

1                   **Characteristics of earthquake cycles: a**  
2                   **cross-dimensional comparison of 1D to 3D simulations**

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7                   **Key Points:**

- 8                   • Models with dimension reduction simulate qualitatively similar quasi-periodic earth-  
9                   quake sequences with quantitative differences.
- 10                  • Reduced influence of velocity-strengthening patches due to dimension reduction  
11                  increases recurrence interval, slip and rupture speed.
- 12                  • We provide guidelines on how to interpret lower-dimensional modeling results of  
13                  interseismic loading and earthquake ruptures.

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**Abstract**

High-resolution computer simulations of earthquake sequences in three or even two dimensions pose great demands on time and energy, making lower-cost simplifications a competitive alternative. We systematically study the advantages and limitations of simplifications that eliminate spatial dimensions, from 3D down to 0/1D in quasi-dynamic earthquake sequence models. We demonstrate that, when 2D or 3D models produce quasi-periodic characteristic earthquakes, their behavior is qualitatively similar to lower-dimension models. Certain coseismic characteristics like stress drop and fracture energy are largely controlled by frictional parameters and are thus largely comparable. However, other observations are quantitatively clearly affected by dimension reduction. We find corresponding increases in recurrence interval, coseismic slip, peak slip velocity, and rupture speed. These changes are to a large extent explained by the elimination of velocity-strengthening patches that transmit tectonic loading onto the velocity-weakening fault patch, thereby reducing the interseismic stress rate and enhancing the slip deficit. This explanation is supported by a concise theoretical framework, which explains some of these findings quantitatively and effectively estimates recurrence interval and slip. Through accounting for an equivalent stressing rate at the nucleation size  $h^*$  into 2/3D models, 0/1D models can also effectively estimate these earthquake cycle parameters. Given the computational efficiency of lower-dimensional models that run more than a million times faster, this paper aims to provide qualitative and quantitative guidance on economical model design and interpretation of modeling studies.

**Plain Language Summary**

Computer simulations are a powerful tool to understand earthquakes and they are often simplified to save time and energy. Dimension reduction - using 1D or 2D models instead of 3D models - is a commonly used simplification, but its consequences are not systematically studied. Here we find that both the overall earthquake recurrence pattern and the magnitude of stress changes on the fault caused by earthquakes remain relatively unchanged by model simplification by dimension reduction. However, some key observations such as the total slip and rupture speed achieved during an earthquake, as well as the precise recurrence interval are larger in lower-dimensional models. These changes are related to the elimination of lateral creeping regions that transmit stress onto the fault, which is an unavoidable consequence of the elimination of a physical dimension.

46 We use simple theoretical calculations to reproduce these observations and justify this  
47 causal relationship. As simplified models are still popular due to their computational ef-  
48 ficiency, this contribution helps their users and developers to understand and anticipate  
49 the potential discrepancies of their results with respect to the three-dimensional situa-  
50 tion that exists in nature. Therefore users can design their models and interpret their  
51 results with this work as a guideline.

## 52 **1 Introduction**

53 Destructive earthquakes every so often take us by surprise, because observations  
54 reveal a complex and opaque pattern of earthquake recurrence. Unraveling this pattern  
55 is challenging as the recurrence of large destructive earthquakes in nature is hardly ob-  
56 served. Even though small to intermediate-size events are observed to recur on the same  
57 fault in nature (e.g., Chlieh et al., 2004; Prawirodirdjo et al., 2010), these and all our  
58 natural observations are largely confined to the earth’s surface, such that they remain  
59 indirect and at a distance to the hypocenter and thus inhibit appropriate measurements  
60 and quantification. Earthquakes can also be generated quasi-periodically in large-scale  
61 laboratory experiments (e.g., Rosenau et al., 2009; McLaskey & Lockner, 2014) while these  
62 experiments are restricted to their millimeter to meter scale, such that they require a  
63 challenging upscaling step to interpret their findings. To complement our observations  
64 in nature and in laboratories, we need a quantitative description of the multi-physics,  
65 multi-scale processes governing fault slip. Numerical models are well-suited to overcome  
66 these spatial-temporal limitations and are thus important to improve our understand-  
67 ing of earthquake sequences and ultimately help to better estimate long-term seismic haz-  
68 ard assessment.

69 Numerical models featuring different degrees of complexity in different dimensions  
70 have been used to simulate earthquake cycles. They can be 0D (e.g., Madariaga, 1998;  
71 Erickson et al., 2008) or 1D models with a 0D fault point (e.g., Gu & Wong, 1991; Ohtani  
72 et al., 2020), 2D models with a 1D fault line (e.g., Lapusta et al., 2000; Van Dinther, Gerya,  
73 Dalguer, Mai, et al., 2013; Herrendörfer et al., 2018; Barbot, 2019; Cattania, 2019), 2.5D  
74 (e.g., Lapusta, 2001; Weng & Ampuero, 2019; Preuss et al., 2020) or 3D models with a  
75 2D fault plane (e.g., Okubo, 1989; Lapusta & Liu, 2009; Barbot et al., 2012; Erickson  
76 & Dunham, 2014; Chemenda et al., 2016; Jiang & Lapusta, 2016). To do better justice  
77 to the large amount of earthquake cycle papers, we refer the reader to a white paper on

78 future challenges for earthquake modeling (Lapusta et al., 2019) and an overview of bench-  
79 marked modeling codes provided in Erickson et al. (2020) and Jiang et al. (2021) for 2D  
80 anti-plane and 3D settings, respectively. Generally, 3D models will produce results most  
81 representative for nature. However, given that they are still very time and energy con-  
82 suming (Uphoff et al., 2017), simplified model setups are still largely adopted by many  
83 researchers and may be a very good choice to answer specific research questions (e.g.,  
84 Allison & Dunham, 2018; Cattania, 2019; van Dinther et al., 2019; Sathiakumar et al.,  
85 2020; Romanet et al., 2020). A key reason for the need of such simplifications is the ex-  
86 tremely high resolution required in both space and time, while at least exploring sen-  
87 sitivities in forward modeling studies (Lambert & Lapusta, 2021). On top of that, com-  
88 putational speed is particularly critical in situations where monotonous repetition of those  
89 forward models is required, for example, for inversion, data assimilation, physics-based  
90 deep learning, uncertainty quantification, and when dealing with probabilities, such as  
91 for probabilistic seismic hazard assessment (e.g., Weiss et al., 2019; Van Dinther et al.,  
92 2019). However, also when trying to understand coupled multi-physics or multi-scale feed-  
93 back these approximations can be really useful (e.g., Van Dinther, Gerya, Dalguer, Corbi,  
94 et al., 2013; Allison & Dunham, 2018; Lotto et al., 2019; Ohtani et al., 2019; Petrini et  
95 al., 2020). To optimize computing resources, researchers have to define suitable model  
96 complexities before and during their numerical simulations. Therefore it becomes a com-  
97 mon concern to what extent lower dimensional models can reproduce nature when com-  
98 pared to 3D models. How are the observed differences in results attributed to the cor-  
99 responding dimension reduction? And under what circumstances is this simplification  
100 justified?

101 These questions have not yet been systematically addressed. Nonetheless, several  
102 papers considered various aspects of this problem, especially via the comparison between  
103 2D and 3D models. Lapusta and Rice (2003); Kaneko et al. (2010); Chen and Lapusta  
104 (2019) suggested ways to interpret their 2D results in more realistic 3D situations, such  
105 that they could be directly compared to 3D results. By doing this, they could compare  
106 velocity-strengthening (VS) barrier efficiency in rupture propagation, seismic moment,  
107 and the scaling law for earthquake recurrence interval and seismic moment between 2D  
108 and 3D models in their studies. For the coseismic phase, simulations with dynamic rup-  
109 ture models of one single earthquake can more generally be conducted in 3D to obtain  
110 a full view of fault plane. This community thus recently did not give much attention to

111 2D models, except for the benchmark community. Harris et al. (2011) introduced two  
 112 benchmark problems for dynamic rupture modelers where 3D simulations produced smaller  
 113 ground motions (peak ground velocities) than in 2D simulations, in both elastic and elasto-  
 114 plastic scenarios. Similar 2D vs. 3D comparisons focusing on coseismic rupture behav-  
 115 ior as well as earthquake recurrence have also been made in the earthquake cycle com-  
 116 munity (e.g., Chen & Lapusta, 2009, 2019) where qualitative differences in earthquake  
 117 magnitude and recurrence interval are discussed. However, these findings are not sys-  
 118 tematic and occasionally lack of necessary theoretical support. Here we fill in this gap  
 119 by comparing earthquake cycle results across all dimensions from 0D to 3D, which in-  
 120 cludes all phases of the earthquake cycle, i.e., interseismic, nucleation, coseismic and post-  
 121 seismic.

122 We perform a systematic investigation of limitations and advantages of each dimen-  
 123 sion. By doing so, we compare physical characteristics and importance of different phys-  
 124 ical processes across dimensions both qualitatively and quantitatively. The aim of this  
 125 paper is to serve as guidelines for modelers designing models and for all researchers in-  
 126 terpreting results developed under necessary limitations. We first introduce the numer-  
 127 ical method and the model setup of a strike-slip fault under rate-and-state friction. The  
 128 code package is validated and benchmarked by Southern California Earthquake Center  
 129 (SCEC) Sequences of Earthquakes and aseismic slip (SEAS) benchmark problems BP1-  
 130 qd (Erickson et al., 2020) and BP4-qd (Jiang et al., 2021) (see Supporting Information  
 131 S1). Next, we systematically compare interseismic and coseismic characteristics of our  
 132 models from 1D to 3D, summarizing and quantifying their advantages and shortcomings.  
 133 The numerical results are explained and supported by a series of theoretical calculations.  
 134 Finally the computational cost is compared. In the discussions, we first discuss under  
 135 what conditions 2D models can substitute 3D models. Related issues on the model choices  
 136 of this research, limitations and future improvements as well as possible applications are  
 137 also discussed.

## 138 **2 Methods**

139 We exploit the flexibility of *Garnet*, a recently developed code library for the par-  
 140 allel solution of coupled non-linear multi-physics problems in earth sciences (Pranger,  
 141 2020). *Garnet* enables its users to formulate problems in a largely dimension-independent  
 142 way by defining a generic set of symbolic differential operators such as `div` and `grad`,

143 which are then realized at compile-time in the appropriate number of dimensions as con-  
 144 crete and performant compute kernels. Garnet implements the classical second-order ac-  
 145 curate staggered grid finite difference discretization of PDEs in space, and adaptive time  
 146 stepping schemes of various orders of accuracy and other characteristics, all based on the  
 147 linear multistep family of time discretizations. The library interfaces to PETSc (Balay  
 148 et al., 1997, 2019b, 2019a) for linear and nonlinear solvers and preconditioners, to MPI  
 149 (MPI Forum, 2015) for coarse scale distributed memory parallelism and intermediate scale  
 150 shared memory parallelism, and to Kokkos (Edwards et al., 2014) (and in turn OpenMP,  
 151 POSIX threads, or CUDA) for fine scale concurrency. In this section we further intro-  
 152 duce the equations and algorithms that define our study.

## 153 2.1 Physics

154 Under the assumption of static stress transfer, the momentum balance equation  
 155 reads

$$156 \quad \nabla \cdot \boldsymbol{\sigma} = 0, \quad (1)$$

157 where  $\boldsymbol{\sigma}$  is the Cauchy stress tensor whose component  $\sigma_{ij}$  denotes the stress acting along  
 158 the  $x_j$  axis on the plane that is normal to the  $x_i$  axis ( $i, j = 1, 2, 3$ ). Both gravity and  
 159 inertia are ignored in our models. Hooke’s law relates stress rate  $\dot{\boldsymbol{\sigma}}$  to strain rate  $\dot{\boldsymbol{\epsilon}}$  by

$$160 \quad \dot{\boldsymbol{\sigma}} = 2G\dot{\boldsymbol{\epsilon}} + \lambda Tr(\dot{\boldsymbol{\epsilon}})\mathbf{I} \quad (2)$$

161 with bulk modulus  $K$ , shear modulus  $G$ , Lamé’s constant  $\lambda := K - 2G/3$  and  $\mathbf{I}$  iden-  
 162 tity tensor.  $Tr(\dot{\boldsymbol{\epsilon}}) := \dot{\epsilon}_{kk}$  is the matrix trace. We assume infinitesimal strain rate  $\dot{\boldsymbol{\epsilon}}$  as  
 163 defined by

$$164 \quad \dot{\boldsymbol{\epsilon}} = \frac{1}{2} (\nabla \mathbf{v} + \mathbf{v} \nabla), \quad (3)$$

165 where  $\mathbf{v}$  is the material velocity whose component  $v_i$  denotes the velocity in the direc-  
 166 tion  $x_i$  ( $i = 1, 2, 3$ ). We use  $(x_1, x_2, x_3)$  and  $(x, y, z)$  to refer to the three axes interchange-  
 167 ably.

168 For a fault with unit normal vector  $\hat{\mathbf{n}}$ , the (scalar) normal stress  $\sigma_n$  (positive in com-  
 169 pression) is given by the projection  $\sigma_n = -\hat{\mathbf{n}} \cdot \boldsymbol{\sigma} \cdot \hat{\mathbf{n}}$ , the shear traction vector  $\boldsymbol{\tau}_s$  by  
 170 the projection  $\boldsymbol{\tau}_s = \boldsymbol{\sigma} \cdot \hat{\mathbf{n}} + \sigma_n \hat{\mathbf{n}}$ , the scalar shear traction  $\tau_s$  by the Euclidean norm  
 171  $\tau_s = \|\boldsymbol{\tau}_s\|$ , and finally the unit fault tangent  $\hat{\mathbf{t}}$  (which defines the orientation of the scalar  
 172 fault slip  $V$ ) by the normalization  $\hat{\mathbf{t}} = \boldsymbol{\tau}_s / \tau_s$ , such that  $\tau_s = \hat{\mathbf{t}} \cdot \boldsymbol{\sigma} \cdot \hat{\mathbf{n}}$ . Further following  
 173 Jiang et al. (2021), the fault is assumed to be governed by the rate-and-state friction law,

174 which was initially proposed based on laboratory friction experiments by Dieterich (1979);  
 175 Ruina (1983). We employ a regularization near zero slip velocity according to Rice and  
 176 Ben-Zion (1996) and Ben-Zion and Rice (1997), so that the friction law that defines the  
 177 relation between shear stress  $\tau_s$  and normal stress  $\sigma_n$  on the fault is given by

$$178 \quad \tau_s = a\sigma_n \operatorname{arcsinh} \left\{ \frac{V}{2V_0} \exp \left[ \frac{\mu_0}{a} + \frac{b}{a} \ln \left( \frac{\theta V_0}{L} \right) \right] \right\} + \eta V. \quad (4)$$

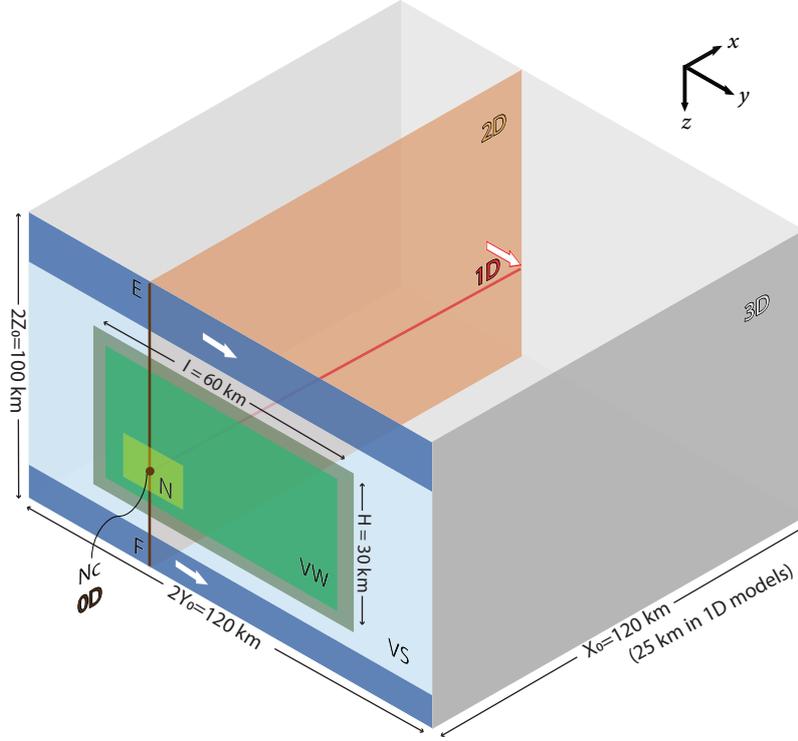
179 The “state”  $\theta$  in turn is governed by the evolution equation

$$180 \quad \dot{\theta} = 1 - \frac{V\theta}{L}, \quad (5)$$

181 corresponding to the so-called “aging law” (Ruina, 1983). Symbols used in (4) and (5)  
 182 include the reference friction coefficient  $\mu_0$ , the reference slip rate  $V_0$ , the characteris-  
 183 tic slip distance  $L$ , and the parameters  $a$  and  $b$  that control the relative influence of di-  
 184 rect and evolutionary effects, respectively. The fault is velocity-weakening (VW) and po-  
 185 tentially frictionally unstable when  $a-b < 0$ , and velocity-strengthening (VS) and gen-  
 186 erally frictionally stable when  $a-b > 0$ . Finally, the parameter  $\eta$  used in (4) refers to  
 187 the “radiation damping term” used in the quasi-dynamic (QD) approximation of iner-  
 188 tia (e.g., Rice, 1993; Cochard & Madariaga, 1994; Ben-Zion & Rice, 1995; Liu & Rice,  
 189 2007; Crupi & Bizzarri, 2013), which is employed in earthquake cycle simulations to re-  
 190 duce the computational costs. However, this is known to introduce qualitative and quan-  
 191 titative differences compared to fully dynamic (FD) modeling results (Thomas et al., 2014).  
 192 The damping viscosity  $\eta = G/(2c_s)$  is equal to half the shear impedance of the elas-  
 193 tic material surrounding the fault.

## 194 **2.2 Model setup**

195 Over the last decade, the SCEC has supported various code comparison projects  
 196 to verify numerical simulations on dynamic earthquake ruptures (e.g. Harris et al., 2009,  
 197 2018). The SEAS benchmark project (Erickson et al., 2020; Jiang et al., 2021), launched  
 198 in 2018, is an extension to evaluate the accuracy of numerical models simulating earth-  
 199 quake cycles. This benchmark initiative provides us with a platform to verify the earth-  
 200 quake cycle implementation in *Garnet* and facilitates the general comparison with other  
 201 established implementations from the community (see Supporting Information S1 where  
 202 GARNET is successfully benchmarked and Jiang et al., 2021). Therefore, we build our  
 203 models based on the setup of SEAS benchmark problem BP4-qd.



**Figure 1.** Numerical model setup of a vertical strike-slip fault embedded in an elastic medium: 3D setup of SEAS benchmark BP4-qd and its simplification to 2D, 1D and 0D. Only one side of the fault (half space  $x \geq 0$ ) is shown and modeled due to symmetry. “VW” and “VS” denotes the VW (light green) and VS (light blue) patches, respectively. The transition between VW and VS patches is shown in dark green. Tectonic loading regions at the top and bottom of the fault (dark blue) are subjected to constant velocities (white arrows). “N” denotes the predefined nucleation zone (yellow) with higher initial slip rate and shear stress, whose center is denoted as “Nc”. “EF” denotes a vertical line through “Nc”. Computational domain in 2D is reduced to  $xz$ -plane (orange) with 1D fault line “EF” (brown). Computational domain in 1D is reduced to the  $x$ -axis (red) with a 0D fault point “Nc” (brown). In this case tectonic loading is applied at the far-away end with constant velocity (white arrow with red frame). Computational domain in 0D is fault point “Nc” without medium extent.

204 The BP4-qd describes a planar vertical fault embedded in a homogeneous, isotropic  
 205 linear elastic medium, observing the physics described in section 2.1 (Fig. 1). The  $x, y, z$   
 206 axes are directions perpendicular to the fault plane, along the strike and along the dip,  
 207 respectively. Following Jiang et al. (2021), the fault condition is prescribed at  $x = 0$ .  
 208 The central part of the fault is assumed to follow the rate-and-state friction formulation  
 209 where a VW region is surrounded by a VS region. The top and bottom parts of the fault  
 210 are not governed by rate-and-state friction and are instead subjected to a constant fault-  
 211 parallel loading velocity  $V_p/2$ . The inherited frictional parameters  $a, b, L$  lead to a large  
 212 nucleation size ( $\sim 12$  km), such that it facilitated benchmarking under low resolution (500  
 213 - 1000 m, Fig. S3) with a reasonable computational load. We are aware that this setup  
 214 allows for simple periodic earthquakes instead of smaller irregular ones but this simple  
 215 earthquake sequence also facilitates the comparison over dimensions and make quanti-  
 216 tative comparisons of some characteristic observations possible. Several simulations at  
 217 resolutions of 25 - 50 m following the SEAS benchmark BP1 (Erickson et al., 2020) con-  
 218 firm the main results presented in this paper (Fig. S4), indicating our final conclusions  
 219 can be generalized to a broader frictional parameter range.

220 Due to the symmetry respective to the fault plane and the resulting anti-symmetry  
 221 of fault-parallel motion, the motion at the fault is taken to be relative to a fictitious op-  
 222 positely moving domain that is not modeled. The computational domain is thus limited  
 223 to the half space  $x \geq 0$ . Since this still proposes an infinitely large half space, the com-  
 224 putational domain needs to be truncated to a finite domain when using a volumetric dis-  
 225 cretization. We use the computational domain  $\Omega(x, y, z) = [0, X_0] \times [-Y_0, Y_0] \times [-Z_0, Z_0]$   
 226 (Fig. 1), where  $X_0, Y_0, Z_0$  are chosen sufficiently large to have negligible impact on the  
 227 fault behavior (Jiang et al., 2021). The top and bottom boundaries  $z = \pm Z_0$  are pre-  
 228 scribed to move at the same constant loading velocity  $V_p/2$ . The remaining three bound-  
 229 aries  $x = X_0, y = -Y_0, y = Y_0$  mimic the conditions at infinity and are set to be traction-  
 230 free. We show that the simulated earthquake sequences are converging in both interseis-  
 231 mic and coseismic phases upon enlarging the medium thickness  $X_0$  and the difference  
 232 is negligible when  $X_0 > 40$  km (Fig. S2). The same parameter study is also implemented  
 233 for  $Y_0$  and  $Z_0$  to achieve convergence (Table 1).

234 The initial conditions are chosen to allow the fault to creep at the imposed slip ve-  
 235 locity  $V_p$  in a steady state at  $t = 0$  (Jiang et al., 2021), namely

$$236 \quad \theta(t = 0) = \frac{L}{V_p} , \quad (6)$$

237 and

$$238 \quad \tau_s(t = 0) = a\sigma_n \operatorname{arcsinh} \left\{ \frac{V_p}{2V_0} \exp \left[ \frac{\mu_0}{a} + \frac{b}{a} \ln \left( \frac{V_0}{V_p} \right) \right] \right\} + \eta V_p . \quad (7)$$

239 We additionally define a highly stressed zone “N” in the VW patch with higher initial  
 240 slip velocity  $V_i$  (Fig. 1) to ensure the first earthquake nucleates at that location when  
 241 the computation starts. In this zone, the state variable  $\theta$  keeps unchanged to achieve the  
 242 high pre-stress, namely

$$243 \quad \tau_s((y, z) \in N, t = 0) = a\sigma_n \operatorname{arcsinh} \left\{ \frac{V_i}{2V_0} \exp \left[ \frac{\mu_0}{a} + \frac{b}{a} \ln \left( \frac{V_0}{V_p} \right) \right] \right\} + \eta V_i . \quad (8)$$

244 This helps us to better compare the coseismic behavior across dimensions. All physical  
 245 and numerical parameters are summarized in Table 1.

### 246 **2.3 Model simplification by progressive elimination of dimensions**

247 In this work we take a structured approach to dimension reduction, eliminating first  
 248 the lateral along-strike dimension, then the vertical dimension, and finally the fault-perpendicular  
 249 dimension. Each of these steps are illustrated in Fig. 1. For clarity, the assumptions and  
 250 variables concerned in each dimension are summarized in Table 2.

251 In 2D, the model is simplified by excluding the along-strike fault direction (denoted  
 252 in orange in Fig. 1). This means that the material and frictional properties, boundary  
 253 and initial conditions are assumed to be homogeneous in this direction. That assump-  
 254 tion thus omits the along-strike heterogeneity introduced by the bounding VS patches  
 255 as well. In this way, any half plane cutting the fault vertically may be taken as repre-  
 256 sentative of the the entire model. The computational domain can thus be reduced to  $\Omega(x, z) =$   
 257  $[0, X_0] \times [-Z_0, Z_0]$ . Furthermore, we omit the along-dip motion  $v_z$  and only model the  
 258 anti-plane motion. As a consequence, only the  $\sigma_{xy}$  and  $\sigma_{yz}$  components of the stress ten-  
 259 sor are required to be evaluated in this anti-plane strain model. To allow a coseismic com-  
 260 parison we keep there the highly stressed nucleation zone defined in 3D and choose to  
 261 model the plane cutting across this zone. The fault is collapsed to the line “EF” (denoted  
 262 in red in Fig. 1). Another common 2D perspective that models a horizontal plane cut-  
 263 ting the fault includes the in-plane strain assumption. While this configuration models

**Table 1.** Physical and numerical parameters

Parameter	Symbol	Value
Density	$\rho$	2.670 g/cm <sup>3</sup>
Shear wave speed	$c_s$	3.464 km/s
Poisson ratio	$\nu$	0.25
Shear modulus	$G$	32.0 GPa
Bulk modulus	$K$	53.4 GPa
Normal stress	$\sigma_n$	50 MPa
Plate rate	$V_p$	10 <sup>-9</sup> m/s
Width of rate-and-state fault	$W_f$	80 km
Length of uniform VW region	$l$	60 km
Width of uniform VW region	$H$	30 km
Width of VW-VS transition zone	$h$	3 km
Reference friction coefficient	$\mu_0$	0.6
Reference slip rate	$V_0$	10 <sup>-6</sup> m/s
Characteristic slip distance	$L$	0.04 m
Rate-and-state direct effect	$a$	
- VW		0.0065
- VS		0.025
Rate-and-state evolution effect	$b$	0.013
Width of predefined nucleation zone “N”	$w_i$	12 km
Distance of nucleation zone to boundary	$h_i$	1.5 km
Initial slip rate		
- inside nucleation zone	$V_i$	10 <sup>-3</sup> m/s
- outside nucleation zone	$V_p$	10 <sup>-9</sup> m/s
Medium extent perpendicular to fault	$X_0$	<i>40/80/120</i> <sup>a</sup> km
Half fault extent along strike	$Y_0$	<i>60/90</i> <sup>a</sup> km
Half fault extent along dip	$Z_0$	<i>50/60</i> <sup>a</sup> km
Grid size	$\Delta x$	<i>500/1000</i> <sup>a</sup> m

<sup>a</sup> Numbers in italic are used in parameter studies.

264 a more complete set of momentum balance and elastic constitutive equations than the  
 265 anti-plane configuration we have chosen, the differences are only expected to manifest  
 266 as a slightly modified elastic loading and corresponding changes in friction and nucle-  
 267 ation size. We therefore choose to use the vertical 2D configuration that keeps the top/bottom  
 268 loading regions for better comparison.

269 The simplified physical equations (1)-(3) in 2D read:

$$\begin{aligned}
 \dot{\sigma}_{xy} &= G \frac{\partial v_y}{\partial x} , \\
 \dot{\sigma}_{yz} &= G \frac{\partial v_y}{\partial z} , \\
 \frac{\partial \sigma_{xy}}{\partial x} + \frac{\partial \sigma_{yz}}{\partial z} &= 0 .
 \end{aligned}
 \tag{9}$$

271 In 1D, we further simplify the model by setting all variables invariant along dip in  
 272 which case only the shear stress component  $\sigma_{xy}$  and the velocity component  $v_y$  remain.  
 273 We thus lose the possibility to model spatial variations of frictional properties as the fault  
 274 reduces to a 0D point at  $x = 0$  in the computational domain  $\Omega(x) = [0, X_0]$ . We choose  
 275 the fault “point” to be velocity-weakening, corresponding to a location inside the pre-  
 276 defined nucleation zone at “Nc” (denoted in red in Fig. 1) to facilitate coseismic com-  
 277 parison . Furthermore, without an along-dip fault extent, the original on-fault tectonic  
 278 loading from the top and bottom is no longer possible. Instead it is added at the far-away  
 279 boundary through a constant creeping rate there. To achieve a comparable interseismic  
 280 stress rate inside the VW patch across dimensions, we adjust the domain size  $X_0$  so that  
 281 the shortest distance between the VW patch and the creeping boundary is the same as  
 282 in higher dimensional models. Namely, we set  $X_0$  equal to  $(W_f - H)/2$ .

283 The simplified physical equations in 1D read:

$$\begin{aligned}
 \dot{\sigma}_{xy} &= G \frac{\partial v_y}{\partial x} , \\
 \frac{\partial \sigma_{xy}}{\partial x} &= 0 .
 \end{aligned}
 \tag{10}$$

285 In 0D, both the medium and the fault become the same point by eliminating the  
 286 fault-perpendicular dimension. In this model without medium extent, physical loading  
 287 is impossible at any medium boundaries. Therefore a “driving force” that can be cho-  
 288 sen arbitrarily (equivalent to loading at the fault point) has to be added to the system  
 289 instead.

290 The simplified physical equation in 0D reads:

$$\dot{\sigma}_{xy} = -kV + \dot{f}_d
 \tag{11}$$

**Table 2.** Simplifications in different dimensional models

Model	Fault	Unknowns	Simplifications
3D	2D	$V, \theta; v_x, v_y, v_z, \sigma_{xx}, \sigma_{xy}, \sigma_{xz}, \sigma_{yy}, \sigma_{yz}, \sigma_{zz}$	No fault opening
2D	1D	$V, \theta; v_y, \sigma_{xy}, \sigma_{yz}$	+ strike-slip only, along-strike invariant
1D	0D	$V, \theta; v_y, \sigma_{xy}$	+ along-dip invariant
0D	0D	$V, \theta$	+ integral perpendicular to fault

where  $k$  is the stiffness of the system and  $\dot{f}_d$  is the applied driving force. This model will be further discussed in section 4.3 where the equivalence of 1D and 0D models will be illustrated.

## 2.4 Numerical algorithm

The nonlinear friction law (4) and evolution law (5) are solved in a point-wise fashion using a Newton-Raphson iteration for the slip rate  $V$  at a given stress  $\boldsymbol{\sigma}$ , given initial conditions (6)-(8) (algorithm flowchart in Fig. S1). The medium is closed with an essential velocity boundary condition  $\mathbf{v} = V\hat{\mathbf{t}}/2$  on the fault ( $x = 0$ ) and the remaining boundary conditions given in the two sections above.

We choose a spatial discretization that ensures that the smallest physical length scale in the rate-and-state friction model – the cohesive zone size  $\Lambda$  – is always well resolved. This cohesive zone size  $\Lambda$  (Rubin & Ampuero, 2005; Day et al., 2005) is given by

$$\Lambda = \Lambda_0 \sqrt{1 - \frac{V_r^2}{c_s^2}} \quad (12)$$

$$\Lambda_0 = \frac{9\pi}{32} \frac{GL}{b(1-\nu)\sigma_n},$$

where  $V_r$  is the rupture speed and  $c_s$  is the shear wave speed.  $\Lambda_0$  is the upper limit of the cohesive zone size when  $V_r \rightarrow 0$ . The dynamic cohesive zone size  $\Lambda$  shrinks with increasing rupture speed  $V_r$ . We find that a high resolution is required for the seismogenic domain and its neighboring off-fault area, while it is not required at medium to large distances to the fault. We improve computational efficiency by considering a grid that is statically refined (ie. remaining fixed over time) near the VW zone. Refinement is realized by designing an orthonormal rectilinear (but not Cartesian) coordinate sys-

313 tem that measures Euclidean space, and sampling this deformed coordinate system, rather  
 314 than the Cartesian reference frame itself, at regular intervals. Differential operators are  
 315 expressed in a general curvilinear coordinate system (see e.g. Simmonds, 1994) before  
 316 discretization, a procedure that preserves the 2<sup>nd</sup>-order accuracy of the numerical method  
 317 (Pranger, 2020).

318 We use adaptive time stepping to deal with the strong variation of the slip veloc-  
 319 ity and state variables in between interseismic and coseismic phases. The critically re-  
 320 solvable time scale is according to the evolution of the friction law (Eq. 5). Following Lapusta  
 321 et al. (2000), we let the time step  $\Delta t$  be given by

$$322 \quad \Delta t = \min \left\{ \zeta \frac{L}{V_{\max}}, (1 + \alpha)\Delta t_{\text{old}}, \Delta t_{\max} \right\}. \quad (13)$$

323 where  $\zeta$  is a factor controlled by the material and frictional parameters (see calculation  
 324 method in Lapusta et al., 2000). We also require the next time step not to be larger than  
 325  $(1+\alpha)$  times the former time step  $\Delta t_{\text{old}}$  to avoid instability in the postseismic phase. A  
 326 maximum time step size  $\Delta t_{\max}$  is further added to keep resolving the interseismic pe-  
 327 riod in sufficient detail. We have used  $\alpha = 0.2$  and  $\Delta t_{\max} = 10^8$  s.

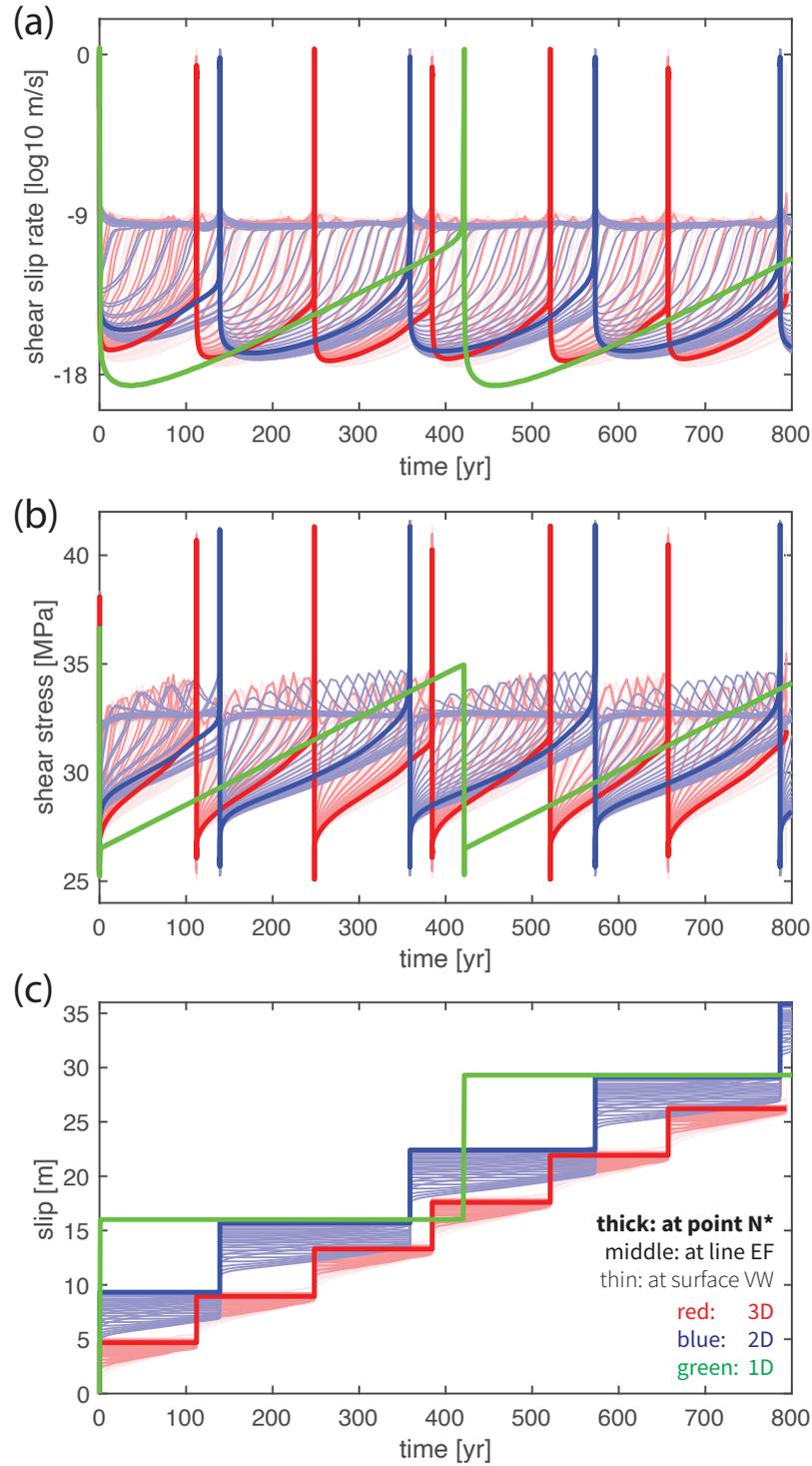
### 328 **3 Results and Analysis**

329 Following the simplifications summarized in Table 2 and Fig. 1, this section com-  
 330 pares and analyzes the 3D to 2D and 1D results, where the fault is modeled in 2D, 1D  
 331 and 0D, respectively.

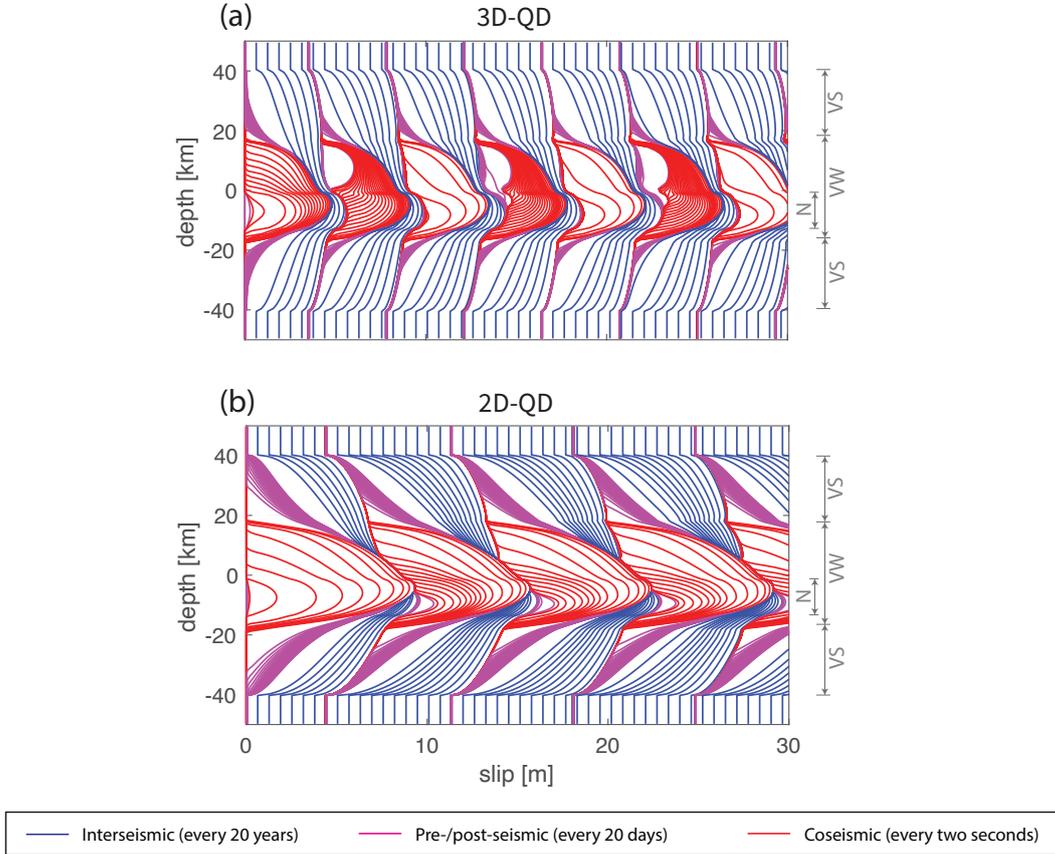
#### 332 **3.1 Interseismic phase**

333 Regardless of dimension, we observe quasi-periodic earthquake sequences (Fig. 2).  
 334 In one earthquake cycle, shear stress is first accumulated from minimum 25 MPa to max-  
 335 imum 35-42 MPa during the interseismic phase and then released in an earthquake (Fig. 2b).  
 336 Accordingly, slip velocity also increases from locked rates of  $10^{-17}$  m/s in 2/3D and  $10^{-20}$   
 337 m/s in 1D to seismic rate  $10^0$  m/s at the same time (Fig. 2a). This similarity indicates  
 338 the possibility of using lower dimensional models to substitute higher dimensional ones  
 339 in earthquake cycle modeling.

340 By dimension reduction, simulated earthquakes become more characteristic (Fig. 2, 3).  
 341 In 3D, all simulated earthquakes nucleate from one corner of the rectangular VW zone



**Figure 2.** Comparison of the long-term time series of (a) slip rate, (b) stress and (c) accumulated slip in 1-3D models. The lines with different thicknesses and degrees of transparency are recorded at different locations on the fault, where the thick lines are recorded at the rim of the nucleation zone “N\*” of the sixth earthquake, the semi-thick lines along the line “EF” cutting across “N\*” vertically and the thin lines elsewhere in the VW patch (see Fig. 6).



**Figure 3.** Cross-dimensional comparison of cumulative seismic and aseismic slip. The cumulative slip profile of (a) the 3D model and (b) the 2D model, along the dip direction “EF” cutting across the predefined nucleation zone “N” (see Fig. 1). “VW”, “VS”, “N” label the range of VW, VS and predefined nucleation zone. The interseismic phase is plotted every 20 years (blue), the pre- and post-seismic phase every 20 days (magenta) and the coseismic rupture every two seconds (red). Note that the slip contour distortions around a depth of -1.5 km and -13.5 km are introduced into these cumulative patterns by the predefined nucleation zone, whose properties increased the amount of slip in that zone for the first earthquake only.

342 and rupture throughout it until the rupture front reaches the transition to the VS zone.  
 343 However, not all earthquakes initiate from the same nucleation zone, as is suggested by  
 344 the slip profile (Fig. 3a). Rather, the nucleation location alternates between the top-left  
 345 and bottom-right corners, resulting in a periodic cycle of two earthquakes with slightly  
 346 different slip and recurrence interval. Similar results in 3D of two or more characteris-  
 347 tic earthquakes repeating as a group have also been reported by Barbot (2019), where  
 348 several possible mechanisms are suggested for this poorly understood phenomenon, in-  
 349 cluding near-stable condition, large geometrical aspect ratio and velocity-strengthening/-  
 350 weakening region interaction (see also Chen & Lapusta, 2019; Cattania, 2019). In 2D,  
 351 earthquakes are more periodic because they all nucleate from the same down-dip limit  
 352 of the VW patch and rupture towards the up-dip limit, instead of alternately nucleat-  
 353 ing from the top and bottom sides (Fig. 3b). The earthquake size is also more identi-  
 354 cal with same recurrence interval. In 1D, we observe purely periodic, characteristic earth-  
 355 quakes of the same size (Fig. 2). This trend is because with fewer dimensions, the in-  
 356 terseismic loading pattern to the VW patch becomes simpler, so that the potential nu-  
 357 cleation locations are also reduced. Earthquakes can potentially nucleate from four cor-  
 358 ners of the VW patch in 3D, but it reduces to two (top and bottom) in 2D and one in  
 359 1D. This demonstrate that as spatial dimensions are eliminated, the simulated results  
 360 typically exhibit a simpler spatio-temporal behavior.

361 From a quantitative point of view, simulated earthquakes reach larger slip and longer  
 362 recurrence interval by dimension reduction (Fig. 3). To quantify the difference in slip we  
 363 compare the total slip (i.e., seismic slip + aseismic slip), because it is largely constant  
 364 throughout the fault plane in one earthquake cycle. Total slip is also equal to the max-  
 365 imum coseismic slip, since the maximum is only achieved where the fault portion is fully  
 366 locked in the interseismic period. This makes it, together with earthquake recurrence in-  
 367 terval, good long-term earthquake cycle characteristics. In 3D, we observe earthquakes  
 368 with average total slip of  $\sim 4.5$  m and recurrence interval of  $\sim 135$  yr (Fig. 3a). In 2D,  
 369 fault slips  $\sim 6.8$  m every  $\sim 215$  yr., about 50% larger than in 3D (Fig. 3b). In 1D, fault  
 370 slips  $\sim 13.3$  m every  $\sim 420$  yr, about three times as large as the 3D results and twice  
 371 the 2D results (Fig. 2c). Note that in calculation of these numbers we excluded the slightly  
 372 larger first earthquake that initiated at the predefined nucleation zone.

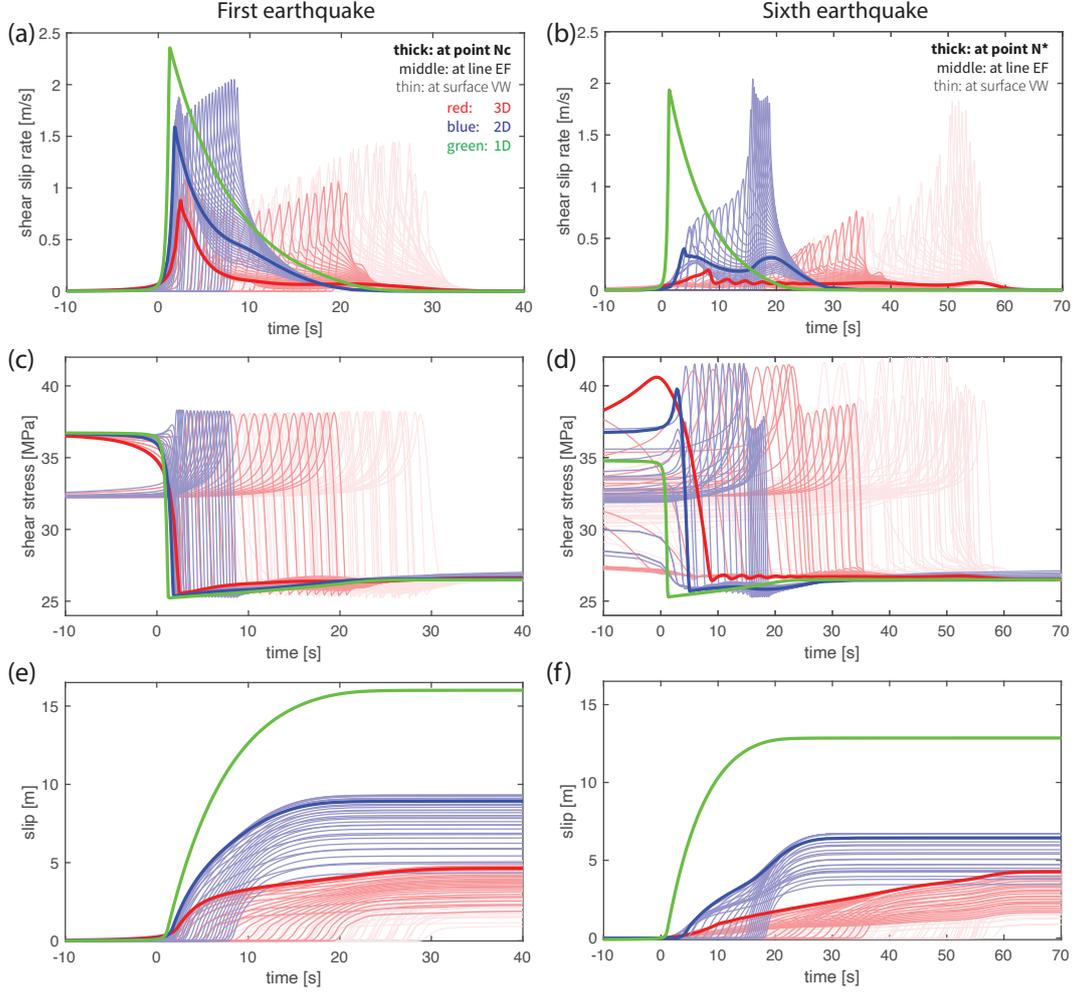
373 We contribute the larger earthquakes simulated in lower dimensional models largely  
 374 to a lower interseismic stress rate. During the interseismic phase, the VS patches are creep-

375 ing at the plate rate so they do not accumulate stress. They only play a role in trans-  
 376 ferring the tectonic loading from the loading boundaries into the VW patch they sur-  
 377 round. In other words, the VW patch is loaded directly by its surrounding VS patches  
 378 rather than the loading boundaries, whether the bulk medium is simulated explicitly or  
 379 not. This clarification is fundamental because in this way the VW patch in 3D is loaded  
 380 from four sides, rather than only from the top/bottom where tectonic loading regions  
 381 are located. While the VW patch in 2D is loaded from two sides, resulting in slower in-  
 382 terseismic stress rate inside the VW patch and hence a longer period before the next earth-  
 383 quake can nucleate (thickest lines in Fig. 2b). Given that the constant creeping rate in  
 384 the VS patches is unchanged, the resulting larger slip deficit in the VW patch has to be  
 385 made up by an earthquake with more slip. This is why larger earthquake slips are ob-  
 386 served in lower dimensional models. Therefore these interseismic differences are largely  
 387 explained by the reduced presence of VS patches due to dimension reduction. Quanti-  
 388 tative calculations based on theoretical considerations, supporting the analysis above,  
 389 will follow in section 3.5.

390 That clarification also implies that the interseismic stress rate in the VW patch does  
 391 not depend on the size of the VS patches  $W_f$  or the distance of the loading boundaries  
 392  $(W_f - H)/2$ , but on the size of the VW patch itself. The smaller the VW patch is, on  
 393 average the faster the loading will be. This explains why larger slip and longer recur-  
 394 rence interval are still observed in 1D even though the distance between the VW fault  
 395 and the far-away loading boundary  $X_0$  is already chosen to be  $(W_f - H)/2$ , the same  
 396 as in higher dimensions (in section 2.3). We wanted to make the stress rate directly caused  
 397 by the loading boundaries comparable to that in 2D and 3D models by this method, but  
 398 the actual stress rate proved to be inadequate. Therefore  $X_0$  has to be shortened to ob-  
 399 tain higher stress rate in order to achieve similar earthquake slip and recurrence inter-  
 400 val (see explanation in section 4.3).

### 401 **3.2 Coseismic rupture of the first earthquake**

402 For the first earthquake (Fig. 4a, c, e), the source time function at all locations within  
 403 the VW patch takes the shape of Kostrov's classic self-similar crack solution (Kostrov  
 404 & Das, 1988) with a short rise time and relatively long deceleration tail. As dimensions  
 405 are reduced, the duration of the rise time decreases while the duration of the deceler-  
 406 ation increases. The deceleration in 1D is the slowest, since the rupture does not inter-

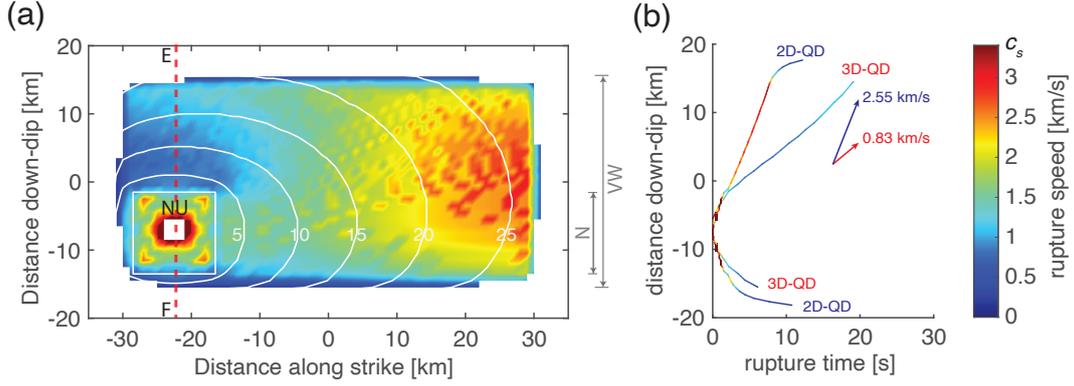


**Figure 4.** Comparison of the coseismic time series of (a, b) slip rate, (c, d) stress and (e, f) accumulated slip in 1-3D models. The first earthquake is shown in (a, c, e), and the sixth earthquake is shown in (b, d, f), where origin time is set at the onset of the respective earthquake. The lines with different thicknesses and degrees of transparency are recorded at different locations on the fault, where the thick lines are recorded at the nucleation location “Nc” (the first earthquake) or “N\*” (the sixth), the semi-thick lines along the line “EF” cutting across it vertically and the thin lines elsewhere in the VW patch (see Fig. 6a, c).

407 act with patches of different stress or strength properties that could decelerate it. For  
 408 the same reason, it is impossible to observe rupture reflections in 1D. While the rupture  
 409 reflection from the VW-VS boundary in 3D is clearly observable as a second slip veloc-  
 410 ity peak (Fig. 4a).

411 Despite this qualitative similarity, we compare slip velocity, rupture speed and stress  
 412 drop for their quantitative differences across dimensions. Peak slip velocity and rupture  
 413 speed are important earthquake characteristics that reflect the dynamic characteristics  
 414 of a fracture. We observe that peak slip velocities reach the same order of magnitude of  
 415 around  $10^0$  m/s regardless of dimension, but they do increase by tens of percent in lower  
 416 dimensional models (Fig. 4a). In 3D, the peak slip velocity is initially  $\sim 0.8$  m/s in the  
 417 predefined nucleation zone and gradually increases to its maximum of  $\sim 1.5$  m/s. In 2D,  
 418 the peak slip velocity starts around  $\sim 1.6$  m/s and gradually increases up to  $\sim 2.0$  m/s.  
 419 In 1D, the maximum slip velocity is  $\sim 2.4$  m/s. We connect this increase again to the  
 420 reduced presence of VS patches due to dimension reduction. In 2D models, the 1D fault  
 421 “line” represents a 2D fault plane in which the VW patch is extended infinitely long along  
 422 strike in a 3D perspective (e.g., Andrews et al., 2007), whereas in 1D models the 0D fault  
 423 “point” represents an infinitely large, fully-VW 2D fault plane. In other words, the VS  
 424 patches are removed from the dimensions that is not explicitly simulated, which would  
 425 originally absorb energy from the rupture if the rupture would interact with them. More  
 426 importantly, every portion of the fault along the not explicitly simulated direction rup-  
 427 tures at the same time as its simulated counterpart. Thus no fracture energy is consumed  
 428 in those directions. The energy that is not consumed in these ways can instead be used  
 429 to achieve higher slip velocities, as evident from the earthquake energy budget consid-  
 430 erations in Kanamori and Rivera (2006).

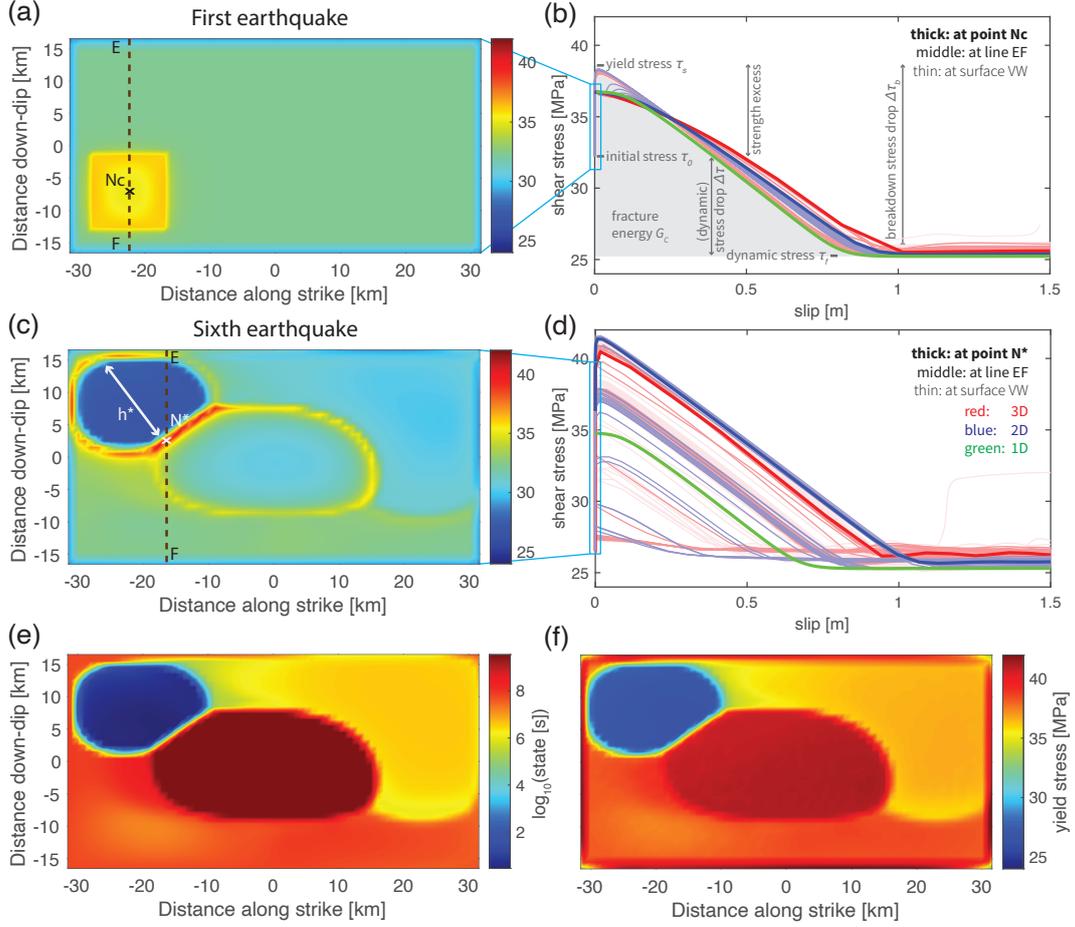
431 Rupture speed across different dimensional models shows larger variation than peak  
 432 slip velocity. In 3D, the total coseismic rupture lasts for  $\sim 30$  s. Rupture propagates faster  
 433 in the horizontal direction than in the vertical direction and it experiences an acceler-  
 434 ation in the last  $\sim 10$  s to reach near-shear speed (Fig. 5a). The rupture front takes  $\sim$   
 435 20 s to propagate along the vertical line “EF”, at a near-constant speed of  $\sim 0.83$  km/s,  
 436 except for the first several seconds and the arrest. In 2D, the rupture takes only  $\sim 10$   
 437 s to reach the up-dip limit, starting from the same nucleation region (Fig. 5b). Accord-  
 438 ingly, the rupture speed of the stable part is  $\sim 2.55$  km/s, almost twice higher than in  
 439 3D. To explain these differences in rupture speed, the same considerations used to ex-



**Figure 5.** Comparison of coseismic rupture propagation. (a) The coseismic rupture speed of the first earthquake in 3D. The arrival time of the coseismic rupture front, which is measured when slip velocity reaching the seismic limit, is plotted every five seconds as contours. The central part of the fault plane is shown where white color means no seismic slip is observed. The red dashed line labels the observation line “EF” introduced in Fig. 1. Note that no reliable rupture speed is measured at rupture onset (left white near “Nc”). (b) The coseismic rupture front arrival time along the vertical line “EF” in 2D and 3D. The line color indicates the rupture speed under the same color scale as (a). Lines end at where slip rates drop below seismic threshold. The average rupture speed in the middle of propagation (i.e., except during nucleation and arrest) is measured as stated.

440 plain the differences in peak slip velocities are applied. In 2D models, no fracture energy  
 441 needs to be overcome to rupture into the strike direction and hence more energy can be  
 442 directed along dip, which allows the rupture to achieve higher speeds. This also short-  
 443 ens the rupture duration and leads to ruptures that propagate deeper into the surround-  
 444 ing VS patches compared to 3D models (Fig. 5b). Given that the difference between 2D  
 445 and 3D models occurs in the horizontal direction while the vertical direction remains iden-  
 446 tical, our results suggest that the (in)existence of the horizontal VS patches has influ-  
 447 ence on the coseismic rupture behavior inside the VW patch, even in the vertical direc-  
 448 tion. This is confirmed in additional models where a second rupture deceleration can be  
 449 observed if the length of the VW patch is shortened to one fourth (see section 4.1, Fig. 9).

450 Given the same initial condition, the stress drop and fracture energy of the first  
 451 earthquake are comparable in all dimensional models, both inside and outside the pre-  
 452 stressed zone (Fig. 6b). The stress drop  $\Delta\tau$ , i.e., the stress difference between the start  
 453 and the end of an earthquake, and the fracture energy  $G_c$ , i.e., the surface area below  
 454 the stress w.r.t slip profile, are important earthquake parameters (see Fig. 6b for more  
 455 definitions of stresses and stress drops used below). Regardless of dimension and at all  
 456 VW locations we first observe the shear stress increasing up to the yield stress and then  
 457 it drops to a constant level corresponding to dynamic friction (Fig. 4c). Both the yield  
 458 stress and the dynamic stress are comparable across dimensions. Therefore the differ-  
 459 ence between the two (so-called breakdown stress drop  $\Delta\tau_b$ , i.e., strength excess + stress  
 460 drop) is also similar. Notice that the initial stress increase is not as large when getting  
 461 close to the nucleation zone and it is nearly zero inside it (thickest line in Fig. 4c). This  
 462 shows that the nucleation zone has to reach its yield stress before the coseismic phase,  
 463 which is usually lower comparing to the maximum achievable yield stress elsewhere. Af-  
 464 ter the stress drop, an immediate small stress increase is observed that is also similar in  
 465 size across dimensions (Fig. 4c). It is worth noting that the stress drop at different lo-  
 466 cations is achieved within a similar amount of slip (Fig. 6b), regarded as the character-  
 467 istic slip weakening distance  $D_c$  in a linear slip-weakening friction formulation. After this  
 468 distance, coseismic slip continues to accumulate until the earthquake arrests. The crit-  
 469 ical slip-weakening distance varies from 0.8 m to 1.1 m from 3D to 1D. Given the sim-  
 470 ilar size of stress drop and slip-weakening distance, the fracture energy  $G_c \approx \Delta\tau_b D_c / 2$   
 471 (Fig. 6b) is also found to be comparable across dimensions and at all VW locations (with  
 472 a minor increase from 1D to 3D).



**Figure 6.** Cross-dimensional comparison of (a, c) the initial stress and (b, d) the coseismic stress evolution w.r.t. slip in 1-3D models for (a, b) the first earthquake and (c, d) the sixth earthquake. (a, c) The initial stress is measured when the maximum slip velocity reaches the seismic threshold. The nucleation size is denoted as  $h^*$ . Due to the high prestress, the coseismic slip of the first earthquake begins from the center of the nucleation zone (denoted as “Nc”). Whereas the coseismic slip of the sixth earthquake begins at the rim of the nucleation zone (denoted as “N\*”). (b, d) The lines with different thicknesses and degrees of transparency are recorded at different locations on the fault, where the thick lines are recorded at point “Nc” (the first earthquake) or “N\*” (the sixth), the semi-thick lines along the vertical line “EF” through it and the thin lines elsewhere in the VW patch (see panels a, c, respectively). (e) The initial state of the sixth earthquake. (f) The yield stress of the sixth event. The definitions of stresses and stress drops used in the text are labeled in panel (b).

473 The differences in stress drop and fracture energy across dimensions are minor. This  
 474 is in line with expectations, since these earthquake parameters are considered to be largely  
 475 controlled by the frictional properties and the normal stress (e.g., Rubín & Ampuero,  
 476 2005) that are homogeneous in this model. However, the modest systematic differences  
 477 in, for example, the critical slip weakening distance that becomes shorter at lower dimen-  
 478 sions, still indicates that the dynamics on the fault play a role in redistributing the earth-  
 479 quake energy budget, so that the stress drop and the slip weakening distance can change  
 480 accordingly. This is more evident when the fault is shorted to one fourth its width where  
 481 yield stress is observed decreasing while rupture propagates (see section 4.1, Fig. 9).

### 482 3.3 Nucleation phase

483 A spontaneous nucleation phase is observed in later earthquakes that experience  
 484 tectonic loading. To understand cross-dimensional differences under more realistic ini-  
 485 tial conditions prevalent after the first earthquake, we also analyze the sixth earthquake.  
 486 This earthquake is representative since earthquakes are essentially characteristic from  
 487 the second onward.

488 Earthquake initiation somewhat differs across dimensions in how much aseismic slip  
 489 is accumulated prior to nucleation and in the nucleation size  $h^*$ . To understand this and  
 490 to understand which fault plane locations are most comparable, we analyze interseismic  
 491 slip velocity and shear stress evolution patterns (Fig. 2). These patterns that depend on  
 492 the distance between the observation point and the VS patches are qualitatively simi-  
 493 lar in all dimensional models. Faster loading occurs near the VS-VW transition and these  
 494 regions start to creep at plate rate the earliest. Slip becomes unstable when the creep-  
 495 ing front propagates into the locked region up to the nucleation size  $h^*$ . Nucleation then  
 496 occurs in one of the four corners in the VW patch in 3D or one of the two ends in 2D.  
 497 The nucleation size is observed to be roughly twice as large in 3D compared to the size  
 498 in 2D (Fig. 3). At the rim of this nucleation zone, highest shear stress is achieved due  
 499 to the largest velocity gradient between creeping and locked zones. In the meantime, the  
 500 inner nucleation zone yields and accelerates, which is accompanied by stresses dropping  
 501 back to their steady-state (Fig. 6c). Based on whether the observation point is inside the  
 502 nucleation zone, at the nucleation rim (e.g., point “N\*” in Fig. 6c) or outside the nucle-  
 503 ation zone, similar loading and nucleating behavior is shared across dimensions, respec-  
 504 tively (Fig. 2). Inside the nucleation zone, faster slip velocity and stress accumulation

505 rates are observed, both with a plateau at steady-state before earthquake starts (mid-  
 506 dle to thin lines that are to the left and above the thickest line in Fig. 2a, b). Outside  
 507 the nucleation zone, at a point closer to the central VW patch that experiences slower  
 508 loading, slip velocity and shear stress increase more slowly. This fault portion remains  
 509 locked before the start of the next earthquake, i.e., slip velocity is always below plate rate  
 510 and shear stress below the aforementioned steady-state stress level (middle to thin lines  
 511 that are to the right and below the thickest line in Fig. 2a, b). Only at the rim of the  
 512 nucleation zone, can slip velocity and shear stress increase at a unique rate that allows  
 513 for the earthquake to occur as soon as the plate rate and the fault strength are reached  
 514 at the same time (e.g., thickest lines in Fig. 2a, b). Since the seismic rate is achieved in-  
 515 stantaneously, no aseismic slip is accumulated at this location during nucleation.

516 In 1D models with a 0D fault “point”, slip also immediately becomes seismic as  
 517 soon as the shear stress reaches the interface strength and thus does not accumulate pre-  
 518 ceding aseismic slip. Therefore, such models mimic the rim of the nucleation zone in higher  
 519 dimensional models (thickest lines in Fig. 2). This is because, as we discussed above, the  
 520 0D fault “point” represents an infinite fully-VW fault plane from a 3D perspective, on  
 521 which earthquakes nucleate simultaneously at all locations as yield stress is reached at  
 522 the same time. This location is where simulation results are best compared across di-  
 523 mensions and are further explored in theoretical calculations (section 3.5).

### 524 **3.4 Coseismic phase of later earthquakes**

525 An important consequence of interseismic loading is that it reshapes the initial stress  
 526 (stress at the beginning of coseismic phase) and initial state to be heterogeneous (Fig. 6c,  
 527 e, also refer to panel b for the definition of below-mentioned stress, stress drop and en-  
 528 ergy). Due to the variable distances to the VS patches and the nucleation process, dif-  
 529 ferent locations in the VW patch are loaded to a spatially variable level of initial stress  
 530 and initial state. The nucleation zone has the lowest initial stress, whereas its rim has  
 531 the highest values close to the yield stress (Fig. 6c). The same holds for initial state ex-  
 532 cept that a high state variable is also achieved in the center of the VW patch (Fig. 6e).  
 533 This is because during the preceding interseismic phase the central VW patch remains  
 534 locked. According to Nakatani (2001)’s definition of interface strength ( $\sigma_n [\mu_0 + b \ln (\frac{\theta V_0}{L})]$ ),  
 535 this region is healed to a much higher interface strength than its surrounding. Conse-

536 quently, the subsequent coseismic phase exhibits characteristics that the first earthquake  
 537 did not show.

538 Our dimensional comparison of the first earthquake regarding the rupture speed  
 539 and slip velocity remains qualitatively valid (Fig. 4b, d, f vs. a, c, e) for the coseismic  
 540 phase of later earthquakes. However, it is worth pointing out that the rupture speed is  
 541 overall about 50% slower than the first earthquake, resulting in twice as long rupture du-  
 542 ration in both 2D and 3D models (Fig. 4b vs. a). The peak slip velocity grows slowly  
 543 at the beginning when the rupture is propagating into the central VW patch. The high  
 544 interface strength suppresses its propagation into this patch and thus limits both rup-  
 545 ture speed and peak slip velocity. Only once the rupture front has passed and is closer  
 546 to the VW-VS transition do the rupture speed and peak slip velocity increase sharply.  
 547 Combining lower slip velocity and longer coseismic duration, the accumulated seismic  
 548 slip is smaller in latter earthquakes than for the first earthquake (Fig. 3, 4f vs. e). Smaller  
 549 seismic slip is thus a result of the lower average initial stresses (and lower slip deficit)  
 550 for spontaneously loaded earthquakes with respect to the highly stressed nucleation zone  
 551 predefined for the first earthquake.

552 Given the same level of dynamic stress after the earthquake, the nonuniform ini-  
 553 tial stress field also results in a nonuniform stress drop  $\Delta\tau$  (Fig. 6d). Additionally, the  
 554 yield stress is spatially variable, making the breakdown stress drop  $\Delta\tau_b$  nonuniform as  
 555 well (Fig. 6d, f, also clearly visible in 4d). The stress-slip profile and fracture energy are  
 556 thus no longer near-identical throughout the VW patch as they are in the first event (Fig. 6d  
 557 vs. b). Compared to the first earthquake, the yield stress becomes higher near the cen-  
 558 tral VW patch and lower closer to the VW-VS transition, making it lower when aver-  
 559 aged over the whole seismogenic zone (Fig. 6f). Fracture energy  $G_c$  varies accordingly:  
 560 it increases near the center, decreases closer to the transition, and decreases on average.  
 561 This illustrates the importance of tectonic loading for the coseismic rupture, as it mod-  
 562 ifies the initial stress, yield stress and energy profiles. Yield stress can thus no longer be  
 563 simply defined by the frictional properties.

564 The 1D models, lacking the space for nucleation and dynamic rupture, never reach  
 565 the initial and yield stress level higher dimensional models achieve in later earthquakes  
 566 (Fig. 4d). This makes them quantitatively dissimilar to 2/3D simulations in the coseis-

567 mic phase, even from the aspect of mimicking the nucleation rim (thickest lines in Fig. 4b,  
 568 d, f vs. a, c, e).

### 569 **3.5 Theoretical considerations**

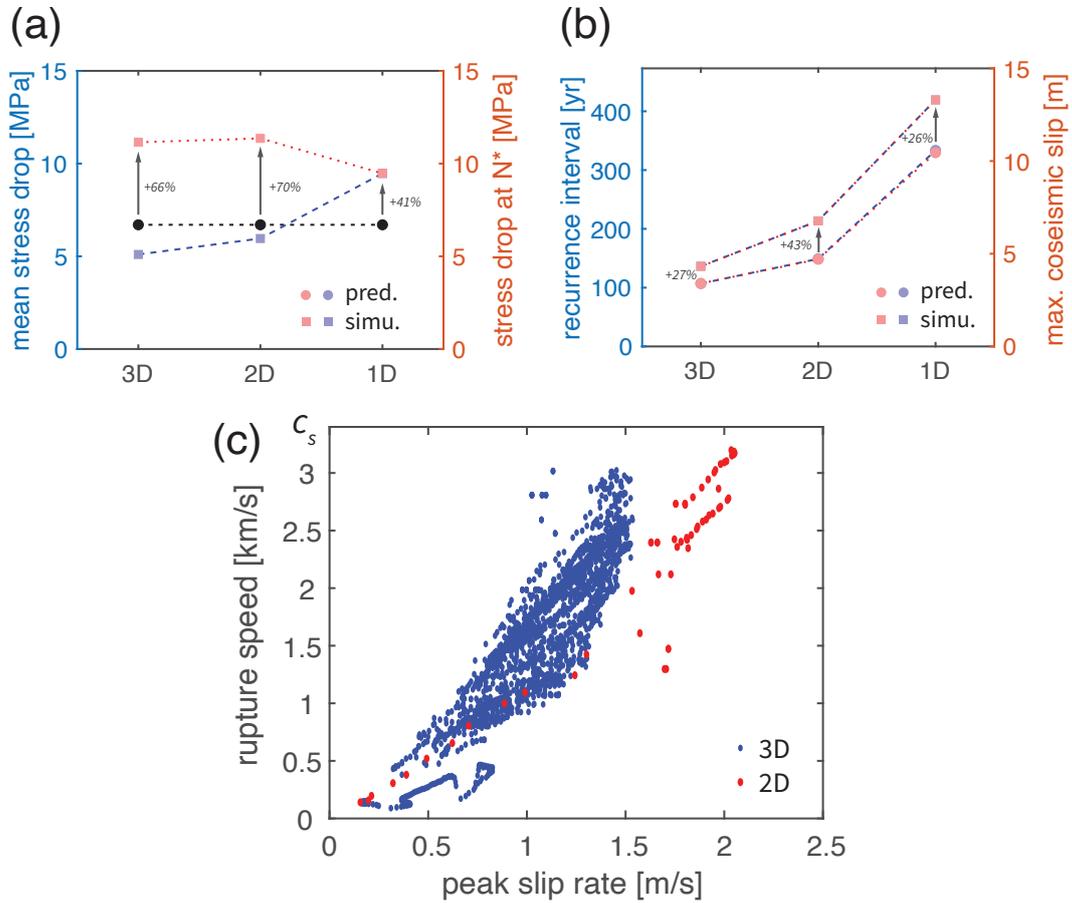
570 To better analyze the similarities and understand the differences across dimensions,  
 571 we utilize theoretical calculations that can estimate the aforementioned characteristic  
 572 observables to the first order.

#### 573 **3.5.1 Earthquake cycle parameters**

574 We estimate earthquake recurrence interval and total slip (i.e., aseismic + seismic  
 575 slip, maximum coseismic slip) by extending the 3D theoretical formulation in Chen and  
 576 Lapusta (2019) to all other dimensions using the analytical crack models of Knopoff (1958)  
 577 and Keilis-borok (1959). Earthquake recurrence interval  $T$  can be estimated when it is  
 578 known how much stress is accumulated and what the interseismic stress rate is, namely  
 579  $T = \Delta\tau/\dot{\tau}$ . Maximum coseismic slip  $D$ , which equals to the interseismic slip deficit,  
 580 can be estimated from the aseismic slip accumulated on the surrounding creeping VS patches  
 581 during the interseismic phase, namely  $D = V_p T$ .

582 To provide a reliable estimate of the interseismic stress rate and its maximum it  
 583 is important to know which fault location is most representative for this purpose. This  
 584 is important because the stress accumulation pattern is non-linear and spatially variable  
 585 (Fig. 2), as explained in the description of the nucleation phase (section 3.3). Give the  
 586 nonuniform initial stress  $\tau_i$  (Fig. 6c) and the generally uniform dynamic stress  $\tau_f$  as a  
 587 starting level, the interseismic stress that needs to be accumulated  $\Delta\tau = \tau_i - \tau_f$  is thus  
 588 not uniform. A similar spatial variation holds for the interseismic stress rate  $\dot{\tau}$  (Fig. 2b).  
 589 Interestingly, the stress accumulates at an approximately linear rate at the rim of the  
 590 nucleation zone, e.g., at location “N\*” in Fig. 6c. Additionally, this location does not  
 591 experience aseismic creep during the nucleation phase, as the slip becomes seismic im-  
 592 mediately. These two observations make a straight-forward theoretical calculation to es-  
 593 timate both recurrence interval  $T$  and maximum coseismic slip  $D$  feasible by analyzing  
 594 the stress accumulation at location “N\*”.

595 This location is at the distance of  $h^*$  inside the VW patch since an earthquake can  
 596 only nucleate when the creep penetrates this distance into the VW patch, where  $h^*$  is



**Figure 7.** Comparison between theoretical predicted and numerically simulated results. (a) Comparison between theoretically predicted (circle) and numerically simulated (square) average stress drop (blue) and stress drop at location “N\*” (red). The prediction is shared by both axis quantities and colored in black. The difference (in percentage) between calculated and simulated stress drop at location “N\*” is labeled aside. (b) Comparison between theoretically predicted (circle) and numerically simulated (square) recurrence interval (blue) and maximum coseismic slip (red). Same labels as in (a). Note that the markers in blue and red are largely overlapped in this panel. (c) Interrelation between rupture speed and peak slip velocity in 3D (blue) and 2D (red) models. The local values are measured at different locations inside the VW patch.

597 the nucleation size. First, the interseismic stress accumulation is estimated by the stress  
 598 drop  $\Delta\tau_{\text{dyn}}$ , which is approximated from the stress difference between the two steady-  
 599 state friction level during the interseismic and coseismic phase (Cocco & Bizzarri, 2002)

$$\begin{aligned} \Delta\tau_{\text{dyn}} &\approx \tau(V_p) - \tau(V_{\text{dyn}}) \\ &\approx \sigma[\mu_0 + (a - b)\ln(V_p/V_0)] - \sigma[\mu_0 + (a - b)\ln(V_{\text{dyn}}/V_0)] \\ &= \sigma(b - a)\ln(V_{\text{dyn}}/V_p) , \end{aligned} \quad (14)$$

601 where dynamic slip velocity  $V_{\text{dyn}}$  is approximated as 1 m/s for simplicity. Second, the  
 602 stress rate is calculated at the desired location that is at the distance of  $h^*$  inside the  
 603 VW patch (in 2D and 3D models, respectively, Rubin & Ampuero, 2005)

$$\begin{aligned} h_{2\text{D}}^* &= \frac{2GLb}{\pi\sigma(b - a)^2} \\ h_{3\text{D}}^* &= \frac{\pi^2}{4}h_{2\text{D}}^* = \frac{\pi GLb}{2\sigma(b - a)^2} \end{aligned} \quad (15)$$

605 for mode III deformation in our models. The factor  $\pi^2/4$  comes from the stress inten-  
 606 sity factor (SIF) that is different for different rupture front curvatures in 2D and 3D (Tada  
 607 et al., 1973). The stress rate  $\dot{\tau}_{h^*}$  at this location can be expressed as (Chen & Lapusta,  
 608 2019; Keilis-borok, 1959; Knopoff, 1958)

$$\dot{\tau}_{h^*} = C \frac{GV_p}{\sqrt{r^2 - (r - h^*)^2}} . \quad (16)$$

610 For a fault segment of half-width  $r$  in 2D models or a circular fault of radius  $r$  in 3D mod-  
 611 els it has the same form with  $C$  a dimension-dependent constant being either  $C_{3\text{D}} =$   
 612  $\frac{\pi(2-\nu)}{8(1-\nu)} = 7\pi/24$  (Keilis-borok, 1959) or  $C_{2\text{D}} = 1/2$  (Knopoff, 1958). This expression  
 613 is directly applicable to our 2D models with  $r = H/2$ . While in 3D models, taken into  
 614 consideration that the width of VW patch  $H$  is shorter than its length  $l$ , we apply this  
 615 expression to our rectangular fault by assuming  $r \approx H/2$ . In 1D, the tectonic loading  
 616 is applied from the far-away boundary. In this case we replace the whole denominator  
 617  $\sqrt{r^2 - (r - h^*)^2}$  by  $X_0$ , the distance between fault and the far-away loading boundary,  
 618 with  $C_{1\text{D}} = 1$ . Third, by combining the interseismic stress rate and coseismic stress drop  
 619 together we approximate the recurrence interval  $T$  by

$$T = \Delta\tau_{\text{dyn}}/\dot{\tau}_{h^*} = \frac{(b - a)\sigma}{CGV_p} \sqrt{r^2 - (r - h^*)^2} \ln \frac{V_{\text{dyn}}}{V_p} . \quad (17)$$

621 Finally, the total slip  $D$ , or the maximum coseismic slip, is estimated by

$$D = V_p T = \frac{(b - a)\sigma}{CG} \sqrt{r^2 - (r - h^*)^2} \ln \frac{V_{\text{dyn}}}{V_p} . \quad (18)$$

623 The theoretically predicted and numerically simulated recurrence interval and max-  
624 imum coseismic slip are in agreement for all dimensions (Fig. 7b). This confirms the ob-  
625 served trend that longer recurrence interval and larger coseismic slip are a result of di-  
626 mension reduction. It also justifies our explanation that the larger coseismic slip is caused  
627 by the larger slip deficit during longer recurrence interval and the longer recurrence in-  
628 terval is caused by the lower interseismic stress rate. The theoretically predicted values  
629 systematically underestimate the numerical simulations by about 30% (Fig. 7b). We no-  
630 tice that the relative difference is nearly identical between the recurrence interval and  
631 the total slip, indicating that the error in slip calculation (18) may be directly inherited  
632 from the recurrence interval calculation (17). The underestimation of the stress drop at  
633 location “N\*” by stress drop  $\Delta\tau_{\text{dyn}}$  is a main contributor to this error (Fig. 7a). Our sim-  
634 ulations show that for the locations at the nucleation rim (point “N\*” in Fig. 6c) ini-  
635 tial stress  $\tau_i$  is notably higher than its surrounding. However, we notice that this under-  
636 estimation of the accumulated stress is stronger than the underestimation of the final  
637 values (Fig. 7a), indicating that the interseismic stress rate  $\dot{\tau}$  is underestimated as well.  
638 This is due to the increased stress rate at the beginning and the end of the interseismic  
639 phase. At the beginning of the interseismic phase, it is increased by the effect of the post-  
640 seismic slip. While near the end of the nucleation phase it is due to the expanding nu-  
641 cleation zone that creeps, introducing additional slip gradient (Fig. 2b). Despite the er-  
642 rors, these theoretical considerations well explained the simulated earthquake cycle pa-  
643 rameters and their trend with dimension reduction as a first order approximation.

### 644 **3.5.2 Coseismic rupture parameters**

645 Unlike the recurrence interval and total slip, coseismic rupture parameters such as  
646 rupture speed and slip velocity vary across the fault. Our theoretical calculations can-  
647 not provide an absolute estimate of the rupture speed. However, both laboratory exper-  
648 iments (Ohnaka et al., 1987) and theoretical considerations (Ida, 1973; Ampuero & Ru-  
649 bin, 2008) suggest that the peak slip velocity  $V_{\text{peak}}$  and the rupture speed  $V_r$  are inter-  
650 related by

$$651 \quad V_r = \alpha_r V_{\text{peak}} \frac{G}{\Delta\tau_b}, \quad (19)$$

652 where  $\alpha_r$  is a factor on the order of 1. This positive correlation is confirmed by our sim-  
653 ulations (Fig. 7c). We measured on average  $\alpha_r$  of 0.82 in 3D and 0.65 in 2D for the first  
654 earthquake respectively, which is similar to what Hawthorne and Rubin (2013) measured

655 (0.50-0.65) in their 2.5D simulations. The lower value of  $\alpha_r$  in 2D suggests that with di-  
 656 mension reduction higher slip velocity can be achieved under the same rupture speed.

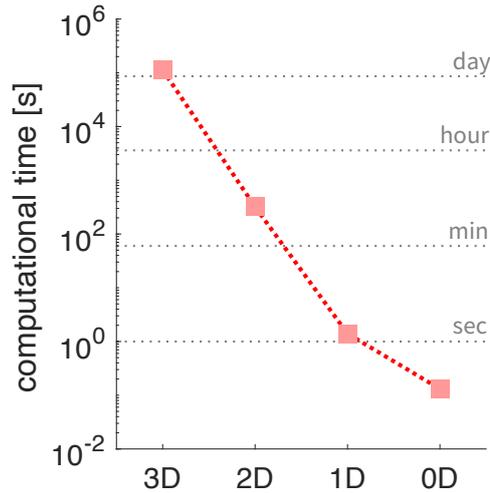
657 Whereas the calculated stress difference from rate-and-state friction between the  
 658 two steady states in the interseismic and coseismic phase (14) is independent of dimen-  
 659 sion and location, the stress drop  $\Delta\tau$  is not uniform across the simulated VW patch. There-  
 660 fore that theoretical prediction only provides an estimation of the average stress drop (Chen  
 661 & Lapusta, 2019)

$$662 \quad \overline{\Delta\tau} \approx \Delta\tau_{\text{dyn}} \approx \sigma(b - a)\ln(V_{\text{dyn}}/V_p) . \quad (20)$$

663 The calculated average stress drop is slightly higher than the simulated results in 2D and  
 664 3D (Fig. 7a). However, it is still satisfying as a first order approximation for both mod-  
 665 els given that the contribution of the changing state has been ignored. It is noticed that  
 666 the 1D model has a higher simulated average stress drop. This is because the “average”  
 667 loses its meaning in this case and the simulated value only represents where the earth-  
 668 quake nucleates in higher dimensional models (point “N\*”). It is well expected that higher  
 669 stress drop is achieved here following the explanation in section 3.3 and the subsection  
 670 above.

### 671 **3.6 Computational efficiency**

672 Lower dimensional models are computationally more efficient without losing the  
 673 qualitative characteristics and the ability to estimate certain earthquake parameters such  
 674 as maximum slip velocity, maximum or average stress drop, and fracture energy. To eval-  
 675 uate the computational efficiency of each model we measure the average computational  
 676 time per earthquake cycle (Fig. 8). The 3D model takes  $10^3$  times longer time than 2D  
 677 and  $10^5$  times longer than 1D. In the following discussions we will see that the 1D model  
 678 can be further simplified to its 0D equivalent by removing the medium content (the  $x >$   
 679 0 axis in 1D models). The 0D model will again save more than 90% running time com-  
 680 pared to 1D, making it more than a million times faster than 3D models. Note that these  
 681 computations do not use distributed memory and therefore ignore related parallel scal-  
 682 ing issues.



**Figure 8.** The average computational time of one earthquake cycle in 0D to 3D models, under the same resolution and domain size, with 12 CPUs Kokkos level parallelization.

## 4 Discussions

We are the first to systematically study and quantify similarities and differences in how models in different dimensions simulate earthquake sequences. While large-scale parallel computing can be exploited to reduce the time to solution of 3D applications, this does not significantly lower the power consumption and consequently the monetary and environmental burden. Moreover, we find that the orders of magnitude difference of speed-up by dimensional reduction are so large (Fig. 8), and can be even larger when higher resolution is necessary, that they readily make the difference between being feasible for scientific and exploratory research or not. Hence lower dimensional models will likely remain essential for scientific exploration in the coming decades (Lapusta et al., 2019). Especially when the researcher’s objectives fall into the scope of what the lower dimensional models can handle, they are encouraged to use them as they could be hundreds to millions times faster than a 3D model with the same resolution.

However, we should also acknowledge that there are research questions whose answers inherently require higher-dimensional spatial or geometrical complexity. For example, rupture arrest in the missing dimension can never be captured in lower-dimensional models, no matter if it is self-arrested or due to the presence of VS patches. Temporally-complex patterns of earthquake occurrence as well as partial ruptures reduce their ex-

701 istence at the same time. We are not aiming at finding substitutes for such cases but rather  
 702 to present the essential differences that are apparent in the simplest setup. The differ-  
 703 ences between models of different dimensions presented in this paper will have no rea-  
 704 son to disappear when more complicated setups are adopted. On the other hand, although  
 705 3D models are necessary for certain studies (e.g., Galvez et al., 2014; Ulrich et al., 2019;  
 706 Wollherr et al., 2019; Madden et al., 2021), simpler models can always be a useful start-  
 707 ing point of an exploration. These results should also serve as guidelines as to how to  
 708 interpret the lower-dimensional modeling results with their limitations ready in hand,  
 709 rather than being regarded solely as restricting model simplifications to being adopted.

#### 710 **4.1 Under what conditions can 2D models substitute 3D models?**

711 We have summarized model similarities over dimensions as well as analyzed how  
 712 model discrepancies due to dimension reduction explain the resulting differences. It is  
 713 worth further exploring in which situations dimension reduction can be used without con-  
 714 siderable side effects or when it should be avoided even if computational efficiency is a  
 715 factor. To simplify the question, we restrict ourselves to the most common discussion  
 716 point: under what conditions can a 3D model be substituted by a 2D model? Since along-  
 717 strike heterogeneities are ignored in the given dimension reduction assumption (section 2.3),  
 718 3D models with different along-strike features are simplified to the same 2D model. How-  
 719 ever, they originally simulate different earthquake sequences. We have chosen the VW  
 720 patch length as one common along-strike heterogeneity to analyze the role of this reduced  
 721 dimension. We vary the VW patch length  $l$  and keep the VW patch width  $H$  fixed. By  
 722 varying the VW patch length from 150 km to 15 km, we change the aspect ratio from  
 723 5:1 to 0.5:1 (Fig. 9). The fault (VW+VS patches) size and the computational domain  
 724  $(X_0, Y_0, Z_0)$  are kept unchanged as well as the predefined nucleation zone as an initial  
 725 condition, which is always set at the left bottom corner with fixed distance  $h_i$  to the VW-  
 726 VS boundary (Fig. 9a). This configuration benefits the coseismic comparison along the  
 727 vertical line “EF” crossing this zone (Fig. 9c-m) to our 2D simulations (Fig. 4, 5).

728 In the long term, longer VW patches result in longer recurrence intervals (Fig. 9b).  
 729 This is because the stress rate at the nucleation zone is lower comparing to a fault with  
 730 a shorter VW patch. Given that the nucleation always starts from a corner of the rect-  
 731 angular VW patch, the nucleation zone in a longer VW patch is mainly loaded from three  
 732 directions as the tectonic loading from the other horizontal direction is farther away. This

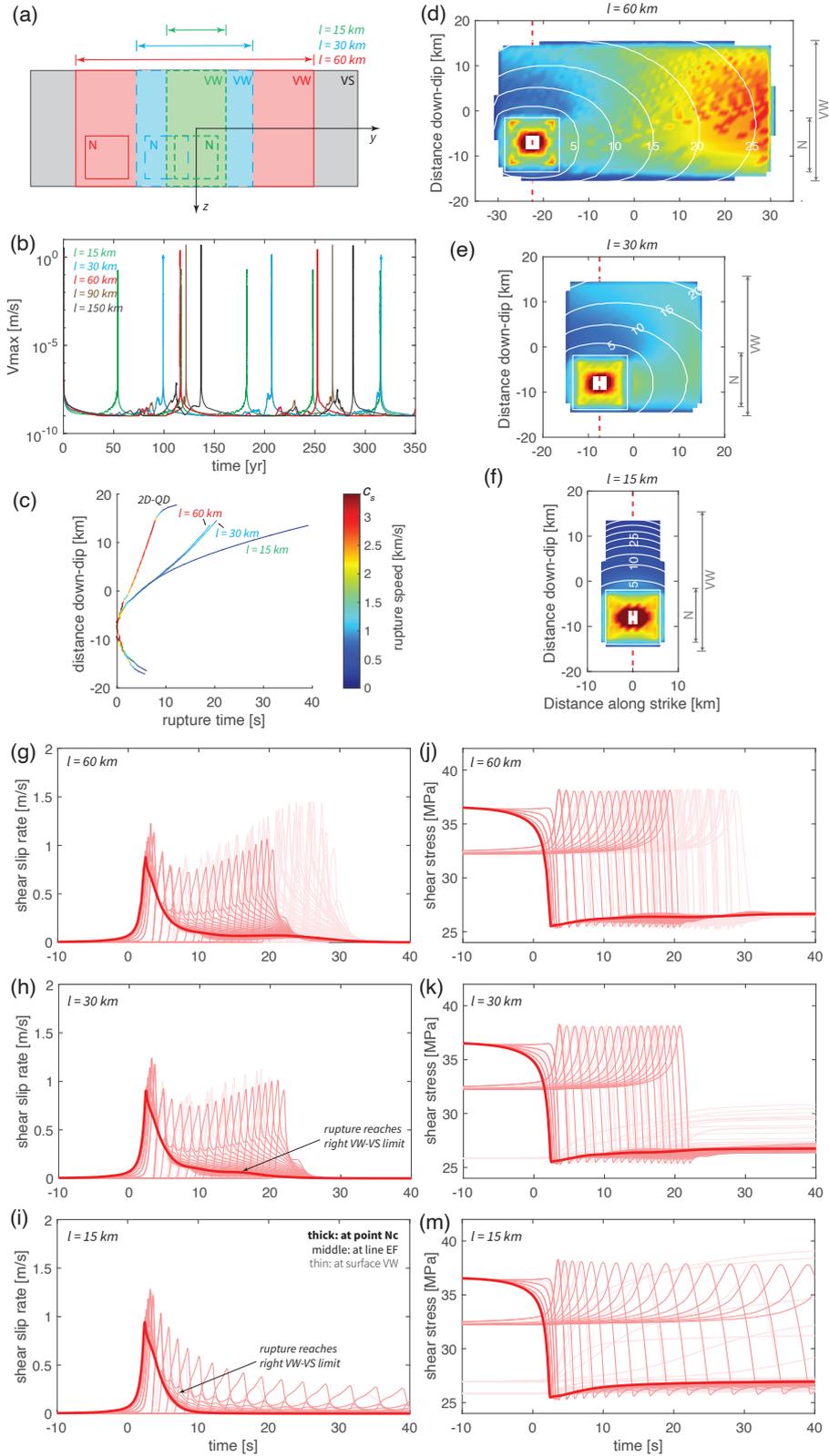


Figure 9. (Caption next page.)

**Figure 9.** (Previous page.) Comparison of the effects of fault length  $l$  (15 - 150 km) in 3D models: (d, g, j) 60 km, (e, h, k) 30 km, and (f, i, m) 15 km. (a) The varied VW patch sizes and varied locations of the predefined nucleation zone in three testing models with  $l$  from 15 km to 60 km. (b) The maximum slip velocity in multiple earthquake cycles for models with  $l$  from 15 km to 150 km. (d-f) The arrival time of the coseismic rupture front of the first earthquake, which is measured when slip velocity reaching the seismic limit. Only the central part of the fault plane is shown, where white color means no seismic slip is observed. Contours are plotted every five seconds. The red dashed line labels the observation line “EF” introduced in Fig. 1. (c) The coseismic rupture front arrival time along the vertical line “EF” under the same color scale. Lines end at where no seismic slip is observed. The rupture time of the corresponding 2D model is plotted as reference. (g-i) The time series of slip velocity in the coseismic phase of the first seismic event, in which origin time is set at the onset of this event. The lines with different thicknesses and degrees of transparency are recorded at different locations on the fault, where the thick lines are recorded at point “Nc”, the semi-thick lines along the line “EF” and the thin lines elsewhere (see Fig. 1). (j-m) The time series of shear stress in the coseismic phase of the first seismic event, with the same line property.

733 is also supported by our theoretical considerations (see section 3.5) where we assumed  
 734 circular fault geometry in 3D and infinitely long fault in 2D. The elongated fault geom-  
 735 etry deviates from the 3D assumption but is closer to the 2D one. Therefore longer re-  
 736 currence intervals are to be expected. Consequently, by prolonging the VW patch length,  
 737 we achieve longer recurrence intervals to fit better what is observed in 2D. In other words,  
 738 higher aspect ratio faults in 3D are better represented by 2D models in the long term.  
 739 However, even extending the 3D patch to 150 km still leads to shorter recurrence inter-  
 740 vals comparing to what is observed in 2D (Fig. 2), as interseismic loading remains more  
 741 effective from three lateral sides than two.

742 On the other hand, a longer VW patch requires longer rupture propagation time  
 743 along strike and thus longer coseismic duration, if the rupture speed remains unvaried  
 744 (Fig. 9d-e). As explain before, 2D models can be seen as 3D models where theoretically  
 745 no time is required to rupture along strike. In this sense, a longer VW patch length is  
 746 not preferred to fit the short coseismic duration observed in 2D. However, even the short-  
 747 est coseismic duration, observed with aspect ratio 1:1, is still about 50% longer than 2D

748 due to its low rupture speed. The rupture propagation time is not further shortened when  
 749 the fault becomes even shorter. On the contrary, rupture speed is even largely decreased  
 750 in the case with aspect ratio 0.5:1, resulting in a fairly long coseismic duration (Fig. 9c,  
 751 f). This speed change happens after the rupture front reaches the horizontal VW-VS tran-  
 752 sition, confirming again that horizontal VW-VS interaction can change vertical rupture  
 753 speed. Accompanying the rupture speed reduction, the slip velocity and the stress drop  
 754 are reduced at the same time (Fig. 9g-m). This is dissimilar to the observations in 2D  
 755 (Fig. 4a, c). From this aspect, a shorter VW patch length is not favored either. In other  
 756 words, medium aspect ratio (close to 1:1) fault is better represented by 2D models in the  
 757 coseismic phase. Additionally, if only what happens along the vertical line “EF” in 3D  
 758 is taken into consideration when compared to 2D, then all models with aspect ratio higher  
 759 than 1:1 can be accepted. This is because we notice that the rupture propagation along  
 760 the vertical line “EF” does not change much with respect to the fault length when the  
 761 aspect ratio is larger than 1:1 (Fig. 9c). Nor do the slip velocity and coseismic slip change  
 762 along this line (Fig. 9d-e, g-h, j-k).

763 To summarize, 2D models can better represent high aspect ratio faults in 3D for  
 764 long-term observations and medium-to-high aspect ratio faults for coseismic observations.  
 765 Whereas for coseismic observations there are definitely inevitable qualitative differences  
 766 in between. Our conclusion suggests that when using empirical scaling relations to in-  
 767 terpret 2D results to a 3D perspective, it is crucial to assume a suitable aspect ratio ac-  
 768 cording to the corresponding research objective. Wesnousky (2008) summarized 36 his-  
 769 torical natural earthquakes and found that they have similar rupture width but varied  
 770 rupture length, resulting in varied aspect ratio from 0.7 to 12. The analysis in this study,  
 771 covering the range 0.5 - 5, can therefore be useful to refer to when comparing or vali-  
 772 dating 2D simulations to 3D natural observations.

## 773 **4.2 Implications for 0/1D models**

774 Our results and theoretical calculations suggest that 1D models reflect some key  
 775 characteristics and thus can be used well to understand and quantify earthquake sequences  
 776 under specific circumstances, which we discuss here. These implications from 1D mod-  
 777 els also hold for 0D models due to their mathematical equivalence. Since physical tec-  
 778 tonic loading has to be removed in 0D models, an arbitrary “driving force” has to be added  
 779 to the system instead (section 2.3). To facilitate comparison, we can integrate the strain

780 rate along the  $x$  direction in 1D models and use it to drive the 0D system. This is how  
 781 the well-known “spring-slider” model is built (Burridge & Knopoff, 1967). Such a 0D  
 782 model is mathematically equivalent to the 1D model. This is because the static momen-  
 783 tum balance equation in 1D gives homogeneous shear stress in the medium. Combined  
 784 with the boundary conditions, the time derivative of stress is given by

$$785 \quad \dot{\sigma}_{xy} = G \frac{V_p - V}{X_0} . \quad (21)$$

786 Since this is an analytical derivation, the resulting model behavior is to remain the same.  
 787 In this case we recommend to replace 1D models with 0D models, because they are more  
 788 computationally efficient (Fig. 8). Nevertheless, the explanation above no longer holds  
 789 when the governing equation (10) does not establish, including when heterogeneity, in-  
 790 elasticity and/or inertia are considered. In these more complex cases 1D models prevail  
 791 in the ability of describing such physics (e.g., Pranger et al., 2021).

792 The domain size  $X_0$  in 1D and the arbitrary driving force  $\dot{f}_d$  in 0D can be flexi-  
 793 bly adapted to fit the earthquake cycle parameters. We have noted that setting the dis-  
 794 tance between the VW patch and the loading boundary  $X_0$  in 1D to be the same as in  
 795 higher dimensions  $(W_f - H)/2$  provides inadequate interseismic stress rate (section 3.1).  
 796 This is because tectonic loading is realized at the VW-VS transition and it is neither de-  
 797 pendent on  $W_f$  nor  $H$ . Relevant observations (section 3.3) and theoretical considerations  
 798 (section 3.5) confirm that the 0D fault point mimics the nucleation rim in higher dimen-  
 799 sional models that is located at a distance  $h^*$  from the VW-VS transition. By using the  
 800 calculated stress rate (16) in 2D and 3D as the 0D “driving force”  $\dot{f}_d$  in (11), recurrence  
 801 intervals of about 133 yr and 250 yr are obtained. These are about 1.5% and 16% dif-  
 802 ferent from the real 3D and 2D simulations, respectively. This minor difference suggests  
 803 that 0/1D models can be used to estimate both interseismic (e.g., earthquake recurrence  
 804 interval) and coseismic (e.g., maximum coseismic slip) characteristics.

805 The commonly observed periodic slow slip events cannot be reproduced in 1D mod-  
 806 els with classical rate-and-state friction, as suggested by our explanation to the coseis-  
 807 mic rupture characteristics (section 3.2). In 1D the nucleation zone suddenly becomes in-  
 808 finitely large as soon as the 0D fault point starts to nucleate. This instability unavoid-  
 809 ably leads to an earthquake (i.e., slip at seismic rate) instead of slow slip events. This  
 810 inference is supported by a parameter study of hundreds of models in which no suitable  
 811 frictional parameters could be found (Diab-Montero et al., 2021). Slow-slip events are

812 only observed (slowly) decaying when the system stiffness is close to but smaller than  
 813 the critical stiffness. Using the consideration that 0D fault point represents an infinitely  
 814 large fully-VW 2D fault, the infinite ratio of VW patch size ( $H$ ) over nucleation size ( $h^*$ )  
 815 is known to lead to seismic slip rates (Liu & Rice, 2007; Herrendörfer et al., 2018). To  
 816 produce slow-slip events in 1D, additional damping needs to be present via, e.g., rate-  
 817 dependent rate-and-state parameters (Im et al., 2020), two-state variable rate-and-state  
 818 friction behavior and/or additional spatio-temporal complexities (Leeman et al., 2018).  
 819 Not only slow-slip events, any earthquake sequences including earthquakes that are not  
 820 periodic, characteristic are hardly possible to be produced in 0/1D models, although they  
 821 are to be expected most of the time in nature. The feature of the infinite VW fault di-  
 822 mension in 0/1D should be the first criterion to decide whether one should run a sim-  
 823 ulation in higher dimensions or not.

### 824 **4.3 Implications for other model setups**

825 Our model was designed according to the SEAS benchmark BP4-qd (Erickson et  
 826 al., 2020) to maximize comparability, interpretability and reproducibility with a com-  
 827 mon setup featuring a simple recurrence pattern of a single earthquake rupturing the en-  
 828 tire seismogenic zone instead of smaller ones with complex temporal patterns (Cattania,  
 829 2019; Barbot, 2019; Chen & Lapusta, 2019). Here we discuss several model setup ad-  
 830 justments, which largely shows that the conclusions drawn from our simulations can be  
 831 generalized to a broader context.

832 We have investigated the similarities and differences in models of different dimen-  
 833 sions using a fully dynamic (FD) approach to extend the applicability of our statements.  
 834 Our conclusions still largely hold with minor quantitative variations. However, we also  
 835 found qualitative differences in coseismic characteristics that demand a deeper discus-  
 836 sion via the comparison between QD vs. FD models, which we for clarity referred to a  
 837 follow-up paper (Li et al., 2021).

838 Tectonic loading is typically applied in two different ways: directly on the fault plane  
 839 (e.g., Kaneko et al., 2011) or indirectly at the far-away boundaries (e.g., Herrendörfer  
 840 et al., 2018). Both types have been adopted by studies for different research purpose.  
 841 We adopted tectonic loading at the top/bottom of the fault plane for 2D and 3D mod-  
 842 els following BP4-qd, but at the far-away boundary for 1D models due to dimensional

843 restriction. To test the influence in the interseismic phase we applied tectonic loading  
844 conditions (a) only on fault surface at top/bottom region with fixed fault width, (b) only  
845 on far-away boundary surface, (c) both (a) and (b). We modeled in 2D with gradually  
846 enlarged computational domain (Table S1). We find that the recurrence interval con-  
847 verges to a set value as the computational domain is enlarged and is hardly affected by  
848 the type of loading when the computational domain is large enough. This invariance with  
849 respect to loading condition is supported by our theoretical calculations (section 3.5).  
850 Because there we explained that the main loading force to the locked VW patch is from  
851 its surrounding creeping VS patches. No matter which type of loading is applied, the stress  
852 rate inside the VW patch is largely defined by its own dimension and independent of the  
853 size of the VS patches or the fault as a whole (Eq. 16). Naturally the velocity gradient  
854 perpendicular to the fault contributes to the loading process as well, but it is minimized  
855 for large enough computational domain where on-fault loading becomes dominant. Dur-  
856 ing the coseismic period, the way in which tectonic loading is applied does not influence  
857 results because of the short duration. Therefore both the interseismic and coseismic char-  
858 acteristics are not sensitive to what kind of loading boundary condition is applied. Com-  
859 parison in the SEAS benchmark BP4-qd of different modeling groups demonstrated the  
860 same idea: numerical results generally agreed with each other when computational do-  
861 main was large enough, where for the numerical method's convenience, either stress-free  
862 or constant-moving boundary condition is chosen at far-away boundaries (Jiang et al.,  
863 2021).

864 As for the initial condition, we have adopted a predefined highly-stressed zone within  
865 the VW patch following BP4-qd. Since the later earthquakes do not necessarily occur  
866 from the same location, this predefined zone facilitated the quantitative coseismic com-  
867 parison across dimensions by forcing the first earthquake to nucleate from this same re-  
868 gion. It is suggested by some former studies that initial conditions have little effect on  
869 subsequent earthquakes (e.g., Takeuchi & Fialko, 2012; Allison & Dunham, 2018), there-  
870 fore this special initial condition should not harm our findings in terms of earthquake  
871 cycle characteristics as well as nucleation behavior. In this study we did notice that the  
872 accumulative slip contour distortions around a depth of -1.5 km and -13.5 km are intro-  
873 duced by the predefined nucleation zone, whose properties increased the amount of slip  
874 in that zone for the first earthquake (Fig. 3). However, for non-accumulative variables  
875 no influence from the initial condition is observed in later earthquakes. Nevertheless, the

876 first earthquake is not completely characteristic in an earthquake cycle even though some  
 877 qualitative characteristics are still shared by later earthquakes. This also becomes ap-  
 878 parent in the comparison to the sixth earthquake.

## 879 **5 Conclusions**

880 In this paper, we addressed a common concern of numerical modelers: how com-  
 881 plex should my model be to answer my research question? Will dimension reduction qual-  
 882 itatively and quantitatively affect my results? And how? For this purpose we have sys-  
 883 tematically investigated different dimensional models from 0D to 3D in terms of their  
 884 interseismic and coseismic characteristics and computational time for earthquake sequences  
 885 and individual quasi-dynamic ruptures.

886 Our results demonstrate that, when 2D or 3D models produce quasi-periodic char-  
 887 acteristic earthquakes, their behavior is qualitatively similar to lower-dimension mod-  
 888 els. The stress accumulation pattern is much the same when observed at the rim of the  
 889 nucleation zone. As for the earthquake cycle parameters, lower dimensional models pro-  
 890 duce longer recurrence intervals and hence larger coseismic slip. This trend is supported  
 891 by our theoretical calculations where the effect of dimension reduction is well quantified.  
 892 We observe that the VS patches play a crucial role in causing differences in the inter-  
 893 seismic phase, because tectonic loading is effectively realized at the VW-VS transition  
 894 by the velocity contrast between the creeping VS patches and the locked VW patch. As  
 895 VS patches are removed when fault dimension is reduced, their absence reduces the in-  
 896 terseismic stress rate inside the VW patch and thus increases the recurrence interval. The  
 897 larger slip deficit built in this period leads to a larger coseismic slip.

898 In the coseismic phase, we find that certain earthquake parameters such as the stress  
 899 drop and fracture energy can be accurately reproduced in each of these simpler models,  
 900 because they are mainly governed by material frictional parameters. This finding is es-  
 901 pecially valid for the first earthquake without physical tectonic loading. For later earth-  
 902 quakes, the statement is only true on average of the VW patch. This is because the ini-  
 903 tial stress, yield stress and effective slip weakening distance can change due to tectonic  
 904 loading and earthquake history. For the coseismic rupture parameters, lower dimensional  
 905 models generally produce higher maximum slip velocities and higher rupture speeds in  
 906 lower dimensional models. Furthermore, we demonstrate that the interaction at the VW-

907 VS transition can modify rupture speed, which is another crucial role the VS patches  
908 play in the coseismic phase. We find that the vertical rupture speed along the vertical  
909 direction in 3D is slower compared to 2D. It can be further slowed down when the fault  
910 length is shortened even more, suggesting that the vertical rupture behavior is influenced  
911 by horizontal frictional properties.

912 The aforementioned findings are supported by our theoretical calculations, which  
913 confirm that geometric differences due to dimension reduction influence the interseismic  
914 loading and finally affect the subsequent coseismic phase. Through accounting for an equiv-  
915 alent stressing rate at the nucleation size  $h^*$  into 2D and 3D models, 0/1D models can  
916 also effectively estimate earthquake cycle parameters such as recurrence interval and to-  
917 tal slip. These theoretical considerations can be generally applied to other earthquake  
918 cycle models as well.

919 Finally, we highlight the power of lower dimensional models in terms of their com-  
920 putational efficiency. We find that under the same (relatively low) resolution 3D mod-  
921 els require  $10^3$  times longer computational time than 2D,  $10^5$  times longer than 1D and  
922  $10^6$  times longer than 0D models. Therefore dimension reduction can not only relieve  
923 the heavy energy-consuming simulations, but also improve the efficiency of projects that  
924 require monotonous repetitions of forward models. This paper may serve as guidelines  
925 to check in simplified models what results can be expected to be accurately modeled as  
926 well as what physical aspects are missing and how they are related to the discrepancies  
927 observed in the results.

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 945 spective folders under [https://bitbucket.org/cpranger/garnet/src/meng-eejit/](https://bitbucket.org/cpranger/garnet/src/meng-eejit/experiments/comparison/)  
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