troposphere-
 292 deep circulations and shallow circulations results from the stratification of
 293 MSE in the atmosphere: h is large in the boundary layer where the humidity
 294 is high, minimum in the lower free troposphere where the humidity is low,
 295 and monotonically increases with altitude in the free troposphere because of
 296 the contribution from the geopotential; at the tropopause it reaches values
 297 similar to the surface values (see Fig. 4 in Glenn and Krueger, 2017). The
 298 vertical integral of h over the middle and upper troposphere is larger than
 299 the vertical integral of h over the boundary layer. Therefore, the upper
 300 branches of troposphere-deep circulations transport more MSE (from the
 301 ascending regions into the subsiding regions) than their lower branches in the
 302 boundary layer (from the subsiding regions into the ascending regions). The
 303 net effect is that troposphere-deep circulations export MSE from ascending,
 304 convective regions of large column-integrated MSE to dry, subsiding regions
 305 with small column-integrated MSE. In contrast, shallow circulations import
 306 MSE from their subsiding branches (where column-integrated MSE is small)
 307 into their ascending branches (where column-integrated MSE is large).

308 Because shallow circulations increase the horizontal gradient of MSE,
 309 they create a positive feedback on the spatial variability: anomalies in MSE
 310 are reinforced by the transport associated with these circulations. As a re-
 311 sult, shallow circulations can be powerful actors in the spatial organization
 312 of convection: warm, convective regions become warmer and moister while
 313 dry, cool regions become cooler and drier. This mechanism of spatial or-
 314 ganization of convection, named “self-aggregation” is documented both in
 315 convection-permitting simulations and in general circulation model (GCM)
 316 simulations even without any external circulation nor the effect of rota-
 317 tion. In particular, low-level radiative cooling can cause the development
 318 of cooler and drier regions, sometimes called “radiative cold pools” that are
 319 instrumental to the development of self-aggregation. Figures 2 and 3 show
 320 examples of such radiative cold pools in a convection-permitting model and
 321 a GCM.

322 Figure 2 shows results of an idealized simulation (see Bellon and Coppin,
 323 2021) using the non-hydrostatic mesoscale model MesoNH (Lafore et al.,
 324 1998, Lac et al., 2018) in a convection-permitting configuration. The do-
 325 main is 90 000 km² with a 3-km horizontal resolution and 48 vertical lev-

els. The configuration prescribes a fixed sea surface temperature of 301 K over the entire domain and a horizontally uniform large-scale subsidence ($0.5 \text{ kg m}^{-2} \text{ s}^{-1}$ at 400 hPa). Figure 2 shows the average variables over one day of the stationary state reached in this simulation.

Figure 2(a) shows the horizontal distribution of precipitable water in the MesoNH simulation described above, with a clear dry patch surrounded by a fairly uniform moist region. Using the bimodality of the distribution of column-integrated MSE, a dry region and a moist region can objectively be identified and the dashed line in Fig. 2(a) shows the boundary between these regions. Figures 2(b) and (c) show the vertical profiles of the mixing ratios of water vapor and cloud condensates averaged over each of these regions. The figures show that the dry column is much drier than the moist column, both in the boundary layer and in the free troposphere, and with hardly any clouds. The moist region is convective, with large amount of cloud condensates throughout the troposphere.

Figure 2(d) shows the radiative heating rates (with negative values indicating radiative cooling) in the dry and moist regions. In the lower troposphere, the LW radiative cooling is larger in the dry region because of the smaller greenhouse effect of water vapor and clouds in the free troposphere above. Conversely, in the upper troposphere, the LW radiative cooling is larger in the moist region because of the re-emission of terrestrial radiation by the large amount of water vapor and clouds there. Except in the boundary layer, the SW radiative heating is larger in the moist region where there is more absorption of solar radiation by water vapor and clouds. The difference is opposite in the boundary layer because the downward solar radiative flux reaching the top of the boundary layer is larger in the dry region. In this simulation, the differences in the LW and SW effects compensate each other in the upper troposphere, but not in the lower troposphere where the net radiative cooling is larger (by about 0.5 K d^{-1}) in the dry region than in the moist region. The radiative cooling of the dry region relative to the moist region creates a shallow circulation with winds diverging from the dry region near the surface and a return flow in the lower free troposphere. Consistently with the discussions above, the shallow circulation increases the contrast in MSE between the dry and moist columns (not shown). Note that in this particular simulation, the radiative effect is mostly a clear-sky effect. But in similar simulations, a strong CRE-AH due to low clouds has been identified, with a similar resulting shallow circulation (Muller and Held, 2012, Muller and Bony, 2015).

Figure 3 shows regional snapshots of 925-hPa wind vectors and temperature (left panel) and precipitable water (right panel) at day 151 of a

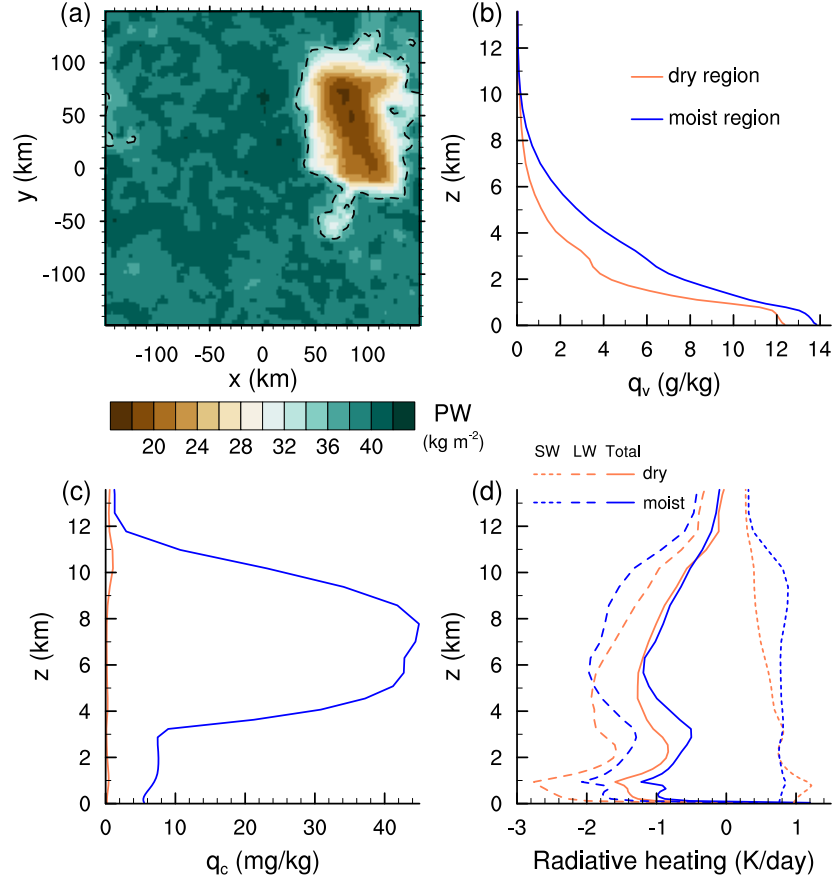


Figure 2: One-day average of a convection-permitting simulation: (a) map of precipitable water with a dashed contour showing the boundary between the moist and dry regions, (b) profile of water vapor mixing ratio, (c) profile of water condensate mixing ratio, and (d) profiles of solar (SW, dotted lines), terrestrial (LW, dashes lines) and net (total, solid lines) radiative heating rates. Blue lines refer to the moist region and red lines to the dry region.

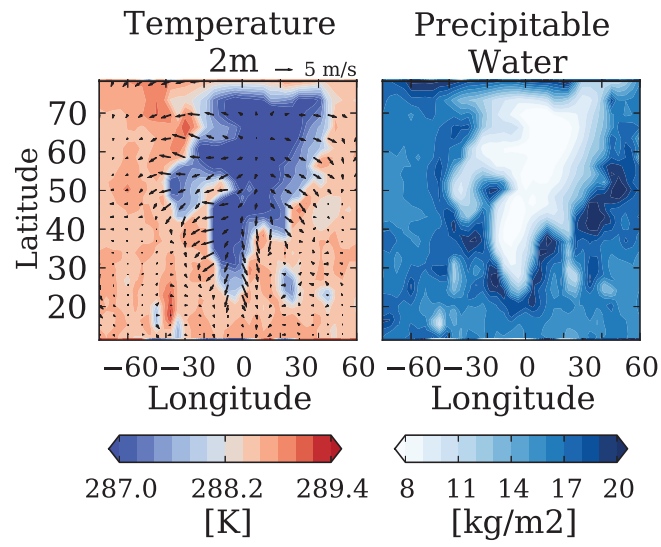


Figure 3: Radiative cold pool in a GCM simulation; left panel: temperature (shadings) and 925-hPa winds (vectors) at day 151 of the simulation; right panel: precipitable water. Adapted from Fig. 4 in Coppin and Bony (2015).

simulation using the GCM LMDz5A (Hourdin et al., 2006). The simulation was in a global radiative-convective-equilibrium configuration (i.e., without rotation and with a prescribed, uniform sea surface temperature) and initialized with horizontally uniform atmospheric conditions. In this case, the sea surface temperature is fairly low (292 K), and the spatial organization of convection results from mechanisms similar to those shown above in convection-permitting simulations. Details on the configuration and the mechanisms of self-aggregation at play in this simulation can be found in Coppin and Bony (2015). Figure 3 shows the development of a dry, cool region with near-surface winds diverging from that region. A return flow with converging winds occurs in the lower free troposphere (not shown). The expansion of this radiative cold pool eventually leads to circumscribing convection to a few limited regions of the globe.

As a final point, we note that while shallow circulations appear as a key mechanism of self-aggregation in a large number of model simulations, other mechanisms can also cause or contribute to self-aggregation (see Wing et al., 2017 for a review). Furthermore, while there are similarities between modeled self-aggregated convection and observed organized convection (see Holloway et al., 2017), it is still unclear whether the mechanisms producing self-aggregation in model simulations are active in the real world.

2.3 Observed shallow circulations

Observing systems have limited capacity to observe the three-dimensional atmospheric velocity fields and indirect estimates using diabatic heating are not robust for troposphere-deep signal, let alone shallow circulations (Bellon et al., 2017). As a result, mesoscale shallow circulations are yet to be observed.

At large scales, shallow meridional circulations (SMCs) have been identified in the tropics around tropical convergence zones. The first of such observation was in the Intertropical Convergence Zone (ITCZ) of the eastern Pacific (Zhang et al., 2004). Figure 4 shows this SMC in the boreal autumn there, with low-level flow convergence around the ITCZ, which is located at 10° – 15° N in this season. The northerly cross-equatorial flow in the boundary layer converges in the ITCZ and is compensated by diverging flows both in the lower free troposphere (at 2–6 km in Fig. 4) and in the troposphere above 6 km, forming both shallow and deep overturning circulations. Similar SMCs have been observed in the central Atlantic ocean (Zhang et al., 2008) and in the Caribbean (Schulz and Stevens, 2018).

These SMCs in the ITCZ were first thought to result from the cross-

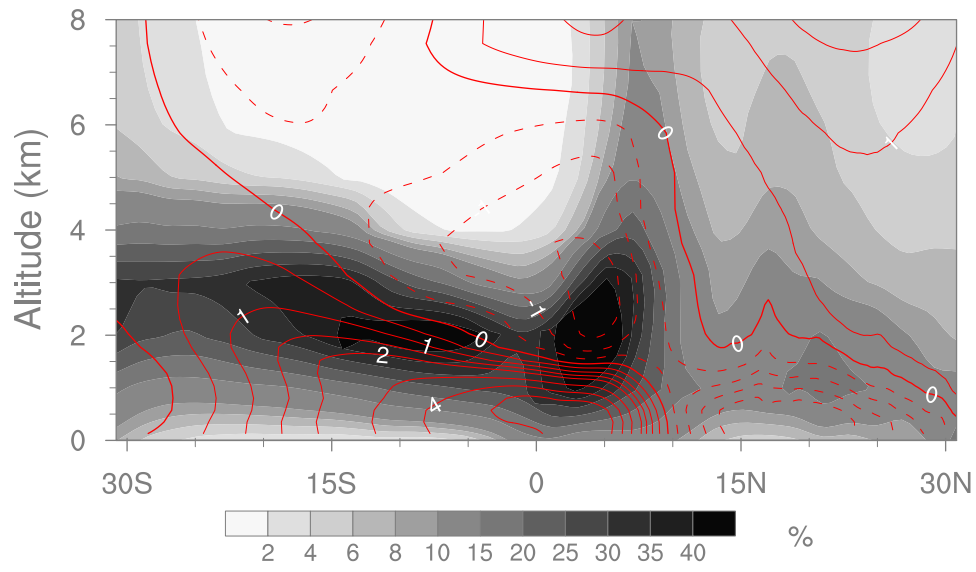


Figure 4: Cloud fraction (shadings, dataset GOCCP, Chepfer et al., 2010) and meridional wind (red contours, dataset ERA5, Hersbach et al., 2020) averaged over the eastern Pacific (90°W–120°W) in the boreal autumn (September–November).

404 equatorial sea surface temperature gradients that are communicated to the
 405 boundary layer air by turbulent fluxes and create pressure gradients that
 406 force the circulations (Nolan et al., 2007, 2010), but more recent work showed
 407 the role of the boundary-layer radiative cooling in the descending branch of
 408 the SMC. Figure 4 shows that the northerly flow in the non-convective region
 409 is co-located with the boundary layer clouds, which lends some credibility
 410 to a role of boundary-layer-top cooling, and particularly the CRE-AH. The
 411 SMC is also more intense if deep convection is momentarily suppressed and
 412 shallow convection is more active (Zhang et al., 2004, Yokoyama et al., 2014),
 413 potentially because the boundary-layer temperature follows more closely the
 414 sea surface temperature if deep convection is suppressed, but also because it
 415 changes the boundary-layer vertical structure and hence its radiative cooling.
 416 Additionally to the diabatic forcing, the momentum constraint allows the
 417 SMC to develop only if the ITCZ is away from the equator (Dixit and
 418 Srinivasan, 2017).

419 SMCs are also observed in monsoon regions such as West Africa, India,
 420 and Australia (Zhang et al., 2008, Zhai and Boos, 2017) with a rising branch
 421 over the monsoon heat low. These result from the pressure gradients between
 422 the equatorial ocean and the heat low over the continent (Zhang et al., 2008).

423 SMCs contribute to moistening the convergence zones, although to a
 424 lesser extent than troposphere-deep circulations. Recall from Section 2.2
 425 that SMCs and deep circulations transport MSE in opposite directions be-
 426 cause the vertical profile of MSE has a minimum in the lower free tropo-
 427 sphere. On the other hand, both types of circulations import moisture into
 428 the convergence zones as water vapor decreases monotonically with height
 429 in the atmosphere (see e.g. Fig. 2b). However, by exporting air in the lower
 430 free troposphere out of the ITCZ, the ITCZ SMCs import less moisture into
 431 the ITCZ than deep circulations (Zhang et al., 2008). Monsoon SMCs even
 432 include a drying contribution from horizontal advection of moisture, which
 433 further decreases the SMCs' moistening effect: as they extend to the heat
 434 low poleward of the convergence zones, they export moist air to that region
 435 in the boundary layer while importing very dry air into the ITCZ in the
 436 lower free troposphere (Zhai and Boos, 2017).

437 **3 Responses of tropical high clouds to the CRE-** 438 **AH**

439 This section describes the motions induced by the CRE-AH in tropical high
 440 clouds and the impacts of these motions on the evolution, lifetime, and

441 the CRE at the TOA of these clouds. The tropical high clouds that are
 442 strongly influenced by the motions induced by their own CRE-AH include
 443 (i) cirrus in the tropical tropopause layer (TTL); these clouds form either
 444 by in-situ ice nucleation or from the remnants of anvil clouds, and (ii) anvil
 445 clouds at various stages of evolution and optical properties, ranging from
 446 very reflective fresh anvils with large ice water contents to optically thin
 447 anvils that spread far away from deep convective cores.

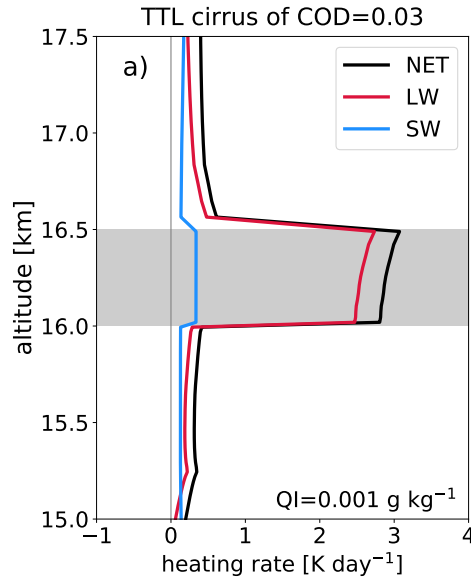


Figure 5: Radiative heating rates for a TTL cirrus assuming typical tropical temperature and moisture profiles. QI refers to ice mixing ratio. The ice crystal effective radius is set to values between 10 μm at the cloud top and 16 μm at the cloud base.

448 The radiative heating rates that result from the interaction of ice crystals
 449 with radiation are shown in Figs. 5 and 6 for typical high cirrus clouds. The
 450 TTL cirrus in Fig. 5 has a cloud optical depth (COD) of 0.03 and the anvil
 451 cirrus in Fig. 6 have CODs of 50, 5, and 1. The radiative heating rates shown
 452 in these figures were calculated using the Rapid Radiative Transfer Model
 453 (RRTM, Mlawer et al., 1997, Iacono et al., 2008). The absorption of LW
 454 radiation results in heating which maximizes either near the cloud top for
 455 the TTL cirrus (Fig. 5) or near the cloud bases for the anvil clouds (Fig. 6).
 456 For the thick anvil clouds that are opaque to LW radiation (Figs. 6a and b),

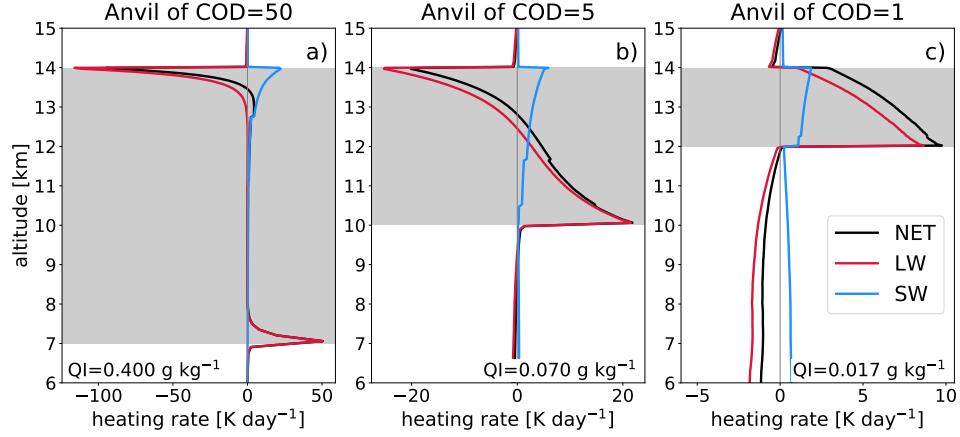


Figure 6: Radiative heating rates for (a) thick, (b) intermediately thick, and (c) thin anvil clouds assuming typical tropical temperature and moisture profiles. QI refers to ice mixing ratio. The ice crystal effective radius is set to values between $40\text{ }\mu\text{m}$ at the cloud top and $70\text{ }\mu\text{m}$ at the cloud base in case (a), $30\text{ }\mu\text{m}$ at the cloud top and $60\text{ }\mu\text{m}$ at the cloud base in case (b), and $20\text{ }\mu\text{m}$ at the cloud top and $30\text{ }\mu\text{m}$ at the cloud base in case (c), roughly in line with satellite observations of anvil clouds by Sokol and Hartmann (2020).

the large emissivities result in LW cooling near the cloud tops. For all the clouds shown, the absorption of SW radiation results in heating (Figs. 5 and 6), but the magnitude of the SW heating is significantly smaller than the LW heating and cooling.

The CRE-AH in both TTL cirrus and anvils can drive mesoscale circulations (see Figs. 1 and 7a). The circulations consist of rising vertical motions within the clouds (or portions of the clouds that are heated diabatically), compensating sinking motions outside the clouds, horizontal outflows near the cloud tops, and horizontal inflows near the cloud bases or below the levels of maximum heating (Ackerman et al., 1988, Lilly, 1988, Durran et al., 2009, Dinh et al., 2010, Gasparini et al., 2019). In addition, long exposure to a strong CRE-AH can bend the isentropic surfaces, forming unstable, convective layers within the high clouds (see Figs. 1 and 7b, and also Dobbie and Jonas, 2001, Dinh et al., 2010, Schmidt and Garrett, 2013).

The magnitude and vertical profile of the CRE-AH and the corresponding dynamical responses are highly sensitive to the COD. In the following,

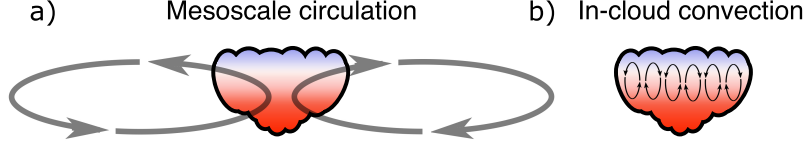


Figure 7: Air motions induced by the CRE-AH in tropical high clouds.

we therefore consider separately thin cirrus in the TTL (Section 3.1) and
anvil clouds which are much thicker (Section 3.2).

3.1 TTL cirrus

Thin cirrus are widespread in the TTL, with reported cloud fractions of
20–50 % (Massie et al., 2002, Tseng and Fu, 2017). Such clouds are nearly
transparent to the human eye, with CODs on the order of 0.01–0.05 (Dessler
and Yang, 2003, Haladay and Stephens, 2009, Lee et al., 2009). They heat
radiatively due to the absorption of LW radiation and to a minor extent SW
absorption, with typical heating rates of about 5 K d^{-1} or less (Fig. 5).

TTL cirrus modulate the amount of water vapor that enters the strato-
sphere and therefore the radiative effect of stratospheric water vapor on
climate (Dinh and Fueglistaler, 2014a). Furthermore, given that the clear-
sky radiative cooling diminishes near zero in the TTL, the CRE-AH of these
clouds plays a critical role in driving cross-isentropic transport of air from
the TTL into the stratosphere (Corti et al., 2006, Dinh and Fueglistaler,
2014b).

The mesoscale dynamical response to the radiative heating in TTL cirrus
can be qualitatively understood based on the simplified framework of a quasi-
hydrostatic, two-dimensional Boussinesq fluid, for which

$$\frac{\partial b}{\partial t} + N^2 w = Q_{\text{rad}}, \quad (8)$$

$$\frac{\partial u}{\partial x} + \frac{\partial w}{\partial z} = 0 \quad (9)$$

(Eqs. 3 and 4 in Durran et al., 2009). Here u and w are respectively the
horizontal and vertical velocities, b is the buoyancy, N is the Brunt–Väisälä

491 frequency, and Q_{rad} is the CRE-AH. As time goes on ($t \rightarrow \infty$),

$$w \rightarrow w_{\text{ss}} = \frac{Q_{\text{rad}}}{N^2}. \quad (10)$$

492 The steady-state vertical velocity (w_{ss}) is thus proportional to and has the
 493 same shape as the heating. Using Eq. (9) and w_{ss} in Eq. (10), the steady-
 494 state horizontal velocity can also be found. The steady-state horizontal
 495 velocity depends on the vertical gradient of the heating and extends laterally
 496 beyond the cloud/heating boundaries (Durran et al., 2009).

497 Following Eqs. (8) and (10), rising motions are induced in the clouds
 498 where the air is heated radiatively. Outside the lateral edges of the clouds,
 499 the buoyancy anomalies result in compensating sinking motions (see Fig. 7a
 500 and Fig. 3 in Dinh et al., 2010). Mass conservation (Eq. 9) leads to horizontal
 501 inflows in the lower halves of the cloud layers and horizontal outflows in the
 502 upper halves of the cloud layers. The developed circulations narrow the
 503 cloud bases, expand the cloud tops, and lead to the spreading and lofting of
 504 the clouds (see Figs. 6 and 7 in Dinh et al., 2010).

505 The mesoscale circulations described above advect environmental air into
 506 the TTL cirrus (Dinh et al., 2010, 2012, 2014). Environmental air is brought
 507 into the clouds by the inflows in the lower halves of the clouds and then
 508 advected upward by the radiatively induced rising motions in the clouds.
 509 This leads to water vapor flux convergence (divergence) inside the clouds if
 510 the ambient air is moist (dry). Therefore, depending on whether the ambient
 511 air is supersaturated or subsaturated (with respect to ice), advection of air
 512 by the mesoscale circulations supports or suppresses depositional growth of
 513 cloud ice crystals, thereby lengthening or shortening the cloud lifetime (Dinh
 514 et al., 2010, 2012, 2014).

515 The vertical gradient of the radiative heating is negative near the tops
 516 of the TTL cirrus (at altitude of 16.5 km in Fig. 5). This can lead to the
 517 formation of shallow unstable layers at the cloud tops that support small-
 518 scale convective motions (see Figs. 4–6 in Dinh et al., 2010). As a result,
 519 the cloud tops become heterogeneous with pockets of updrafts with higher
 520 ice water contents and areas of downdrafts mixed with environmental air
 521 leading to ice sublimation.

522 The relevance of the mesoscale circulations induced by the CRE-AH for
 523 TTL cirrus evolution remains disputed. In-situ measurements show that
 524 ice crystal radii are typically larger than 5–10 μm (Lawson et al., 2008,
 525 Krämer et al., 2020). Gravitational settling of large ice crystals may not
 526 allow sufficient time for the circulations to develop in response to the CRE-
 527 AH (Jensen et al., 2011). However, given that TTL cirrus can last for several

528 days (Winker and Trepte, 1998), it is more likely than not that these in-
 529 situ observations did not sample the cloud formation period (the first 12 h
 530 or so), during which the freshly nucleated ice crystals remain small in size.
 531 The presence of wind shear and gravity wave temperature fluctuations (Dinh
 532 et al., 2016) were also shown to lead to a faster TTL cirrus decay, therefore
 533 diminishing the potential impacts of the circulations (Jensen et al., 2011,
 534 Podglajen et al., 2016). These simulations testing the roles of wind shear
 535 and temperature fluctuations were carried out for individual cloud cases
 536 only. Simulations of large cloud ensembles are needed to further investigate
 537 the sensitivity of the strength of the circulations induced by the CRE-AH
 538 to initial and environmental conditions.

539 **3.2 Anvil clouds**

540 The deep convective plumes of cloudy air, initially of nearly uniform po-
 541 tential temperature, flatten and stretch after being injected into a stably
 542 stratified environment (Lilly, 1988). The convective plumes are self-lofted
 543 by the strong latent heating within the convective updrafts until reaching
 544 the level of neutral buoyancy, which is constrained by the clear-sky radiative
 545 cooling profile (see Hartmann and Larson, 2002 and Section 1 above). The
 546 tops of the convective outflows are colder than the surrounding environment
 547 and therefore sink, while the bottoms are warmer and rise, leading to verti-
 548 cal compression and horizontal expansion of the convective outflows (Lilly,
 549 1988) forming thick anvil clouds. From then on, cloud-radiative interactions
 550 start to play important roles in modulating the morphology and life cycle
 551 of anvil clouds.

552 As a difference from TTL cirrus, freshly detrained anvil clouds of CODs
 553 larger than about 4 develop a radiative dipole (Wall et al., 2020) character-
 554 ized by LW radiative heating near cloud bases and LW cooling near cloud
 555 tops (Figs. 6a and b). The cloud tops are in addition heated by the absorp-
 556 tion of SW radiation by the cloud condensates. The SW heating reaches
 557 comparable magnitudes to the LW cooling at the cloud tops in the middle
 558 of the day when insolation values exceeds 1000 W m^{-2} (Wall et al., 2020,
 559 Sokol and Hartmann, 2020). However, averaged over both day and night,
 560 the SW heating is of secondary importance and the net CRE-AH follows
 561 closely the LW component.

562 The resulting CRE-AH drives mesoscale circulations. In the simulations
 563 by Gasparini et al. (2019) shown in Fig. 8, the primary circulation includes
 564 an ascent in the middle of the cloud between 7 km and 11 km and a strong
 565 outflow at about 10–12 km (Fig. 8b). The primary circulation cell is closed

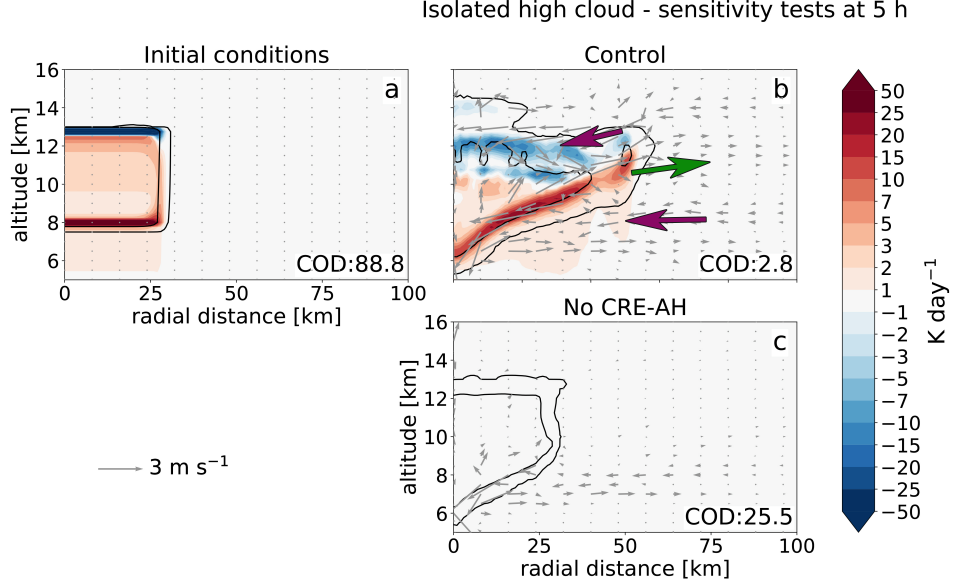


Figure 8: CRE-AH and wind vectors at (a) the initialization and (b) and (c) hour 5 after initialization of an optically thick anvil cloud simulated in a cloud-resolving model (adapted from Gasparini et al., 2019). Black contours represent ice water mixing ratios of 0.1 and 0.0001 g kg^{-1} . The vertical velocities are multiplied by a factor of 8 for a better visualization. The purple arrows highlight the inflows toward the cloud and the green arrow highlights the outflow.

566 by subsidence at the domain edge and an inflow at about 8–9 km altitude.
 567 The circulation spreads the upper half of the cloud and narrows the lower
 568 half of the cloud, thereby significantly changing the shape of the cloud re-
 569 lative to the initialization time (Fig. 8a).

570 Also shown in Fig. 8(b), the cloud-top radiative cooling induces down-
 571 drafts that sink the cloud top and thin the cloud. The radiative cooling
 572 further induces an inflow of drier environmental air that erodes the cloud
 573 top. This secondary circulation leads to the formation of an upper thin cir-
 574 rus cloud (at about 14 km in Fig. 8b), which is later detached from the main
 575 anvil cloud. Similar clouds were observed in in-situ aircraft measurements
 576 (Garrett et al., 2004) and satellite remote sensing (Sokol and Hartmann,
 577 2020).

578 Last but not least, the negative vertical gradient of the radiative heating

579 rate (cooling above 11 km, heating below 11 km) destabilizes the air at the
 580 cloud top, resulting in convective motions and cell-like heterogeneous cloud
 581 elements there (see the 0.1 g kg^{-1} contour in Fig. 8b).

582 The CRE-AH strongly affects the CRE at the TOA of anvil clouds. The
 583 CRE at the TOA is the difference between the all-sky and clear-sky net (LW
 584 plus SW) incoming (downward minus upward) radiative fluxes at the TOA.
 585 In the simulations shown in Fig. 8, when the CRE-AH is turned off (Fig. 8c),
 586 the cloud at hour 5 after initialization has a COD higher than 25 and a CRE
 587 at the TOA of about -100 W m^{-2} . In contrast, in the presence of the CRE-
 588 AH (Fig. 8b), the cloud at hour 5 is optically much thinner with a COD of
 589 about 3 and a CRE at the TOA of only about -6 W m^{-2} . Integrated over
 590 the whole cloud life cycle, the net CRE at the TOA is strongly negative in
 591 the simulation without the CRE-AH, while the simulation with the CRE-
 592 AH is close to being net CRE neutral at the TOA. The latter is consistent
 593 with satellite observations that the CRE at the TOA is close to zero for
 594 tropical convective clouds over the Indo-Pacific Warm Pool (Ramanathan
 595 et al., 1989, Hartmann et al., 2001, Hartmann and Berry, 2017).

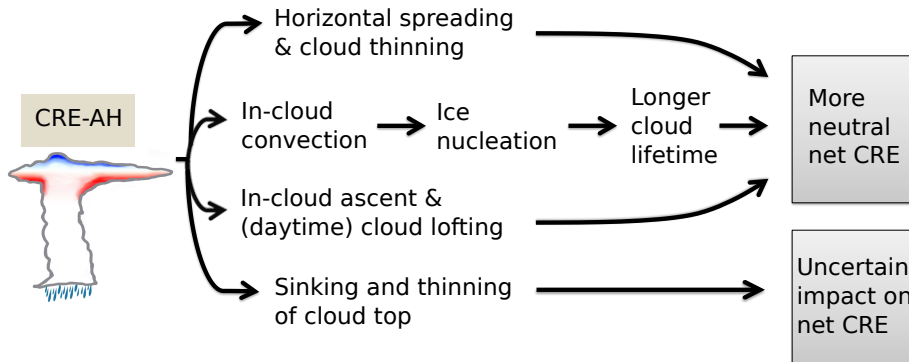


Figure 9: Mechanisms of the CRE-AH influencing the morphology and life cycle of tropical anvil clouds and their CRE at the TOA.

596 Figure 9 summarizes the mechanisms by which the CRE-AH of anvil
 597 clouds influences their CRE at the TOA. The dominant effect comes from the
 598 horizontal spreading of the clouds by the radiatively induced mesoscale cir-
 599 culations. The aging, optically thin, and horizontally extensive anvil clouds
 600 have a positive CRE at the TOA (Kubar et al., 2007, Gasparini et al.,
 601 2019), counteracting the strongly negative CRE contribution from freshly
 602 detrained, thick but much smaller anvil clouds.

603 The motions induced by the CRE-AH also affect the persistence and life-
 604 time of the clouds. Within the updrafts of the small-scale convective cells at
 605 the cloud tops, nucleation of new ice crystals can take place. Freshly nucle-
 606 ated ice crystals are much smaller in size and therefore sediment much more
 607 slowly than the pre-existing detrained ice crystals. The matured, optically
 608 thin anvil clouds can last a long time as they are replenished with the new
 609 ice crystals at their tops. As a result, the net CRE at the TOA integrated
 610 over the entire life cycle of anvil clouds becomes more positive (Hartmann
 611 et al., 2018).

612 In addition, the cloud radiative heating drives in-cloud ascents, which
 613 counteract ice crystal sedimentation, prolonging the cloud lifetime. On av-
 614 erage, the cloud radiative heating comes mainly from the LW absorption,
 615 but during the day the SW absorption can significantly increase the net
 616 heating rate (Ruppert and Hohenegger, 2018, Wall et al., 2020). Therefore,
 617 during the day, the radiatively induced updrafts can be strong enough to
 618 overcome ice crystal sedimentation, lifting the clouds to higher levels and
 619 colder temperatures, therefore exerting a stronger LW CRE at the TOA
 620 (Ruppert and Klocke, 2019, Wall et al., 2020). Finally, the LW cooling at
 621 the cloud tops leads to the sinking and erosion of the cloud tops, decreasing
 622 the lifetime of the anvil clouds. However, as the sinking and thinning of the
 623 clouds decrease both the LW and SW CRE at the TOA, the net effect on
 624 the TOA radiative fluxes is uncertain.

625 In summary, past observational and modeling work have highlighted the
 626 importance of the motions induced by the CRE-AH for tropical anvil clouds’
 627 evolution and radiative climatic impacts. However, we note that existing
 628 modeling studies are limited to individual cloud cases only and may not
 629 capture the full range of variation of cloud properties. Both the local CRE-
 630 AH and the CRE at the TOA of tropical high clouds are highly sensitive
 631 to the microphysical properties of ice crystals, such as their effective ra-
 632 dius and asymmetry parameter (Järvinen et al., 2018, Bantges et al., 2020).
 633 Simulations of the tropical atmosphere in which the life cycles of a diverse
 634 cloud population are captured will be needed to thoroughly evaluate how
 635 the CRE-AH influences tropical cloud distribution and radiative effects.

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