

ABSTRACT

11 Satellite observations of tropical maritime convection indicate an afternoon maximum in anvil
12 cloud fraction that cannot be explained by the diurnal cycle of deep convection peaking at night.
13 We use idealized cloud-resolving model simulations of single anvil cloud evolution pathways,
14 initialized at different times of the day, to show that tropical anvil clouds formed during the
15 day are more widespread and longer lasting than those formed at night. This diurnal difference
16 is caused by shortwave radiative heating, which lofts and spreads anvil clouds via a mesoscale
17 circulation that is largely absent at night, when a different, longwave-driven circulation dominates.
18 The nighttime circulation entrains dry environmental air that erodes cloud top and shortens anvil
19 lifetime. Increased ice nucleation in more turbulent nighttime conditions supported by the longwave
20 cloud top cooling and cloud base heating dipole cannot overcompensate for the effect of diurnal
21 shortwave radiative heating. Radiative-convective equilibrium simulations with a realistic diurnal
22 cycle of insolation confirm the crucial role of shortwave heating in lofting and sustaining anvil
23 clouds. The shortwave-driven mesoscale ascent leads to daytime anvils with larger ice crystal size,
24 number concentration, and water content at cloud top than their nighttime counterparts.

25 *Significance statement.* Deep convective activity and rainfall peak at night over the tropical
26 oceans. However, anvil clouds that originate from the tops of deep convective clouds reach their
27 largest extent in the afternoon hours. We study the underlying physical mechanisms that lead to
28 this discrepancy by simulating the evolution of anvil clouds with a high-resolution model. We
29 find that the absorption of sunlight by ice crystals lofts and spreads the daytime anvil clouds
30 over a larger area, increasing their lifetime, changing their properties and thus influencing their
31 impact on climate. Our findings show that it is not only important to simulate the correct onset of
32 deep convection but also to correctly represent anvil cloud evolution for skillful simulations of the
33 tropical energy balance.

34 **1. Introduction**

35 Anvil clouds are both the most frequent and the most radiatively important cloud type in tropical
36 deep convective regions (Hartmann and Berry 2017; Berry and Mace 2014). On average they exert
37 strong shortwave (SW) and longwave (LW) cloud radiative effects (CRE) and therefore significantly
38 modulate both the incoming and outgoing radiative fluxes in the tropical atmosphere. However,
39 their instantaneous effects on both the top-of-the-atmosphere (TOA) radiative fluxes as well as the
40 radiative heating within the atmosphere are strongly influenced by the diurnal cycle of insolation.
41 During the day, an optically thick, fresh anvil cloud will have a strong net negative TOA CRE of
42 up to -500 W m^{-2} , dominated by the strong SW shading effect due to its large albedo. On the other
43 hand, at night the net CRE will be composed only of the LW component and can exceed 150 W
44 m^{-2} . Given the large diurnal cycle in tropical anvil clouds CRE, it is important for climate models
45 to capture both (1) the correct timing of deep convection and (2) the subsequent evolution and thin-
46 ning of anvil clouds in order to balance radiative fluxes and correctly simulate changes in climate.

47

48 Over the tropical oceans, the majority of rainfall and upper tropospheric anvil clouds originates
49 in large clusters of deep convective activity called mesoscale convection systems (MCS, see e.g.
50 Houze (2004) for a review). Observational data from tropical maritime regions robustly show
51 a diurnal cycle of MCS activity with a peak in the early morning hours (Gray and Jacobson
52 1977; Chen and Houze 1997; Randall et al. 1989; Nesbitt and Zipser 2003). Similar diurnal
53 pulses of convection and the associated precipitation have been also observed in the Intertropical
54 convergence zone (Bain et al. 2010; Ciesielski et al. 2018) and in tropical cyclones (Dunion
55 et al. 2014; Bowman and Fowler 2015). The precise mechanisms behind this diurnal cycle are
56 still under debate. Possibilities include the stabilization of the environment during daytime by
57 SW heating (lapse-rate mechanism, Kraus 1963; Randall et al. 1989), a daytime decrease in
58 relative humidity due to SW heating of clear sky areas (Tao et al. 1996; Dai 2001), changes in the
59 large-scale overturning circulation between convective and nonconvective regions (cloudy-clear
60 sky differential radiation mechanism, Gray and Jacobson 1977), insolation-driven changes in sea
61 surface temperatures that can excite convectively coupled equatorial waves (Chen and Houze
62 1997), and convectively forced diurnal gravity waves originating from nearby land (Mapes et al.
63 2003; Ruppert et al. 2020). Recent idealized simulations of organized deep convection (Ruppert
64 and Hohenegger 2018) point at the primary importance of the lapse-rate mechanism to strengthen
65 convection at night by the radiative destabilization of the atmosphere by LW cooling. This in
66 turn increases convective heating particularly in the lower troposphere and leads to an increased
67 low level circulation due to a sharp heating gradient between the clear sky region, cooled by LW
68 radiation, and the moist region, warmed by convective heating initiating the cloudy-clear sky
69 differential radiation mechanism. In contrast, during the afternoon hours the SW heating near
70 cloud tops was found to intensify the mesoscale circulation in the upper troposphere.

71

72 While numerous studies have so far been dedicated to understanding deep convection, we focus
73 on the evolution of detrained anvil clouds to better understand the processes controlling their decay
74 and explain the discrepancy between the early morning peak in deep convection and the number
75 of MCS and the afternoon peak in anvil cloud cover (Fu et al. 1990; Feofilov and Stubenrauch
76 2019; Chepfer et al. 2019; Sokol and Hartmann 2020). As a difference from the nighttime MCS
77 that define the diurnal cycle of precipitation (Nesbitt and Zipser 2003), the relatively less frequent
78 daytime MCS lead to substantial climatic effects by producing more extensive anvil cloud shields
79 (Wall et al. 2020).

80 Recent modeling work shows differences between the diurnal cycles of convective activity and
81 ice water path (IWP, the vertically integrated amount of ice in the atmosphere) over tropical
82 oceans (Ruppert and Klocke 2019). While rainfall peaks in the early morning hours, IWP was
83 shown to have two diurnal maxima: one in the early morning hours, coincident with the peak in
84 rainfall and deep convective activity, and one in the afternoon hours, coincident with the diurnal
85 peak in anvil cloud cover. Ruppert and Klocke (2019) explained the secondary peak in IWP as
86 an anvil cloud response to increased SW heating within clouds that enhances the local mesoscale
87 updraft motion, promoting the formation and maintenance of high ice clouds, which we term the
88 anvil lifting hypothesis. Durran et al. (2009) and Dinh et al. (2010) described a similar circulation
89 response for thin tropical tropopause layer cirrus. A greater knowledge of anvil cloud evolution is
90 needed to bridge the gap in our understanding between the early morning peak in deep convection
91 and the afternoon peak in anvil coverage.

92
93 Hartmann and Berry (2017) proposed that radiative heating first promotes the rapid decay of thick
94 anvil clouds until they are thin enough for a LW heating dipole (cloud top cooling combined with
95 the cloud base heating) to support its maintenance. This was subsequently modelled in idealized

96 simulations by Hartmann et al. (2018) who found that radiatively driven turbulence extended the
97 cloud lifetime by supporting within-anvil convection that triggered new ice crystal nucleation. The
98 small, newly nucleated ice crystals are only weakly affected by sedimentation compared with larger,
99 aged ice crystals, therefore prolonging the anvil cloud lifetime. We refer to this mechanism as the
100 microphysical cycling hypothesis. Sokol and Hartmann (2020) used CloudSat-CALIPSO satellite
101 data to show that the radiative structure of heating within anvil clouds drives the distribution of anvil
102 optical thicknesses to peak preferentially at cloud optical depths (COD) between 1 and 2. Anvils
103 of such COD were found to be particularly susceptible to radiative destabilization by both LW and
104 SW radiation and to contain larger ice crystal number concentrations than anvils at slightly higher
105 or lower COD, indicating a possible role of new ice crystal nucleation in anvil cloud maintenance.

106 An observational study by Wall et al. (2020) used geostationary satellite data to evaluate the anvil
107 lifting and microphysical cycling hypotheses. They evaluated the two hypotheses by comparing
108 observations of daytime and nighttime anvil clouds and their persistence. Nighttime anvils are
109 influenced only by LW radiation, and therefore should evolve according to the LW heating-cooling
110 dipole that is central to the microphysical cycling hypothesis. During the day, SW heating
111 dominates, suggesting that anvil lifting is favored. Wall et al. (2020) found strong evidence for the
112 dominant role of SW-initiated daytime anvil lifting that increases anvil cloud lifetime and no indi-
113 cation for excessive new ice crystal formation near anvil cloud top in more persistent daytime anvils.

114
115 Deng and Mace (2008) studied the diurnal cycle in anvil cloud properties and air motion with
116 the help of the cloud radar observations from two Tropical Western Pacific (Nauru and Manus)
117 and one midlatitude (Southern Great Plains) Atmospheric Radiation Measurement Program sites.
118 The tropical measurements showed a pronounced diurnal cycle in cloud properties and residual air
119 motion. Cloud top height and cloud geometrical thickness both peak in the early afternoon hours,

120 shortly after the midday peak in in-cloud air motion, and reach a minimum in the early morning
121 hours. Similar variations were also measured in cloud microphysical and optical properties, all
122 peaking in the early afternoon hours. Their results are consistent with Wall et al. (2020) and point
123 at the important role of radiative heating in the maintenance and microphysical structure of anvil
124 clouds.

125
126 This study extends recent work to study anvil cloud maintenance from an idealized modeling
127 perspective. We first examine the lifecycles of anvil clouds from a sink perspective, by monitoring
128 the decay of identical thick anvil clouds initialized in the middle of a model domain at different
129 times of day. Similarly to Wall et al. (2020), we take advantage of the diurnal cycle of insolation,
130 further simplified by examining cloud evolution during perpetual night and midday conditions. We
131 support these idealized experiments with an analysis of a statistically representative ensemble of
132 anvil clouds from a simulation in radiative-convective equilibrium (RCE) with a realistic diurnal
133 cycle of insolation. RCE is a simplified description of the climate system, in which radiative
134 cooling of the atmosphere must be balanced by latent heating from convective cloud processes. It
135 is a useful representation of the tropical atmosphere particularly at large spatial and long temporal
136 scales (Jakob et al. 2019). While Ruppert and Hohenegger (2018) and Ruppert and Klocke (2019)
137 investigated diurnal cycle impacts on organized convection, this study focuses on anvil cloud
138 dynamics, circulations, microphysics, and their radiative impacts in non-organized convection.

139 2. Methods

140 *a. Model*

141 We use the version 6.10 of the System for Atmospheric Modeling (SAM) cloud resolving model
142 (Khairoutdinov and Randall 2003). The model is coupled with the RRTMG radiative transfer
143 model (Mlawer et al. 1997; Iacono et al. 2008) and uses a Smagorinsky-type 1.5-order closure
144 scheme to represent the subgrid-scale motions. The radiation called every sixth, 30-s long, model
145 timestep. The model allows for substepping to ensure the Courant-Friedrich-Levy criterion and
146 is set to use periodic lateral boundary conditions. Microphysical processes are represented with
147 the Predicted Particle Properties (P3) bulk microphysical scheme (Morrison and Milbrandt 2015),
148 version 3.1.4, with the following deviations from the default P3 microphysics:

- 149 • The maximum ice crystal number concentration limit is increased from 0.5×10^6 to 10×10^6
150 kg^{-1} in order to allow for realistic simulations of fresh deep convective outflow with high
151 ice crystal number concentrations (Heymsfield et al. 2017; Jensen et al. 2018; Krämer et al.
152 2020).
- 153 • Freezing in mixed-phase clouds is parameterized following Meyers et al. (1992) with an
154 additional constraint that allows ice nucleation only in the presence of cloud droplets, since
155 deposition freezing is thought to be negligible in mixed-phase conditions (e.g., Ansmann et al.
156 2008; DeMott et al. 2010; Hoose and Möhler 2012; Lohmann et al. 2016).
- 157 • Freezing below the homogeneous freezing temperature of water (-38°C) follows the descrip-
158 tion of Shi et al. (2015), as implemented in CAM5, CAM6, and E3SM general circulation
159 models. The formulation is largely based on the parameterization by Liu and Penner (2005)
160 that simulates the competition between homogeneous and heterogeneous freezing in cirrus

161 clouds. The competition for vapor between freezing and pre-existing ice crystals follows the
162 description published in Kärcher et al. (2006). The number of ice nuclei considered by the
163 Liu and Penner (2005) parameterization is due to the absence of an interactive aerosol module
164 set to 2 L^{-1} , typical for low aerosol concentration in the upper troposphere of the Tropical
165 Western Pacific (e.g., Gasparini and Lohmann 2016). The number of sulfate aerosols available
166 for homogeneous freezing is set to 20 cm^{-3} .

- 167 • The saturation vapor pressure for liquid water and ice is parameterized by the Murphy and
168 Koop (2005) formulation.

169 The simulated ice cloud properties were found to generally agree with the observed tropical
170 maritime cloud data, despite a small underestimation in cloud water content at temperatures
171 between 0°C and -80°C and the underestimation of ice crystal number at temperatures colder than
172 -60°C . A short model evaluation comparing model output with cloud properties observed in three
173 tropical aircraft field campaigns, consolidated in a uniform dataset by Krämer et al. (2020), can be
174 found in Appendix A.

175 *b. Simulations*

176 We use two different simulation strategies of differing model complexities. In the simplest setup,
177 we initiate a thick ice cloud with uniform ice mixing ratio of about 0.6 g kg^{-1} and a diameter of 60
178 km in the middle of a $256 \times 256 \text{ km}$ model domain, as described in Gasparini et al. (2019). All of the
179 described simulations use 128 vertical levels with the upper tropospheric vertical resolution of 250
180 m and the horizontal resolution of $1 \times 1 \text{ km}$ that is able to resolve part of the within-anvil convection
181 that drives a significant proportion of the within-anvil microphysical process rates (Gasparini et al.
182 2019). The model typically uses two substeps within one model timestep in the first few hours

183 of the simulation, decreasing the effective model timestep from 30 to 15 s. The simulations are
184 initialized without the presence of any mean winds from a typical tropical temperature and moisture
185 profile. The model mean horizontal wind fields are nudged to zero.

186 The cloud is representative of observed freshly detrained thick anvils in the tropics, with a cloud
187 top altitude at 13 km and cloud base at 8 km. The cloud's initial diameter is set to 60 km in all but
188 small-real and large-real simulations. We simulate the evolution of the cloud by either assuming
189 a realistic diurnal cycle of insolation and varying the simulation starting time or by fixing the
190 insolation to a constant value representing the typical midday (1300 W m^{-2}) or night (0 W m^{-2})
191 conditions. In addition, we conduct several sensitivity tests with changes to physical processes
192 that influence the ice cloud evolution, namely SW and LW atmospheric cloud radiative effects
193 (ACRE), ice crystal sublimation, ice sedimentation, and ice nucleation (Table 2).

194
195 Secondly, we perform a 50-day simulation of a cloud field in RCE with a realistic diurnal cycle
196 of insolation typical for the equator. The simulation is initialized from a temperature and moisture
197 profile generated from the average over the last 20 days of an earlier 100 day-long RCE simulation
198 with a smaller model domain. Only the last 30 days of the hourly model output, after the simulated
199 climate reaches a statistical equilibrium, are considered in this analysis. The sensible and latent
200 heat fluxes are computed interactively. The model typically uses 5-9 substeps within one model
201 timestep, decreasing the effective model timestep from 30 to 3-6 s. The RCE simulations are
202 performed in a 128×128 km domain, which is too small to allow the development of convective
203 organization.

204 *c. Himawari satellite data*

205 We use 3 months (June 1 - August 31 2016) of Himawari-8 geostationary satellite observations
206 (Bessho et al. 2016) of brightness temperature (BT) at the infrared channel (11.2 μm). The
207 downloaded product was subsequently regrided to 0.25° by averaging the native grid pixels
208 within the new grid boundaries. The dataset's temporal resolution is 1 hour.

209 **3. Results**

210 *a. Diurnal cycle of brightness temperature from geostationary satellite observations*

211 Figure 1a shows the geostationary satellite measurements of BT in the ocean-covered areas of
212 the Tropical Western Pacific (20°S to 20°N, 130°E to 180°E). The BT roughly corresponds to
213 the cloud top temperature for optically thick clouds with emissivity values near 1 (Protopapadaki
214 et al. 2017). The BT signal from thinner clouds includes a mixture of the clouds' emission and the
215 emission from lower, warmer atmospheric levels. Most of such clouds can be classified as anvil
216 clouds in different stages of their lifecycle. Appendix B contains a detailed discussion explaining
217 why most pixels with BT < 290 K correspond to high clouds.

218
219 The BT observations are clustered into 10 K bins to better represent the transition from deep
220 convective cores (BT < 210 K) to anvil clouds of various optical thickness (210 < BT < 290 K).
221 The relationship between BT and high cloud COD is explained in more detail in Appendix B. The
222 BT values typical of deep convection occur most often in the early morning hours, while the BT
223 bins associated with anvil clouds peak 7-18 hours later (Fig. 1). Interestingly, the frequency of
224 pixels with BT of 210 - 220 K peaks at 14 local time (LT). This BT bin corresponds to a mixture
225 of weaker deep convective systems that are frequent in the afternoon hours (Nesbitt and Zipser

226 2003) and thick anvil clouds. This peak is followed by successive peaks in BT bins between 220
227 and 290 K in the afternoon and evening hours, when deep convective activity remains low (Fig.
228 1b). The transition from BT maxima of 210-220 K at 14 LT to 250-260 K at 20 LT reflects a
229 BT warming rate of 15 K hour^{-1} . This corresponds to a thinning of the median anvil COD from
230 about 30 to about 2 within 6 hours, as confirmed by a combination of DARDAR cloud profile
231 and MODIS BT data (Appendix B). The thinning slows down after the anvils reach a COD of ~ 2
232 that was found to be preferred based on radiative flux considerations (Hartmann and Berry 2017;
233 Sokol and Hartmann 2020). These results agree with a study using the spaceborne lidar data
234 from the CATS instrument that showed an increase in high opaque clouds in the afternoon hours
235 (Chepfer et al. 2019) and another that relied on infrared sounder data (Feofilov and Stubenrauch
236 2019). Moreover, Sokol and Hartmann (2020) found a larger coverage of anvil clouds in the
237 Tropical Western Pacific and Tropical Indian Ocean during the afternoon A-Train overpass (13.30
238 LT) compared with the night one (1.30 LT), which is consistent with the observed afternoon peak
239 in the BT bins of 210-260 K.

240
241 The clouds from the afternoon/evening anvil cloud peak cannot be generated by the diurnal peak
242 in convective activity that occurs 6-8 hours earlier. While the transition from convective cores to
243 thin anvils can take up to 10 hours, the optically thick phase of anvil evolution that corresponds
244 to BT of up to 220-240 K and COD of 5-15 (Fig. B1) is unlikely to persist in the atmosphere for
245 more than about 5 hours (e.g., Mace et al. 2006; Wall et al. 2020; Jensen et al. 2018; Gasparini
246 et al. 2019, 2021, appendix B of this manuscript). Additional physical mechanisms must therefore
247 play a role in the formation and maintenance of the afternoon and evening anvil clouds. This
248 result is consistent with the work by Wall et al. (2020), which concluded that the daytime anvil

249 clouds must be more persistent and/or more widespread compared with their nighttime counterparts.

250

251 *b. Idealized simulations*

252 Figure 2 shows the time evolution of the IWP for two identical high clouds initialized at two
253 different times during the diurnal cycle. The first cloud is initialized at 21 LT and undergoes a
254 rapid thinning and spreading until disappearing about 8 hours after the initialization, at 5 LT,
255 just before sunrise. The cloud initialized at 9 LT persists for more than 15 hours, spreading over
256 a larger portion of the domain (Fig. 2b). The clouds initialized at 9 and 21 LT represent the
257 two extremes among clouds initialized throughout the diurnal cycle: on one side the persistent
258 and widespread daytime anvil cloud, and on the other side the shorter lived nighttime anvil.
259 Additional simulations of anvil cloud lifecycles initialized at each of the 24 hours of the day fall
260 in between the selected two cases in terms of IWP, cloud fraction, and cloud persistence (not shown).

261

262 The TOA radiative effects also vary significantly depending on the simulation start time. Fig.
263 3 represents values of SW, LW, and NET CRE averaged over the whole domain and 16 hour
264 duration of the simulations for each of the simulations initialized at different times of the day.
265 Simulations that start in the morning hours (particularly 7-11 LT) lead to a large LW CRE and
266 an even larger SW CRE, with a negative net CRE of -5 to $-10 \text{ W m}^{-2} \times \text{day}$, when averaged over
267 the entire anvil lifecycle. In contrast, simulations starting in the late evening or night (between
268 approximately 15 and 3 LT) exert no or a very small SW CRE caused by the lack of insolation
269 and a smaller LW CRE due to their smaller extent and shorter lifetime, leading to a net positive
270 integrated CRE of $1 \text{ W m}^{-2} \times \text{day}$ over the course of the anvil lifecycle. Only a small change

271 in the starting time of the anvil cloud can therefore cause a substantially different net climatic effect.

272

273 The radiative effects of anvil clouds with different initialization times vary not only because of
274 insolation differences, but also because of differences in cloud optical properties. Figure 4 shows
275 the COD evolution of a daytime and nighttime simulation composite. Daytime simulations are
276 influenced by strong insolation of 900 W m^{-2} or more in the first 8 hours. The two composites
277 do not differ substantially in the first two hours of the evolution, when the COD distribution
278 of both composites peaks near 100 (Fig. 4a). For a cloud age of 3-5 hours, however, the
279 daytime composite shows a bimodal distribution with COD peaks near 100 and 3, as opposed
280 to thinner nighttime clouds peaking between COD of 3 to 30 (Fig. 4b). A large majority of
281 nighttime clouds of age 6-8 hours are optically thin (Fig. 4c), with COD smaller than 0.5,
282 and disappear almost completely by hour 9-11 of the simulation (Fig. 4d). In contrast, 6- to
283 11-hour-old daytime anvils cover a large portion of the domain with a COD distribution peak
284 that slowly shifts from ~ 1 to ~ 0.1 before fully disappearing at hour 14-16 of the simulation (Fig. 2b).

285

286 At this point we further simplify the modeling setup to isolate the differences between the
287 day and night simulations by simulating cloud evolution in perpetual midday conditions with
288 insolation values of 1300 W m^{-2} (referred to as "day-only") and perpetual night conditions (no
289 insolation, referred to as "night-only") as shown by Fig. 5a,b. The IWP evolution of the night
290 cloud strongly resembles the 21 LT case from Fig. 2a, while the day cloud resembles the 9 LT case
291 from Fig. 2b. The main difference between the evolution of the day-only and night-only cases is
292 best represented by the Fig. 6. The daytime anvil is quickly lofted by about 1.5 km due to a strong
293 SW heating that overcompensates the cloud-top LW cooling effect (Fig. 6b). The heating-induced
294 updraft (Fig. 6d) supports higher relative humidities with respect to ice (RH_{ice}), limiting the cloud

295 decay by sublimation (not shown). Nevertheless, sublimation remains the largest microphysical
296 tendency due to cloud spreading and mixing with environmental air that is subsaturated with
297 respect to ice (Fig. 7a-c). Despite the SW-driven updraft, the net sedimentation flux remains
298 substantial throughout the first 16 hours of cloud evolution (Fig. 7d). The sinking motion near
299 cloud base that appears in both day-only and night-only simulations (Fig. 6c,d) is caused by latent
300 cooling due to ice crystal sublimation, which is by far the largest ice crystal number sink (Fig. 7e).

301
302 On the other hand, the top of the nighttime anvil remains at an approximately constant altitude
303 in the first 2-4 hours of the simulation despite a strong LW cloud top cooling and the associated
304 downdrafts (Fig. 6a,c). At the same time, the center of the cloud undergoes depositional heating,
305 which helps counteract the sinking motion near the cloud top. The latent heating tendency
306 decreases through time, and the cloud gradually dissipates by sublimation and sedimentation (Fig.
307 7a-c) before completely disappearing within 8 hours of the initialization (Fig. 6a). Sublimation
308 is stronger at night because the cloud sinks down to higher temperatures and lower RH_{ice} that
309 support faster sublimation. Interestingly, there is substantially more ice crystal nucleation at night
310 than there is during the day (Fig. 7f), indicative of a stronger turbulence at night caused by the LW
311 radiative heating dipole and depositional heating within the cloud. The new ice crystal nucleation
312 is expected to prolong the cloud lifetime; however, the sublimation tendency is substantially
313 stronger, leading to a rapid cloud decay. This is confirmed by a simulation in which freezing was
314 not allowed, which show a similar evolution compared to the reference case (Figs. 5a-d and 8a-d).

315
316 The diurnal differences in cloud evolution are also modulated by differences in cloud top circu-
317 lation. The night-only simulation develops a two cell circulation (Fig. 9a,b), with a main, lower
318 branch driving the spreading of the cloud and a secondary branch near cloud top, similar to what

319 was shown by Gasparini et al. (2019) for daily average conditions. The upper circulation cell,
320 driven by LW cooling, largely disappears due to SW heating in the day-only case. The day-only
321 simulation develops only one circulation cell that leads to strong spreading and lofting of the cloud
322 (Fig. 9c,d), keeping the cloud top at near saturated conditions. The nighttime circulation erodes
323 the cloud from the top by mixing in subsaturated environmental air which decreases the cloud top
324 altitude and accelerates the cloud decay.

325 1) SENSITIVITY SIMULATIONS

326 A sensitivity test in which the clouds are transparent to radiation (no-ACRE) shows little difference
327 in cloud evolution between the two insolation setups (Figs. 5e,f in 8e,f). The no-ACRE clouds do
328 not spread and thin, but just slowly sediment out of the atmosphere and sublimate as shown by
329 the decreasing cloud top altitude in Fig. 8e,f. The absence of the radiatively-driven circulation
330 in the no-ACRE nighttime cloud prevents cloud spreading and mixing with the subsaturated
331 environmental air and prolongs the cloud lifetime when compared with the night-only simulation.
332 The domain average radiative impact of such slowly sedimenting and sublimating clouds is quite
333 limited due to their small surface area and dominated by SW CRE, leading to a net cooling effect
334 on climate (not shown).

335
336 The no-sublimation sensitivity tests lead to long-lived clouds in both day and night simulations
337 (Fig. 5g,h). The night no-sublimation experiment contains several times larger IWP than the day
338 case (confront Fig. 5g and h). This is caused by the lower cloud temperature in the daytime one,
339 when the cloud top is lofted from about 13 to about 16 km (Fig. 8g,h), experiencing about 20 K
340 colder temperatures. The colder temperatures inhibit a large portion of the depositional growth of

341 ice in the higher and colder day cloud compared with the night cloud.

342

343 Given the importance of the sedimentation flux, we analyze an additional sensitivity simulation
344 in which there is no ice crystal sedimentation (no-sedimentation). Fig. 5i,j show very similar IWP
345 time evolution in the two simulations, despite a higher cloud top in the day simulation (Fig. 8i,j).
346 Interestingly, the strong LW heating near cloud base and latent heating by deposition within the
347 cloud gradually overcompensate the LW cooling related downdraft near cloud top in the nighttime
348 simulation. Between hour 5 and 15 of the simulation, when the cloud is thinner due to its spreading
349 in the surrounding clear sky air, the heating-induced updraft velocity lofts it about 2 km (Fig. 8i).
350 The sensitivity tests reveal that cloud radiative heating, sublimation, and sedimentation all shape
351 anvil cloud evolution.

352

353 Additional sensitivity tests are performed to investigate how the diurnal cycle effect on cloud
354 evolution depends on cloud size. We hypothesize that a larger initial cloud initialized at 21 LT
355 will experience proportionally less entrainment of drier environmental air, which is maximized
356 in absence of SW heating at night. In order to test this, we performed experiments in which
357 the initial cloud diameter was halved (small-real) and doubled (large-real) compared with the
358 control simulation (ctrl-real) with a diameter of 60 km. The clouds with which the simulations are
359 initialized represent freshly detrained anvils, tightly related to the actively convective part of the
360 MCS. An actively convective surface area larger than 5000 km^2 (the equivalent of an initial cloud
361 diameter of 40 km) is therefore unlikely to exist within a single MCS (Houze 2004).

362 Figure 10 shows the ratio of the domain averaged IWP and cloud fraction between the nighttime
363 cloud initialized at 21 LT and the daytime cloud initialized at 9 LT. The smaller the fraction, the
364 quicker the nighttime cloud decays in comparison to its daytime equivalent, and the larger is the

365 impact of the diurnal cycle on the cloud evolution. As expected, both IWP and cloud fraction are
366 smaller in the nighttime clouds; the fraction is thus below 1 for all cases for most of the cloud
367 lifetimes. The impact of the diurnal cycle is thus the largest for the small-real cloud and smallest
368 for the large-real cloud. The diurnal cycle effect on cloud evolution therefore decreases with the
369 increase of the initial cloud size.

370 *c. RCE simulations*

371 To understand whether the day-night differences seen in simulations of individual clouds above
372 are present in extended simulations of clouds and convection, we perform additional simulations
373 of a cloud field in RCE. In Fig. 11, selected variables are plotted as a function of IWP, with
374 IWP decreasing from left to right. This gives an intuitive view of the anvil cloud evolution, from
375 freshly detrained anvils at the highest IWP, to aged thin anvil clouds at low IWP (please refer to
376 the Appendix C for a detailed description of the IWP binned perspective on anvil cloud evolution).
377 This view is confirmed by Fig. 11a,b that show how much time has elapsed since a parcel was last
378 in a buoyant cloudy updraft with vertical velocity larger than 1 m s^{-1} , which is representative of
379 deep convective cores. This is therefore a meaningful proxy for anvil cloud age, which increases
380 from about 1.5 hours near the main deep convective detrainment level at around 12 km altitude to
381 about 10 hours at low IWP values, typical for aged anvil clouds or in-situ formed cirrus.

382
383 The variables are shown separately as an average between 0-4 LT (typical for nighttime conditions,
384 left column), 12-16 LT (typical for daytime conditions, middle column) and the anomaly between
385 the two times (right column). The general pattern of cloud age does not change significantly
386 between day and night: however, the transition from a high IWP deep convective core to thin anvil
387 is faster at night. The 6 hour isochrone reaches the 50th IWP percentile at night (Fig. 11a) but only

388 the 70th percentile during the day (Fig. 11b), implying faster nighttime cloud decay. Moreover, the
389 clouds at levels above 12 km in all IWP bins except the highest few are fresher during daytime (Fig.
390 11c). Therefore, while the level of convective detrainment remains nearly the same throughout the
391 day, the subsequent anvil cloud evolution takes a different pathway, which is, as in the idealized
392 simulations, modulated by differences in ACRE. Strong LW cooling dominates the cloud top at
393 high IWP percentiles (thick anvil clouds) during the night, with LW heating below (Fig. 11d). In
394 the day, the SW heating is strong enough to neutralize the LW cooling, leading to no significant
395 ACRE near the tops of thick anvil clouds (Fig. 11e). However, the SW heating effect dominates in
396 the intermediate and thin anvils and induces a slow mesoscale updraft motion of about $1\text{-}7\text{ cm s}^{-1}$
397 (Fig. 11h) that supports the maintenance of anvils. In contrast, the nighttime cloud top cooling
398 leads to a downdraft motion that reaches values of about 5 cm s^{-1} on average (Fig. 11g), enhancing
399 the removal of ice crystals by sedimentation (Fig. 7d).

400 The streamfunction, computed as in Gasparini et al. (2019), shows a strong main upper
401 tropospheric branch with a maximum near the main level of deep convective outflow at 12 km,
402 extending throughout most of the domain at all times (Fig. 11j). At night, a secondary circulation
403 driven by the LW cloud-top cooling flows in the opposite direction, similarly to what shown in
404 Fig. 9a for the night-only simulation. This upper level circulation pattern nearly disappears during
405 the day (Fig. 11k). In addition, the peak of the main circulation that drives the spreading of anvil
406 clouds shifts towards higher altitudes and lower IWP percentiles (thinner anvil clouds) during the
407 day, driven by the SW ACRE.

408
409 ACRE-driven dynamical changes lead also to changes in RH_{ice} . Figure 12 provides a more
410 detailed perspective on diurnal changes in RH_{ice} , temperature, and updraft velocities in thick anvil
411 clouds (88-98 IWP percentile, COD range of 10 to 50), intermediately thick anvils (70-88 IWP

412 percentile, COD range of 2.5 to 10) and thin anvils (30-70 IWP percentile, COD range of 1-2.5).
413 The strong radiatively driven ascent in thick anvils increases RH_{ice} during daytime hours (Fig. 12a).
414 However, the increase is only modest, rarely exceeding 1 % and is not observed in thinner anvil
415 clouds. In contrast, the RH_{ice} decreases during the day in the rest of the model domain, particularly
416 in the clear sky areas (Fig. 12b). This is caused by a combination of weak diurnal heating of the
417 clear sky portion of the domain by the SW absorption by water vapor (Fig. 12c) and conservation
418 of mass, which implies a stronger compensating subsidence in clear sky regions at times of elevated
419 upward mass flux in the anvil-covered part of the domain. The simulated diurnal changes in clear
420 sky RH_{ice} are comparable to those in Megha-Tropique satellite observations (Chepfer et al. 2019).
421 The dynamical cooling effect caused by within-anvil updraft motions during daytime is not strong
422 enough to compensate for the heating due to the SW absorption, leading to a slightly increased
423 anvil temperature in the afternoon hours (Fig. 12c).

424 1) DIURNAL VARIATIONS IN TURBULENCE AND MESOSCALE ASCENT

425 Figure 12d confirms that the frequency of updraft motions within anvil clouds (defined as updrafts
426 $> 1 \text{ cm s}^{-1}$) is higher during daytime hours, with a clear peak around 12 LT for thick anvils, and
427 a similar, but less pronounced peak for intermediate anvils peaking 1-2 hours later in the early
428 afternoon. The peak in updraft frequency within thin anvils is delayed until approximately 16 LT
429 due to a slow dynamical response to their weak heating rate. Interestingly, the occurrence frequency
430 of strong updraft motions, representative of turbulence, shows the opposite behavior, peaking in the
431 night, and reaching minimum values during the afternoon hours (Fig. 12e). Turbulence is favored
432 when there is a heating dipole comprised of cloud-top radiative cooling and internal heating due
433 to radiation and latent heat release, which initiates in-cloud convection (Fig. 11d). The standard
434 deviation of in-cloud updraft velocity (Fig. 12f) shows a similar diurnal cycle, with a nighttime

435 peak and a minimum at about 14 LT for both thick and intermediate anvil clouds, and a delayed
436 afternoon minimum for thin anvils at about 17 LT.

437 2) DIURNAL VARIATIONS IN ICE MICROPHYSICAL PROPERTIES

438 Anvil cloud ice mixing ratio can vary from values close to 1 g kg^{-1} in fresh anvils to 10^{-3} g
439 kg^{-1} in thin anvil clouds (Fig. 13a,b). Similarly, the simulated ice crystal number concentrations
440 often exceed 1000 L^{-1} in fresh anvils, with concentrations between 5 and 100 L^{-1} typical for
441 thinner anvil clouds (Fig. 13d,e). Ice crystal effective radius is inversely proportional to altitude;
442 the model simulates particle sizes of about $70 \mu\text{m}$ at 8 km altitude, which decreases to about
443 $10 \mu\text{m}$ at 15 km as a result of gravitational settling of larger ice crystals and the slowdown of
444 depositional growth at cold temperatures (van Diedenhoven et al. 2020). Ice crystals are larger in
445 deep convective cores and fresh anvils, as the strong updrafts can overcompensate sedimentation
446 of both smaller and larger ice crystals (Fig. 13g,h).

447
448 Changes in ACRE lead to differences in anvil cloud microphysical properties. Both ice mixing
449 ratio and ice crystal number concentration are more top heavy in the day compared with night (Fig.
450 13a-f). Most of the simulated anvil ice crystals originate from freezing within deep convective
451 updrafts. The variations in anvil ice crystals size and number are therefore indicative of changes
452 in detrained air parcel trajectories and not of new nucleation events outside of deep convective
453 cores as demonstrated by the small influence of ice nucleation on the evolution of idealized cloud
454 simulations (Figs. 5c,d and 8c,d). Upward motions during the day counteract sedimentation and
455 therefore support anvil clouds with larger ice crystal radii, particularly for intermediately thick and
456 thin anvil clouds (Fig. 13h).

3) DIURNAL VARIATIONS IN CONVECTIVE UPDRAFTS AND FRESHLY DETRAINED ICE MICROPHYSICAL PROPERTIES

Diurnal variations in anvil cloud properties may partially depend also on the convective processes, particularly the updraft velocity and its microphysical implications. Figure 14a,b shows the mean values of updraft velocity in cloudy updrafts with vertical velocities larger than 1 m s^{-1} that are positively buoyant and its anomalies with respect to diurnal mean values. The convective updraft velocities do not vary much throughout the day, with substantial anomalies occurring only above the peak anvil detrainment level, where deep convective updrafts occur infrequently, leading due to small sample sizes only to random fluctuations in updraft strength. Moreover, the fluctuations largely disappear when computing median instead of mean velocities (not shown). Panels 14c-h similarly show mean values (left column) and their anomalies with respect to diurnal mean (right column) for ice cloud properties of freshly detrained anvil clouds, with a cloud age of less than 1 hour. The variability of freshly detrained ice properties at the main detrainment level between 9 and 13 km is very limited and possibly related to variations in cumulus congestus and not anvil clouds.

4. Discussion

This work agrees with recent modeling (Ruppert and Hohenegger 2018; Ruppert and Klocke 2019) and observational studies (Deng and Mace 2008; Wall et al. 2020; Sokol and Hartmann 2020) that point at the important role of daytime cloud heating by SW absorption in modulating the anvil lifecycle. Our results confirm both hypotheses posed by Ruppert and Klocke (2019): SW heating of anvils causes a daytime upper tropospheric increase in upward motion and consequently leads to longer lived and more widespread anvil clouds. While Ruppert and Klocke (2019) and Ruppert and O'Neill (2019) considered the role of SW heating in organized convection, our work points out at an important role of the SW-driven ascent for non-organized convective systems, that were a

480 focus of our idealized and RCE simulations. SW radiative heating was based on ground radar mea-
481 surements hypothesized to drive diurnal variations in both cloud macrophysical and microphysical
482 properties (Deng and Mace 2008), which was largely confirmed by our idealized model simulations.

483
484 Our work shows that despite being less frequent, daytime MCS play an important role in the
485 climate system by spawning anvil clouds supported by solar heating that ultimately cover a larger
486 fraction of the tropical maritime areas compared to anvils initialized in more frequent nocturnal
487 and early morning MCS. MCS were previously shown to contribute most to the total precipitation
488 in most of the tropics, thus controlling also the diurnal cycle of precipitation with a peak in the
489 early morning hours (Zipser and LeMone 1980; Fu et al. 1990), when the number of MCS is
490 maximal. This coincides with the diurnal BT frequency peak for $BT < 210$ K shown in Fig. 1. In
491 contrast, the relatively less frequent daytime convection and MCS drives the afternoon-evening
492 peak in anvil cloud fraction of decreasing cloud optical depths and thus exhibits a strong control
493 on both SW and LW radiative fluxes.

494
495 Tropical anvil clouds are affected not only by slow, laminar, mesoscale circulations associated
496 with the diurnally enhanced in-cloud ascent but also by in-cloud convection. Ground radar mea-
497 surements from the Tropical Western Pacific presented in Wall et al. (2020) show a larger variance
498 in updraft velocities during the night for thick and intermediate anvil clouds, which is consistent
499 with our findings and indicative of higher turbulence. The cloud top ice crystal number was found
500 to be smaller during night in CloudSat-CALIPSO observations (Wall et al. 2020), despite more
501 turbulent environmental conditions, favorable for new ice nucleation, which is agreement with our
502 modeling results. Our simulations indicate that most of ice crystals detrain from deep convection,
503 and thus subsequent ice nucleation within or at the edge of anvil clouds is not frequent enough to

504 significantly affect the ice crystal number budget. This is in contrast to Hartmann et al. (2018) who
505 found that new ice nucleation is an important mechanism prolonging anvil cloud lifetime. However,
506 their simulations used a fully cloud covered domain, in which the cloud could not dissipate by
507 spreading into neighboring air. This spreading also disperses the cloud's turbulent kinetic en-
508 ergy over a larger area, decreasing the potential for in-cloud convection (Schmidt and Garrett 2013).

509
510 Our work offers support for hysteresis in anvil clouds. Anvil evolution takes a different pathway
511 depending on the amount of insolation during the fresh anvil stage. Anvils subjected to insolation
512 of about 800 W m^{-2} or more maintain a constant cloud top height or even undergo lofting and
513 enhanced spreading that cannot be achieved at night, in the early morning, or in the late afternoon
514 (Fig. 15). This is consistent with the observational finding of Sokol and Hartmann (2020) that
515 fresh anvil clouds sink after detrainment at night but are maintained at higher altitudes during the
516 day. They speculated that the altitude, geometric thickness, and radiative heating rates of aged
517 anvil clouds are influenced by the time of day at which the cloud was detrained. Our findings are
518 consistent with this notion.

519 We also find that the time at which an anvil cloud is detrained influences the cloud's climatic
520 effects. In RCE simulations, deep convective activity peaks at 5 LT. A mere one-hour shift in
521 the timing of this peak could lead to substantially different anvil net CRE. A hypothetical shift of
522 convective detrainment from 5 to 6 LT would lead to a $3 \text{ W m}^{-2} \times \text{day}^{-1}$ more negative integrated
523 net CRE (or a $2 \text{ W m}^{-2} \times \text{day}^{-1}$ more positive integrated net CRE in the case of an opposite
524 shift from 5 to 4 LT) based on the simulated single cloud evolution simulations (Fig. 3). A
525 modeling study using a general circulation model in present and 4K warmer climate found a 4-hour
526 delayed convective activity peak in the warmer climate compared with the reference climate, that
527 contributed to a significant negative diurnal component of the cloud feedback (Gasparini et al.

528 2021). However, more work is needed to understand whether a change in the diurnal cycle of deep
529 convection and anvil clouds in a warmer climate is a robust response to increased greenhouse effect
530 or only an artifact of a single climate modeling study.

531 **5. Conclusions**

532 In this study we first analyzed the diurnal variations in BT from Himawari geostationary satellite
533 observations in the Tropical Western Pacific, which indicate an afternoon diurnal peak in anvil
534 cloud fraction, in contrast to the early morning peak in deep convective activity and rainfall. The
535 large time gap between the peak in convection and in anvil cloud fraction implies that the evolution
536 of anvil clouds must differ between daytime and nighttime. In particular, the daytime anvils must
537 be more widespread and/or long-lived compared with the nighttime anvils.

538 In order to explain this observed behavior we used idealized simulations with the SAM cloud-
539 resolving model. We initialized each of the simulations with a cylindrical-shaped cloud, comparable
540 to freshly detrained, thick anvil clouds and let the cloud evolve freely. The only difference between
541 the simulations is their starting time; we started identical clouds at each hour, from 0 to 23 LT. The
542 clouds' evolution pathways differ substantially in terms of cloud lifetime, coverage, and climatic
543 effects. The absorption of SW radiation by ice crystals was found to be the key driver of diurnal
544 differences between simulated anvil clouds (Fig. 15). The anvil clouds exposed to insolation of
545 about 800 W m^{-1} or more are able to support a mesoscale ascent that partially counteracts the
546 sedimentation of ice crystals and supports favorable conditions for cloud maintenance by keeping
547 the cloudy parcels saturated. The heating that the cloud experiences in tropical regions around
548 noon can be strong enough to loft the cloud. Moreover, the SW heating intensifies the radiatively
549 driven circulation, leading to a faster spreading of the cloud that in turn covers a larger surface area
550 (Fig. 15). On the other hand, nighttime anvil cloud top is dominated by the LW cooling, which

551 drives a circulation near cloud top that entrains drier environmental air into the cloud, eroding the
552 cloud top and shortening its lifetime. This effect weakens for more extensive anvil cloud systems.

553 The RCE simulation with a realistic diurnal cycle provides additional support for the results
554 of the idealized simulations. The SW-driven mesoscale ascent both increases the cloud top
555 altitude during the day and allows more and larger ice crystals near the anvil cloud top. Despite
556 experiencing elevated levels of turbulence that trigger more ice nucleation, nighttime anvils
557 contain fewer ice crystals near cloud top where nucleation is most likely to occur. The source of
558 ice crystal number by in-situ ice nucleation was found to be only of secondary importance for
559 anvil evolution, behind the dominant source of ice crystals by cloud droplet freezing within deep
560 convective updrafts. Cloud properties were not found to vary substantially at or immediately after
561 the deep convective detrainment.

562
563 The evolution and climatic effect of anvil clouds largely differ based on the time of cloud
564 initialization. It is crucial that models successfully reproduce the timing of deep convection and
565 correctly represent the radiative-microphysical-dynamical interactions driving anvil decay. Only
566 in this way can climate and cloud-resolving models successfully reproduce the tropical energy
567 balance and lend credibility to their projections of future climate.

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581 der <https://doi.org/10.34730/266ca2a41f4946ff97d874bfa458254c> (Krämer et al. 2020). Data and
582 analysis scripts necessary to generate the figures in the manuscript are available at 10.5281/zen-
583 odo.5534641.

584 APPENDIX A

585 **Comparison of modelled tropical ice cloud properties with in-situ data**

586 Cloud properties from a 30-day long free running RCE simulation are compared with 69
587 hours of aircraft observational data used in Krämer et al. (2020) from 3 field campaigns
588 in the Tropical Western Pacific ocean, namely: The NASA Airborne Tropical Tropopause
589 Experiment (ATTREX) (Jensen et al. 2017), The NASA Pacific Oxidants, Sulfur, Ice, De-
590 hydration, and cONvection (POSIDON) Experiment (<https://espo.nasa.gov/posidon>), and The
591 Convective Transport of Active Species in the Tropics (CONTRAST) Experiment (Pan et al.
592 2017). ATTREX and POSIDON measurements were focused on the tropical tropopause region,
593 collecting data mainly from thin cirrus at temperatures between -90°C and -60°C. In CONTRAST
594 Experiment, as a difference, clouds were sampled between the marine boundary layer and the
595 bottom of the tropical tropopause region at about 14 km altitude, including the altitude of main

596 deep convective detrainment. The plotted quantities refer to ice only properties at tempera-
597 tures colder than -35°C and a mixture of cloud ice and liquid in the mixed-phase temperature range.

598

599 Despite its simple simulation setup, the model is able to reproduce many features of the tropical
600 climate, in particular the balance between the radiative cooling of the cloud-free atmosphere
601 and the convective heating, which initiates deep convection along with detrained ice clouds of
602 decreasing optical thickness. Sufficiently moist and cool upper tropospheric air parcels subjected
603 to updraft motion initiated by gravity waves can, moreover, nucleate in-situ cirrus clouds through
604 both homogeneous and/or heterogeneous ice nucleation (Shi et al. 2015). The median total water
605 content (TWC) decreases with decreasing temperature from values of 10^{-3} to 10^{-2} g m^{-3} at
606 temperatures warmer than -40°C to 10^{-5} g m^{-3} at T of -80°C (Fig. A1a), as expected by the
607 decreasing availability of vapor for deposition growth (van Diedenhoven et al. 2020). In contrast,
608 cloud number concentrations increase with decreasing temperatures, although the variation is not as
609 pronounced as for TWC (Fig. A1d). The mean mass radius increases with increasing temperatures
610 until a maximum size is reached at about -35°C . The subsequent decrease is a result of a mixture of
611 large ice crystals with smaller and numerous cloud droplets and ice crystals formed by secondary
612 ice production (Fig. A1g).

613 The model is able to reproduce most of the observed relationships as shown by the middle
614 column. Nevertheless, the comparison reveals a general underestimation of the TWC (Fig. A1c),
615 an underestimation of ice crystal number at temperatures colder than -60°C (Fig. A1f) and a slight
616 underestimation of ice radius at temperatures between -60°C and -40°C (Fig. A1i). There are two
617 possible origins of the mentioned biases:

618 1. the models' tendency to produce too numerous very thin ice clouds due to numerical diffusion.
619 Such clouds, however, do not exert any significant climate forcing and therefore do not
620 significantly bias the modeled radiative balance.

621 2. The biases may be partly attributed to the limitations in in-situ retrievals, given that the clouds
622 containing low concentrations of small ice crystals cannot be detected with current particle
623 measurement techniques (Krämer et al. 2016; Baumgardner et al. 2017).

624 Finally, the model lacks the Brewer-Dobson circulation, which leads to a warm bias in the
625 tropopause region and the underestimation of the in-situ formed thin tropopause cirrus. The
626 increase in all ice properties at the coldest modeled temperatures is a result of penetrating deep
627 convective outflow, which is infrequent and not sampled by the observational dataset.

628 APPENDIX B

629 **Relationship between brightness temperature and high cloud optical depth**

630 In this appendix, we justify our claim from Section 3a that variability in the BT distribution
631 reflects the evolution of anvil clouds. We examine the relationship between BT and COD using
632 BT measurements from MODIS and cloud property, cloud top height, and COD retrievals from
633 DARDAR-CLOUD v2.1.1. We use a full calendar year (2009) of measurements from the Tropical
634 Western Pacific (12°S-12°N, 150°E-180°E). The MODIS 11- μm BT measurements are obtained
635 from the Level 2 Cloud Product (Platnick et al. 2017) and have a 5×5 -km resolution. The DARDAR
636 (raDAR-liDAR) retrievals combine measurements from CloudSat's radar and CALIPSO's lidar to
637 estimate the optical and microphysical properties of ice clouds (Delanoë and Hogan 2008). The
638 vertical resolution is 60 m and the retrieval profiles have a horizontal spacing of about 1.1 km. We
639 correct for the diurnal cycle of lidar sensitivity by removing cloudy pixels that were detected by

640 the lidar only if they have a visible extinction coefficient below 0.12 km^{-1} , as described in Sokol
641 and Hartmann (2020). For each DARDAR retrieval profile, we calculate COD for each individual
642 cloud layer by vertically integrating the visible extinction coefficient. We then use nearest-neighbor
643 interpolation to find the associated BT, which is only considered valid if the distance between the
644 retrieval profile and the center of the nearest MODIS pixel is less than 3.5 km. Because the BT
645 pixel dimensions are larger than DARDAR's horizontal resolution, each BT measurement can be
646 associated with several COD retrievals.

647 There are several factors that cause the COD distribution associated with any particular BT to be
648 wide. Some of these factors are physical. For example, the emission temperature of a cloud with
649 fixed COD will vary depending on cloud altitude and microphysical structure, and BT can further
650 be affected by the presence of additional cloud layers below a high, thin cirrus. Then there are the
651 factors associated with the retrievals themselves, such as the DARDAR-CLOUD retrieval error (see
652 Cazenave et al. (2019) for an in-depth discussion) and the fact that retrievals are only performed
653 for ice-phase clouds. The latter's influence is likely small, since the liquid-phase clouds of the
654 boundary layer have emission temperatures similar to that of the surface. Finally, there are factors
655 related to the collocation methods we have used to match MODIS BT and DARDAR-CLOUD
656 COD observations. The main source of error here is the previously noted discrepancy between
657 the MODIS and DARDAR horizontal resolutions. Consider a hypothetical but illustrative case
658 in which a 25-km^2 area is covered in part by a deep convective core and in part by cloud-free
659 conditions. The core and ocean surface are associated with BTs in the realm of 200 and 300 K,
660 respectively. The MODIS observation for this area will record a BT somewhere in between these
661 two extremes, while some of the associated DARDAR retrievals will high COD and others will
662 have zero COD. Despite these sources of error, we believe the analysis presented here allows for a
663 solid understanding of the relationship between BT and COD.

664 The COD distributions for 10-K BT bins are shown in Fig. B1. The left column shows COD
665 distributions for the 67% of cloudy profiles that contain one ice cloud layer. Figure B2 shows
666 a joint histogram of BT and cloud top height (CTH) for these one-layer profiles. BTs between
667 190-200 K correspond to optically thick clouds with CTH above 14 km; these are deep convective
668 cores and fresh, optically thick anvils. As BT increases from 220 to 290 K, the COD distribution
669 shifts progressively to smaller values. At the same time, the CTH distribution varies very little,
670 remaining centered in the 14.5-16 km range. There are a small number of observations with CTH
671 below 10 km in the 250-290 K BT range, which we suspect are mid-level clouds with glaciated
672 tops. But these instances are rare, suggesting that BT is controlled by high cloud optical thickness
673 rather than cloud altitude.

674 The right column of Fig. B1 shows COD distributions for the 25% of cloudy profiles that contain
675 two ice cloud layers. The uppermost cloud layers in these profiles are nearly always cirrus clouds
676 with CTH above 10 km. As expected, their COD distributions (blue shading) follow a pattern
677 similar to that seen in one-layer profiles. The lower layers, on the other hand, are more diverse.
678 About half of the lower layers between 200-290 K are also cirrus clouds, with CTH above 10 km
679 and relatively small COD. The remainder have CTH below 10 km and a wide range of COD. We
680 speculate that these are mid-level, partially glaciated cumulus clouds that produce a COD signal
681 corresponding only to their glaciated portions. In profiles near deep convection, it is also possible
682 that the lower layers are mid-level outflow plumes from convective cores. Profiles with three or
683 more layers (not shown) account for only 7% of cloudy profiles.

684 The warmest BT bin (290-300 K) accounts for 42% of the BT measurements in our data set. A
685 majority of the profiles in this BT range do not contain any ice cloud layers (58%). Nearly all of the
686 cloud-containing profiles contain one or two cirrus layers with CTH above 10 km and an average
687 COD of 0.28.

688 The relationships between BT and COD examined here suggest that BT is most often a reflection
689 of cirrus COD, with the exception of the lowest BTs associated with deep convective cores. Figure
690 B2 supports this finding, showing that the CTH distribution in one-layer profiles is relatively
691 constant across the observed BT range. This conclusion is to be expected, first because cirrus are
692 the dominant cloud type in tropical convective regions, and second because cirrus altitude varies
693 little compared to cirrus COD. Based on these findings, it is reasonable to attribute variations in
694 the BT distribution to cirrus cloud evolution.

695 APPENDIX C

696 **Anvil cloud representation binned by their respective ice water path**

697 Free tropospheric clouds in tropical deep convective regions are dominated by anvil clouds of
698 various COD and IWP. The evolution of tropical high clouds of significant COD typically begins
699 with deep convective detrainment: such clouds contain the highest IWP (on the order of kg m^{-2})
700 and the largest COD. They quickly lose ice by precipitation and sublimation and continue their
701 lifecycle as anvil clouds of decreasing COD until reaching the thin cirrus stage, when they become
702 difficult to distinguish from the very thin in-situ nucleated clouds typical of the tropical tropopause
703 layer.

704 We therefore group tropical high clouds by their IWP into 50 bins. Each of the bins contains
705 the same amount of data points (2%) and thus covers exactly the same portion of the total surface
706 area of the domain. We implemented a new model tracer that is set to 1 in all positively buoyant
707 grid boxes with updrafts larger than 1 m s^{-1} that contain at least $10^{-3} \text{ g kg}^{-1}$ of condensed water
708 (either liquid or ice) and decays with a half-life of 30 minutes elsewhere. The tracer helped us
709 estimate the time that has passed since the deep convective detrainment. The cloudy air parcels in
710 the highest IWP bin have been detrained from deep convective updrafts about 1.7 hours earlier, on

711 average. The cloud age increases quickly, reaching 5 hours at the 84th IWP percentile with COD
712 of about 7 and an IWP of 100 g m^{-2} (Fig. C1a-c). Shortly thereafter, at COD of about 4 and age of
713 6 hours, the LW CRE becomes dominant over the SW CRE, and the cloud on average shifts from
714 a state with net negative towards net positive CRE (Fig. C1b). The cloud continues to lose IWP
715 until reaching values of about 10 g m^{-2} near 60th percentile bin at an average cloud age of about 7
716 hours. The cloud evolution slows down at this stage as indicated by the flattening of the cloud age
717 trajectory, despite continuing to lose IWP. As a difference, the lowest 20 percentile bins result in a
718 steep increase in cloud age, indicating a change of regime, which may be associated with optically
719 very thin in-situ formed cirrus that may not be directly connected with the initial deep convective
720 detrainment. Typical COD for such clouds range between 0.01 and 1, significantly lower than
721 what shown by the COD plot in Fig. C1b, likely because of the effect of the underlying clouds.
722 Interestingly, the SW CRE increases with increasing IWP percentile values until reaching the 95th
723 percentile. The thickest anvils and deep convective outflow preferentially occur during the early
724 morning hours in absence of insolation, therefore decreasing the SW CRE while still contributing
725 to an increasing LW CRE.

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TABLE 1. List of abbreviations.

Abbreviation	Meaning
ACRE	atmospheric cloud radiative effect
BT	brightness temperature
CRE	cloud radiative effect
CNC	cloud number concentration
COD	cloud optical depth
CTH	cloud top height
LT	local time
IWC	ice water content
IWP	ice water path
LW	longwave radiation
RCE	radiative-convective equilibrium
R_{cloud}	cloud mean mass radius
RH_{ice}	relative humidity with respect to ice
SAM	System for Atmospheric Modeling
SW	shortwave radiation
TWC	total water content

TABLE 2. A list of performed simulations.

Simulation	insolation	Description
1. Cloud in the middle of the domain		
ctrl-real	realistic diurnal cycle	full physics, 24 simulations initialized between 0 and 23 LT
small-real	realistic diurnal cycle	full physics, as ctrl-real but with initial cloud diameter of 30 km
large-real	realistic diurnal cycle	full physics, as ctrl-real but with initial cloud diameter of 120 km
day/night-only	day (1300 W m^{-2}) and night (0 W m^{-2})	full physics, as ctrl-real but with constant insolation
no-freezing	day (1300 W m^{-2}) and night (0 W m^{-2})	as day/night-only but with no ice nucleation
no-ACRE	day (1300 W m^{-2}) and night (0 W m^{-2})	as day/night-only but with no ACRE
no-sublimation	day (1300 W m^{-2}) and night (0 W m^{-2})	as day/night-only but with no sublimation
no-sedimentation	day (1300 W m^{-2}) and night (0 W m^{-2})	as day/night-only but with no sedimentation
2. RCE	realistic diurnal cycle	50-day simulation in radiative-convective equilibrium

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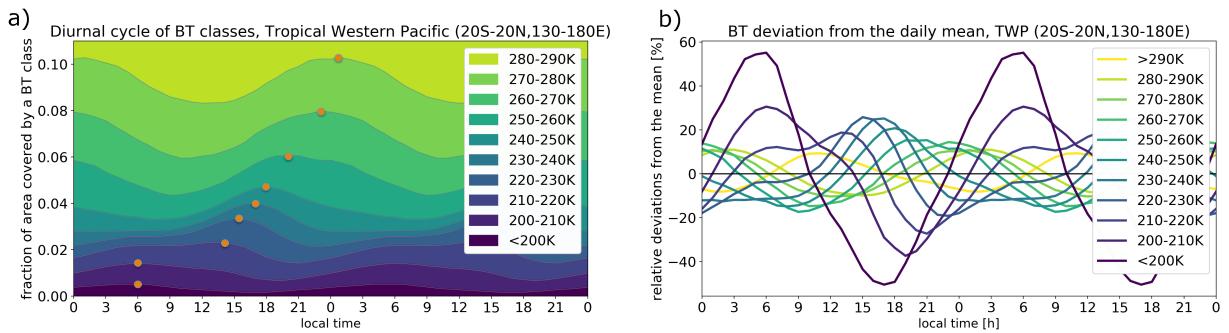
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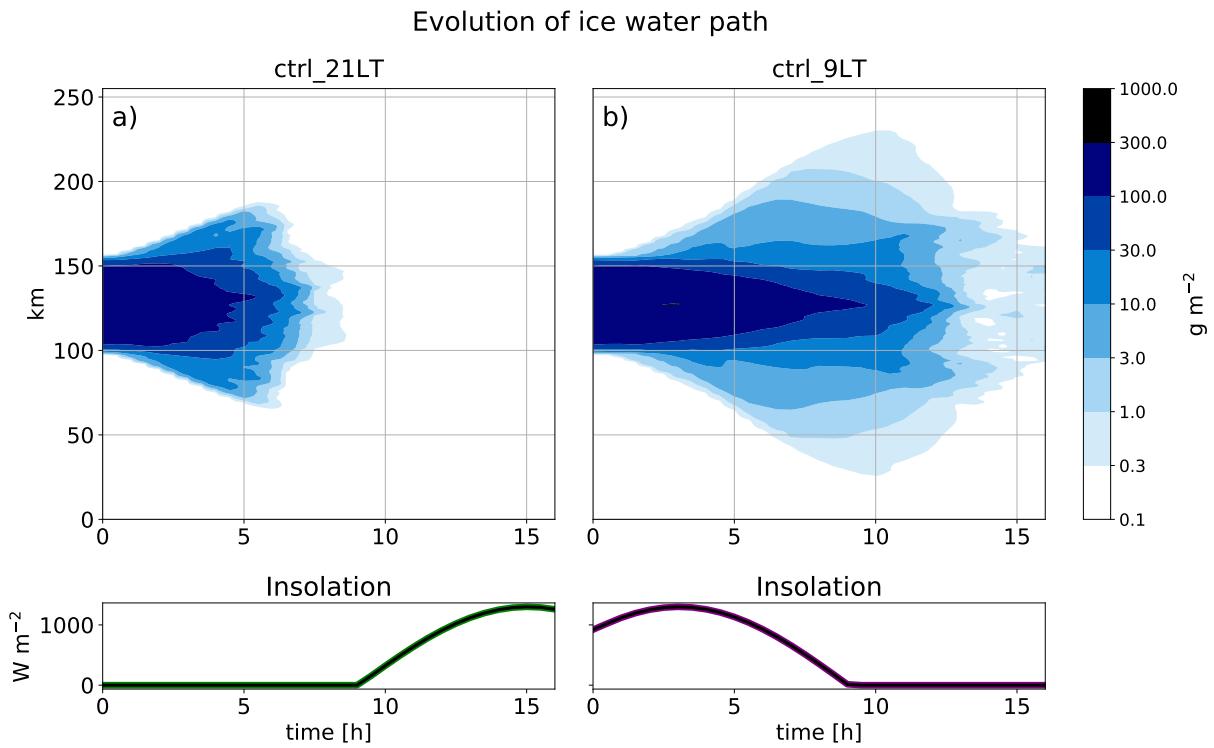
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 952 LT compared to the simulation started at 9 LT. The small-real initial cloud diameter is 30
 953 km, ctrl-real is 60 km, and large-real is 120 km. 57

954 **Fig. 11.** Cloud age (a-c), radiative heating (d-f), vertical velocity (h-i) and streamfunction (j-l) binned
 955 by ice water path (IWP) for night (0-4 local time, left column) and day (12-16 local time,
 956 middle column). The right column represents the absolute anomaly between day (left column)
 957 and night (middle column) quantities. The black contour lines represent cloud fraction of

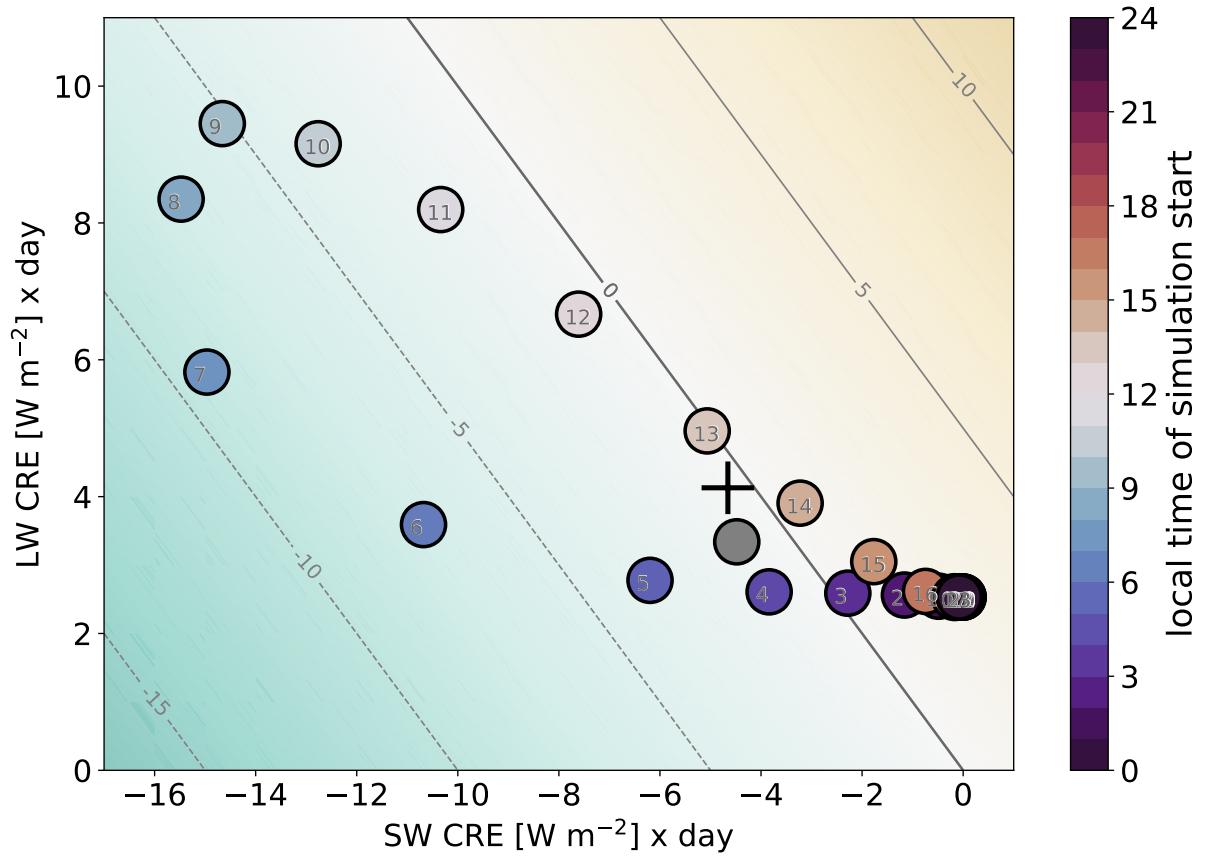
958	0.9, 0.5, and 0.1. Hatching is applied in the right column to areas that not significant at 1	
959	percent level.	58
960	Fig. 12. Diurnal cycle of RH_{ice} for thick, intermediate and thin anvil clouds (a) and clear sky regions	
961	(b) averaged for altitudes between 10 and 15 km. The deviation of the temperature from the	
962	mean over the diurnal cycle between 10-15 km altitude is plotted in panel (c). Panels d-f	
963	show an in-cloud vertical velocity analysis for the upper portions of the anvil clouds (12-15	
964	km altitude), namely: the frequency of vertical velocity $> 1 \text{ cm s}^{-1}$ (d), frequency of vertical	
965	velocity $> 50 \text{ cm s}^{-1}$ (e), standard deviation of vertical velocity (f).	59
966	Fig. 13. In-cloud ice mixing ratio (a-c), ice crystal number (d-f), and ice crystal radius (g-i) binned by	
967	ice water path (IWP) for night (0-4 local time, left column) and day (12-16 local time, middle	
968	column). The values are averaged over the cloudy portion of the domain (condensed water	
969	$> 1 \text{ mg kg}^{-1}$). The right column represents the absolute anomaly between day (left column)	
970	and night (middle column) quantities. The black contour lines represent cloud fraction of	
971	0.9, 0.5, and 0.1. Hatching is applied in the right column to areas that not significant at 1	
972	percent level.	60
973	Fig. 14. Diurnal variations of the mean deep convective updraft velocity, diagnosed only for updrafts	
974	stronger than 1 m s^{-1} and of the microphysical properties for clouds within the first hour after	
975	detrainment. The right column represents the anomalies from the diurnal average values	
976	computed separately for each vertical layer.	61
977	Fig. 15. Main mechanisms that lead to diurnal changes in anvil clouds.	62
978	Fig. A1. Total water content (TWC, a-c), cloud number concentration (CNC, d-f), and cloud mean	
979	mass radius (R_{cloud} , g-i) from in-situ measurements sampled in 3 tropical Pacific field	
980	campaigns (left column) and from the RCE model simulation (middle column). The mass	
981	mean radius is defined as $R_{cloud} = (3TWC/4\pi\rho N_{cloud})^{1/3}$. The data are sorted in 4°C	
982	temperature bins. The colors represent the occurrence frequency of one of the 3 cloud	
983	properties, normalized to reach 100% in each of the temperature bins. The green and blue	
984	lines represent the median values of the in-situ and model data in all subplots, including the	
985	right column. The colors in the right column represent the occurrence frequency anomaly	
986	between the first two columns.	63
987	Fig. B1. Distributions of cloud optical depth for different brightness temperature classes. Left column:	
988	retrieval profiles with one ice cloud layer. Right column: profiles with two ice cloud layers.	64
989	Fig. B2. Joint histogram of brightness temperature and cloud top for profiles with a single ice cloud	
990	layer. The histogram is normalized by brightness temperature bin such that the values in	
991	each column sum to unity. The navy bar chart shows the relative frequency of each BT bin	
992	in the study region. Data are for both day and night.	65
993	Fig. C1. Anvil cloud age (a), cloud optical depth (b), ice water path (IWP) (c) and top of the atmosphere	
994	cloud radiative effects (CRE) (d) binned by ice water path percentiles.	66



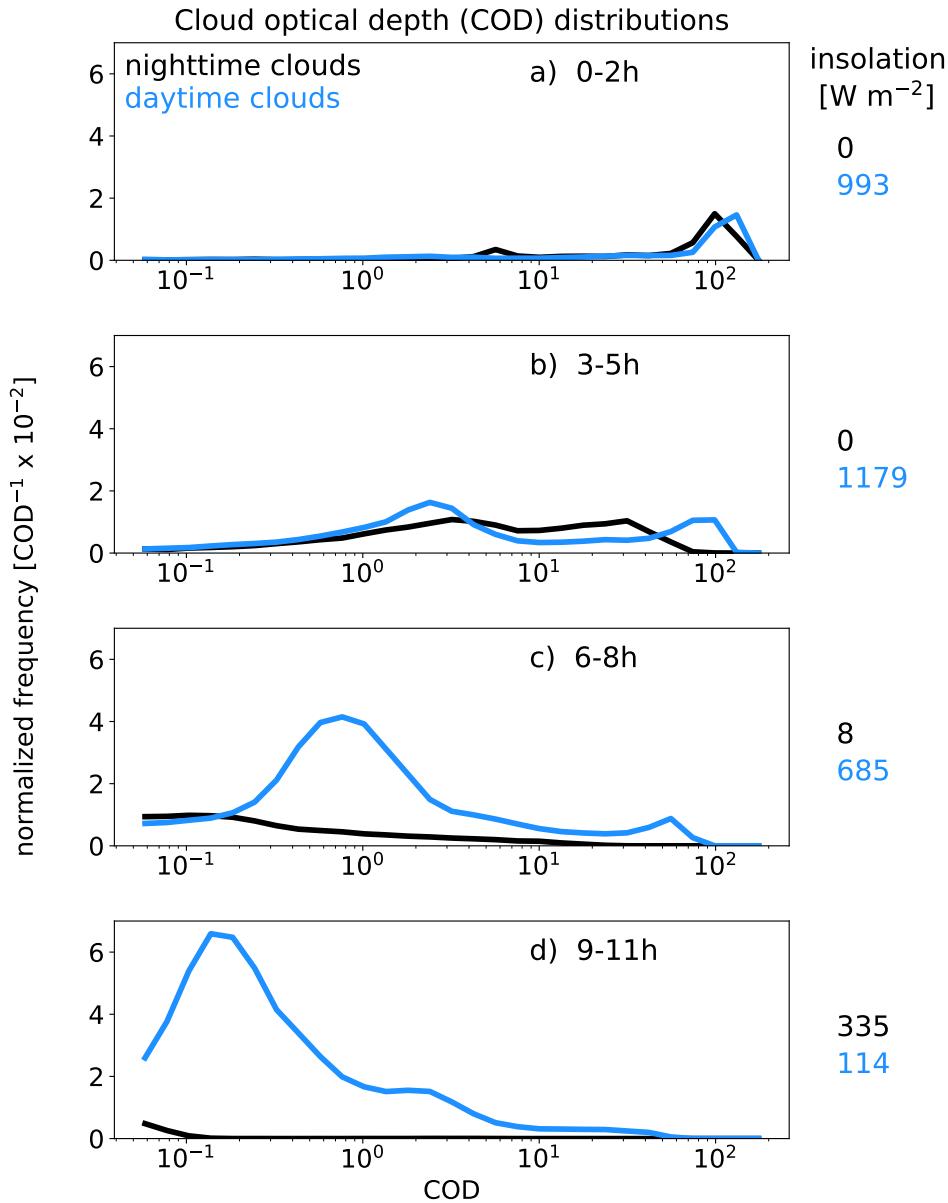
995 FIG. 1. Diurnal cycle of 10 K brightness temperature (BT) bins in the Tropical Western Pacific; (a) variations
 996 of occurrence frequency and (b) relative deviations from the diurnal means. The diurnal peak in occurrence
 997 frequency in of each BT bin in (a) is marked by orange dots.



998 FIG. 2. Time evolution of ice water path for a cloud initialized at 21 LT (a) and 9 LT (b), averaged over one of
 999 the two horizontal dimensions. The respective insolation profiles are shown in the lower panels.

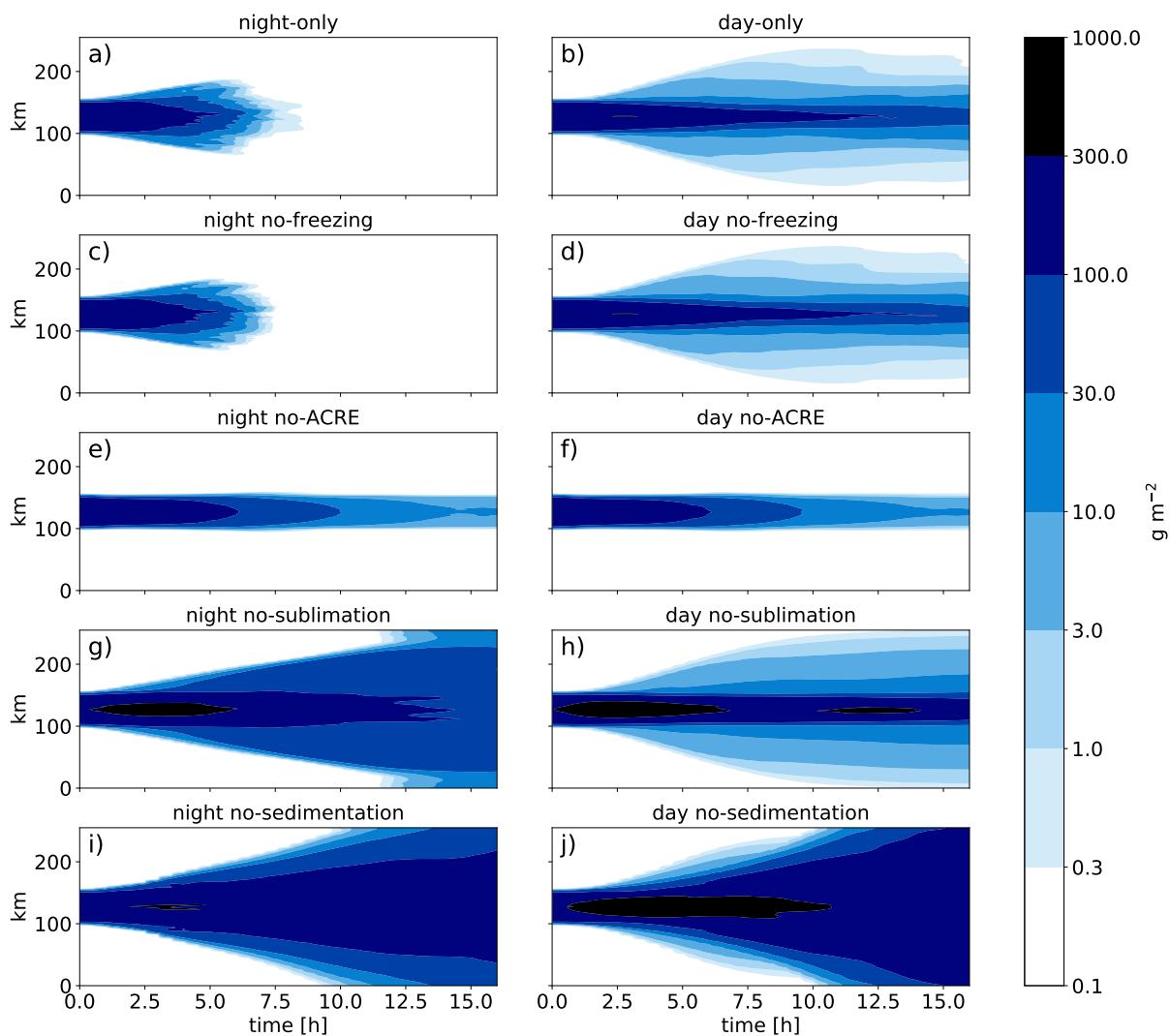


1000 FIG. 3. Domain- and time-integrated cloud radiative effect (CRE) for simulations with variable local time of
 1001 simulation start. The background color represents the net integrated CRE. The gray circle represents the values
 1002 for the simulation at perpetual diurnally averaged insolation. The black plus sign represents the average of all 24
 1003 simulations.

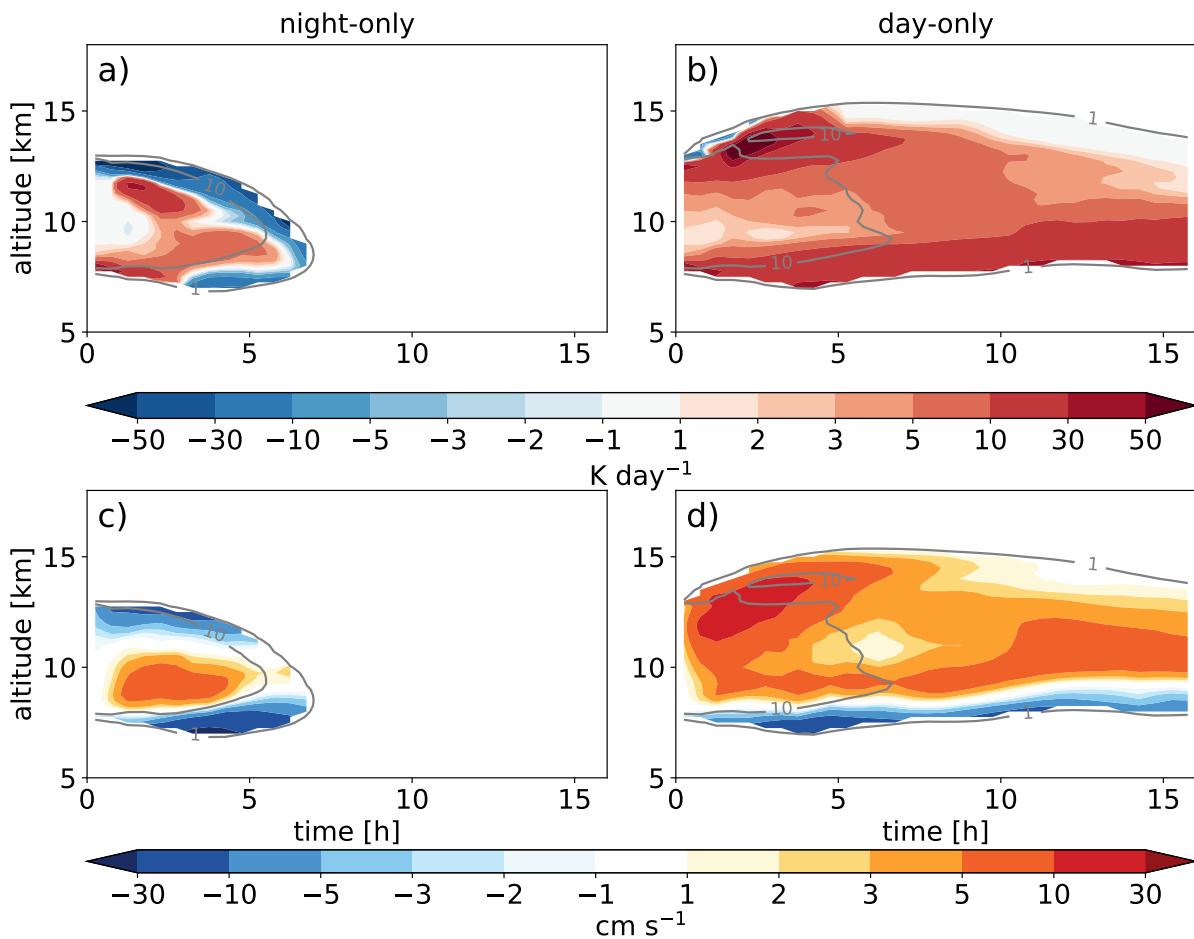


1004 FIG. 4. Evolution of the cloud optical depth distribution over the anvil lifecycle. Daytime anvil composite
 1005 represents simulations started between 7 and 11 LT, nighttime composite represents simulations started between
 1006 19 and 23 LT. (a)–(d) The fraction of the domain covered by each COD bin for different values of cloud age. A
 1007 cloud age of zero corresponds to the starting time for each of the simulations.

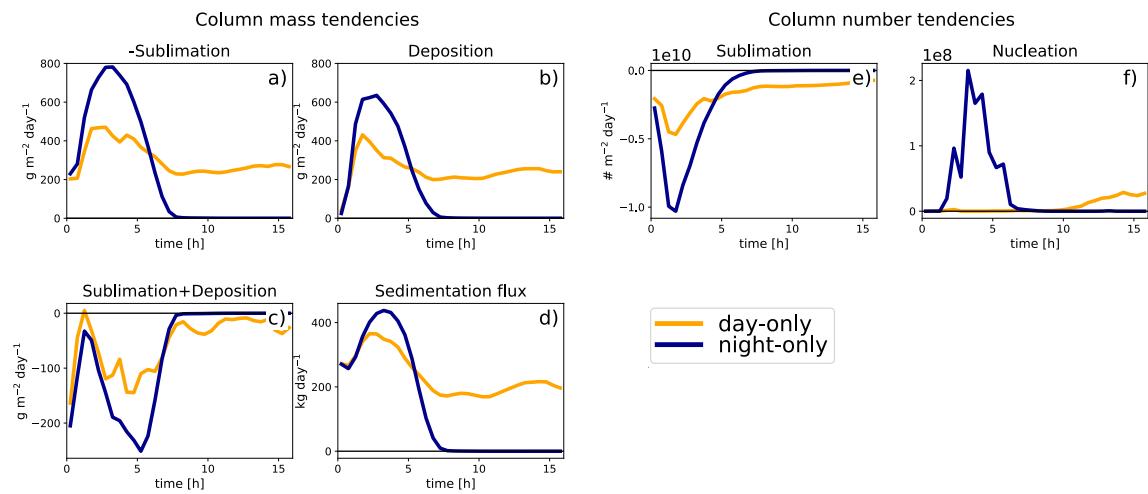
Evolution of ice water path



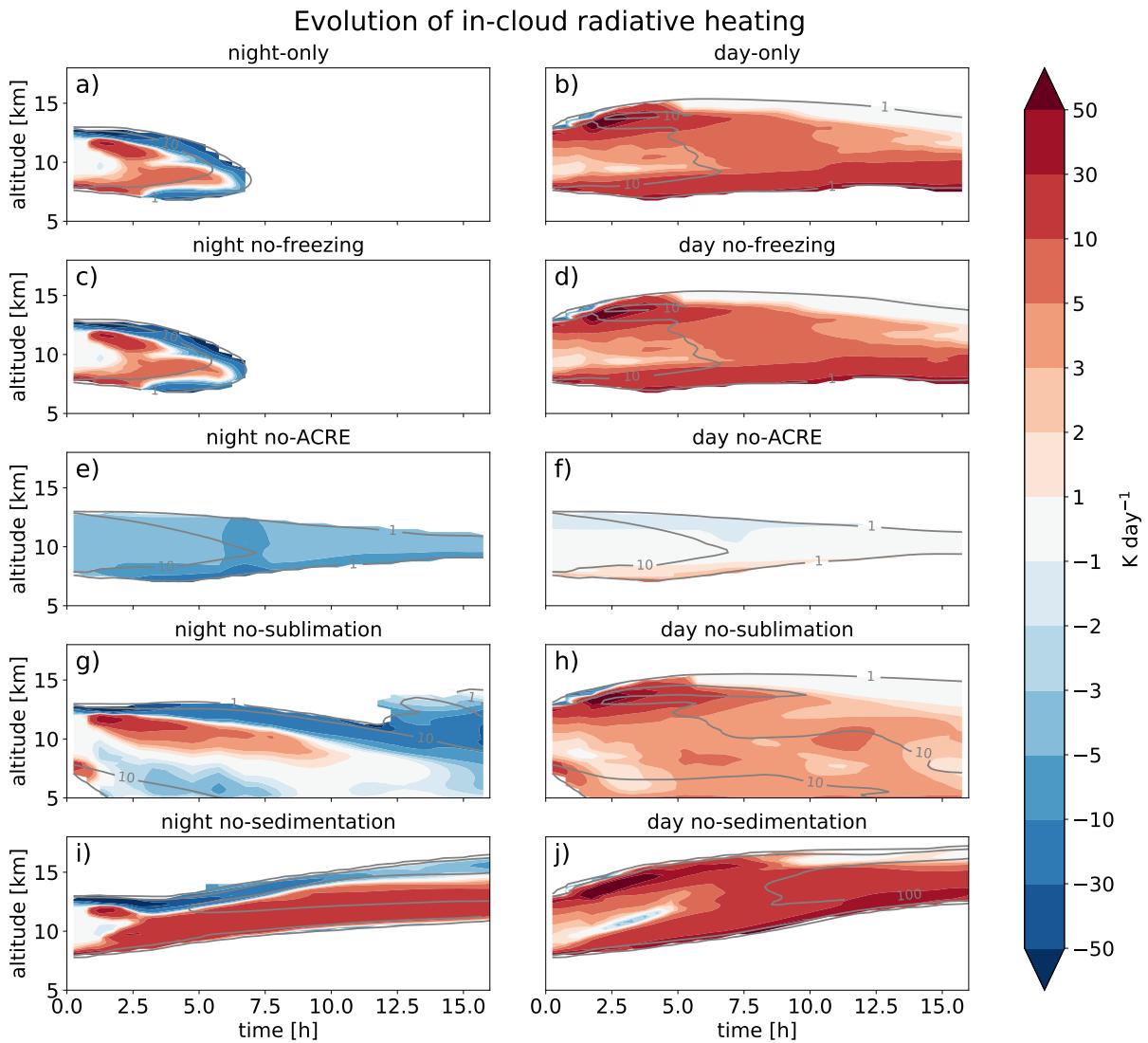
1008 FIG. 5. Time evolution of ice water path averaged over one of the two horizontal dimensions for the control
 1009 simulations (a,b) and 4 sensitivity experiments (c-j) in perpetual night (no insolation) and perpetual midday
 1010 conditions (insolation of 1300 W m^{-2}).



1011 FIG. 6. Time evolution of radiative heating (a,b) and vertical velocity (c,d) for clouds in perpetual night (a,c)
 1012 and perpetual midday conditions (insolation of 1300 W m^{-2}) averaged over the cloudy portion of the domain
 1013 (where condensed water $> 10 \text{ mg kg}^{-1}$). Gray contour lines represent ice mixing ratio isolines of 1 and 10 mg
 1014 kg^{-1} .

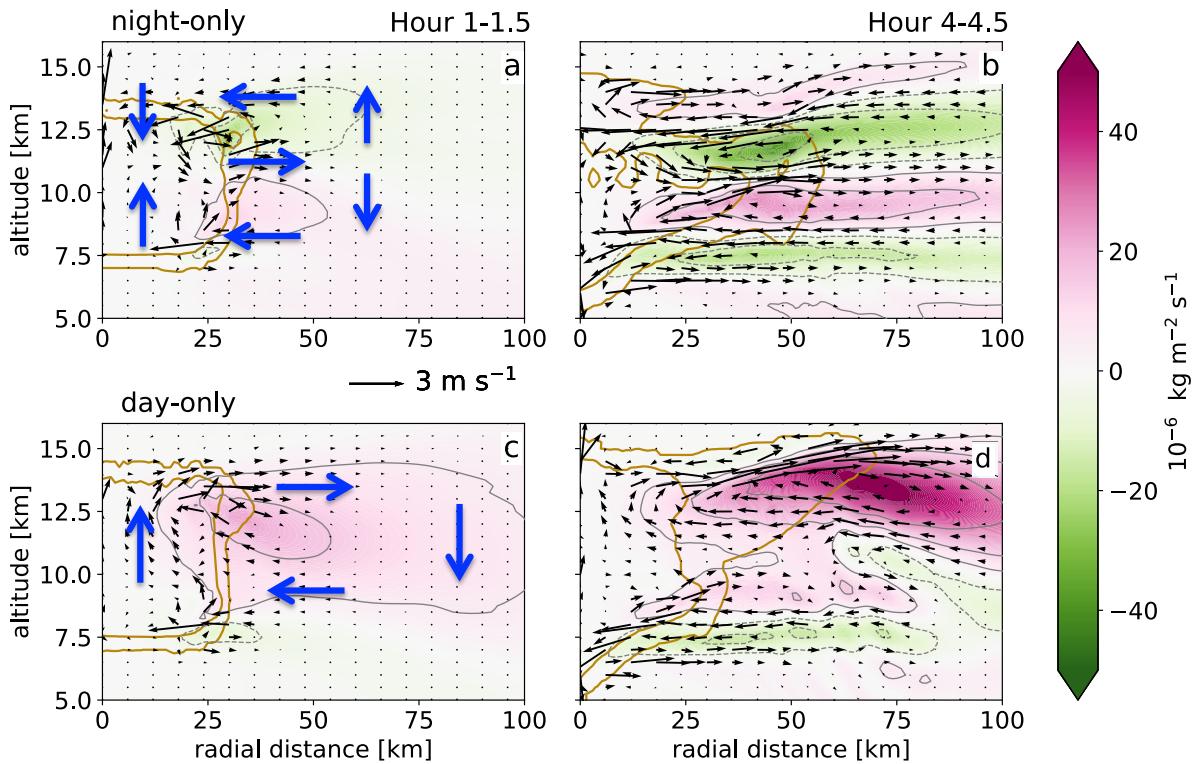


1015 FIG. 7. Selected column vertically integrated mass (a-c) and number (e-g) microphysical tendencies, including
 1016 the sedimentation flux (d) for perpetual day and night simulations.

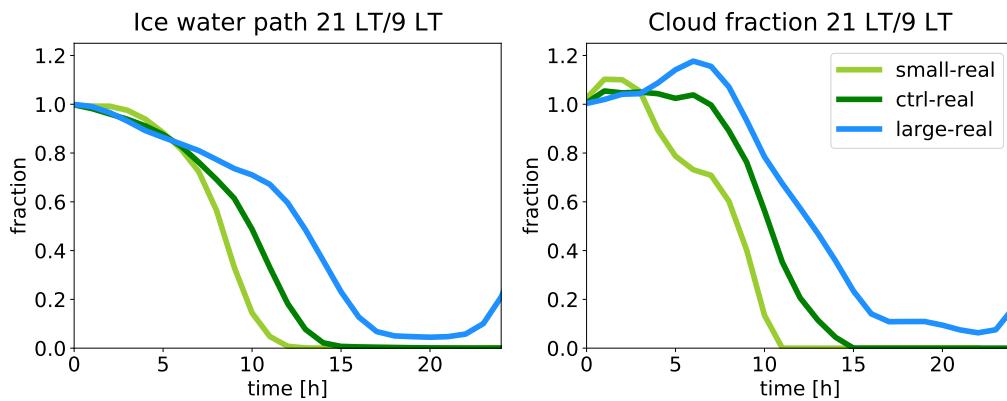


1017 FIG. 8. Time evolution of in-cloud radiative heating for perpetual day and night control (a-b) and 4 sensitivity
 1018 experiments (c-j). Gray contour lines represent ice mixing ratio contours of 1 and 10 mg kg^{-1} .

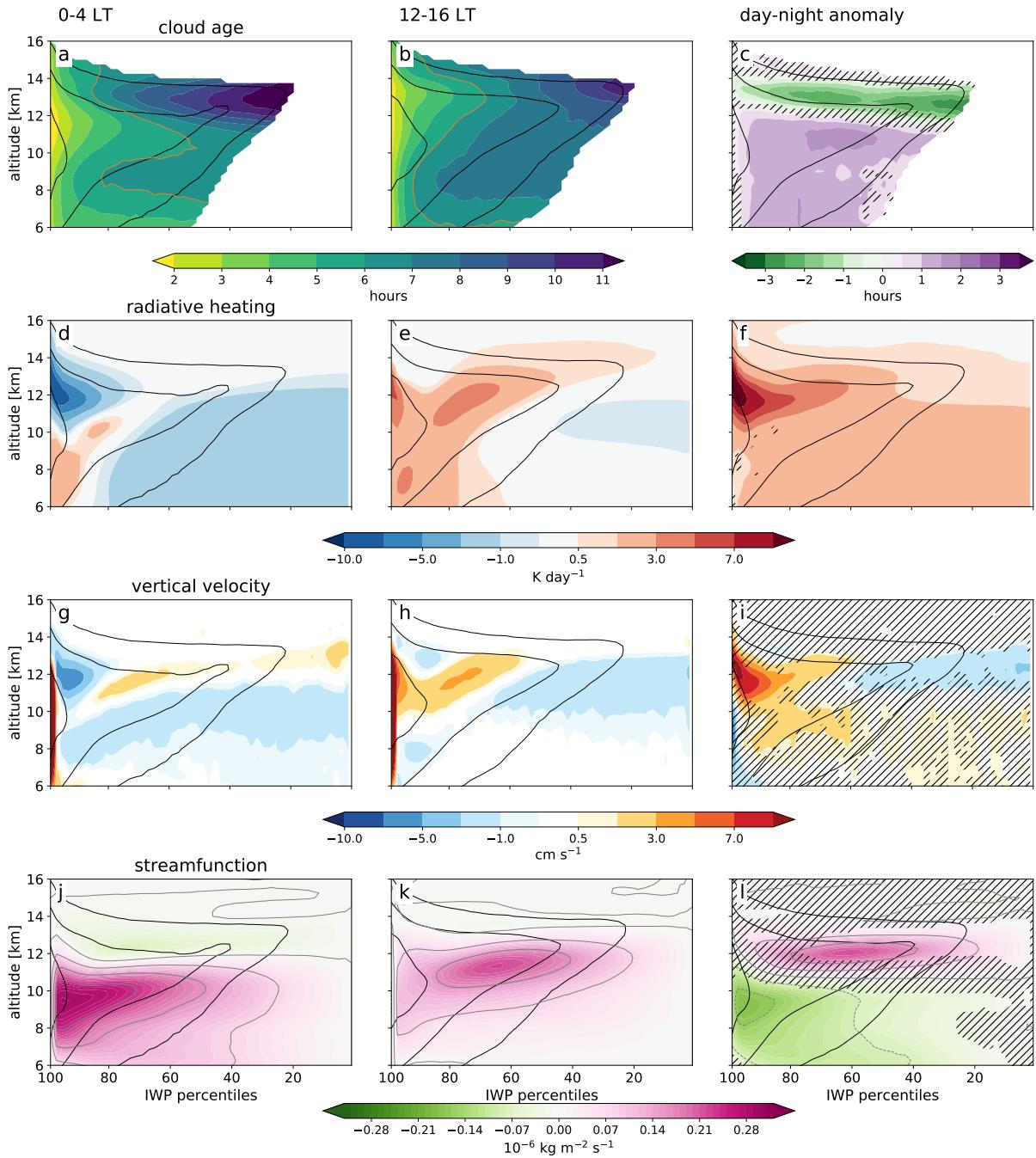
Streamfunction and winds



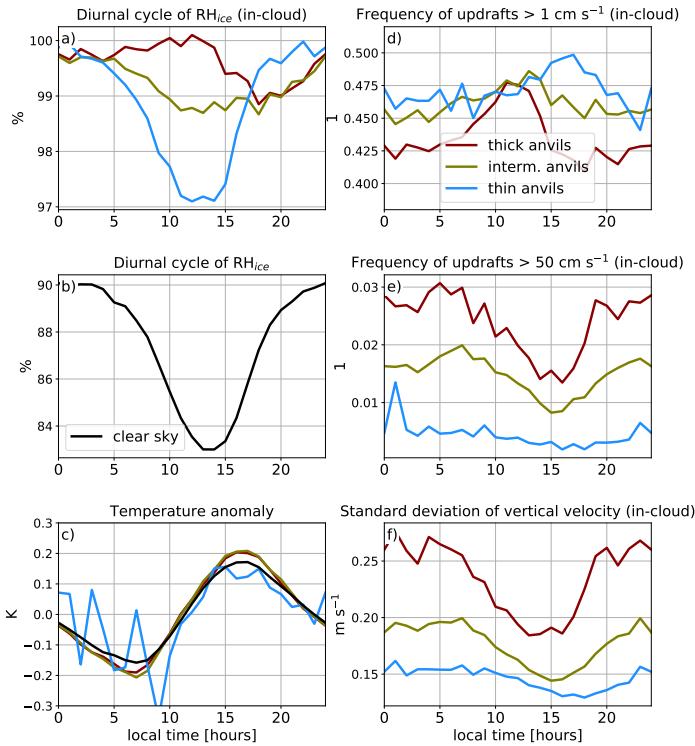
1019 FIG. 9. Wind vectors and streamfunction (in filled contours) for perpetual night (a,b) and day (c,d) simulations
 1020 at hour 1-1.5 and 4-4.5 of the evolution. The key circulations are on panels a) and c) highlighted by blue arrows.
 1021 Brown contour lines represent ice mixing ratio contours of 100 and 0.1 mg kg⁻¹.



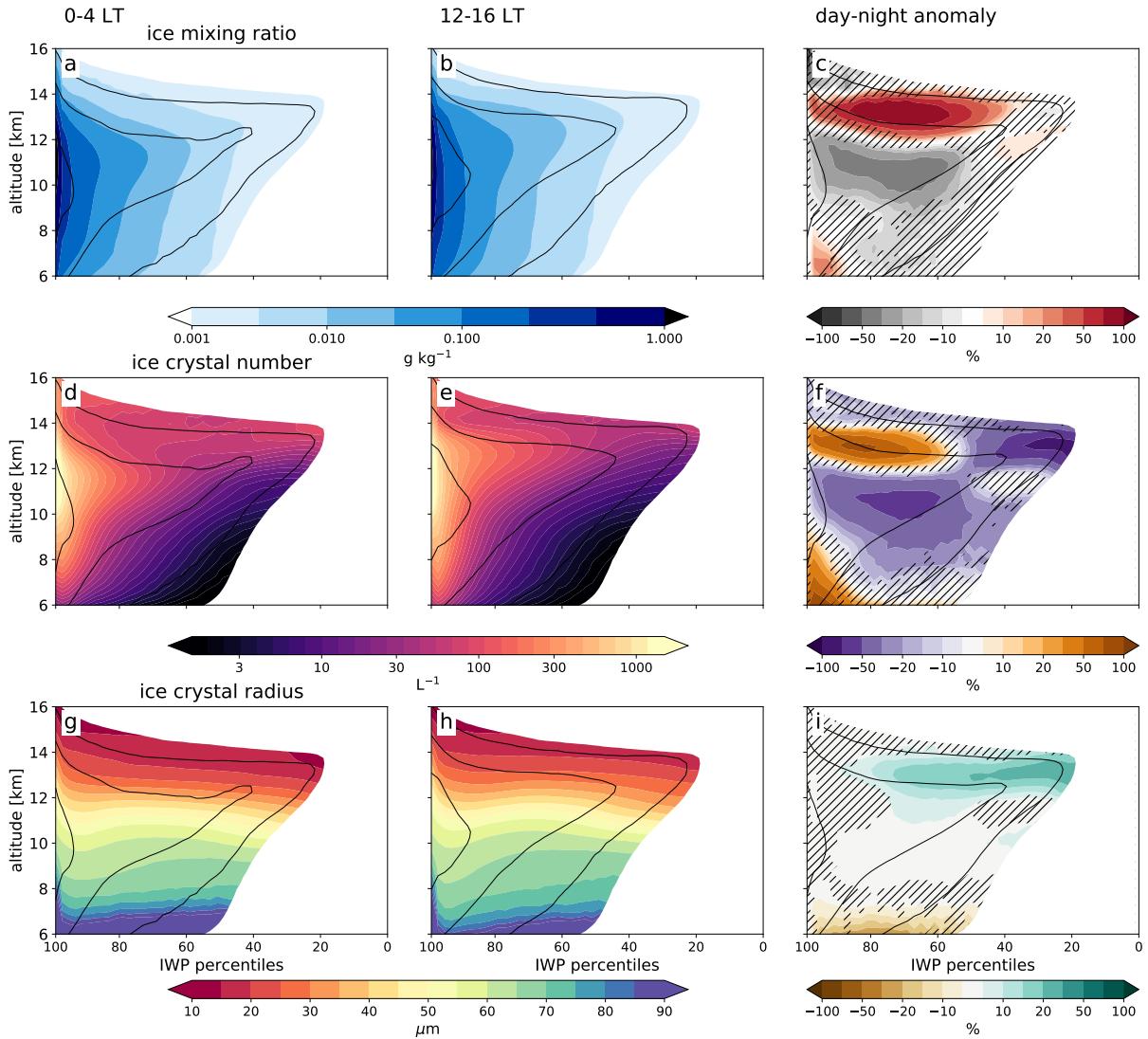
1022 FIG. 10. The ratio of IWP (a) and cloud fraction (b) between simulations started at 21 LT and 9 LT. A fraction
 1023 smaller than 1 means that the selected quantity is at the given time smaller in the simulation started at 21 LT
 1024 compared to the simulation started at 9 LT. A fraction larger than 1 means that the selected quantity is at the
 1025 given time larger in the simulation started at 21 LT compared to the simulation started at 9 LT. The small-real
 1026 initial cloud diameter is 30 km, ctrl-real is 60 km, and large-real is 120 km.



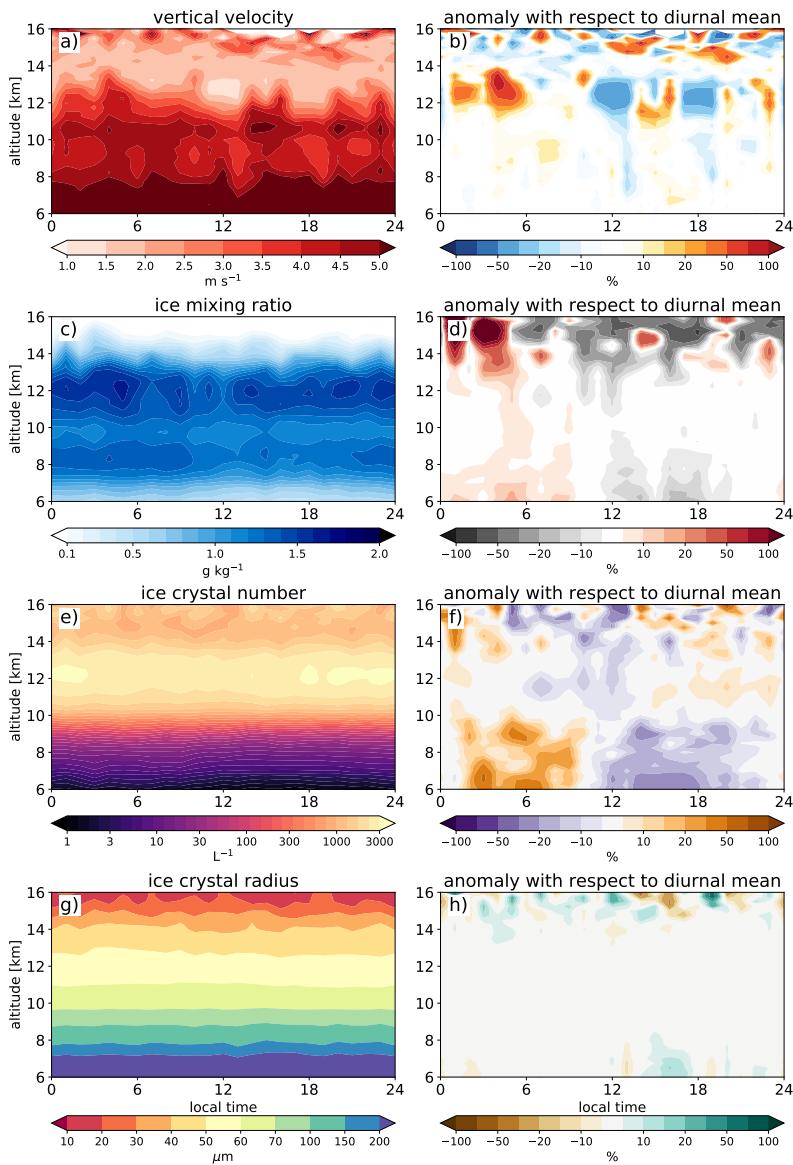
1027 FIG. 11. Cloud age (a-c), radiative heating (d-f), vertical velocity (h-i) and streamfunction (j-l) binned by ice
 1028 water path (IWP) for night (0-4 local time, left column) and day (12-16 local time, middle column). The right
 1029 column represents the absolute anomaly between day (left column) and night (middle column) quantities. The
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 1031 that not significant at 1 percent level.



1032 FIG. 12. Diurnal cycle of RH_{ice} for thick, intermediate and thin anvil clouds (a) and clear sky regions (b)
 1033 averaged for altitudes between 10 and 15 km. The deviation of the temperature from the mean over the diurnal
 1034 cycle between 10-15 km altitude is plotted in panel (c). Panels d-f show an in-cloud vertical velocity analysis for
 1035 the upper portions of the anvil clouds (12-15 km altitude), namely: the frequency of vertical velocity $> 1 \text{ cm s}^{-1}$
 1036 (d), frequency of vertical velocity $> 50 \text{ cm s}^{-1}$ (e), standard deviation of vertical velocity (f).



1037 FIG. 13. In-cloud ice mixing ratio (a-c), ice crystal number (d-f), and ice crystal radius (g-i) binned by ice
 1038 water path (IWP) for night (0-4 local time, left column) and day (12-16 local time, middle column). The values
 1039 are averaged over the cloudy portion of the domain (condensed water $>1 \text{ mg kg}^{-1}$). The right column represents
 1040 the absolute anomaly between day (left column) and night (middle column) quantities. The black contour lines
 1041 represent cloud fraction of 0.9, 0.5, and 0.1. Hatching is applied in the right column to areas that not significant
 1042 at 1 percent level.



1043 FIG. 14. Diurnal variations of the mean deep convective updraft velocity, diagnosed only for updrafts stronger
 1044 than 1 m s^{-1} and of the microphysical properties for clouds within the first hour after detrainment. The right
 1045 column represents the anomalies from the diurnal average values computed separately for each vertical layer.

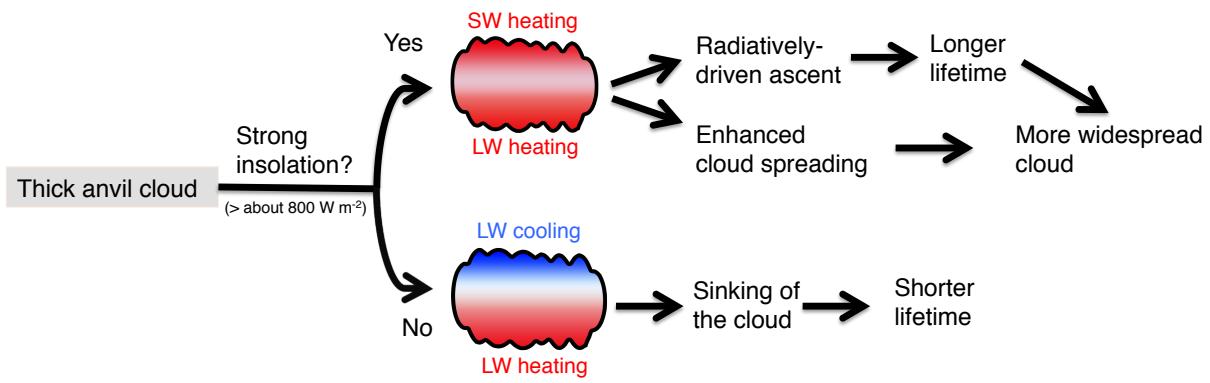
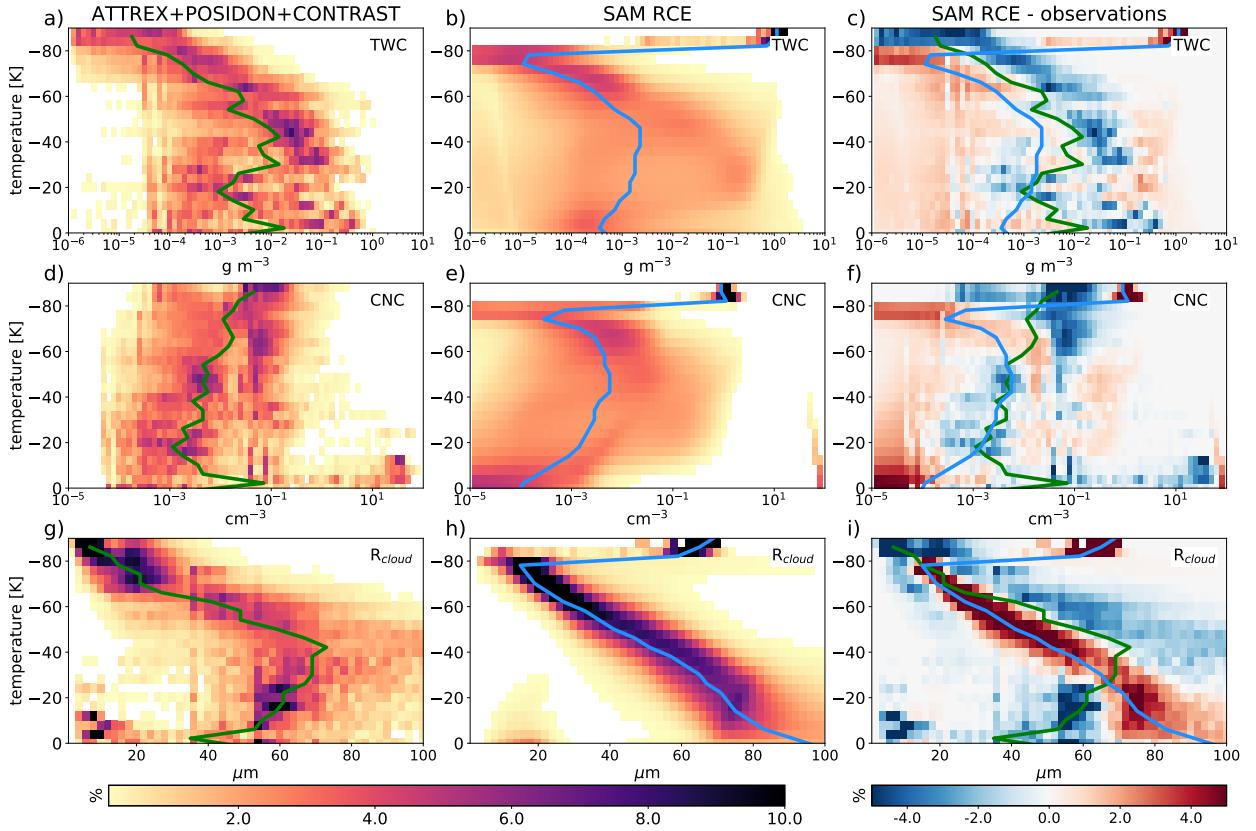
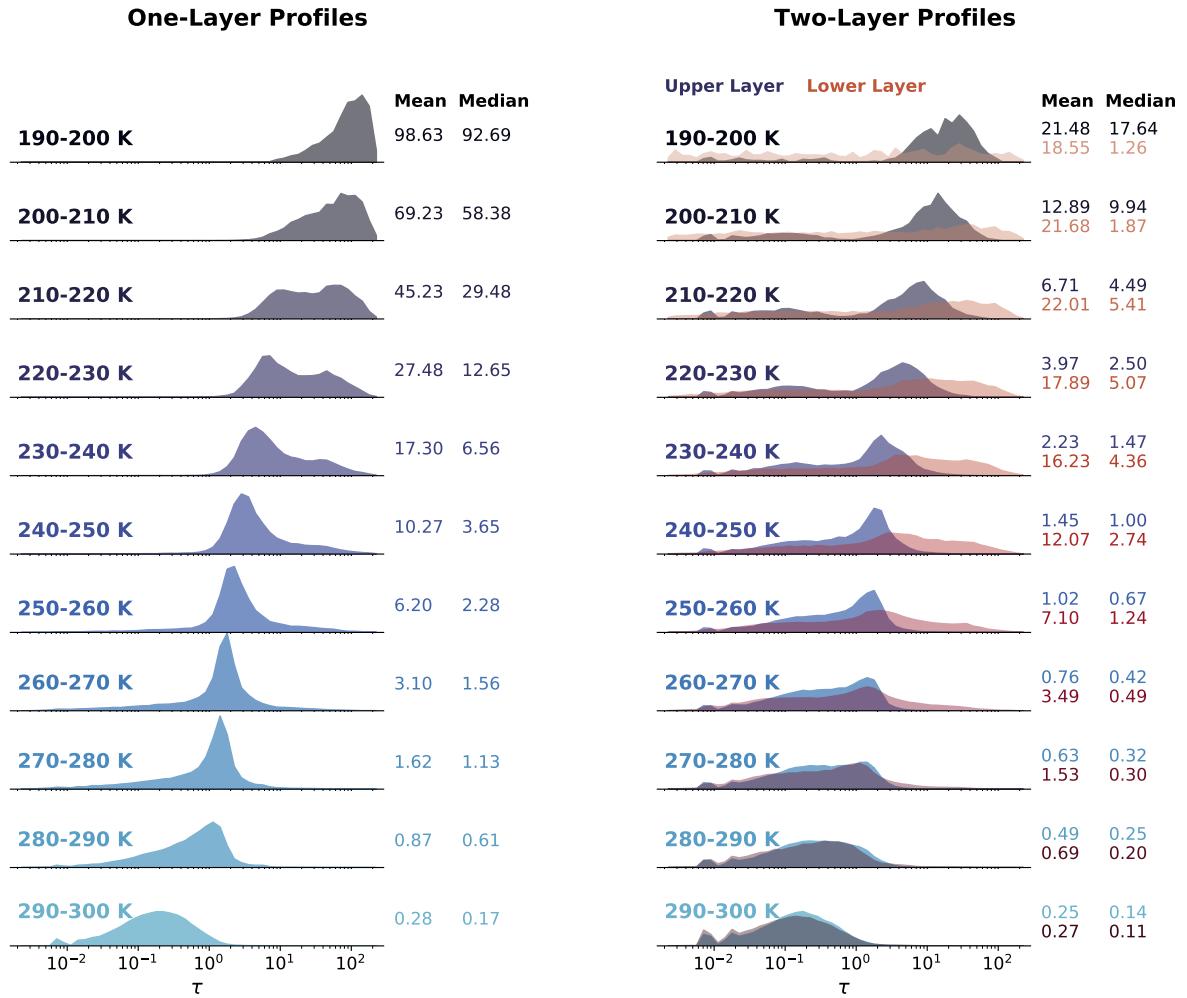


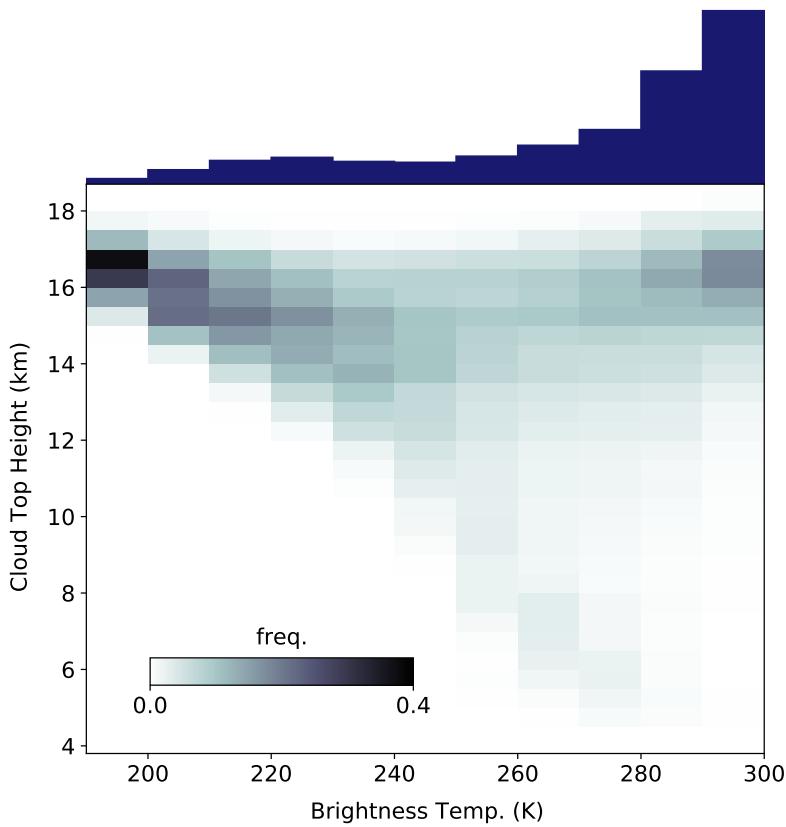
FIG. 15. Main mechanisms that lead to diurnal changes in anvil clouds.



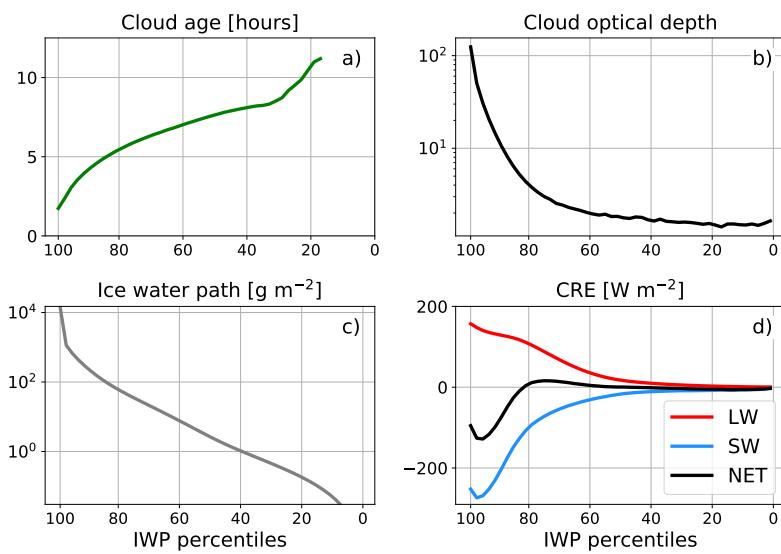
1046 Fig. A1. Total water content (TWC, a-c), cloud number concentration (CNC, d-f), and cloud mean mass radius
 1047 (R_{cloud} , g-i) from in-situ measurements sampled in 3 tropical Pacific field campaigns (left column) and from the
 1048 RCE model simulation (middle column). The mass mean radius is defined as $R_{cloud} = (3TWC/4\pi\rho N_{cloud})^{1/3}$.
 1049 The data are sorted in 4°C temperature bins. The colors represent the occurrence frequency of one of the 3 cloud
 1050 properties, normalized to reach 100% in each of the temperature bins. The green and blue lines represent the
 1051 median values of the in-situ and model data in all subplots, including the right column. The colors in the right
 1052 column represent the occurrence frequency anomaly between the first two columns.



1053 Fig. B1. Distributions of cloud optical depth for different brightness temperature classes. Left column:
 1054 retrieval profiles with one ice cloud layer. Right column: profiles with two ice cloud layers.



1055 Fig. B2. Joint histogram of brightness temperature and cloud top for profiles with a single ice cloud layer. The
 1056 histogram is normalized by brightness temperature bin such that the values in each column sum to unity. The
 1057 navy bar chart shows the relative frequency of each BT bin in the study region. Data are for both day and night.



1058 Fig. C1. Anvil cloud age (a), cloud optical depth (b), ice water path (IWP) (c) and top of the atmosphere cloud
 1059 radiative effects (CRE) (d) binned by ice water path percentiles.