

1 A time-dependent two-dimensional model simulation of lower  
2 ionospheric variations under intense SAID

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15 **Abstract.** The subauroral ion drift (SAID) denotes a latitudinally narrow channel of fast  
16 westward ion drift in the subauroral region, often observed during geomagnetically disturbed  
17 intervals. The recently recognized subauroral optical phenomena, the Strong Thermal Emission  
18 Velocity Enhancement (STEVE) and the Picket Fence, are both related to intense SAIDs. In this  
19 study, we present a 2D time-dependent model simulation of the self-consistent variations of the  
20 electron/ion temperature, density, and FAC, under strong SAID, with more focus in the lower  
21 ionosphere. Our simulation reproduces many key features of SAID, such as the anomalous  
22 electron heating in the E-region, the strong electron temperature enhancement in the upper F-  
23 region, the intense ion frictional heating, and the plasma density depletion. Most importantly, the  
24 ion Pedersen drifts is found to play a crucial role in the density variations and FAC dynamics in  
25 the lower ionosphere. The transport effect of ion Pedersen drifts leads to strong density depletion  
26 in the lower ionosphere in a large portion of SAID. The FAC inside SAID is mainly downward  
27 with magnitude  $\leq \sim 1 \mu\text{A}/\text{m}^2$ . At the poleward edge of SAID, the ion Pedersen drift leads to a  
28 pileup of the plasma density and an upward FAC. Our simulation results also corroborate the  
29 presence of strong gradients of plasma density, temperature, and flows, at the edge of SAID,  
30 which may be conducive to certain plasma instabilities. Our model provides a useful tool for the  
31 future exploration of the generation mechanisms of STEVE and Picket Fence.

## 32 **1. Introduction**

33 During geomagnetically disturbed intervals, a latitudinally narrow yet longitudinally  
34 elongated zone of fast westward ion drift (or equivalently strong poleward electric field) often  
35 appears in the evening to midnight sector equatorward of the auroral oval. Galperin et al. [1973]  
36 first reported such phenomena and called them polarization jets. They were subsequently termed  
37 as “subauroral ion drift” (SAID) by Spiro et al. [1979]. References to early observations and to  
38 subsequent clarifications of the properties and signatures of SAID can be found in Anderson et al.  
39 [1993]. Later, Foster and Burke [2002] suggested an inclusive name, subauroral polarization  
40 streams (SAPS), to encompass both the narrow and intense SAIDs and the broader regions of  
41 relatively weaker westward subauroral plasma drifts [e.g., Yeh et al., 1991] However, it is now  
42 generally recognized that SAID and SAPS (without SAID) differ in a number of fundamental  
43 aspects [Mishin et al., 2017; Nishimura et al., 2020]. SAIDs have been studied in both ground  
44 and space-based observations, such as in electric field measurements [e.g. Puhl-Quinn, et al.,  
45 2007], radar measurements [e.g., Foster et al., 1994], and ion drift measurements [Anderson et al.,  
46 1993, 2001; Archer et al., 2018; 2019a; Nishimura et al., 2019; 2020]. Elevated electron/ion  
47 temperatures and depleted electron densities are typically observed within SAID [Moffett et al.  
48 1998; Andersen et al., 1993; 2001; Archer et al., 2018; 2019a; Nishimura et al., 2020]. Motivated  
49 by the observations, numerous model simulations of the ionosphere have been performed to  
50 study the ionospheric processes related to the observed signatures of SAID, for example, the  
51 plasma density depletion and electron temperature enhancement in the upper F-region [e.g.,  
52 Moffett et al., 1992; 1998], and the strong ion upflows in the topside ionosphere [e.g., Heelis et  
53 al., 1993].

54 In recent years, the recognition and observations of the Strong Thermal Emission Velocity  
55 Enhancement (STEVE) and the Picket Fence optical phenomena have further lifted the research  
56 interest in SAID. The generation mechanisms for the STEVE and Picket Fence remain unclear to  
57 date. This stated, it is now well established that STEVE's are collocated with intense SAID  
58 channels [Archer et al., 2019a; Nishimura et al., 2019; 2020; Chu et al., 2019], while Picket  
59 Fences are situated in close vicinity, likely near the poleward edge, of STEVE [Gillies et al.,  
60 2020; Semeter et al., 2020]. The consensus has now emerged that intense SAIDs have to play a  
61 pivotal role in the generation of STEVE and Picket Fence optical emissions [Harding et al., 2020;  
62 Nishimura et al., 2020; Semeter et al., 2020; Liang et al. 2021]. Important unresolved issues are:  
63 (1) a major component of STEVE emissions is not from known atomic or molecular auroral  
64 optical emissions but is instead made of a notably very wide broadband emission [e.g., Gillies et  
65 al, 2019; Liang et al., 2019]; (2) the green line in the Picket Fence emissions is not accompanied  
66 by  $N_2^+$  emissions implying that the emissions may not be generated by an auroral type of  
67 electron precipitation [e.g. Mende et al., 2019]. Existing studies on their emission altitudes have  
68 unveiled that, the Picket Fence and the lower-altitude part of the STEVE occur in the lower  
69 ionosphere (<200 km) [Archer et al., 2019b; Liang et al., 2019; Semeter et al., 2020] and  
70 possibly own their production mechanisms to chemical/physical processes in the lower  
71 ionosphere [Liang et al., 2019; Hedin et al. 2020; Semeter et al., 2020]. However, despite  
72 decades of observations and model simulations of SAID, existing SAID-related studies have  
73 been mostly focused on the upper F-region/topside ionosphere, yet the variations/structures in  
74 the E-region and lower F-region led by SAID is largely unreported. The lack of definite  
75 knowledge about the lower ionospheric variations under intense SAID hampers the exploration  
76 of the underlying mechanism of STEVE and Picket Fence.

77       The present study is motivated by the need to establish the state of the ionosphere in STEVE  
78 and Picket Fences situations. A model specially tailored to SAID conditions is built for such a  
79 research purpose. We shall investigate the plasma densities, temperatures, conductivities, and  
80 electrodynamics in the lower ionosphere under the effect of an intense SAID channel. The  
81 plasma densities in the region of interest need to be assessed in the presence of attendant  
82 Pedersen currents known to carry plasma across the SAID channels [Banks and Yasuhara, 1978],  
83 and in the presence of elevated electron/ion temperatures, including electron temperature  
84 enhancements from plasma wave heating in the E region (e.g. St-Maurice and Goodwin [2021],  
85 and references therein). The ionospheric variations and structures across the SAID channel  
86 achieved from this study would aid in the ongoing exploration of the underlying mechanisms of  
87 STEVEs and Picket Fences.

88       Existing ionospheric models can be broadly categorized into three classes. The first class is a  
89 1D model, e.g., the FLIP model [Richards, 2001], the GLOW model [Solomon et al., 1988], and  
90 the now-termed TReX-ATM model [Liang et al., 2016; 2017]. They typically solve the plasma  
91 parameters and/or the auroral emission rates along a magnetic field line. The second class is a  
92 global 3D model, such as TIEGCM [Richmond et al., 1992], SAMI [Huba et al., 2000], and  
93 GITM [Ridley et al., 2002], which typically simulates the evolution and structures of the global  
94 or regional ionosphere (and thermosphere) under externally driving forces. However, the  
95 time/latitude resolution of those global models is not optimal for our specific research objective,  
96 namely the lower ionospheric variations in a narrow SAID channel. The third class of models is  
97 often 2D, and typically deals with certain specific small- or meso-scale structures, e.g., a  
98 precipitation-enhanced region with sharp boundaries [Noel et al., 2000; 2005; deBoer et al.,  
99 2010], the auroral downward current region [Zettergren and Semeter, 2012], and the ionospheric

100 Alfvén resonator [Sydorenko et al., 2013]. A noteworthy effort was done by deBoer et al. [2010],  
101 who also incorporated the ion Pedersen drift in their model and highlighted the role of ion  
102 Pedersen transport under a tilted field geometry in the lower ionospheric dynamics, though their  
103 research interest is focused on the discrete auroral arc with uniform ambient electric field yet  
104 sharp precipitation boundary. The model we develop and present in this paper belongs to the  
105 third class, and is specifically tailored to intense SAID conditions, with weak precipitation yet  
106 strong and narrow electric field structures. Most of the key physical processes that are  
107 understood or expected to play a role in SAID, such as the ion Pedersen transport, the anomalous  
108 electron heating, the ion upflows, and the enhanced vibrational excitation of  $N_2$ , are all  
109 incorporated into one synthesized model. The current paper is intended to serve as the first of a  
110 series of upcoming studies, based upon the developed model, to investigate more subtleties and  
111 anomalies of the ionospheric electrodynamics that could potentially contribute to the STEVE and  
112 Picket Fence production under a variety of SAID and ambient ionospheric conditions.

113 The rest of this paper is organized as follows. In section 2 we describe the basic equations  
114 and numerical schemes of our model. In section 3, we depict the ambient ionospheric condition  
115 surrounding STEVE that we shall use to set up our model runs. The simulation results are  
116 presented in Section 4. We discuss a few important implications of our results in the context of  
117 the Picket Fence phenomenon in Section 5 before reaching our conclusions in Section 6.

118

## 119 **2. Model description**

120 The model to be described and used in this study inherited from the Transition Region  
121 Explorer Auroral Transport Model (TReX-ATM), which we had developed for years [Liang et  
122 al., 2016; 2017]. For the specific research purpose of this study, we have made a few key

123 improvements to our previous model: (a) We extend the model to 2D (MLAT/altitude) geometry.  
124 (b) We include the electron anomalous heating and the ion Pedersen drift, two pronounced  
125 effects of intense SAID in the lower ionosphere, and the FAC is self-consistently computed from  
126 the divergence of ion Pedersen currents. (c) In terms of chemical processes, while keeping all ion  
127 species and excited neutrals in our previous model, we also consider the change of atomic  
128 nitrogen, the nitric oxide, and the vibrational excitation of molecular nitrogen in the model. We  
129 emphasize again that the main research interest of this study is in the lower ionosphere (<200 km  
130 altitude), which enables us to make a few key assumptions/simplifications of our model. We first  
131 introduce the geometry and those key assumptions/simplifications of our model as follows.

132 1. The SAID plasma convects in the azimuthal ( $y$ ) direction that is deemed aligned with  
133 magnetic L-shell. We assume an azimuthal homogeneity (i.e.,  $\partial/\partial y = 0$ ) throughout this study.  
134 Anderson et al. [2001] suggested that SAID may exist simultaneously over at least  $\sim 3$  h MLT.  
135 Optical observations of STEVE also indicated that it might span over  $\sim 2.5$  h MLT sectors  
136 [Gallardo-Lacourt et al., 2018b; Nishimura et al., 2020]. Therefore, the timescale of plasma  
137 flowing through the SAID is longer than the other timescales of interest, e.g., that of the ion and  
138 electron heating, and the density and FAC variation timescale related to the ion Pedersen drift, in  
139 the lower ionosphere. That said, the finite azimuthal width of SAID has some effects in the upper  
140 ionosphere where the variations tend to be more gradual, and may affect the interpretation of  
141 some of our results in the upper F-region, as we shall elucidate later in Section 4.

142 2. While the electron/ion temperature and density are self-consistently calculated, the major  
143 constituents of neutrals (such as  $N_2/O_2/O$ ), as well as the neutral temperature, are kept unchanged  
144 in our model. There is little doubt that ionosphere-thermosphere (IT) interaction is operative

145 under SAID, and there is evidence of such IT interaction based upon neutral observations in  
 146 conjunction with STEVE [Liang et al., 2021]. However, the coupling to the thermosphere and  
 147 the resultant change of major neutral constituents would presumably be less important in the  
 148 lower ionosphere at subauroral latitudes, where the plasma concentration is usually far lower  
 149 than neutrals. We do include the density variations of some minor neutral species, such as N, NO,  
 150 and the vibrationally excited N<sub>2</sub> in the model. We assume all neutrals to be stagnant, i.e., we  
 151 neglect neutral winds.

## 152 2.1 Basic equations

153 In a nutshell, our model consists of the electron and ion energy equations, the continuity  
 154 equations of ions/electrons as well as some minor and excited neutrals, and the current continuity  
 155 equation. When the effect of viscous heating is ignored, the electron energy equation is given by  
 156 [e.g., Rees and Roble, 1975; Schunk and Nagy, 2009],

$$157 \quad \frac{3}{2}k \frac{D}{Dt} (N_e T_e) = -\frac{5}{2}N_e k T_e \nabla \cdot \mathbf{u}_e - \nabla \cdot \mathbf{q}_e + Q_e - L_e \quad , \quad (1)$$

158 where

$$159 \quad \frac{D}{Dt} = \frac{\partial}{\partial t} + \mathbf{u}_e \cdot \nabla \quad ,$$

160 in which  $\mathbf{u}_e$  is the electron bulk drift velocity,  $k$  is the Boltzmann constant,  $\mathbf{q}_e$  is the electron heat  
 161 flow vector.  $Q_e$  is the electron heating rate which, in the context of SAID, consist of three parts:  
 162 the classical friction heating in both perpendicular directions and parallel directions, the  
 163 anomalous heating (to be specifically addressed in section 2.2), and the heating due to collisions  
 164 with secondary electrons produced by the primary auroral precipitation.  $L_e$  denotes the electron  
 165 cooling rate. For detailed breakdown and formulas of all heating/cooling rates and heat flow, see  
 166 supplementary material. The electron drift  $\mathbf{u}_e$  contains two components: one perpendicular to the

167 ambient magnetic field  $\mathbf{u}_{e\perp}$  and the other parallel to the magnetic field  $\mathbf{u}_{e\parallel}$ . For ionospheric  
 168 electrons the perpendicular component is essentially  $\mathbf{E}\times\mathbf{B}$  convective drift which is virtually  
 169 incompressible in the ionosphere, so that  $\nabla\cdot\mathbf{u}_{e\perp}\approx 0$ . The electron Pedersen drift starts to matter  
 170 at below  $\sim 100$  km, which is in practice close to the bottom boundary of our model. The explicit  
 171 expression of  $\mathbf{u}_{e\parallel}$  is to be given in equation (10) later in this section. Using the continuity  
 172 equation,

$$173 \quad \frac{\partial N_e}{\partial t} + \nabla\cdot(N_e\mathbf{u}_e) = P_{ne} - L_{ne} \quad , \quad (2)$$

174 in which  $P_{ne}$  and  $L_{ne}$  denote the production and loss of electrons due to precipitations and  
 175 chemical reactions, equation (1) can be converted to,

$$176 \quad \frac{3}{2}N_ek\frac{\partial T_e}{\partial t} = -\frac{3}{2}kT_e(P_{ne} - L_{ne}) - \frac{3}{2}N_ek\mathbf{u}_{e\parallel}\cdot\nabla_{\parallel}T_e - N_ekT_e\nabla_{\parallel}\mathbf{u}_{e\parallel} - \nabla_{\parallel}q_{e\parallel} + Q_e - L_e . \quad (3)$$

177 Note that in our geometry the electron  $\mathbf{E}\times\mathbf{B}$  drift is along the  $y$ -direction, and  $\partial/\partial y = 0$  is  
 178 assumed in our 2D model, so that the perpendicular advective term vanishes for electrons. Also,  
 179 we have neglected the perpendicular heat flow component which is usually much smaller than  
 180 the parallel heat flow for ionospheric electrons [Schunk and Nagy, 2009].

181 The ion energy equation can be derived similarly,

$$182 \quad \frac{3}{2}N_ik\frac{\partial T_i}{\partial t} = -\frac{3}{2}kT_i(P_{ni} - L_{ni}) - \frac{3}{2}N_ik\mathbf{u}_i\cdot\nabla T_i - N_ikT_i\nabla\cdot\mathbf{u}_i + Q_{ji} - L_{ie} - L_{in} \quad , \quad (4)$$

183 in which  $Q_{ji}$  represents the ion heating rate due to the friction Joule heating.  $L_{ie}$  and  $L_{in}$  represents  
 184 the cooling rate due to collisions with electrons and neutrals, respectively. Note that in deriving  
 185 (4) we have also implicitly utilized the ion continuity equation,

$$186 \quad \frac{\partial N_i}{\partial t} + \nabla\cdot(N_i\mathbf{u}_i) = P_{ni} - L_{ni} . \quad (5)$$

187 The ion drift velocity  $\mathbf{u}_i$  in equation (4) and (5) is given by

188 
$$\mathbf{u}_i = \frac{\kappa_i^2}{1+\kappa_i^2} \frac{\mathbf{E} \times \mathbf{B}}{B^2} + \frac{\kappa_i}{1+\kappa_i^2} \frac{\mathbf{E}}{B} + \mathbf{u}_{i//} \quad , \quad (6)$$

189 in which  $\kappa_i$  is the ratio between the ion gyrofrequency and the ion-neutral collision frequency.

190 The ion parallel drift  $u_{i//}$  is to be given in equation (9) later. Note that equation (6) represents a

191 steady-state solution of the ion momentum equation. The underlying rationale of such a treatment

192 is that, at the ionospheric altitudes of interest the steady-state ion drift is established at an ion-

193 neutral collisional timescale, much faster than other transport or chemical timescales of interest

194 in our model. Furthermore, the pressure-gradient drifts and diamagnetic drifts are ignored. We

195 infer from our simulation result that, even in the presence of strong heating within SAID, the

196 pressure-gradient associated perpendicular drift is still found to be 3 orders of magnitude smaller

197 than the electric drift, so that the former is ignored. The first two terms on the left-side of

198 equation (6) are conventionally called “Hall drift” and “Pedersen drift”, respectively. As in the

199 case for electrons, the Hall drift does not play a role in the equation under the azimuthally

200 homogeneous geometry. The ion Pedersen drift however, can be very important to the plasma

201 dynamics in the lower ionosphere. As can be inferred from equation (6), the maximum ion

202 Pedersen drift can be up to half the SAID flow velocity. For our research interest of the STEVE-

203 related SAID, whose width is typically no more than a few tens of km, ions traverse the SAID

204 channel in tens of seconds under the enhanced Pedersen drift. This can be faster than the

205 recombination rate of ions in the subauroral ionosphere. Thus, the transport effect led by the

206 SAID-enhanced ion Pedersen drift may act as the principal process controlling the density

207 variations in the lower ionosphere, as first suggested by Banks and Yasuhara [1978]. The

208 Pedersen drift is dependent upon ion species. In our model, we consider the Pedersen drift of  
209 three major ions in the ionosphere,  $\text{NO}^+$ ,  $\text{O}_2^+$ , and  $\text{O}^+$ .

210 It should be noted that we actually model the so-called “average” ion temperature in equation  
211 (4). (a) The temperature is averaged over all ion species. In practical calculation, all heating and  
212 cooling sources in equation (5) are summed over ion species, and  $\mathbf{u}_i$  in equation (6) represents  
213 the density-averaged bulk drift velocity of  $\text{NO}^+$ ,  $\text{O}_2^+$ , and  $\text{O}^+$ . (b) The temperature is averaged  
214 over the parallel and perpendicular directions. For more explanations of the implication of such  
215 an average ion temperature under frictional heating and its partitioning into parallel and  
216 perpendicular directions, see St-Maurice et al. [1999] and Goodwin et al. [2018]. Such an  
217 average ion temperature suffices for most of our research purpose (e.g., calculating reaction  
218 rates). However, we shall consider the temperature anisotropy and rectify the  $\text{O}^+ T_{i\parallel}$  when we  
219 calculate the ambipolar diffusion velocity (see details later in this section).

220 We have neglected the ion heat flow conduction in the ion energy equation. The ion heat  
221 flow is generally believed to be likely much smaller than the electron heat flow [e.g., Rees and  
222 Roble, 1975], though to the authors’ knowledge a definite value of the ion heat flux has not yet  
223 been reliably evaluated experimentally in the existing literature. It was also ignored in some  
224 existing ionospheric models such as TIEGCM [Wang et al., 1999]. As we shall elucidate in the  
225 upcoming simulation results, under intense SAID the frictional heating is extremely strong over a  
226 broad range of altitudes, and the response time of the ion temperature to the frictional heating is  
227 very fast in the lower ionosphere. In fact,  $T_i$  is basically determined by a local equilibrium  
228 between the frictional heating and the collisional cooling with neutrals over the ionospheric  
229 altitudes of interest. We have numerically tested and found that the inclusion of ion heat  
230 conduction (as in our previous model Liang et al. [2017]) introduces trivial only changes to the  $T_i$

231 profile in the lower ionosphere, but incurs heavy computational time costs. Therefore, based  
 232 upon the above theoretical and practical considerations we ignore the heat conduction in the ion  
 233 energy equation for the specific purpose of this study.

234 The parallel electron and ion drifts in equations (3) and (6) are derived from the steady-state  
 235 solution (and neglecting advective terms) of the ion and electron momentum equations.

$$236 \quad -N_i m_i v_{in} u_{i//} - N_i m_i v_{ie} (u_{i//} - u_{e//}) - \nabla_{//} p_{i//} - N_i m_i g + N_i e E_{//} = 0 \quad (7)$$

$$237 \quad -N_e m_e v_{en} u_{e//} - N_e m_e \sum v_{ei} (u_{e//} - u_{i//}) - \nabla_{//} p_{e//} - N_e m_e g - N_e e E_{//} = 0 \quad (8)$$

238 Neglecting terms of the order of  $m_e/m_i$ , together with  $j_{//} = n_e e (\sum u_{i//} - u_{e//})$  these parallel  
 239 drifts are solved as,

$$240 \quad u_{i//} = -\frac{g_{//}}{v_i} - \frac{\nabla p_{i//}}{N_i m_i v_i} - \frac{\nabla p_{e//}}{N_e m_i v_i} \quad (9)$$

$$241 \quad u_{e//} = -\frac{j_{//}}{N_e e} + \frac{\sum N_i u_{i//}}{N_e} \quad (10)$$

242 in which  $g_{//}$  denotes the field-aligned component of the gravitational acceleration.  $p_{i//}$  and  $p_{e//}$   
 243 denote the parallel ion and electron pressure, respectively. The sum in (8) and (10) is over ion  
 244 species.  $O^+$  is often the dominant ion species in the upper/topside ionosphere where the  
 245 ambipolar diffusion becomes important, so that in some existing models (such as TIEGCM),  
 246 only the ambipolar diffusion of  $O^+$  is considered. However, for our specific research interest,  
 247  $NO^+$  is found to replace  $O^+$  to become the major constituent in the upper F-region under intense  
 248 SAID. Therefore, we shall consider two ion species,  $NO^+$  and  $O^+$ , for the ambipolar diffusion in  
 249 our model. For these two ions, their parallel flux  $n_i u_{i//}$  is rewritten in the following form,

$$\begin{aligned} (N_i u_{i//})^{O^+} &= -g_{i//} \left( \frac{N_i}{v_{in}} \right)^{O^+} - k \cdot \frac{(\nabla T_{i//})^{O^+} + \nabla T_{e//}}{(m_i v_{in})^{O^+}} (N_i)^{O^+} - k \cdot \frac{(T_{i//})^{O^+} + T_{e//}}{(m_i v_{in})^{O^+}} \cdot \nabla (N_i)^{O^+} \\ &\quad - \frac{k T_{e//}}{N_e (m_i v_{in})^{O^+}} \cdot [(N_i)^{O^+} \cdot \nabla (N_i)^{NO^+} - (N_i)^{NO^+} \cdot \nabla (N_i)^{O^+}] \end{aligned}$$

$$\begin{aligned}
(N_i u_{i//})^{NO+} = & -g_{i//} \left( \frac{N_i}{v_{in}} \right)^{NO+} - k \cdot \frac{(\nabla T_{i//})^{NO+} + \nabla T_{e//}}{(m_i v_{in})^{NO+}} (N_i)^{NO+} - k \cdot \frac{(T_{i//})^{NO+} + T_{e//}}{(m_i v_{in})^{NO+}} \cdot \nabla (N_i)^{NO+} \\
& - \frac{k T_{e//}}{N_e (m_i v_{in})^{NO+}} \cdot [(N_i)^{NO+} \cdot \nabla (N_i)^{O+} - (N_i)^{O+} \cdot \nabla (N_i)^{NO+}]
\end{aligned} \tag{11}$$

250

251

The superscript in (11) denotes the ion species. We have used the approximation  $n_e \approx$

252

$(n_i)^{NO+} + (n_i)^{O+}$  in the derivation. The calculation of the ambipolar diffusion velocity involves

253

the parallel electron/ion pressure. The electron pressure is assumed to be isotropic in our model.

254

It is however known that ions, especially  $O^+$ , can become notably anisotropic in the presence of

255

strong frictional heating [St-Maurice et al., 1999; Goodwin et al., 2018]. More quantitatively, Via

256

Monte Carlo simulations Goodwin et al. [2018] showed that, when the ion-ion and ion-electron

257

collisions are considered, the  $O^+$  ion temperature is essentially isotropic for ion drift  $u_{i\perp} < 800$  m/s,

258

but the parallel temperature is about half of the average temperature at  $u_{i\perp} \sim 4$  km/s. In this regard,

259

we use the following empirical formula fitted from the ratio between  $T_{i//}$  and the average  $T_i$

260

versus different ion drift velocity for  $O^+$  ions, in the study of Goodwin et al. [2018]:

$$T_{i//}^{O+} = \begin{cases} T_n + (T_i^{ave} - T_n) \cdot [1 - 3.507 \times 10^{-4}(u_{i\perp} - 800) + 6.076 \times 10^{-8}(u_{i\perp} - 800)^2] & u_{i\perp} > 800 \text{ m/s} \\ T_i^{ave} & u_{i\perp} < 800 \text{ m/s} \end{cases}$$

261

in which  $T_i^{ave}$  represents the average ion temperature solved from equation (4), and  $T_n$  is the

262

neutral temperature. For the  $NO^+$  ions, its parallel temperature is much closer to the average

263

temperature. More specifically, even at  $u_{i\perp} \sim 4$  km/s, contingent on the background neutral

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concentration the  $NO^+$  parallel temperature is found to be  $\sim 80\%$ - $86\%$  of the average temperature

265

[Goodwin et al., 2018]. Therefore,  $NO^+$  ion temperature is deemed isotropic in our model.

266

The FAC is computed according to the current continuity equation,

267

$$\nabla_{//} \cdot j_{//} + \nabla_{\perp} \cdot (\sum N_i e \mathbf{u}_{i\perp}) = 0 \tag{12}$$

268 The existence of FAC and the ambipolar diffusion naturally implies the presence of a parallel  
 269 electric field  $E_{//}$ , which can be derived from equation (8). Except for the Alfvénic process which  
 270 is not considered in our model, the electric field in the ionosphere is essentially electrostatic.

$$271 \quad \mathbf{E}_{//} = -\nabla_{//}\Phi = \frac{\mathbf{j}_{//}}{\sigma_{//}} - \frac{\nabla_{//}v_e}{N_e e} - \frac{m_e v_{en}}{N_e e} \sum N_i u_{i//} \quad , \quad (13)$$

$$272 \quad \mathbf{E}_{\perp} = -\nabla_{\perp}\Phi \quad (14)$$

273 in which  $\Phi$  is the electric potential,  $\sigma_{//} = N_e e / m_e (v_{en} + \sum v_{ei})$  is the parallel conductivity. The  
 274 electron gravity is ignored here. The last term in (13) is often dismissed in the existing literature  
 275 [e.g., Schunk and Nagy, 2009] under the assumption that the ion ambipolar drift is much slower  
 276 than the electron drift as the FAC carrier. This condition may become marginal in intense SAID  
 277 cases with very strong ion upflows yet moderate FAC intensity [e.g., Heelis et al., 1993;  
 278 Nishimura et al., 2020]. Such a term is included in our model simulation. The perpendicular  
 279 electric field would change with the perturbed electric potential. This modifies the ion Pedersen  
 280 drift and in turn the FAC. Such an interaction/feedback between the electric field and the FAC  
 281 was found to be capable of generating fine structures of electric fields (including  $E_{//}$ ) under some  
 282 circumstances [e.g., Noel et al., 2000; deBoer et al., 2010].

283 Our model also contains 7 excited/minor neutrals (see supplementary material). They all  
 284 follow the continuity equation in the same format as (2), but without the transport term since no  
 285 neutral wind is considered in our model. The calculation of the vibrationally excited populations  
 286 of  $N_2$  will be specifically addressed later in Section 2.3.

287 Equations (2) through (14) constitute the basic equation set of our model. Except for the  
 288 anomalous electron heating, which will be specifically discussed in the next subsection, all other  
 289 heating and cooling rates, as well as all chemical reactions involved in this study, are provided in

290 supplementary material. A special note is given here. Since our research objective features  
291 extremely high electron and ion temperatures, and that many reactions are temperature  
292 dependent, special care has been taken in checking the validity of empirical formulas of reaction  
293 rates at higher electron/ion temperature. In particular, some of the published empirical rates are  
294 based upon polynomial fitting of measured data in a certain range of temperature, and may not  
295 necessarily guarantee their validity beyond the intended temperature range. Our general scheme  
296 is that, if there are several reported empirical formulas with different validity ranges of  
297 temperature, we choose to adopt the one that has the highest upper temperature bound and/or is  
298 convergent toward high temperature. For example, for the dissociative recombination between  
299  $O^+$  and molecular neutrals, the reaction rates used in this study are from St.-Maurice and  
300 Laneville [1998], which remain valid for an effective ion temperature up to  $\sim 30000$  K. Upon a  
301 careful check of all temperature-dependent rates in our model, we notice that many of them are  
302 indeed fairly stable toward high temperature, even beyond the labeled upper temperature limit.  
303 For a few rate formulas that seem not to be convergent beyond the given upper temperature limit,  
304 when the simulated temperature is exceedingly high, we shall use the rate value at the upper  
305 temperature limit.

## 306 2.2 Anomalous electron heating (AEH)

307 An accurate calculation of  $T_e$  led by AEH is a formidable or even unachievable task at the  
308 current stage. First, a rigorous and computationally manageable theory of AEH is still lacking to  
309 date. Secondly, existing observations of AEH under very strong convection flows ( $V_E > 3$  km/s)  
310 are somehow scarce. This is not only because larger  $V_E$  is geophysically rare, but also due to that  
311 the signal strength may fall below the Incoherent Scatter Radar (ISR) detectability levels due to  
312 large electron-ion temperature ratio [Bahcivan, 2007]. Thus, instead of a rigorous theory and

313 solution of AEH, our model goal is to make the best attempts toward a reasonable estimate of  $T_e$   
314 in the E-region under intense SAID, based upon available AEH observations.

315 While it is known that the AEH stems from certain E-region instability/turbulence, the  
316 current state of E-region instability theory does not give us accurate spectra of the density and  
317 electric field perturbations as a function of the external electric field and ionospheric parameters.  
318 Some simplified models of nonlinearly saturated disturbance, albeit all heuristic to a certain  
319 degree, were usually applied to evaluate AEH in the E-region ionosphere [e.g., Robinson, 1986;  
320 Dimant and Milikh, 2003]. One noteworthy attempt along this route was the Dimant and Mikilh  
321 [2003] (hereafter referred to as DM03) model. Though based upon a few heuristic assumptions  
322 and simplifications (see Hysell et al. [2013]), the DM03 model has achieved certain success and  
323 practical applicability [deBoer et al., 2010; Dimant and Oppenheim 2011a; 2011b; Liu et al.,  
324 2016]. For the purpose of this study, we have extensively tested the DM03 model against the  
325 realistic AEH events assembled in St-Maurice and Goodwin [2021]. We find that the DM03  
326 results in general show acceptable agreement with realistic observations for convection velocity  
327  $V_E < 2$  km/s, but tend to deviate notably from realistic observations for  $V_E > 2$  km/s. We footnote  
328 that, to the authors' knowledge existing comparisons between AEH theories and observations  
329 were usually limited to  $V_E < 2$  km/s [Milikh and Dimant 2003; Williams et al., 1992]. St-Maurice  
330 and Goodwin [2021] suggested that the anomalous heating rate may be approximated by a 3<sup>rd</sup>-  
331 order polynomial of  $V_E$  for  $V_E < \sim 2$  km/s, but is better described by a 4<sup>th</sup>-order polynomial when  
332  $V_E$  is larger. This finding partly explains why the agreement between the simulated  $T_e$  and the  
333 observations becomes relatively poor at strong  $V_E (> 2$  km/s), since the DM03 (and also  
334 Robinson [1986]) heating rate basically represents a 3<sup>rd</sup>-order polynomial of  $V_E$ . On the other  
335 hand, the DM03 model also incorporates a kinetic modification of the electron cooling rate,

336 which was inferred from a kinetic simulation [Milikh and Dimant 2003] that is not easily  
337 replicated in our model.

338 We elect to resort to the approach of an observation-based empirical model. Recently, the  
339 behavior of AEH was revisited by St-Maurice and Goodwin [2021] based upon a rich dataset of  
340 realistic observations; a strong tendency of linear dependence of E-region electron temperature  
341 versus electric field magnitude is found in their study. A similar conclusion was also reached in  
342 Foster and Ericson [2000]. More specifically, St-Maurice and Goodwin [2021] suggest the  
343 following empirical formula,

$$344 \quad T_e = T_{e0} + S \cdot (V_E - 800\text{m/s}) \quad . \quad (15)$$

345  $T_{e0}$  represents a base level when the AEH is supposed to play little or none effect ----- the  
346 instability leading to AEH is supposed to have an E-field threshold, e.g., see equation 14 in  
347 DM03).  $V_E$  represents that F-region ion flows observed by ISR (evaluated at 300 km altitude).  
348  $T_{e0}$  is expected to be event-dependent, contingent upon parameters such as the ambient neutral  
349 temperature and other heating/cooling sources at play. In our model, we resolve  $T_e$  with all other  
350 heating and cooling sources (in the absence of AEH but including the classical frictional heating)  
351 for  $V_E$  up to 800 m/s, and hereby determine  $T_{e0}$ . The slope  $S$  used in our model is based upon St-  
352 Maurice and Goodwin [2021]; the values in their Table 1 are slightly smoothed and  
353 interpolated to our model grids in the 100-120 km altitude range. Figure 1 displays the altitudinal  
354 profile of  $S$  used in our model. In supplementary material, we provide a simple subroutine that  
355 can be used to evaluate the enhancement of  $T_e$  under AEH with the convection flow strength  $V_E$ ,  
356 without the necessity of complicated modeling effort. We also point out that, though a complete  
357 theory of AEH is unavailable to date, according to existing theories and reasonable theoretical  
358 expectations, the AEH heating rate and the dominant cooling terms (elastic and inelastic

359 collisions with neutrals) would presumably all be proportional to the electron density. Therefore,  
360 the AEH  $T_e$  enhancement is expected to be insensitive to electron density variations [e.g., Liu et  
361 al., 2016].

362 One may question that, since existing AEH observations are generally limited to  $V_E < 3.5$   
363 km/s, we may have to assume a linear extrapolation beyond that range. St-Maurice and Goodwin  
364 [2021] suggested that the linear trend may sustain to higher  $V_E$ , since the aspect angle of the  
365 plasma instability structures responsible for the heating is basically proportional to the ambient  
366 electric field. Readers are referred to their paper for more theoretical details of their proposal. To  
367 partially relieve the uncertainty in extrapolation, in the following run we shall use a peak  $V_E$  of  
368  $\sim 4$  km/s --- this is not up to the extreme SAID events in existing reports, but fairly close to (when  
369 mapped to the Swarm altitudes) the median value of Swarm observations of STEVE-related  
370 SAID events as reported in Archer et al. [2019a]. Given the current status of AEH theories and  
371 observations under intense  $V_E$ , it is fair to say that neither a semi-heuristic model approach (such  
372 as DM03) nor an empirically data-based approach can be completely free of uncertainty, and it is  
373 difficult to assert which approach is inherently better. Anyway, the empirical approach we elect  
374 to use is incontrovertibly advantageous in computation efficiency. We have made test runs using  
375 DM03 for the AEH module and found that, while the DM03 model may produce somehow  
376 different  $T_e$  profile in the E-region, the major results of this study, such as the plasma depletion  
377 and conductance reduction in the lower ionosphere, are not qualitatively changed.

### 378 2.3 Vibrationally excited $N_2$ distribution

379 Under SAID, the vibrational excitation of  $N_2$  plays an important role in the electron density  
380 depletion in the upper/topside ionospheric altitude where  $T_e$  is significantly elevated. In short,  
381  $N_2^*$  at higher vibration levels has a much faster reaction rate with  $O^+$  and thus effectively

382 converts  $O^+$  to  $NO^+$ . Since  $NO^+$  has a faster recombination rate than  $O^+$ , the total plasma density  
 383 is reduced accordingly. However, as explained in Campbell et al. [2006], a time step simulation  
 384 is not practical for the calculation of  $N_2^*$  populations because the wide range of radiative  
 385 transition probabilities would require a prohibitively large number of small time intervals. As  
 386 done in many previous studies [e.g., Cartwright et al., 2000; Campbell et al., 2006], in our model  
 387 we consider only the steady-state equilibrium distribution of the vibrationally excited  $N_2$  states.  
 388 The equation for the statistical equilibrium of each vibrational level  $\nu$  of  $N_2$  is given by,

$$\begin{aligned}
 & k_{\nu 0}n_0 + \sum_K CP_v^K + \sum_i A_{i\nu}n_i + \sum_i VV_{(\nu\pm 1)\nu}^{(i\mp 1)i}n_{\nu\pm 1}n_{i\mp 1} + Q_{\nu+1}n_{\nu+1} \\
 & = \left( \sum_i A_{\nu i} + \sum_K CL_v^K + \sum_i VV_{\nu(\nu\pm 1)}^{i(i\mp 1)}n_i + Q_\nu \right) \cdot n_\nu
 \end{aligned}
 \tag{16}$$

389 in which  $k_{\nu 0}$  denotes the electron impact excitation rate of vibrational level  $\nu$  (we assume the  
 390 impact excitation stems from the ground state with density  $n_0$ ).  $CP_v^K$  and  $CL_v^K$  denote the  
 391 production and loss rate of vibrational level  $\nu$  due to chemical reactions.  $A_{i\nu}$  is the transition  
 392 probability between the vibrational level  $\nu$  and  $i$ .  $VV_{(\nu\pm 1)\nu}^{(i\mp 1)i}$  is the rate of vibrational exchange  
 393 where a collision between levels  $\nu \pm 1$  and  $i \mp 1$  leaves them in level  $\nu$  and  $i$ .  $Q_\nu$  is the rate of  
 394 stepwise quenching of level  $N_2^*$  by collisions with O atoms. The vibration-translational transition  
 395 and the molecular diffusion of  $N_2$  are ignored in the model. We consider up to the 10<sup>th</sup> level of  
 396 the vibrational  $N_2$  state. For other details of the calculation of  $N_2^*$  distribution, see Newton et al.  
 397 [1974], Cartwright et al. [2000], and Campbell et al. [2006]. The calculation of electron impact  
 398 excitation, as well as all  $N_2^*$ -involved chemical processes and their reaction rates, are identical to  
 399 those in Campbell et al. [2006]. The vibrational-vibrational exchange rate is from Newton et al.  
 400 [1974]. The transition probabilities between vibrational levels are from Parlov [1998]. Note that  
 401

402 the vibrational excitation of  $N_2$  is also one of the major electron cooling processes, and the  
403 cooling rate is self-consistently calculated from the transition probability coefficients in our  
404 model.

405 Once the  $N_2^*$  distribution is determined, we use the formula in St.-Maurice and Laneville  
406 [1998] for the reaction rate between  $O^+$  and ground-state  $N_2$ , and use the coefficients in  
407 Schmeltekopf et al. [1968] for the relative enhancement of reaction rates at higher vibrational  
408 levels of  $N_2$  (see table S3 in supplementary material). An effective reaction rate between  $O^+$  and  
409  $N_2$  is calculated accordingly [e.g., Campbell et al., 2006].

#### 410 2.4 Numerical Scheme

411 The energy equations and the continuity equations are solved alternatively using a Strang  
412 time-splitting approach. Schematically,  $T_e$  and  $T_i$  advance at the integer time grid ( $t^n \rightarrow t^{n+1}$ ),  
413 while the ion densities of all species and FAC advance at the half-integer time grid ( $t^{n-1/2} \rightarrow$   
414  $t^{n+1/2}$ ). Note that as our convention here the upper script denotes the timestep. A dipole  
415 magnetic field configuration is used in the model. The spatial grid is two-dimensional: one along  
416 a dipole field line and equally spaced in the vertical ( $z$ ) direction, the other horizontally along the  
417 magnetic meridian ( $x$ -direction, positive northward) and equally spaced in MLAT in the  
418 AACGM sense. In all simulation runs presented in this paper, we adopt a time step of 0.1 s. The  
419 vertical grid interval is 1 km and the horizontal grid resolution is  $0.025^0$  MLAT. In such a grid  
420 coordinate system, using Jacobi transform we express the parallel and perpendicular gradient  
421 operator as  $\nabla_{//} = \frac{\partial}{\partial s} = \frac{\partial}{\partial z} \sin I$ ,  $\nabla_{\perp} = \frac{\partial}{\partial x} \cos I + \frac{\partial}{\partial s} \cot I$ , in which  $I$  is the magnetic dip angle.

422 One major challenge in the implementation of our model lies in the dramatic differences  
423 among, and the altitudinal variations of, the timescales of the chemical/physical processes

424 involved. To deal with such a difficulty, we use a combination of the steady-state solution, the  
 425 Runge-Kutta method, and the numerical difference approach, in our numerical scheme. At  
 426 altitudes below 120 km, the heating rates for both electrons and ions are strong, and the response  
 427 timescales of  $T_e$  and  $T_i$ , which are controlled by the electron- and ion-neutral interactions, are  
 428 very fast (timescale typically on order of  $\sim 0.1$ s or smaller). Therefore, at those altitudes we adopt  
 429 a steady-state solution for  $T_e$  and  $T_i$ , For  $V_E > 800$  m/s,  $T_e$  is obtained from equation (15). For  $T_e$   
 430 with  $V_E < 800$  m/s and  $T_i$ , we neglect the time derivative and non-local terms in equations (3) and  
 431 (4) and jointly solving the two energy equations via Newton's method [Press et al., 2007]. This  
 432 also sets up the bottom boundary condition for subsequently solving the time-dependent  
 433 electron/ion energy equations. Note that we still consider the time evolution of the plasma  
 434 density and FAC at altitudes  $< 120$  km, since the chemical reaction timescales and the transport  
 435 timescale led by the ion Pedersen drift and are typically much longer than 0.1s.

436 Above 120 km, the time evolutions and non-local transport effect of  $T_e$  and  $T_i$  are considered.  
 437 The energy equations are solved using a semi-implicit finite difference method; the involved  
 438 difference schemes are similar to that in Huba et al. [2000] and Zhu et al. [2016]. Schematically,  
 439 the model uses the backward difference for the time derivative. Each source term partially  
 440 containing a linear dependence on the temperature is split into two parts, one with a linear  
 441 dependence, and the other without the linear dependence. The linear terms are evaluated at the  
 442 current timestep  $t^n$ , while the other terms are evaluated at the previous timestep  $t^{n-1}$ . The plasma  
 443 density involved in the energy equation is taken as the value at the previous half timestep  $t^{n-1/2}$ .  
 444 For example, the electron cooling term due to elastic collision with neutrals is expressed as  
 445  $L_{en} = Q_n(N_e^{n-1/2}, T_e^{n-1}) \cdot [T_e^n - T_n]$ , in which  $Q_n(N_e, T_e)$  is a nonlinear function of  $T_e$   
 446 dependent on neural species [Schunk and Nagy, 2009]. The above semi-implicit method is found

447 to be numerically stable. An upwind difference scheme is used in treating the advective term in  
448 the ion/electron energy equation. The electron/ion field-aligned drifts are calculated according to  
449 equations (9) and (10). However, the terms involving the temperature gradients in (9) and (10)  
450 are dropped in electron/ion energy equations. For the electron energy equation which involves  
451 thermal conduction, the upper boundary of our model is set at 800 km altitude, where an external  
452 electron heat flow is imposed as the upper boundary condition.

453 The electron and ion energy equations are weakly coupled via an electron-ion collision term.  
454 In the lower ionosphere, the electron-ion collision is fairly minor compared to other  
455 heating/cooling terms. In our algorithm, in each time step,  $T_e$  and  $T_i$  are first solved separately  
456 with their own energy equation by using values in the previous time step in the electron-ion  
457 collision term. We then adopt an iterative approach to obtain convergent solutions of  $T_e$  and  $T_i$ ,  
458 i.e., we replace  $T_i$  or  $T_e$  in the electron-ion collision term with the last obtained values and iterate.  
459 In practice, we find that at most two iterations generally suffice for convergent solutions of  $T_e$   
460 and  $T_i$  with satisfying precision, namely that the relative difference of  $T_e$  and  $T_i$  between two  
461 successive iterations is smaller than  $10^{-5}$  at all altitudes of interest as our criterion.

462 The densities of ions and minor neutrals are solved at the half-integer time grid. A similar  
463 semi-implicit method is also applied to the continuity equations of ion and neutral species  
464 involved (except for the vibrationally excited  $N_2$ ). We use the backward difference for the time  
465 derivative. At each timestep  $t^{n+1/2}$ , the production rate is evaluated at the previous timestep  $t^{n-1/2}$ ,  
466 while the loss rate is written in the form  $L_i = \mathcal{L}N_i = \mathcal{L}(t^{n-1/2}) \cdot N_i^{n+1/2}$ .  $T_e^n$  and  $T_i^n$  obtained at  
467 the time step  $t^n$  are used in calculating the temperature-dependent reaction coefficients. We take  
468 into consideration of the Pedersen drift of  $NO^+$ ,  $O_2^+$ , and  $O^+$  in their continuity equations up to  
469 350 km altitudes. We adopt the “donor cell” numerical scheme [Huba et al., 2000] in treating the

470 Pedersen transport term. For minor ions  $N^+$  and  $N_2^+$ , their chemical loss timescale tends to be  
471 shorter than the Pedersen transport, so that we ignore the latter and use the 4<sup>th</sup>-order Runge-Kutta  
472 method to solve their time-evolving continuity equations. While each ion or neutral species is  
473 solved separately, we again apply an iterative approach (with similar procedure and criterion to  
474 that described for  $T_e$  and  $T_i$ ) to obtain convergent solutions of all densities involved. For the  
475 vibrationally excited  $N_2$ , we only compute the steady-state solution by solving the equation set  
476 (17) via Newton's method. The bottom boundary is set at 90 km. At this altitude, the ionosphere  
477 is assumed to be under a steady-state local chemical balance; all transport terms related to the  
478 Pederson drift and the ambipolar diffusion are dismissed. The upper boundary condition is to be  
479 discussed later in this subsection. As to the boundary conditions in the latitudinal direction, the  
480 lower-latitude boundary is set at where  $V_y$  is constant zero as per our SAID specification (see  
481 equation 19 later), so that the plasma density at this lower boundary is solved in 1D geometry  
482 without the Pedersen transport. The unidirectional (always poleward) property of the Pedersen  
483 drift and our numerical scheme imply that no poleward boundary condition is required.

484 The ambipolar diffusion term is discretized using a Keller-box method [Keller, 1970]. The  
485 coupling term between the two ion species (the last term in equation 11) is treated via an iterative  
486 approach similar to that dealing with the ion-electron coupling in their energy equations. The  
487 above numerical scheme is found to be stable, as long as the diffusion coefficient  
488  $k(T_{i//} + T_e)/m_i v_i$  is not too large. In practice, we limit the upper boundary at 500 km in solving  
489 the time-dependent ambipolar diffusion equation of  $NO^+$  and  $O^+$  ions. This is due to both  
490 scientific and numerical considerations. We recall that equations (9) and (10) are derived under a  
491 steady-state assumption and with the neglecting of the advective term  $(\mathbf{v} \cdot \nabla)\mathbf{v}$  in the momentum  
492 equations. At higher altitudes with an increasing magnitude of ambipolar drifts, the above

493 assumptions may become questionable. In SAID/STEVE cases the ion upflows may reach a few  
494 km/s [e.g., Nishimura et al., 2020], i.e., be supersonic, in the topside ionosphere, and the ion-ion  
495 collision also becomes important at those altitudes. Even if we dismiss the above theoretical  
496 complication and adopt equation (9) anyway, the very large diffusion coefficient and ambipolar  
497 drift speed at high altitudes impose a serious challenge to the stability of the numeral scheme and  
498 considerably increase the computational cost. At last, we emphasize again the main research  
499 interest of the current study is in the lower ionosphere (<200 km altitude). A more accurate  
500 description of the ionospheric variations and ion upflows in the topside ionosphere under SAID  
501 would require a different model, probably involving the full electron/ion momentum equations  
502 [e.g., Loranc and St-Maurice, 1994; Sydorenko and Rankin, 2013], which will be left for future  
503 studies.

504 Due to the above considerations, we run the time-dependent continuity equation up to 500  
505 km altitude, with the upper boundary condition specified by  $u_{i//}$ . The way we specify  $u_{i//}$  at the  
506 boundary is to be given in section 4.1 when we introduce the model run setup. Beyond 500 km  
507 altitude, we continue to calculate the plasma density up to 800 km by assuming a flux  
508 conservation  $\frac{n_i u_{i//}}{B} = \text{const}$ , corresponding to a steady-state ionosphere under ambipolar diffusion  
509 in the absence of chemical production/loss. With such an assumption, equation (11) consists of  
510 coupled first-order ODEs for  $\text{NO}^+$  and  $\text{O}^+$  densities, which are solved via a Runge-Kutta method  
511 starting from 500 km altitude. Extensive numerical tests have been performed and confirmed that,  
512 while the uncertainty in the specification of the upper boundary condition for the ion continuity  
513 equation would affect the solutions in the upper/topside ionosphere, the main research interest in  
514 this study, namely the plasma dynamics in the lower ionosphere and the FAC variations (which

515 is dominantly accumulated in the lower ionosphere), is relatively insensitive to the upper  
 516 boundary condition.

517 We solve the FAC via numerical integration,

$$518 \quad j_{//}(z) = -B \cdot \int_{z_0}^z \frac{\nabla_{\perp} \cdot (\sum N_i \mathbf{u}_{i\perp})}{B \sin I} \cdot dz \quad . \quad (17)$$

519 The bottom boundary  $z_0$  is set at 90 km. The integral is performed over field-aligned grids, and  
 520 we adopt the Newton-Cotes formula in the numerical integration [Press et al., 2007]. When  $j_{//}$  is  
 521 evaluated in the topside ionosphere, equation (17) is equivalent to the well-known form of  
 522  $-\nabla \cdot (\Sigma_p \mathbf{E})$ , in which  $\Sigma_p$  is the height-integrated (more precisely field-line-integrated) Pedersen  
 523 conductance. In this study, both  $\Sigma_p$  and FAC are evaluated up to the altitude of 500 km, i.e., the  
 524 nominal Swarm satellite altitude, to facilitate comparison with Swarm observations, the main  
 525 data source of SAID/STEVE to date.

526 Finally, we shall deal with the perturbation of electric fields due to the rise of the  $E_{//}$  (see  
 527 equation 13). The electric potential perturbation is obtained via a numerical integral along the  
 528 field line from an upper boundary  $z_{top}$ ,

$$529 \quad \delta\Phi = - \int_z^{z_{top}} \left( \frac{j_{//}}{\sigma_{//}} - \frac{\nabla p_e}{N_e e} - \frac{m_e v_{en}}{N_e e} \sum N_i u_{i//} \right) \cdot \frac{dz}{\sin I} \quad . \quad (18)$$

530 The perturbed perpendicular electric field is then calculated via  $\delta\mathbf{E}_{\perp} = -\nabla_{\perp} \delta\Phi$  and applied to  
 531 adjust the ion Pedersen drift and in turn the FAC. Iteration is made until convergent solutions of  
 532  $j_{//}$ ,  $E_{//}$  and  $\delta\Phi$  are reached at each timestep.  $z_{top}$  is set as 500 km altitude in our following run,  
 533 where the external SAID electric field is imposed. A boundary condition  $\delta\Phi=0$  is assumed at  
 534 500 km altitude. We have numerically tested with higher upper boundary altitudes of  $\delta\Phi$ , and

535 find that they produce virtually indiscernible difference to the result. More specifically, changing  
536  $z_{top}$  from 500 km to 800 km would result in only ~1% difference to the final FAC outcome.

537

### 538 **3. Electron precipitation surrounding SAID/STEVE**

539 To simulate the ionospheric variations under SAID/STEVE, we first need to know the  
540 ambient condition of the ionosphere surrounding SAID. SAID/STEVE is located in the nightside  
541 subauroral region. However, ionization sources are not entirely absent there. First, even on the  
542 nightside the geocorona scattering consistently provides weak ionization sources [Thomas, 1963].  
543 Such nightside ionization sources are considered in our model using the same specification  
544 embedded in the TIEGCM and GLOW models [Solomon, 2017]. More importantly, existing  
545 observations of STEVE suggested that the electron precipitation is weak but not zero  
546 surrounding STEVE. In the following we shall review two such observations in the existing  
547 literature, with new datasets and aspects added. The first event was reported by Gallardo-Lacourt  
548 et al. [2018a]. Figure 2 shows the POES/NOAA satellite data. The upper panel gives the Total  
549 Electron detector (TED) observations of the total electron precipitation fluxes in the whole TED  
550 energy range 50 eV-20 keV. It is key to notice that the STEVE arc is located amid a weak ( $<0.1$   
551  $\text{erg/cm}^2/\text{s}$ ) yet non-zero electron precipitation region with increasing fluxes toward higher  
552 latitudes. The bottom panel of Figure 2 shows the energy channel of the TED sensors where the  
553 differential electron fluxes maximize, which is often used to evaluate the characteristic energy of  
554 the electron precipitation. Such max-flux energy bins are found to be relatively stable at ~1-2  
555 keV as the ionospheric footprint of NOAA-17 traverses STEVE.

556 The other event was reported by Gillies et al. [2019]; their Figure 1 is copied as Figure 2b  
557 here. In short, the authors sampled the Transition Region Explorer (TREx) spectrometer

558 measurements on STEVE and its surrounding neighbors. The optical spectrum of STEVE shows  
559 a continuous enhancement over its ambient neighbors over a broad range of wavelengths, which  
560 constitutes the main source of the STEVE brightness. Our interest here is focused on the small  
561 yet distinct peak around 428 nm wavelength that exists in both STEVE and its ambient neighbors.  
562 This presumably comes from the 427.8 nm blue-line emission of the  $N_2^+$  1NG system. Such an  
563 emission requires  $\sim 19$  eV excitation energy, and is thus generally recognized as a sign of auroral  
564 electron precipitation. Similar 427.8 nm emissions are also observed in Liang et al [2019]'s  
565 STEVE event. It is important to notice that the STEVE does not show appreciable enhancement  
566 over surrounding neighbors in terms of the blue-line intensity, so that the 427.8 nm emissions  
567 constitute an ambient background, instead of a characteristic emission line, of STEVE. To view  
568 the latitudinal profile of the blue-line emission, we sample the meridional distribution of the  
569 427.8 emission intensity during 0640-0641 UT, when the STEVE was the brightest, from TReX  
570 spectrometer data. To calculate the 427.8 nm emission intensity, we subtract the out-of-band  
571 spectral intensity, taken as the average in 420-425 nm and 430-435 nm wavelength ranges, from  
572 the measured spectra, and then integrate the subtracted spectral intensity in 425-430 nm range.  
573 Figure 2c shows the distribution of the obtained 427.8 nm emissions versus MLAT. It is  
574 interesting to note that the STEVE arc is located amid an increasing slope (toward north) of the  
575 blue-line intensity, which is consistent with the POES/NOAA observation in the previous event.

576 The above inference that STEVE is located amid a region of weak yet increasing (toward  
577 high latitudes) electron precipitation is compatible with some other existing observations. Based  
578 on DMSP observations He et al. [2014] and Nishimura et al. [2020] both found that the electron  
579 fluxes increase across SAID toward high latitudes. Vis optical data Yadav et al. [2021] found  
580 that STEVE is embedded in a region with weak but increasing diffuse emissions toward high

581 latitudes. On the other hand, based on magnetospheric observations Chu et al. [2019] and  
582 Nishimura et al. [2019] both noticed that the magnetospheric root of STEVE/SAID is situated in  
583 a transition from the plasmopause into the electron plasma sheet, where electron fluxes increase  
584 toward tail across the magnetospheric SAID structure. To summarize, existing observations  
585 invoke the necessity of the inclusion of electron precipitation into the frame of a SAID model.  
586 This is particularly important if one considers the current generator mechanism of SAID, which  
587 we shall briefly discuss in Section 5. We emphasize again that the weak electron precipitation  
588 surrounding STEVE cannot by itself directly account for the optical brightness of STEVE  
589 [Gillies et al., 2019], but whether such weak precipitation may play certain indirect roles [e.g.,  
590 Chu et al., 2019] in the STEVE mechanism is a pending question to be examined in the future.  
591 We also admit that detailed knowledge about the electron precipitation associated with STEVE  
592 and Picket Fence is still limited (and to a certain degree controversial) to date, based upon  
593 unabundant events, so that our specification of the precipitation profile is not without uncertainty  
594 in this study. The ambient electron precipitation is embedded in our model as a necessary yet  
595 adjustable component.

596

#### 597 **4. Model simulation**

598 We now present the model run and the results. We first clarify that, the current paper is  
599 mainly intended to introduce our model and demonstrate a few key aspects and results from the  
600 new model. We have made many test runs with different specifications and profiles of SAID as  
601 well as of the ambient ionosphere, and are convinced that the main results and conclusion of this  
602 study are not quantitatively changed. It is however inappropriate to elaborate all those test runs in  
603 the current paper. In the interest of brevity we will be content, in this paper, to demonstrate two

604 runs that use typical SAID parameters, leaving for a separate publication a more comprehensive  
 605 examination of the subtlety of ionospheric dynamics, including certain neutral constituents that  
 606 may potentially contribute to STEVE, under different SAID and ambient  
 607 ionospheric/precipitation conditions.

#### 608 4.1 Model run setup

609 The ambient and initial conditions of the subauroral ionosphere are set up as follows. We  
 610 assume a weak yet gradually increasing (from 0.02 to 0.06 erg/cm<sup>2</sup>/s across SAID) ambient  
 611 electron precipitation. The precipitation flux spectrum is assumed to be Maxwellian with  
 612 characteristic energy of 2 keV. The above specification is partly based upon the realistic  
 613 observations in Gallardo-Lacourt [2018a]. The Boltzmann transport of precipitating auroral  
 614 electrons is solved via a two-stream electron transport code [Banks, 1974; Solomon et al., 1988]  
 615 in our model. The plasma convection is initially set as zero, and the electron heat flow at the  
 616 upper boundary is initially set as a quiet-time value (2×10<sup>9</sup> eV/cm<sup>2</sup>/s, e.g., Fallen and Watkins  
 617 [2013]). We start from the IRI-2016 model with parameters conformal to the realistic  
 618 geophysical/geomagnetic conditions in the 10 April, 2018 event [Gillies et al., 2019], and run our  
 619 model (without flow) to a chemical-diffusion equilibrium, which will be then used as the  
 620 initial/ambient condition of the subsequent run with SAID.

621 The latitudinal profile of SAID plasma flows is as follows:

$$622 \quad V_y = \begin{cases} 0 & x < -d \\ V_{y0} \cos^2\left(\frac{\pi x}{2d}\right) & -d < x < 0 \\ V_{y0} \left[ \alpha + (1 - \alpha) \cos^2\left(\frac{\pi x}{2d}\right) \right] & d > x > 0 \\ \alpha V_{y0} & x > d \end{cases} \quad (19)$$

623 in which  $V_{y0}$  denotes the peak SAID speed, and  $d$  controls the width of the SAID channel. The  
 624 flow profile is imposed at 500 km altitude and mapped along a dipole field geometry. Note that  
 625 in our specification there is a constant weaker azimuthal flow, parametrized by a small  $\alpha$ ,  
 626 poleward of SAID. This is motivated by the observations that, in many realistic cases, weaker yet  
 627 nontrivial westward plasma flows were often found to exist immediately poleward of SAID, e.g.,  
 628 Anderson et al. [2001] (see their Figure 1), Archer et al. [2019a] (panel a and b in their Figure 1),  
 629 Nishimura et al. [2019] (see their Figure 3), and Nishimura et al. [2020] (see their Figure 2).  
 630 Clues of the existence of such westward flows just poleward of STEVE may also be indirectly  
 631 hinted from the neutral observations in Liang et al. [2021]. Westward neutral winds were found  
 632 to be strongly intensified ( $\geq 200$  m/s) at latitudes higher than STEVE yet remain weak  
 633 equatorward of STEVE. Upon a reasonable premise that the neutral winds at subauroral latitudes  
 634 are mainly driven by ion drag, one may infer the existence of nontrivial westward plasma flows  
 635 of several hundred m/s poleward of STEVE/SAID. The above observations are also consistent  
 636 with the fact that, during major substorm intervals SAPS-like westward plasma flow  
 637 enhancements are often found to exist equatorward of auroras and extend to subauroral latitudes  
 638 [Nishimura et al., 2009; Zou et al., 2012; Lyons et al., 2015]. In the following run we set  $V_{y0}$   
 639  $= 4250$  m/s,  $d = 0.3^{\circ}$  MLAT, and  $\alpha = 1/8$ . The peak SAID velocity is selected here according to the  
 640 median value of eight Swarm-STEVE conjunctive events in Archer et al. [2019a] (see their  
 641 Figure 2).

642 Our model has an electron heat flow as the boundary condition at 800 km altitude. Such a  
 643 heat flow is set to follow the function form  $a + b\cos^2(\pi x/2d)$ , with a peak of  $2.8 \times 10^{10}$   
 644 eV/cm<sup>2</sup>/s at the center ( $x=0$ ) of SAID and a quiet-time value of  $2 \times 10^9$  eV/cm<sup>2</sup>/s outside SAID  
 645 ( $|x| > d$ ). The external electron heat flow is so specified that it can reproduce the realistic  $T_e$

646 observations within intense SAID in the topside ionosphere, as we shall elucidate in the  
647 following subsection. The SAID and external heat flow are turned on at  $t=0$ , and we shall trace  
648 the time evolution of the plasma temperature, density, and currents afterward.

649 The other boundary condition is the ion field-aligned drift at 500 km altitude. We assume  
650  $u_{i//}^{500}=0$  for the ambient ionosphere run. For the SAID run, under the notion that the ion upflows  
651 in the upper/topside ionosphere are driven by the frictional heating which, to the first order of  
652 approximation, is proportional to  $V_y^2$  [e.g., St-Maurice et al., 1999], we use a heuristic  
653 specification for the ion upflows at 500 km altitude.  $u_{i//}^{500} = \gamma \cdot V_y^2$ . In our following model run  
654 the factor  $\gamma$  is set as  $3 \times 10^{-5}$  s/m for  $O^+$  and  $2 \times 10^{-5}$  s/m for  $NO^+$ . Their ratio 1.5 is set according to  
655 a rough comparison of their  $m_i v_{in}$  values in the topside ionosphere. The peak  $O^+$  and  $NO^+$   
656 upflow speeds are thus  $\sim 540$  m/s and  $\sim 360$  m/s in the center SAID at 500 km altitude in our  
657 model run.

658 As afore-mentioned, existing STEVE observations indicate that its azimuthal extension may  
659 span over  $\sim 2.5$ h MLT sectors [Gallardo-Lacourt et al., 2018b; Nishimura et al., 2020]. Assuming  
660 this represents the azimuthal scale of a SAID segment, a 4250 km/s (at 500 km altitude) SAID  
661 flows would have a lifetime of  $\sim 9$  min in the SAID segment. In other words, any new plasma fed  
662 into the SAID channel by the ambient global convection has a duration of no more than  $\sim 10$  min  
663 to undergo SAID-imposed changes, even though the SAID itself may last longer. In practical in-  
664 situ observations, contingent upon the relative location of the satellite in the SAID segment, the  
665 interaction time between the new plasma's SAID entry and its detection by the satellite is  
666 typically limited to several minutes. Certainly, such an interaction time is flow-velocity  
667 dependent, and is longer at the edge of the SAID channel. Based on the above considerations, we

668 set the maximum simulation time at latitude  $x$  to be 18 min or  $L_0/V_y(x)$ , whichever is smaller.  $L_0$   
669 is set as 2.5 h MLT, and  $V_y(x)$  comes from our SAID profile specification (19). For  
670  $t > L_0/V_y(x)$ , the ionospheric profiles at the corresponding latitude are deemed to be no longer  
671 time-varying.

## 672 4.2 Simulation results

673 Movies showing the full time evolution of  $T_e$ ,  $T_i$ ,  $N_e$ , and  $\mathbf{j}$ , are given in supplementary  
674 material. The latitudinal profiles of SAID and the background precipitation are plotted on top for  
675 reference. It should be noted that the height profile presented in all movies and subsequent  
676 figures actually represents the altitudinal distribution along a magnetic field line. Figures 3 to 5  
677 exemplify the  $T_e$ ,  $T_i$ , and  $N_e$  profiles, respectively, at  $t=0$ , 30 sec, 2 min, 5 min, 10 min, and 15  
678 min. As one can see from the movie,  $T_e$  increases rapidly in the E-region right after the onset of  
679 SAID, which indicates the AEH effect. Later on,  $T_e$  also increases in the upper F-region, and  
680 appears to follow a two-step evolution: first a rapid yet weaker enhancement over a broad range  
681 of altitudes, then a stronger yet more gradual enhancement that shows a downward propagation  
682 trend from the topside ionosphere. Such a  $T_e$  enhancement in the upper F-region is led by heat  
683 flux conduction from the topside ionosphere [e.g., Rees and Roble, 1975; Moffett et al. 1998].  
684 As afore-mentioned, when considering the finite azimuthal extension of SAID, contingent upon  
685 the azimuthal location of the satellite passage, the plasma captured by the satellite at the peak  
686 flow latitude usually undergoes SAID intensification for no more than several minutes. Our  
687 simulation indicates that, at  $t=5$  min, the peak  $T_e$  at the center latitude of SAID reaches  $\sim 7500$  K  
688 at 500 km altitude, close to the median value of peak  $T_e$  enhancements under SAID as reported in  
689 Archer et al. [2019a].

690 As to the ion temperature,  $T_i$  dramatically increases due to ion frictional heating. The  
 691 enhancement first occurs in the lower ionosphere, and quickly expands to higher altitudes.  
 692 Overall, SAID leads to intense ion frictional heating over a broad range of altitudes. There is a  
 693 slight decrease of  $T_i$  at  $>300$  km altitude after  $\sim 2$  min, which is due to the adiabatic cooling  
 694 associated with ion upflows [Wang et al., 2012].  $T_i$  reaches  $\sim 16000$  K in the lower ionosphere at  
 695 the center of SAID in our simulation, which is compatible with existing theories and simulations  
 696 of frictional heating. Assuming a balance between the ion frictional heating and the collisional  
 697 cooling with neutrals, a simple equation of ion temperature can be written as  $T_i = T_n + \frac{\langle m_n \rangle}{3k} V_i^2$   
 698 [e.g., St-Maurice et al., 1999], in which  $\langle m_n \rangle$  denotes the collision-frequency-weighted averaged  
 699 neutral mass. In the lower ionosphere where  $N_2$  is the major neutral constituent,  $V_E \sim 4$  km/s  
 700 would lead to  $\sim 18000$  K ion temperature according to the above theory. Moffett et al. [1998] also  
 701 predicted  $T_i$  up to  $\sim 15000$  K in a numerical simulation of SAID with  $V_E=4$  km/s. In an event with  
 702  $T_i$  measurement onboard DE-2 satellite, Anderson et al. [1991] (see their Figure 1) found that  $T_i$   
 703 at  $\sim 388$  km altitude exceeded  $10000$  K when the SAID  $V_y$  reached  $\sim 4$  km/s. Notwithstanding the  
 704 uncertainty in  $T_i$  measurements by ISR [Akbari et al.; 2017; Goodwin et al., 2018], St-Maurice et  
 705 al. [1999] reported a case in which  $T_i$  obtained from EISCAT observations (though closer to  $T_{i//}$   
 706 under their radar geometry) exceeded  $10000$  K in the lower F-region when the convective  
 707 electric field temporarily reached  $\sim 225$  mV/m.

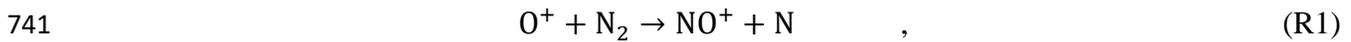
708 We turn next to the plasma density variations under SAID. As one can see from the movie,  
 709 after the start of SAID,  $N_e$  in the E- and lower F-region begins to increase in the poleward  
 710 portion of the SAID channel and to decrease in the equatorward portion of SAID. As time  
 711 evolves the equatorward density depletion slowly propagates a bit poleward into the center of  
 712 SAID, as well as extends upward to higher altitudes. These variations are led by the transport

713 term  $\nabla \cdot (N_i \mathbf{u}_{pi})$  in the continuity equation. More specifically,  $N_i \nabla \cdot \mathbf{u}_{pi}$  and  $\nabla N_i \cdot \mathbf{u}_{pi}$  are both  
714 depletion terms in the equatorward side of the SAID channel. With growing density variations  
715 the  $\nabla N_i \cdot \mathbf{u}_{pi}$  term gradually drives the density depletion to the poleward side of SAID (except at  
716 the very edge of SAID where the  $N_i \nabla \cdot \mathbf{u}_{pi}$  term leads to a pileup) as well as upward to higher  
717 altitudes, conformal to the  $\mathbf{u}_{pi}$  direction under a tilted field-line geometry. The role of ion  
718 Pedersen drift in depleting the lower ionosphere was initially addressed by Banks and Yasuhara  
719 [1978]. The plasma density variation in the lower ionosphere shows the most dynamic change in  
720 the first couple of minutes, yet becomes slowly changing and/or relatively stable afterward.

721 At first sight, the above results appear to be at odds with the simulation results in Noel et al.  
722 [2005], Milikh et al. [2006], and Liu et al. [2016], which all predicted an increase of the plasma  
723 density in the AEH region due to the decrease of recombination rate of  $\text{NO}^+$  with enhanced  $T_e$ .  
724 However, it is important to note that the effect of ion Pedersen drift and the latitudinal width of  
725 the AEH structure were not considered in the above studies. We have made test runs without the  
726 ion Pedersen drift, and indeed reproduced that  $N_e$  gradually increases in the AEH region.  
727 However, when the effects of ion Pedersen drift and narrow width of SAID channel are  
728 considered, in the ionosphere E-region where AEH actually operates, the transport effect led by  
729 the ion Pedersen drift and its divergence/convergence dominates over the chemical  
730 recombination process in terms of their contributions to density variations. As we have  
731 mentioned in section 2.1, with their Pedersen drift the E-region ions typically traverse the SAID  
732 channel in several tens of seconds, while the recombination timescale of  $\text{NO}^+$  is much slower.  
733 Using the reaction rate in Parlov [2014], in the AEH region with much elevated  $T_e$  (up to  $\sim 5000$   
734 K) and lowered density, the  $\text{NO}^+$  recombination timescale is estimated to be on the order of  $\sim 10^3$   
735  $- 10^4$  s. The rapid density depletion in the lower ionosphere is almost purely led by the ion

736 Pedersen transport effect. We note that density depletion due to a similar process is also reported  
737 in Zettergren and Semeter [2012].

738 The plasma density variations in the upper ionosphere where the ion Pedersen drift vanishes  
739 are driven by fundamentally different processes. One well-recognized mechanism of such a  
740 plasma depletion in the F-region ionosphere is a conversion from  $O^+$  to  $NO^+$  ions via the reaction,



742 whose reaction rate increases rapidly with enhanced ion temperature and electron temperature  
743 [St-Maurice and Laneville; 1998, Moffet et al., 1992b; 1998], causing  $NO^+$  to replace  $O^+$  to  
744 become the major ion species in the F-region under strong SAID. Since  $NO^+$  has a faster  
745 recombination rate than  $O^+$  --- this is true even under elevated  $T_e$  --- the plasma density decreases  
746 accordingly. However, it should be noted that such a chemistry-driven density depletion does not  
747 work effectively in the lower ionosphere where  $NO^+$  is inherently the dominant ion species. The  
748 other important process contributing to the plasma density variations in the upper/topside  
749 ionosphere is the ion upflows [Anderson et al., 1991; 1993]. As one can see from the movie and  
750 Figure 5, there is a gradual decrease of the F-region peak density at ~300-350 km, which is  
751 primarily led by the above-depicted reaction R1. Above 400 km, the density is temporarily  
752 enhanced during the first minute, which is driven by the thermal expansion of plasma via  
753 upflows under elevated temperature. Later on, as the plasma density continues to drop in the  
754 entire F-region, notable density depletion throughout the upper ionosphere becomes evident  
755 around the center of SAID after ~2 min, and gradually deepens with time.

756 Figure 6 demonstrates the altitudinal profile of the densities of  $N_e$ ,  $NO^+$ , and  $O^+$  at the center  
757 ( $x=0$ ) of SAID at  $t=0$ , 1 min, and 5 min, and 10 min. Initially,  $NO^+$  is the dominant ion species in  
758 the lower ionosphere, while  $O^+$  is dominant at  $>250$  km height. At  $t=1$  min,  $NO^+$  density is

759 enhanced substantially and starts to exceed the  $O^+$  density in the F-region ionosphere due to the  
760 reaction R1. The  $O^+$  density continues to drop significantly in the entire upper ionosphere due to  
761 a combined effect of the chemical process and the upflow evacuation [Anderson et al., 1991;  
762 1993], and  $NO^+$  becomes the major ion species there, though its density also drops with time in  
763 the upper ionosphere due to recombination and upflows. The simulation results predict that  $N_e$  in  
764 the upper/topside ionosphere would drop to the order of a few  $10^3 \text{ cm}^{-3}$  at the center of SAID,  
765 compatible with existing observations [Archer et al., 2019a; Nishimura et al., 2019; 2020].

766 Figure 7 shows the altitudinal profile of the Pedersen conductivity at the center of SAID at  
767  $t=30 \text{ sec}$ , 2 min, 5 min, and 10 min. The initial Pedersen conductivity ( $t=0$ ) is overplotted in a  
768 dotted line for reference. Due to the density depletion, the Pedersen conductivity decreases at  
769 almost all altitudes of interest, but the conductivity peak is always confined to the lower  
770 ionosphere. In terms of the height-integrated Pedersen conductance  $\Sigma_P$ , most of the contributions  
771 would come from the lower ionosphere. Movies showing the full time evolution of the MLAT-  
772 altitude distribution of the current vectors, as well as of the  $\Sigma_P$  and FAC at 500 km altitude, are  
773 given in supplementary material. We demonstrate the latitudinal profiles of  $\Sigma_P$  and FAC at  $t=0$ ,  
774 30 sec, 2 min, 5 min, and 15 min in Figure 8. Quickly following the start of SAID,  $\Sigma_P$  decreases  
775 significantly and drops to very low levels ( $\sim 0.1 \text{ S}$ ) in the equatorward and center portion of  
776 SAID, yet increases at the poleward edge of SAID. Banks and Yasuhara [1978] reported a  
777 similar change of  $\Sigma_P$  in their model. The FAC is initially large upon the incidence of SAID, but  
778 quickly decreases in magnitude due to the reduction of  $\Sigma_P$ . We further note that the change of  $\Sigma_P$   
779 and FAC is dynamic in the first 2 minutes elapsed time, but becomes slowly varying after that  
780 time and even quasi-stable after  $\sim 5 \text{ min}$ . This indicates that the conductance drop comes more  
781 from the Pedersen-transport-driven density depletion in the lower ionosphere than from the

782 gradual density depletion in the upper ionosphere driven by chemical processes and upflows.  
783 When reaching a quasi-steady state, the simulated FAC in a main portion of SAID is downward  
784 with magnitude smaller than and/or close to  $\sim 1 \mu\text{A}/\text{m}^2$  or, compatible with observations [Archer  
785 et al., 2019a; Chu et al., 2019; Nishimura et al., 2019; 2020]. We have also made other test runs  
786 with stronger SAID  $V_y$  magnitude, and noticed that the steady-state downward FAC level is  
787 relatively insensitive to the peak flow magnitude. The reason is that, with stronger SAID the ion  
788 Pedersen drift is also enhanced, leading to a deeper density depletion in the lower ionosphere and  
789 the reduction of Pedersen conductance, so that the FAC level remains more or less the same.

790 On the other hand, a stronger upward FAC appears at the poleward edge of the SAID channel.  
791 We note that many existing proposals of the generation mechanism of SAID postulated the  
792 existence of upward FACs at the poleward edge of SAID [e.g., Anderson et al., 1993; 2001; De  
793 Keyser et al., 1998]. Such upward FACs were indeed observed near the edge of SAID, and are  
794 deemed as related to the Picket Fence phenomenon [Nishimura et al., 2019], though their  
795 observed intensity ( $< 1 \mu\text{A}/\text{m}^2$ ) tends to be weaker than that in our simulation (peak at  $\sim 2 \mu\text{A}/\text{m}^2$ ).  
796 Chu et al. [2019] reported an event (see their Figure 2) that an upward FAC peaked at  $\sim 1.2$   
797  $\mu\text{A}/\text{m}^2$  at the poleward edge of SAID. We shall recall that the number of existing events under  
798 intense SAID condition and with in-situ FAC measurements remains limited to date, and that the  
799 technique to derive FAC density from single-satellite magnetic field measurements relies on a  
800 current sheet assumption, whose credibility in the case of small-scale FAC structures is  
801 questionable [Forsyth et al., 2017]. The latitudinal scale of the upward FACs in our simulation is  
802  $< 10$  km, which is marginal for the single-satellite FAC technique. For reference, existing FAC  
803 observations under intense SAID came predominantly from DMSP and Swarm 1 Hz magnetic  
804 field data, both of which have a spatial resolution of  $\sim 8$  km. It is thus not impossible that the

805 existing FAC observations based on single-satellite measurements tend to underestimate the peak  
806 upward FAC density. Using high-resolution (50 Hz) Swarm magnetic field data, Nishimura et al.  
807 [2019] obtained a much larger FAC density (up to  $\sim 10 \mu\text{A}/\text{m}^2$  spike, see their Figure 2), though  
808 the accuracy of the FAC determination at this temporal/spatial scale may be questionable  
809 [Forsyth et al., 2017].

810 The discrepancy between the simulated upward FAC intensity and the realistic observations  
811 may also result from uncertainties in our model parameters. Since the upward FAC is contributed  
812 by the convergence between the Pedersen current inside the poleward edge of the SAID and that  
813 outside the SAID, the overestimation of upward FACs may be relieved in two ways: by adjusting  
814 the flow gradient and level surrounding the poleward edge of SAID, and/or by adjusting the  
815 ambient Pederson conductance surrounding the poleward edge of SAID. In this paper we only  
816 demonstrate the former possibility. In the previous run we assumed a flow of 1/8 the peak SAID  
817 speed, or  $\sim 530 \text{ m/s}$  in practice, poleward of the SAID channel. In the following run, we assume a  
818 higher constant flow of  $850 \text{ m/s}$  ( $\alpha=1/5$  in equation 19) poleward of STEVE. Figure 9 displays  
819 the altitude-latitude distribution of  $N_e$  and the latitudinal profile of FAC at  $t=15 \text{ min}$  from the  
820 new run. The plasma density enhancement and FAC at the poleward edge of SAID become  
821 substantially weaker than those in the previous run. The peak upward FAC at the poleward edge  
822 of SAID is now limited to  $<1 \mu\text{A}/\text{m}^2$ . Vice versa, we have also tested the case that the flow  
823 magnitude is reduced to zero poleward of STEVE, and found that the resulting upward FAC  
824 density rises significantly (peak at  $\sim 4.5 \mu\text{A}/\text{m}^2$ , not shown). We thus infer that the upward FAC  
825 level is fairly sensitive to the flow condition surrounding the poleward edge of SAID; a moderate  
826 relaxing (steepening) of the attenuation edge of SAID would cause a substantial decrease  
827 (increase) of upward FAC density there. This shall not be unexpected. A smoother  $V_y$  gradient

828 around the edge of SAID imposes double-fold effects on the FAC: in addition to weaker  
829 convergence of electric fields, a smoother change of  $V_y$  also leads to weaker convergence of ion  
830 Pedersen drifts and thus less density buildup, and in turn smaller  $\Sigma_p$ . The FAC is thus expected to  
831 vary nonlinearly with the  $V_y$  gradient. Some other possible reasons for the discrepancy between  
832 our simulated upward FAC intensity and the realistic observations will be discussed in Section 5.

833

## 834 **5. Discussion**

835 To date, existing observations and model simulations of SAID-related ionospheric variations  
836 have been focused on the upper F-region and topside ionosphere, yet the variations and  
837 structures in the E-region and lower F-region ionosphere led by SAID remain largely unexplored.  
838 In this study, we present a time-dependent 2D model simulation of self-consistent variations of  
839 the electron/ion temperature, density, and FAC, under strong SAID, with main focus in the lower  
840 ionosphere. In particular, the ion Pedersen drift and its resultant density and FAC variations are  
841 self-consistently incorporated into the model. While some uncertainties admittedly exist due to  
842 insufficient observations to date, we have made decent attempts to evaluate the AEH and the  
843 ambient precipitation conditions surrounding SAID/STEVE based upon current understanding  
844 and available observations. Therefore, we have the ground to believe that our model represents  
845 the best effort to date in simulating the dynamic variations and structures in the lower ionosphere  
846 under intense SAID. While direct observations of the lower ionospheric variations under SAID  
847 are still lacking to date, we expect that some of our model results may be validated by the  
848 incoming EISCAT3D observations (to be fully operational in 2022).

849 Our simulation reproduces many key features of SAID that are consistent with the realistic  
850 observations and/or theoretical expectations, such as AEH in the E-region, strong electron

851 temperature enhancement in the upper F-region, intense ion frictional heating, and density  
852 depletion in the upper F-region. Most importantly, we highlight the key role of ion Pedersen  
853 drifts in the variations of the plasma density, the ionospheric conductance, and the FAC. Existing  
854 in-situ FAC observations under intense SAID often allude to much reduced Pedersen  
855 conductance within the SAID channel. We confirm in this study that a significant reduction of  
856 ionospheric conductance indeed occurs within SAID. Such a reduction of ionospheric  
857 conductance is mainly owing to the plasma density depletion in the lower ionosphere led by the  
858 transport effect associated with the ion Pedersen drift [Banks and Yasuhara, 1978], rather than  
859 driven by chemical processes, as the recombination is slowed down due to the elevated electron  
860 temperature. The simulated FAC inside SAID is mainly downward with magnitude  $\leq \sim 1 \mu\text{A}/\text{m}^2$ ,  
861 compatible with observations, though a stronger upward FAC exists at the poleward edge of  
862 SAID.

863 This study aims to investigate the ionospheric variations under an established SAID, instead  
864 of the generation mechanism of SAID. The exact formation mechanism of SAID is not entirely  
865 clear to date. The idea of the SAID mechanism being associated with a magnetospheric source  
866 acting either as a voltage or as a current generator has been a subject of discussion. Readers are  
867 referred to Figueiredo et al. [2004] for a detailed discussion in this regard and arguments for the  
868 co-existence of both voltage and current drivers. In our model run, the SAID  $V_y$  profile is  
869 externally specified, and is thus more aligned with the view of a voltage driver of SAID.  
870 Nevertheless, the essence of our study remains valid, namely that the dynamic ionospheric  
871 variations and the resulting changes of conductivities under SAID must act in a way to self-  
872 consistently adjust the ionospheric current and the E-field, no matter which one is the main  
873 driver of the SAID. That said, the potential operation of a current driver may lead to certain

874 possible adjustments to our model. While the downward FAC is carried by proton precipitation  
875 and/or outflowing ionospheric electrons, the upward FACs, from a current continuity perspective,  
876 should be largely conformal to the suprathermal electron precipitation on top of the ionosphere.  
877 As addressed in Section 3, existing observations indicated the presence of electron precipitation  
878 surrounding STEVE, particularly in its poleward vicinity (see e.g., Nishimura et al. [2019;  
879 2020]), but the FAC carried by such precipitation is lower than the upward FAC density obtained  
880 in our simulation. Via numerical tests, we found that the upward FAC level strongly depends on  
881 the  $V_y$  gradients at the poleward edge of SAID. To match the observed upward FAC densities, a  
882 larger flow magnitude immediately poleward of SAID is needed. This, from a current generator  
883 perspective, can be rephrased in a way that the moderate upward FAC modifies the ionospheric  
884 convection and result in a smoother flow gradient at the poleward edge of SAID. A refinement of  
885 our model to accommodate the possible involvement of a current generator, particularly  
886 regarding the upward FAC carried by electron precipitation at the poleward edge of FAC, is  
887 currently under way and shall be the content of a separate publication in a near future.

888 Our simulation results indicate the presence of strong latitudinal gradients of plasma density,  
889 temperature, and flows, at the edge of SAID. Figure 10 shows the latitudinal profiles of plasma  
890 flows,  $T_e$ ,  $T_i$ , and  $N_e$ , averaged over 100-150 km altitudes. As one can see, strong gradients of  
891 plasma density, temperature, and flows exist at the edge of SAID. It is interesting to note that the  
892 density gradients are stronger at the poleward side of SAID than at the equatorward side. Such  
893 density/temperature/flow gradients are hotbeds of a number of plasma instabilities (see Kelley  
894 [2009] for a thorough discussion of potential plasma instabilities in the ionosphere). For example,  
895 the temperature gradient and density gradient are strong and oppositely directed at  $\sim 0.1-0.25^{\circ}$   
896 poleward of SAID, which is known to be conducive to the temperature gradient drift instability

897 [e.g., Hudson and Kelley, 1976]. Such temperature/density gradients are of course contingent  
898 upon the actual SAID profile, and it is not impossible that in some cases the gradients can be  
899 even steeper than that presented in our simulation with  $0.025^0$  MLAT grid resolution. These  
900 instabilities may become an intrinsic part of the plasma dynamics at the poleward edge of SAID.  
901 We speculate that those instabilities, when well developed, can reach a level that may have  
902 macroscopic effects on the plasma distributions and variations. For example, the instabilities at a  
903 nonlinear stage may lead to the presence of nonlinear currents ( $e\langle\delta N_e \cdot (\delta V_i - \delta V_e)\rangle$ ), and in  
904 turn modify the local FAC configuration [e.g., Dimant and Oppenheim, 2011], which constitute  
905 another possible reason for the discrepancy between our modeled and observed FAC intensity at  
906 the poleward edge of SAID.

907       The potential operation of instabilities in the presence of sharp plasma gradients in the lower  
908 ionosphere may have particular importance to the Picket Fence phenomenon. Picket Fence  
909 occurs at ~100-120 km altitude and is typically found at the poleward edge of STEVE [Semeter  
910 et al., 2020; Gillies et al., 2020]. It is dominated by green-line emission (excitation energy 4.19  
911 eV) and also contains some N<sub>2</sub> 1PG emissions (7.35 eV), but lacks the blue-line emissions (18.75  
912 eV) [Gillies et al., 2019; Mende et al., 2019]. Clues of electron precipitation were found in  
913 association with Picket Fence [Nishimura et al., 2019], but the precipitation fluxes tend to be too  
914 weak to directly account for the optical brightness of Picket Fence. A number of researchers  
915 suggested the possibility that Picket Fence be generated by suprathermal electrons ( $\leq\sim 10\text{eV}$ )  
916 locally accelerated in the lower ionosphere [Mende et al., 2019; Gillies et al., 2020; Semeter et  
917 al., 2020]. However, the underlying mechanisms of such local acceleration remain elusive to date.  
918 Semeter et al. [2020] suggested that such electron heating mechanisms might be intrinsically  
919 related to certain local plasma instabilities at play in the lower ionosphere near the boundary of

920 SAID, in concert with our above proposal. A dedicated exploration of the possible plasma  
921 instabilities is beyond the scope of the current paper and shall be left to future studies.  
922 Nevertheless, our results in this study have laid the foundation to, and prepared a quantitative  
923 context for, such an exploration in the future.

924

## 925 **6. Summary and conclusion**

926 While it is now established that the STEVE and Picket Fence phenomena are inherently  
927 related to SAID, existing observations and models related to SAID have been limited to the  
928 upper F-region/topside ionosphere. The lack of definite knowledge of the lower ionospheric  
929 dynamics under intense SAID hampers the exploration of the underlying mechanism of STEVE  
930 and Picket Fence. In this study, we present a 2D time-dependent model simulation of the self-  
931 consistent variations of the electron/ion temperature, density, and FAC, under strong SAID, with  
932 main focus in the lower ionosphere. We reproduce many known or expected features of SAID,  
933 such as AEH in the E-region, strong electron temperature enhancement in the upper F-region,  
934 intense ion frictional heating, and plasma density depletion. Most importantly, the inclusion of  
935 ion Pedersen drifts is proved to be crucial to the density variations and FAC dynamics in the  
936 lower ionosphere. We find that the ionospheric conductance is significantly reduced within  
937 SAID, and indicate that the conductance reduction is mainly owing to the plasma density  
938 depletion in the lower ionosphere, which is primarily driven by the transport effect of ion  
939 Pedersen drifts instead of chemical effects. The simulated FAC inside SAID is mainly  
940 downward with magnitude  $\leq 1 \mu\text{A}/\text{m}^2$ , in line with existing observations. Our simulation also  
941 predicts that the plasma density in the lower ionosphere and in turn the Pedersen conductance  
942 increase at the poleward edge of the SAID channel, leading to an upward FAC there that is

943 qualitatively consistent with, but tends to be somehow larger than, the realistic observations. Via  
944 numerical tests, we note that this upward FAC is sensitive to the flow condition surrounding the  
945 poleward edge of SAID. Given the potential limitation (e.g., a current-sheet approximation and  
946 latitudinal resolution) of the FAC data drawn from in-situ observations, a moderate discrepancy  
947 between the model simulation and the realistic FAC observations should not be deemed  
948 unreasonable, though we cannot exclude the possibility that the discrepancy stems from certain  
949 limitations of our current model.

950 One other key aspect of this study is that, our simulation results corroborate the presence of  
951 strong gradients of plasma density, temperature, and flows, at the edge of SAID. These gradients  
952 are potentially conducive to a number of plasma instabilities. The potential operation of  
953 instabilities in the presence of sharp plasma gradients in the lower ionosphere may have  
954 particular importance to the Picket Fence phenomena, which are usually found near the poleward  
955 edge of STEVE. The simulation results of the plasma dynamics and structures under SAID  
956 achieved in this study establish the context of, and pave the road to, a future investigation of the  
957 possible plasma instabilities at the edge of a SAID channel, our next-step task to carry on this  
958 study.

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961 at: [http://data.phys.ucalgary.ca/sort\\_by\\_project/other/publication\\_datasets/2019GL083272/](http://data.phys.ucalgary.ca/sort_by_project/other/publication_datasets/2019GL083272/). We  
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964  
965 **References.**

966 Akbari, H., Goodwin, L. V., Swoboda, J., St.-Maurice, J.-P., and Semeter, J. L. (2017), Extreme  
967 plasma convection and frictional heating of the ionosphere: ISR observations, *J. Geophys. Res.*  
968 *Space Physics*, 122, 7581– 7598, doi:[10.1002/2017JA023916](https://doi.org/10.1002/2017JA023916).

969 Anderson, P. C., Heelis, R. A., and Hanson, W. B. (1991), The ionospheric signatures of rapid  
970 subauroral ion drifts, *J. Geophys. Res.*, 96( A4), 5785– 5792, doi:[10.1029/90JA02651](https://doi.org/10.1029/90JA02651).

971 Anderson, P. C., D. L. Carpenter, K. Tsuruda, T. Mukai, and F. J. Rich (2001), Multisatellite  
972 observations of rapid subauroral ion drifts (SAID), *J. Geophys. Res.*, 106(A12), 29,585–  
973 29,599, doi:10.1029/2001JA000128.

974 Anderson, P. C., W. B. Hanson, R. A. Heelis, J. D. Craven, D. N. Baker, and L. A. Frank (1993),  
975 A proposed production model of rapid subauroral ion drifts and their relationship to substorm  
976 evolution, *J. Geophys. Res.*, 98(A4), 6069–6078, doi:10.1029/92JA01975.

977 Archer, W. E., & Knudsen, D. J. (2018). Distinguishing subauroral ion drifts from Birkeland  
978 current boundary flows. *Journal of Geophysical Research: Space Physics*, 123, 819– 826.

979 Archer, W. E., Gallardo-Lacourt, B., Perry, G. W., St.-Maurice, J.-P., Buchert, S. C., & Donovan,  
980 E. F. (2019a). Steve: The optical signature of intense subauroral ion drifts. *Geophysical*  
981 *Research Letters*, 46, 6279– 6286. <https://doi.org/10.1029/2019GL082687>

982 Archer, W. E., St.- Maurice, J.-P., Gallardo-Lacourt, B. (2019b). The vertical distribution of the  
983 optical emissions of a Steve and Picket Fence event. *Geophysical Research Letters*, 46,  
984 10719– 10725, <https://doi.org/10.1029/2019GL084473>

985 Bahcivan, H. (2007), Plasma wave heating during extreme electric fields in the high latitude E  
986 region, *Geophysical Research Letters*, 34 (15). <https://doi.org/10.1029/2006GL029236>

987 Banks, P. M., C. R. Chappell, and A. F. Nagy (1974), A new model for the interaction of auroral  
988 electrons with the atmosphere: Spectral degradation, backscatter, optical emission, and  
989 ionization, *J. Geophys. Res.*,79(10), 1459–1470, doi:[10.1029/JA079i010p01459](https://doi.org/10.1029/JA079i010p01459).

990 Banks, P.M. and Yasuhara, F. (1978), Electric fields and conductivity in the nighttime E-region:  
991 A new magnetosphere-ionosphere-atmosphere coupling effect. *Geophys. Res. Lett.*, 5: 1047-  
992 1050. <https://doi.org/10.1029/GL005i012p01047>

993 Campbell, L., D. C. Cartwright, M. J. Brunger, and P. J. O. Teubner (2006), Role of electronic  
994 excited N<sub>2</sub> in vibrational excitation of the N<sub>2</sub> ground state at high latitudes, *J. Geophys.*  
995 *Res.*, **111**, A09317, doi:[10.1029/2005JA011292](https://doi.org/10.1029/2005JA011292).

996 Cartwright, D. C., M. J. Brunger, L. Campbell, B. Mojarrabi, and P. J. O. Teubner (2000), Nitric  
997 oxide excited under auroral conditions: Excited state densities and band emissions, *J.*  
998 *Geophys. Res.*, 105, 20,857 –20,867.

999 Chu, X., Malaspina, D., Gallardo-Lacourt, B., Liang, J., et al (2019). Identifying STEVE's  
1000 magnetospheric driver using conjugate observations in the magnetosphere and on the  
1001 ground. *Geophysical Research Letters*, 46.<https://doi.org/10.1029/2019GL082789>.

1002 deBoer, J. D., J.-M. A. Noël, and J.-P. St-Maurice (2010), The effects of mesoscale regions of  
1003 precipitation on the ionospheric dynamics, electrodynamics and electron density in the  
1004 presence of strong ambient electric fields, *Ann. Geophys.*, 28, 1345– 1360,  
1005 doi:10.5194/angeo-28-1345-2010.

1006 Dimant, Y. S., and G. Milikh (2003), Model of anomalous electron heating in the E region: 1.  
1007 Basic theory, *Journal of Geophysical Research: Space Physics*, 108 (A9).

1008 Dimant, Y., and M. Oppenheim (2011), Magnetosphere-ionosphere coupling through E region  
1009 turbulence: 2. Anomalous conductivities and frictional heating, *Journal of Geophysical*  
1010 *Research: Space Physics*, 116 (A09304), doi:10.1029/2011JA016649.

1011 De Keyser, J., M. Roth, and J. Lemaire (1998), The magnetospheric driver of subauroral ion  
1012 drifts, *Geophys. Res. Lett.*, 25(10), <https://doi.org/10.1029/98GL01135>.

1013 Fallen, C. T., and B. J. Watkins (2013), Diurnal and seasonal variation of electron heat flux  
1014 measured with the Poker Flat Incoherent-Scatter Radar, *J. Geophys. Res. Space Physics*, 118,  
1015 5327–5332, doi:10.1002/jgra.50485.

1016 Figueiredo, S., T. Karlsson, and G. T. Marklund (2004), Investigation of subauroral ion drifts  
1017 and related field-aligned currents and ionospheric Pedersen conductivity distribution, *Ann.*  
1018 *Geophys.*, 22, 923–934, doi:10.5194/angeo-22-923-2004.

1019 Forsyth, C., Rae, I. J., Mann, I. R., and Pakhotin, I. P. (2017), Identifying intervals of temporally  
1020 invariant field-aligned currents from Swarm: Assessing the validity of single-spacecraft  
1021 methods, *J. Geophys. Res. Space Physics*, 122, 3411– 3419, doi:10.1002/2016JA023708.

1022 Foster, J. C., and P. J. Erickson (2000), Simultaneous observations of E-region coherent  
1023 backscatter and electric field amplitude at F-region heights with the Millstone Hill UHF radar,  
1024 *Geophysical Research Letters*, 27 (19), 3177-180.

1025 Foster, J. C., and W. J. Burke (2002), SAPS: A new categorization for sub-auroral electric fields,  
1026 *Eos. Trans. AGU*, 83(36), 393, doi:10.1029/2002EO000289.

1027 Foster, J. C., M. J. Buonsanto, M. Mendillo, D. Nottingham, F. J. Rich, and W. Denig (1994),  
1028 Coordinated stable auroral red arc observations: Relationship to plasma convection, J.  
1029 Geophys. Res., 99(A6), 11,429–11,439, doi:10.1029/93JA03140.

1030 Gallardo-Lacourt, B., Nishimura, Y., Donovan, E., Gillies, D. M., Perry, G. W., Archer, W. E., et  
1031 al. (2018a). A statistical analysis of STEVE. *Journal of Geophysical Research: Space Physics*,  
1032 123, 9893–9905. <https://doi.org/10.1029/2018JA025368>

1033 Gallardo-Lacourt, B., Liang, J., Nishimura, Y., and Donovan, E. (2018b). On the origin of  
1034 STEVE: Particle precipitation or ionospheric skyglow? *Geophys. Res. Lett.*, 45, 7968–  
1035 7973. <https://doi.org/10.1029/2018GL078509>

1036 Gallardo-Lacourt, B., Nishimura, Y., Lyons, L. R., Mishin, E. V., Ruohoniemi, J. M., Donovan,  
1037 E. F., Angelopoulos, V., & Nishitani, N. (2017). Influence of auroral streamers on rapid  
1038 evolution of ionospheric SAPS flows. *Journal of Geophysical Research: Space*  
1039 *Physics*, 122, 12,406– 12,420. <https://doi.org/10.1002/2017JA024198>

1040 Galperin, Y. I., Y. N. Ponomarov, and A. G. Zosinova (1973), Direct measurements of ion drift  
1041 velocity in the upper atmosphere during a magnetic storm, *Kosm. Issled.*, 11, 273.

1042 Gillies, D. M., E. Donovan, D. Hampton, J. Liang, M. Connors, Y. Nishimura, B. Gallardo-  
1043 Lacourt, and E. Spanswick, First observations from the TREx Spectrograph: the Optical Spectrum of  
1044 STEVE and the Picket Fence Phenomena, *Geophysical Research Letters*, 46.  
1045 <https://doi.org/10.1029/2019GL083272>

1046 Gillies, D. M., Liang, J., Donovan, E., & Spanswick, E. (2020). The apparent motion of STEVE  
1047 and the Picket Fence phenomena. *Geophysical Research Letters*, 47,  
1048 e2020GL088980. <https://doi.org/10.1029/2020GL088980>

1049 Goodwin, L. V., J.-P. St.-Maurice, H. Akbari, R. J. Spiteri (2008), Incoherent Scatter Spectra  
1050 Based On Monte Carlo Simulations of Ion Velocity Distributions Under Strong Ion Frictional  
1051 Heating, *Radio Science*, 10.1002/2017RS006468, 53, 3, 269-287.

1052 Harding, B. J., Mende, S. B., Triplett, C. C., & Wu, Y.-J. J. (2020). A mechanism for the STEVE  
1053 continuum emission. *Geophysical Research Letters*, 47, 2020GL087102. [https://doi.org/  
1054 10.1029/2020GL087102](https://doi.org/10.1029/2020GL087102)

1055 He, F., X.-X. Zhang, and B. Chen (2014), Solar cycle, seasonal, and diurnal variations of  
1056 subauroral ion drifts: Statistical results, *J. Geophys. Res. Space Physics*, 119, 5076–5086,  
1057 doi:10.1002/2014JA019807.

1058 Heelis, R. A., Bailey, G. J., Sellek, R., Moffett, R. J., and Jenkins, B. (1993), Field-aligned drifts  
1059 in subauroral ion drift events, *J. Geophys. Res.*, 98(A12), 21493-21499,  
1060 doi:10.1029/93JA02209.

1061 Huba, J. D., Joyce, G., & Fedder, J. A. (2000). SAMI2 (Sami2 is another model of the  
1062 ionosphere): A new low - latitude ionosphere model. *Journal of Geophysical Research*, 105,  
1063 23,035- 23,054.

1064 Hudson, M. K., and M. C. Kelley (1976), The temperature gradient instability at the equatorward  
1065 edge of the ionospheric plasma trough, *J. Geophys. Res.*, 81, 3913– 3918.

1066 Hysell, D., R. Miceli, and J. Huba (2013), Implications of a heuristic model of auroral Farley  
1067 Buneman waves and heating, *Radio Science*, 48 (5), 527-534.

1068 Kelley, M. C. (2009), *The Earth's Ionosphere, Plasma Physics and Electrodynamics*, Int.  
1069 *Geophys. Ser.*, 2nd ed., Elsevier, New York.

1070 Liang J., B. Yang, E. Donovan, J. Burchill, and D. Knudsen (2017), Ionospheric electron heating  
1071 associated with pulsating auroras: A Swarm survey and model simulation, *J. Geophys. Res.*  
1072 *Space Physics*, 122, 8781–8807, doi:[10.1002/2017JA024127](https://doi.org/10.1002/2017JA024127).

1073 Liang, J., E. Donovan, B. Jackel, E. Spanswick, and M. Gillies (2016), On the 630 nm red-line  
1074 pulsating aurora: Red-line Emission Geospace Observatory observations and model  
1075 simulations, *J. Geophys. Res. Space Physics*, 121, 7988–8012, doi:[10.1002/2016JA022901](https://doi.org/10.1002/2016JA022901).

1076 Liang, J., Donovan, E., Connors, M., Gillies, D., St-Maurice, J. P., Jackel, B., et al.  
1077 (2019). Optical spectra and emission altitudes of double-layer STEVE: A case  
1078 study. *Geophysical Research Letters*, 46, 13630–13639. [https://doi.org/10.1029/](https://doi.org/10.1029/2019GL085639)  
1079 [2019GL085639](https://doi.org/10.1029/2019GL085639)

1080 Liang, J., Zou, Y., Nishimura, Y., Donovan, E., Spanswick, E., & Conde, M. (2021). Neutral  
1081 wind dynamics preceding the STEVE occurrence and their possible preconditioning role in  
1082 STEVE formation. *Journal of Geophysical Research: Space Physics*, 126,  
1083 e2020JA028505 <https://doi.org/10.1029/2020JA028505>

1084 Liu, J., W. Wang, M. Oppenheim, Y. Dimant, M. Wiltberger, and S. Merkin (2016), Anomalous  
1085 electron heating effects on the E region ionosphere in TIEGCM, *Geophys. Res. Lett.*, 43,  
1086 2351–2358, doi:[10.1002/2016GL068010](https://doi.org/10.1002/2016GL068010).

1087 Loranc, M., and St-Maurice, J.-P. (1994), A time-dependent gyro-kinetic model of thermal ion  
1088 upflows in the high-latitude *F* region, *J. Geophys. Res.*, 99( A9), 17429–17451,  
1089 doi:[10.1029/93JA01852](https://doi.org/10.1029/93JA01852).

1090 Lyons, L. R., Nishimura, Y., Gallardo-Lacourt, B., Nicolls, M. J., Chen, S., Hampton, D.  
1091 L., ... Angelopoulos, V. (2015). Azimuthal flow bursts in the inner plasma sheet and possible  
1092 connection with SAPS and plasma sheet earthward flow bursts. *Journal of Geophysical*  
1093 *Research: Space Physics*, **120**, 5009– 5021. <https://doi.org/10.1002/2015JA021023>

1094 MacDonald, E. A., Donovan, E., Nishimura, Y., Case, N., Gillies, D. M., Gallardo-Lacourt, B.,  
1095 et al. (2018). New science in plain sight: Citizen Scientists lead to the discovery of optical  
1096 structure in the upper atmosphere. *Science Advances*, 4(3), eaaq0030. [https://doi.org/10.1126/](https://doi.org/10.1126/sciadv.aaq0030)  
1097 [sciadv.aaq0030](https://doi.org/10.1126/sciadv.aaq0030)

1098 Mende, S. B., Harding, B. J., & Turner, C. ( 2019). Subauroral green STEVE arcs: Evidence for  
1099 low-energy excitation. *Geophysical Research Letters*, 46, 14256–  
1100 14262. <https://doi.org/10.1029/2019GL086145>

1101 Milikh, G., and Y. S. Dimant (2003), Model of anomalous electron heating in the E region: 2.  
1102 Detailed numerical modeling, *Journal of Geophysical Research: Space Physics*, 108 (A9).

1103 Milikh, G. M., L. P. Goncharenko, Y. S. Dimant, J. P. Thayer, and M. A. McCready (2006),  
1104 Anomalous electron heating and its effect on the electron density in the auroral electrojet,  
1105 *Geophys. Res. Lett.*, 33, L13809, doi:10.1029/2006GL026530.

1106 Mishin, E., Nishimura, Y., and Foster, J. ( 2017), SAPS/SAID revisited: A causal relation to the  
1107 substorm current wedge, *J. Geophys. Res. Space Physics*, 122, 8516– 8535,  
1108 doi:[10.1002/2017JA024263](https://doi.org/10.1002/2017JA024263).

1109 Moffett, R. J., A. E. Ennis, G. J. Bailey, R. A. Heelis, and L. H. Brace (1998), Electron  
1110 temperatures during rapid subauroral ion drift events, *Ann. Geophys.*, 16, 450 – 459

- 1111 Moffett, R. J., G. J. Bailey, and B. Jenkins (1992b), Effects of greatly increased O<sup>+</sup> loss in the  
1112 ionospheric F-region, *Planet. Space Sci.*, 40, 1631
- 1113 Moffett, R. J., R. A. Heelis, R. Sellek, and G. J. Bailey (1992a), The temporal evolution of the  
1114 ionospheric signatures of subauroral ion drifts. *Planet. Space Sci.*, 40, 663.
- 1115 Newton, G. P., J. C. G. Walker, and P. H. E. Meijer (1974), Vibrationally excited nitrogen in  
1116 stable auroral red arcs and its effect on ionospheric recombination, *J. Geophys. Res.*, 79, 3807  
1117 – 3818.
- 1118 Nishimura, Y., Gallardo-Lacourt, B., Zou, Y., Mishin, E., Knudsen, D. J., Donovan, E. F., et al  
1119 (2019). Magnetospheric signatures of STEVE: Implication for the magnetospheric energy  
1120 source and inter-hemispheric conjugacy. *Geophysical Research Letters*, 46.  
1121 <https://doi.org/10.1029/2019GL082460>.
- 1122 Nishimura, Y., Donovan, E. F., Angelopoulos, V., & Nishitani, N. (2020). Dynamics of auroral  
1123 precipitation boundaries associated with STEVE and SAID. *Journal of Geophysical Research:  
1124 Space Physics*, 125, e2020JA028067. <https://doi.org/10.1029/2020JA028067>.
- 1125 Noël, J., St.-Maurice, J., and Blelly, P. (2000), Nonlinear model of short-scale electrodynamics  
1126 in the auroral ionosphere. *Annales Geophysicae* **18**, 1128–1144. [https://doi.org/10.1007/  
1127 s00585-000-1128-1](https://doi.org/10.1007/s00585-000-1128-1).
- 1128 Noël, J.-M. A., J.-P. S.-Maurice, and P.-L. Blelly (2005), The effect of E-region wave heating on  
1129 electrodynamic structures, *Ann. Geophys.*, 23, 2081– 2094, doi:10.5194/angeo-23-2081-  
1130 2005.
- 1131 Pavlov, A. (2014). Photochemistry of ions at D-region altitudes of the ionosphere: A review.  
1132 *Surveys in Geophysics*, 35(2), 259–334.

1133 Pavlov A. V. (1998), New electron energy transfer rates for vibrational excitations of N<sub>2</sub> , Ann.  
1134 Geophys., 16, 176–182.

1135 Press, W. H., S. A. Teukolsky, W. T. Vetterling, and B. P. Flannery (2007), Numerical Recipes  
1136 3rd Edition: The Art of Scientific Computing (3rd. ed.). Cambridge University Press, USA.

1137 Puhl-Quinn, P. A., H. Matsui, E. Mishin, C. Mouikis, L. Kistler, Y. Khotyaintsev, P. M. E.  
1138 Décréau, and E. Lucek (2007), Cluster and DMSP observations of SAID electric fields, J.  
1139 Geophys. Res., 112, A05219, doi:10.1029/2006JA012065.

1140 Rees, M. H., and R. G. Roble (1975), Observations and theory of the formation of stable auroral  
1141 red arcs, Rev. Geophys., 13(1), 201–242, doi:10.1029/RG013i001p00201.

1142 Richards, P. G. (2001), Seasonal and solar cycle variations of the ionospheric peak electron  
1143 density: Comparison of measurement and models, J. Geophys. Res., 106( A7), 12803– 12819,  
1144 doi:10.1029/2000JA000365.

1145 Richmond, A. D., E. C. Ridley, and R. G. Roble (1992), A thermosphere/ionosphere general  
1146 circulation model with coupled electrodynamics, *Geophys. Res. Lett.*, **19**, 601–604,  
1147 doi:[10.1029/92GL00401](https://doi.org/10.1029/92GL00401)

1148 Ridley, A. J., Y. Deng, and G. Tóth (2006), The global ionosphere–thermosphere model, Journal  
1149 of Atmospheric and Solar-Terrestrial Physics, Volume 68, Issue 8, 839-864.

1150 Robinson, T. (1986), Towards a self-consistent non-linear theory of radar auroral backscatter,  
1151 Journal of atmospheric and terrestrial physics, 48 (5), 417-422.

1152 Schunk, R., and A. Nagy (2009), Ionospheres: physics, plasma physics, and chemistry,  
1153 Cambridge university press.

1154 Semeter, J., E. Macdonald, M. Hunnekuhl, M. Hirsch, N. Zeller, A. Chernenkoff, and J. Wang  
1155 (2020), The Mysterious Green Streaks Below STEVE, *Earth and Space Science*,  
1156 [doi:10.1002/essoar.10502878.2](https://doi.org/10.1002/essoar.10502878.2)

1157 Schmeltekopf, A. L., E. E. Ferguson, and F. C. Fehsenfeld (1968), Afterglow studies of the  
1158 reactions  $\text{He}^+$ ,  $\text{He}(2^3\text{S})$ , and  $\text{O}^+$  with vibrationally excited  $\text{N}_2$ , *J. Chem. Phys.*, 48, 2966–2973.

1159 Solomon, S. C., P. B. Hays, and V. J. Abreu (1988), The auroral 6300 Å emission: Observations  
1160 and modeling, *J. Geophys. Res.*, 93, 9867–9882, doi:10.1029/JA093iA09p09867.

1161 Solomon, S. C. (2017), Global modeling of thermospheric airglow in the far-ultraviolet, *J.*  
1162 *Geophys. Res.*, 122, doi:10.1002/2017/JA024314.

1163 Spiro, R., R. Heelis, and W. Hanson (1979), Rapid subauroral ion drifts observed by  
1164 Atmospheric Explorer C, *Geophys. Res. Lett.*, 6, 657–660.

1165 St-Maurice, J.-P., and Laneville, P. J. (1998), Reaction rate of  $\text{O}^+$  with  $\text{O}_2$ ,  $\text{N}_2$ , and NO under  
1166 highly disturbed auroral conditions, *J. Geophys. Res.*, 103(A8), 17519–17521,  
1167 doi:[10.1029/98JA01387](https://doi.org/10.1029/98JA01387).

1168 St-Maurice, J.-P., & Goodwin, L. (2021). Revisiting the behavior of the *E*-region electron  
1169 temperature during strong electric field events at high latitudes. *Journal of Geophysical*  
1170 *Research: Space Physics*, 126, e2020JA028288. <https://doi.org/10.1029/2020JA028288>

1171 St-Maurice, J.-P., C. Cussenot, and W. Kofman (1999), On the usefulness of E region electron  
1172 temperatures and lower F region ion temperatures for the extraction of thermospheric  
1173 parameters: a case study, *Annales Geophysicae*, 17 (9), 1182-1198.

- 1174 Sydorenko, D., and Rankin, R. (2013), Simulation of O<sup>+</sup> upflows created by electron  
1175 precipitation and Alfvén waves in the ionosphere, *J. Geophys. Res. Space Physics*, 118, 5562–  
1176 5578, doi:[10.1002/jgra.50531](https://doi.org/10.1002/jgra.50531).
- 1177 Thomas, G. E. (1963), Lyman  $\alpha$  scattering in the Earth's hydrogen geocorona: 1., *J. Geophys.*  
1178 *Res.*, 68( 9), 2639– 2660, doi:10.1029/JZ068i009p02639.
- 1179 Richmond, A. D., E. C. Ridley, and R. G. Roble (1992), A thermosphere/ionosphere general  
1180 circulation model with coupled electrodynamics, *Geophys. Res. Lett.*, **19**, 601–604,  
1181 doi:[10.1029/92GL00401](https://doi.org/10.1029/92GL00401)
- 1182 Wang, W., Talaat, E. R., Burns, A. G., Emery, B., Hsieh, S., Lei, J., and Xu,  
1183 J. (2012), Thermosphere and ionosphere response to subauroral polarization streams (SAPS):  
1184 Model simulations, *J. Geophys. Res.*, 117, A07301, doi:[10.1029/2012JA017656](https://doi.org/10.1029/2012JA017656).
- 1185 Williams, P., B. Jones, and G. Jones (1992), The measured relationship between electric field  
1186 strength and electron temperature in the auroral E-region, *Journal of atmospheric and*  
1187 *terrestrial physics*, 54 (6), 741-748.
- 1188 Yadav, S., Shiokawa, K., Otsuka, Y., Connors, M., & St Maurice, J.-P. (2021). Multi-wavelength  
1189 imaging observations of STEVE at Athabasca, Canada. *Journal of Geophysical Research:*  
1190 *Space Physics*, 126, e2020JA028622. <https://doi.org/10.1029/2020JA028622>.
- 1191 Yeh, H.-C., J. C. Foster, F. J. Rich, and W. Swider (1991), Storm time electric field penetration  
1192 observed at mid-latitude, *J. Geophys. Res.*, 96(A4),5707–5721, doi:10.1029/90JA02751.

1193 Zettergren, M., and Semeter, J. (2012), Ionospheric plasma transport and loss in auroral  
1194 downward current regions, *J. Geophys. Res.*, 117, A06306, doi:10.1029/2012JA017637.

1195 Zhu, J., A. J. Ridley, and Y. Deng (2016), Simulating electron and ion temperature in a global  
1196 ionosphere thermosphere model: Validation and modeling an idealized substorm, *J. Atmos.*  
1197 *So. Terr. Phys.*, 138, 243-260.

1198 Zou, S., L. R. Lyons, and Y. Nishimura (2012), Mutual evolution of aurora and ionospheric  
1199 electrodynamic features near the Harang reversal during substorms, *Geophysical Monograph*  
1200 *Series*, 197, 159–169, doi:10.1029/2011GM001163.

1201

1202 **Figure Caption:**

1203 Figure 1. The slope of Te enhancement versus  $V_E$  for the AEH calculation used in this study.

1204

1205 Figure 2. (a) POES/NOAA-17 observations. The upper panel gives the Total Electron detector (TED)  
1206 observations of the total electron precipitation fluxes; the bottom panel shows the energy channel where  
1207 the differential electron fluxes maximize in the  $0^0$ -sensor and  $30^0$ -sensor (both sensors are within the loss  
1208 cone). (b) Copied from Gillies et al. [2019] showing the optical spectra of STEVE compared to its  
1209 ambient neighbors. (c) The 427.8 blue-line emission intensity derived from TREx spectrograph  
1210 measurement as a function of MLAT. In (a) and (c), a vertical dashed line marks the position of STEVE  
1211 arc.

1212

1213 Figure 3. Simulation outcome of altitude-MLAT profile of Te at six elapsed times. The latitudinal profiles  
1214 of SAID and the background precipitation are plotted on top for reference. Zero relative latitude  
1215 indicates the center of SAID.

1216

1217 Figure 4. Same as Figure 3 but for Ti.

1218

1219 Figure 5. Same as Figure 3 but for Ne.

1220

1221 Figure 6. Altitudinal profile of densities of Ne, NO<sup>+</sup> and O<sup>+</sup> at the center of SAID at (a)  $t=0$ ; (b)  $t=1$  min;  
1222 (c)  $t=5$  min; and (d)  $t=10$  min. In subfigures (b)-(d), The initial ( $t=0$ ) Ne profile is plotted in dotted line  
1223 for reference.

1224

1225 Figure 7. Altitudinal profile of Pedersen conductivity at the center of SAID at (a)  $t=30$  sec; (b)  $t=2$  min;  
1226 (c)  $t=5$  min; and (d)  $t=10$  min. The initial ( $t=0$ ) Pederson conductivity profile is plotted in dotted line for  
1227 reference.

1228

1229 Figure 8. latitudinal profiles of  $\Sigma_p$  and FAC at different elapsed times. The latitudinal profiles of SAID  
1230 and the background precipitation are plotted on top for reference.

1231

1232 Figure 9. Latitude-altitude profile of Ne, and the latitudinal profile of FAC at  $t=15$  min for a new run with  
1233 higher flow poleward of SAID. The latitudinal profiles of SAID and the background precipitation are  
1234 plotted on top for reference.

1235

1236 Figure 10. Latitudinal profiles of plasma flows, Te, Ti, and Ne, averaged over 100-150 km altitudes.

1237

**Figure 1-10.**

Figure 1

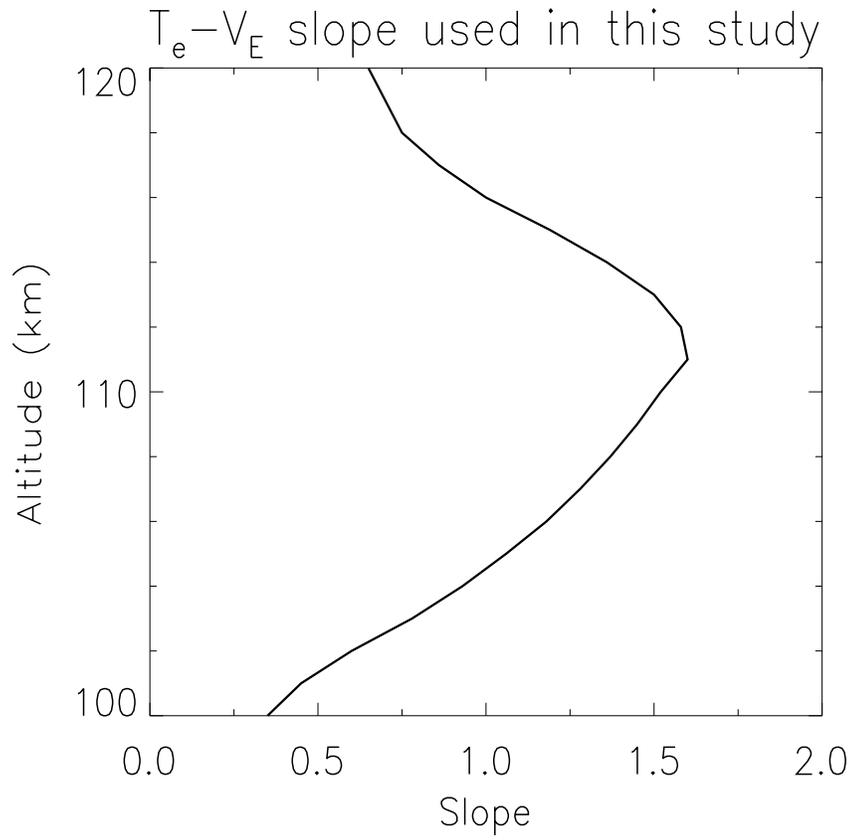


Figure 1. The slope of  $T_e$  enhancement versus  $V_E$  for the AEH calculation used in this study

Figure 2

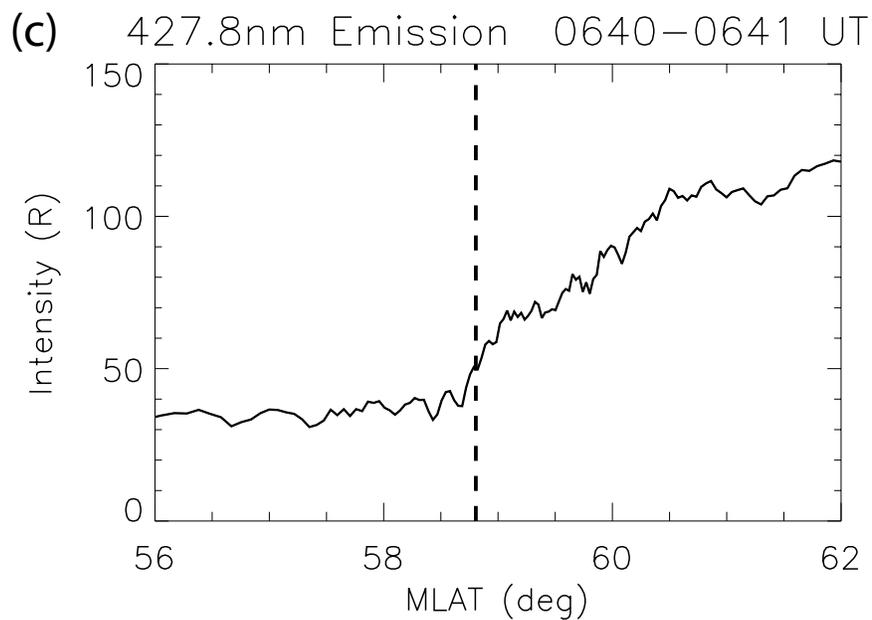
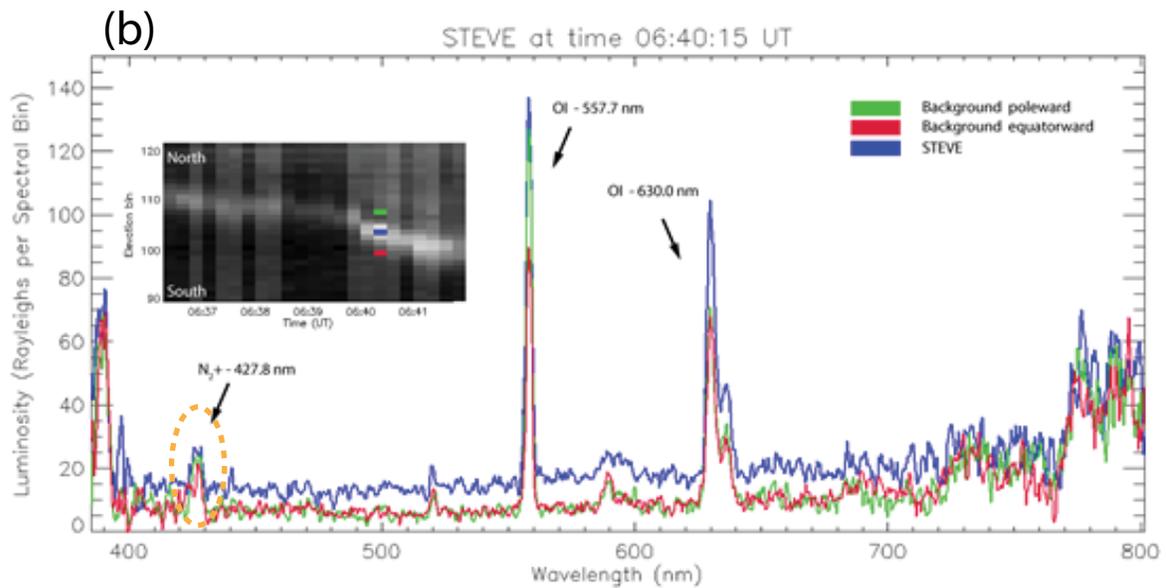
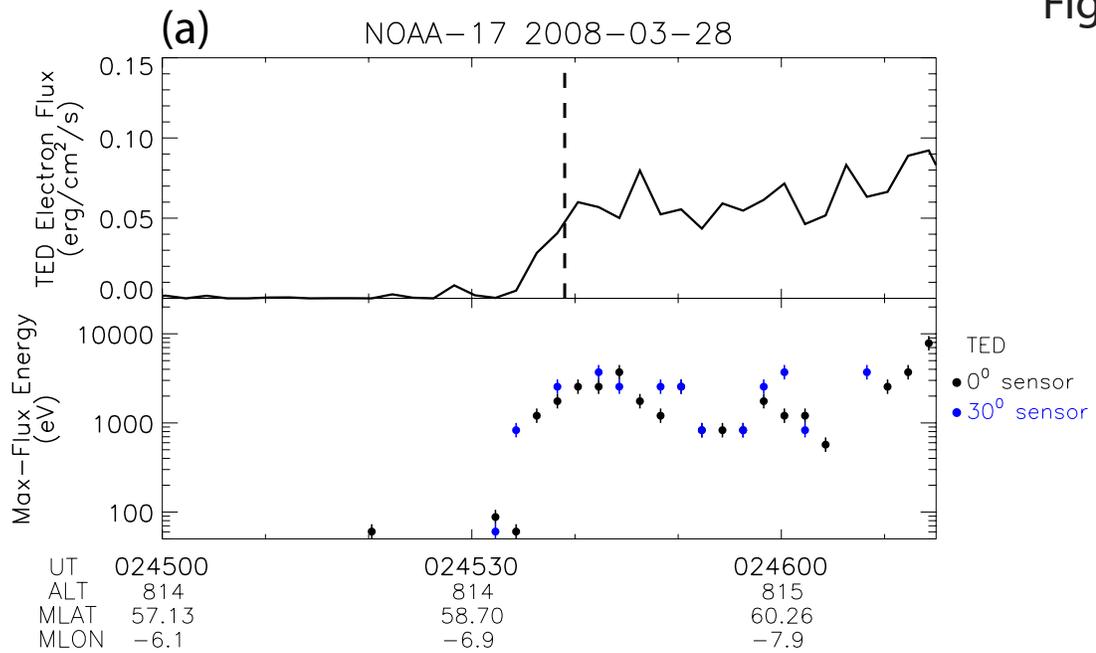


Figure 2. (a) POES/NOAA-17 observations. The upper panel gives the Total Electron detector (TED) observations of the total electron precipitation fluxes; the bottom panel shows the energy channel where the differential electron fluxes maximize in the 00-sensor and 300-sensor (both sensors are within the loss cone). (b) Copied from Gillies et al. [2019] showing the optical spectra of STEVE compared to its ambient neighbors. (c) The 427.8 blue-line emission intensity derived from TREx spectrograph measurement as a function of MLAT. In (a) and (c), a vertical dashed line marks the position of STEVE arc

Figure 3

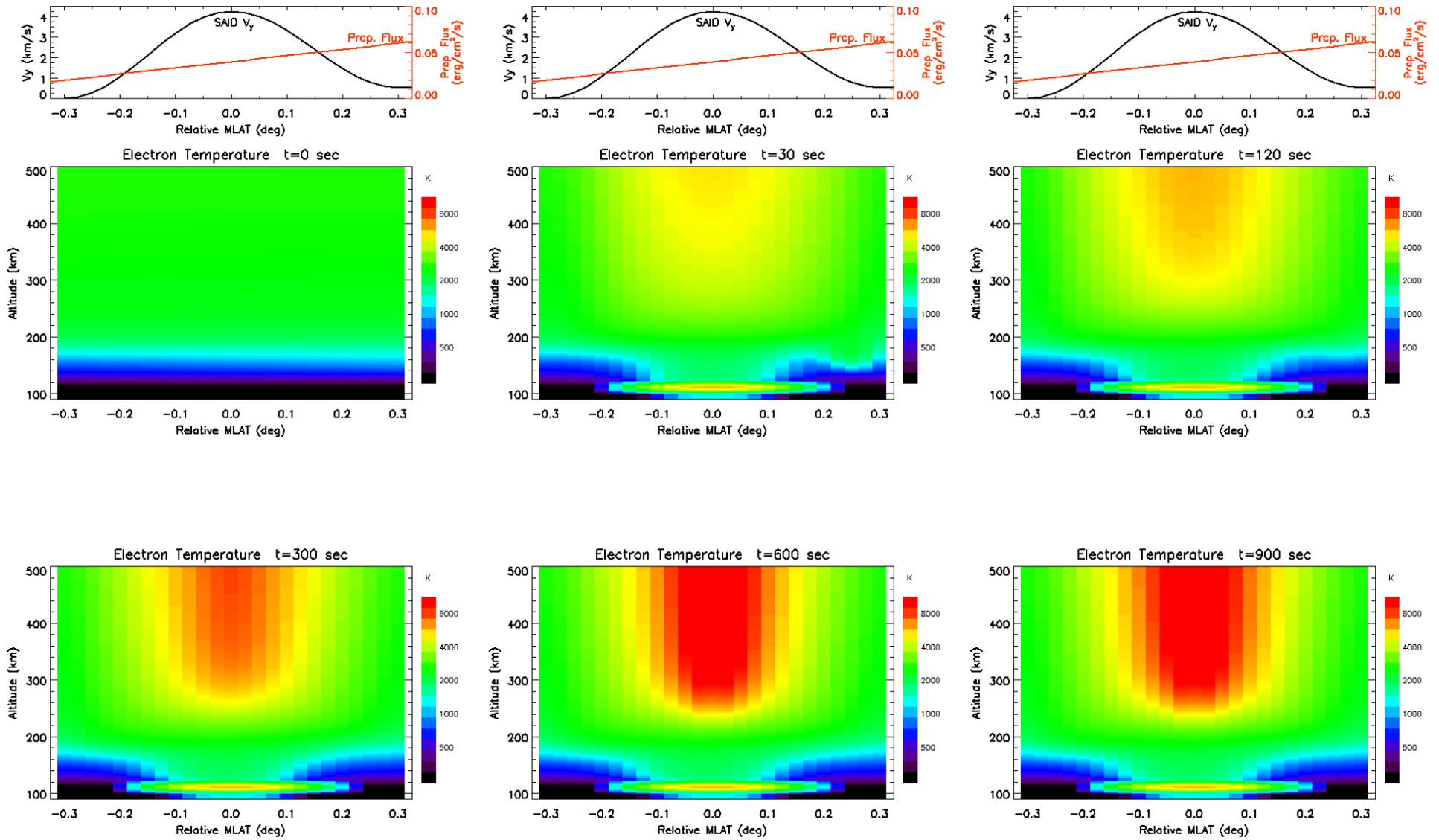


Figure 3. Simulation outcome of altitude-MLAT profile of Te at six elapsed times. The latitudinal profiles of SAID and the background precipitation are plotted on top for reference. Zero relative latitude indicates the center of SAID

Figure 4

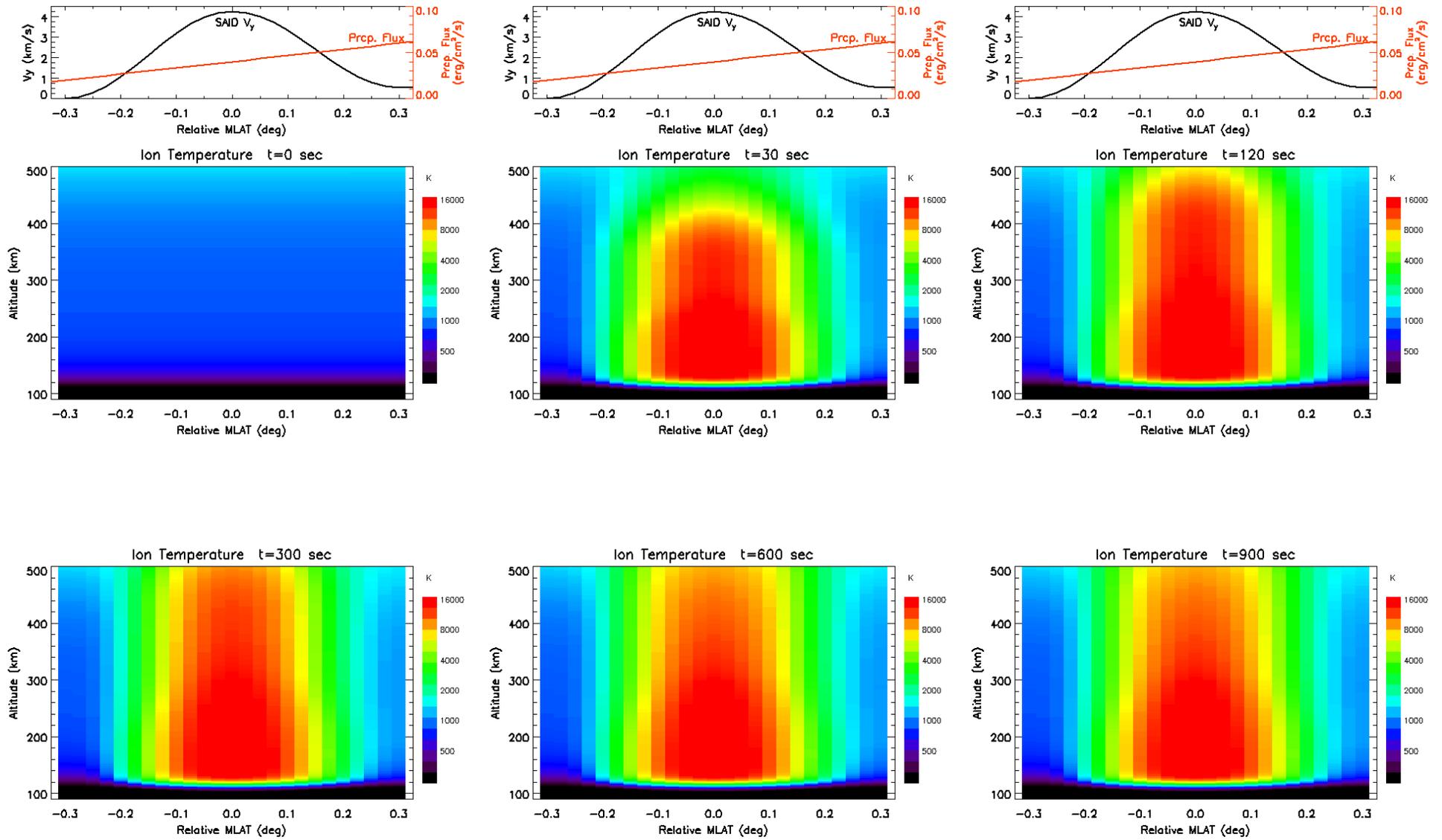


Figure 4. Same as Figure 3 but for Ti

Figure 5

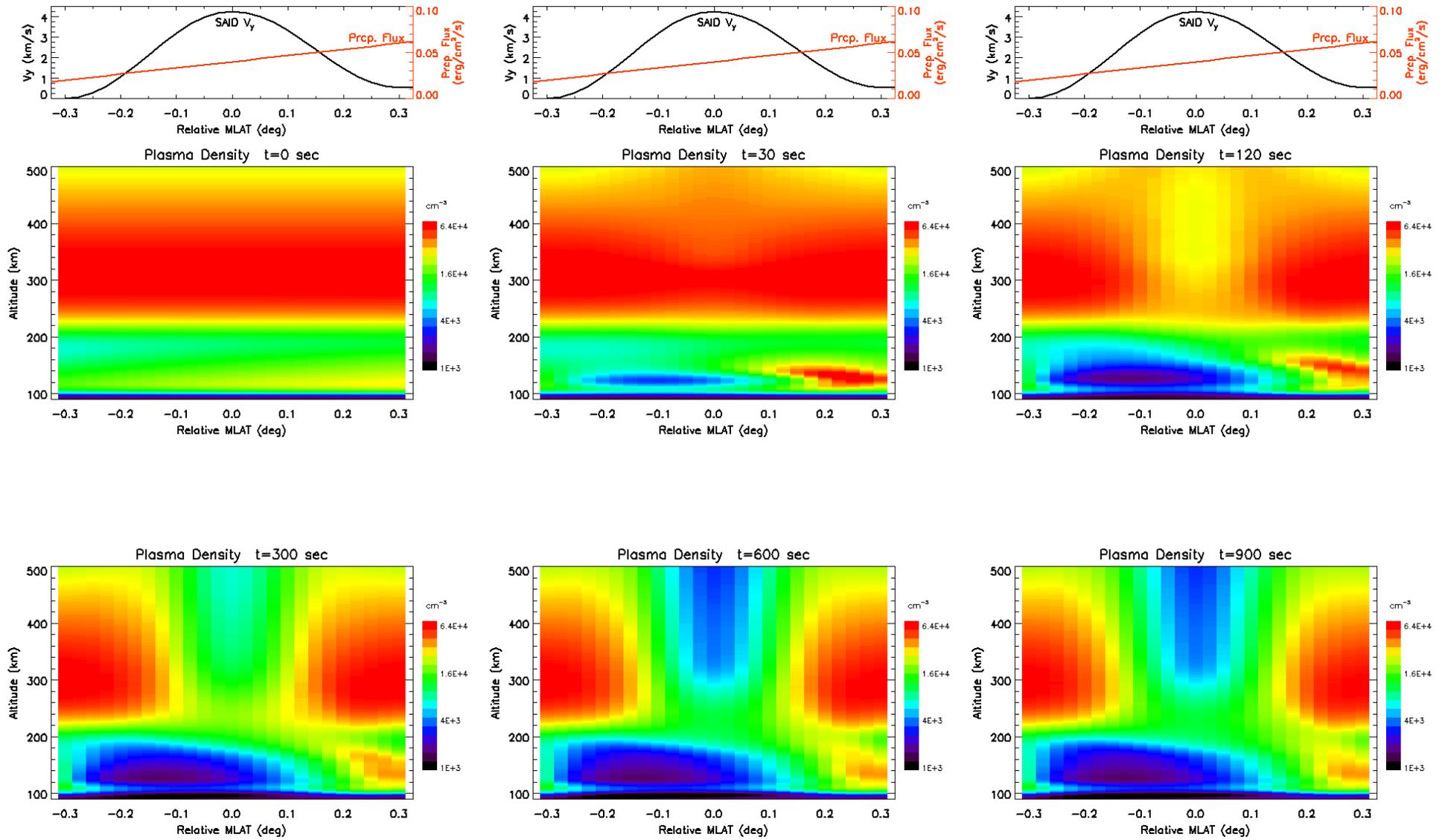


Figure 5. Same as Figure 3 but for Ne

Figure 6

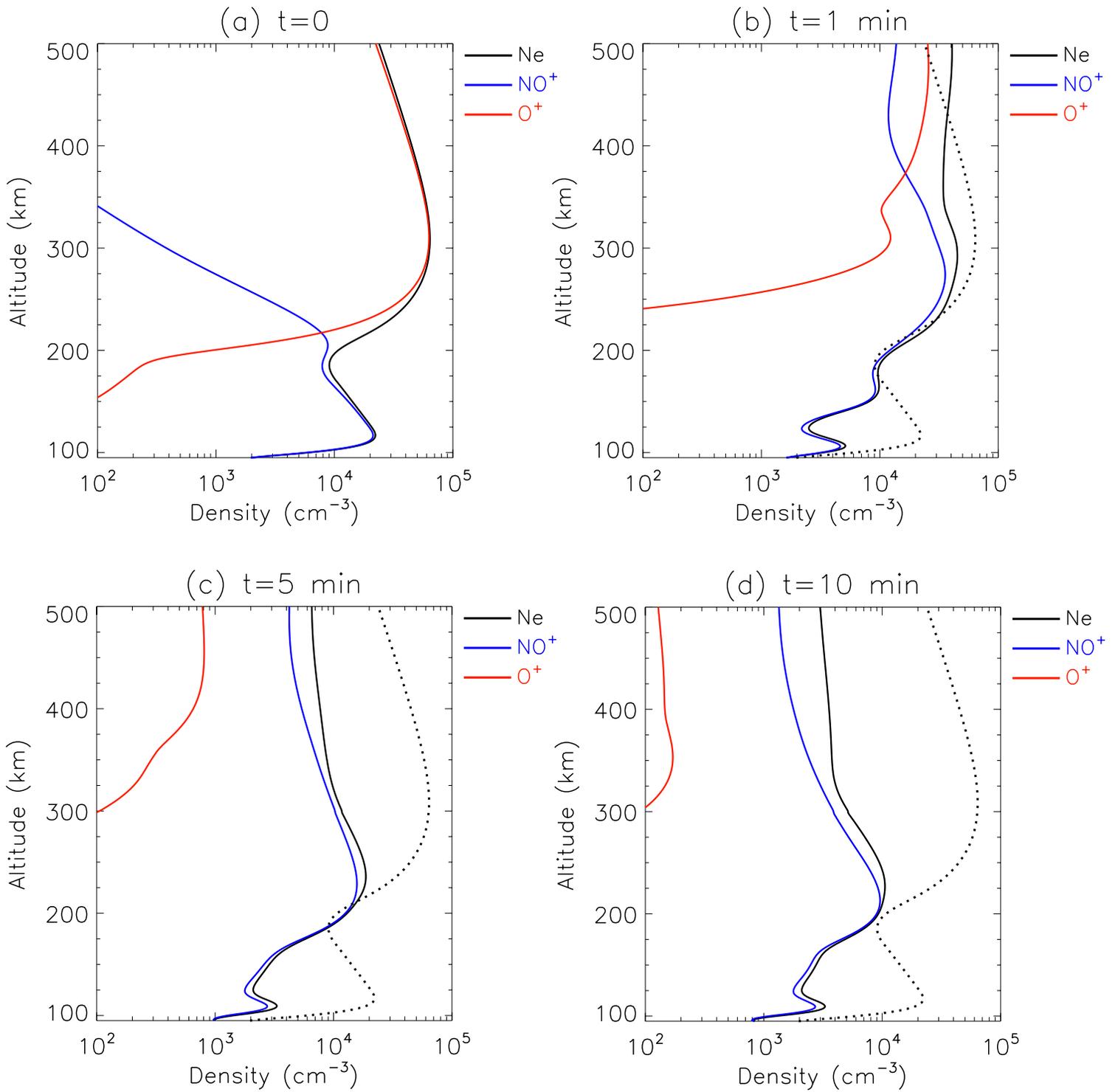


Figure 6. Altitudinal profile of densities of Ne, NO<sup>+</sup> and O<sup>+</sup> at the center of SAID at (a) t=0; (b) t=1 min; (c) t=5 min; and (d) t=10 min. In subfigures (b)-(d), The initial (t=0) Ne profile is plotted in dotted line for reference

Figure 7

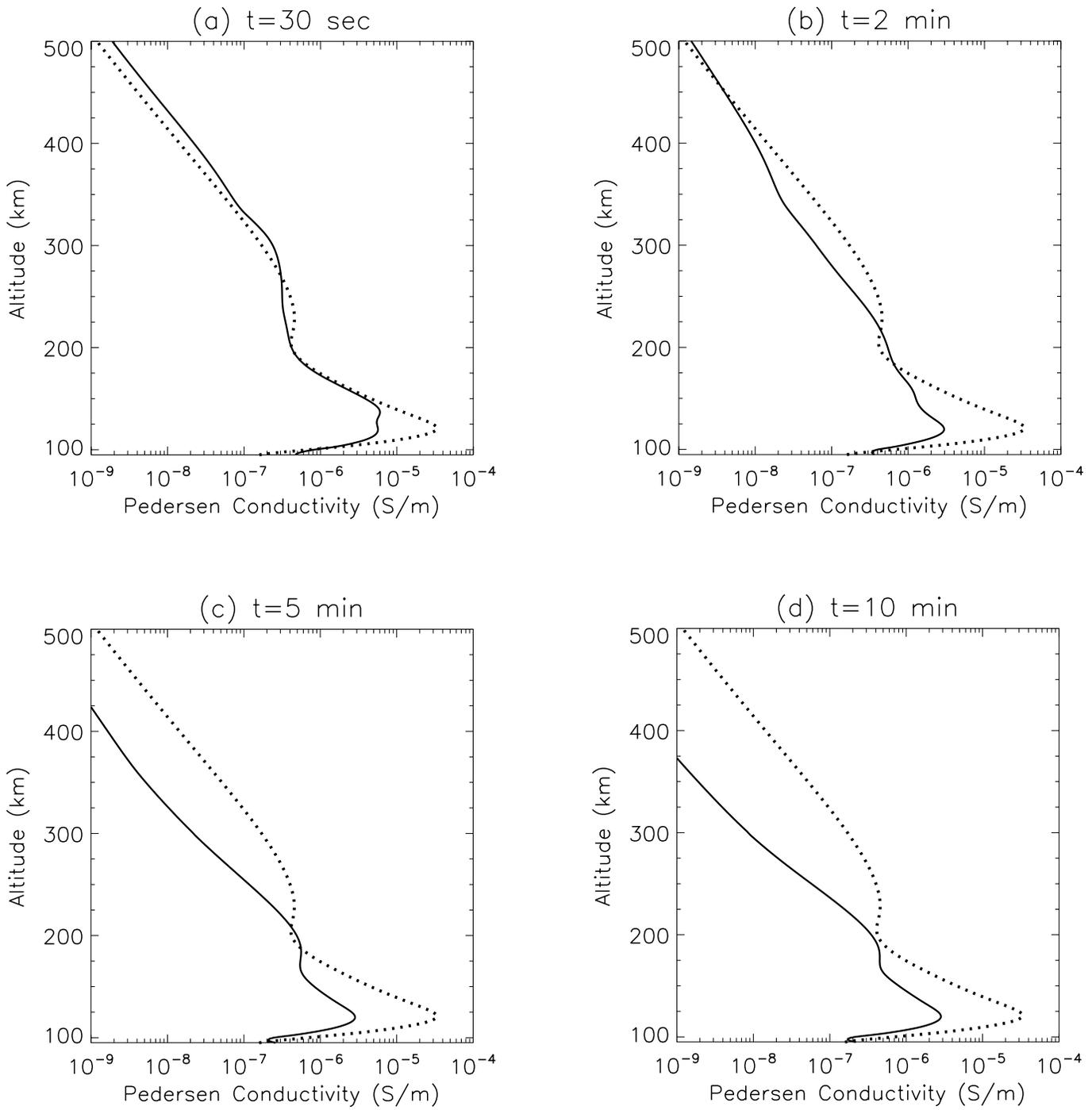


Figure 7. Altitudinal profile of Pedersen conductivity at the center of SAID at (a)  $t=30$  sec; (b)  $t=2$  min; (c)  $t=5$  min; and (d)  $t=10$  min. The initial ( $t=0$ ) Pedersen conductivity profile is plotted in dotted line for reference

Figure 8

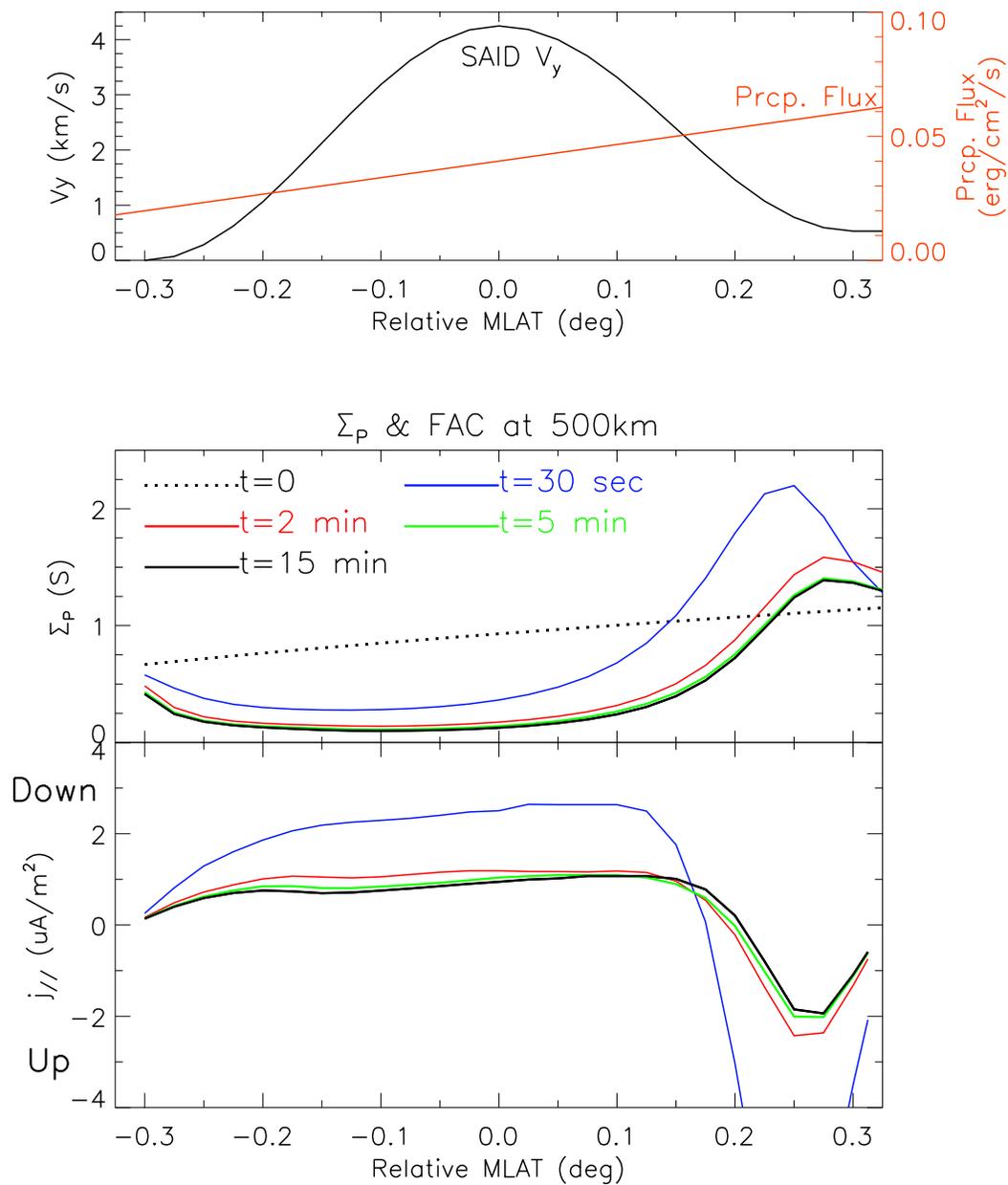


Figure 8. latitudinal profiles of Pedersen conductance and FAC at different elapsed times. The latitudinal profiles of SAID and the background precipitation are plotted on top for reference

Figure 9

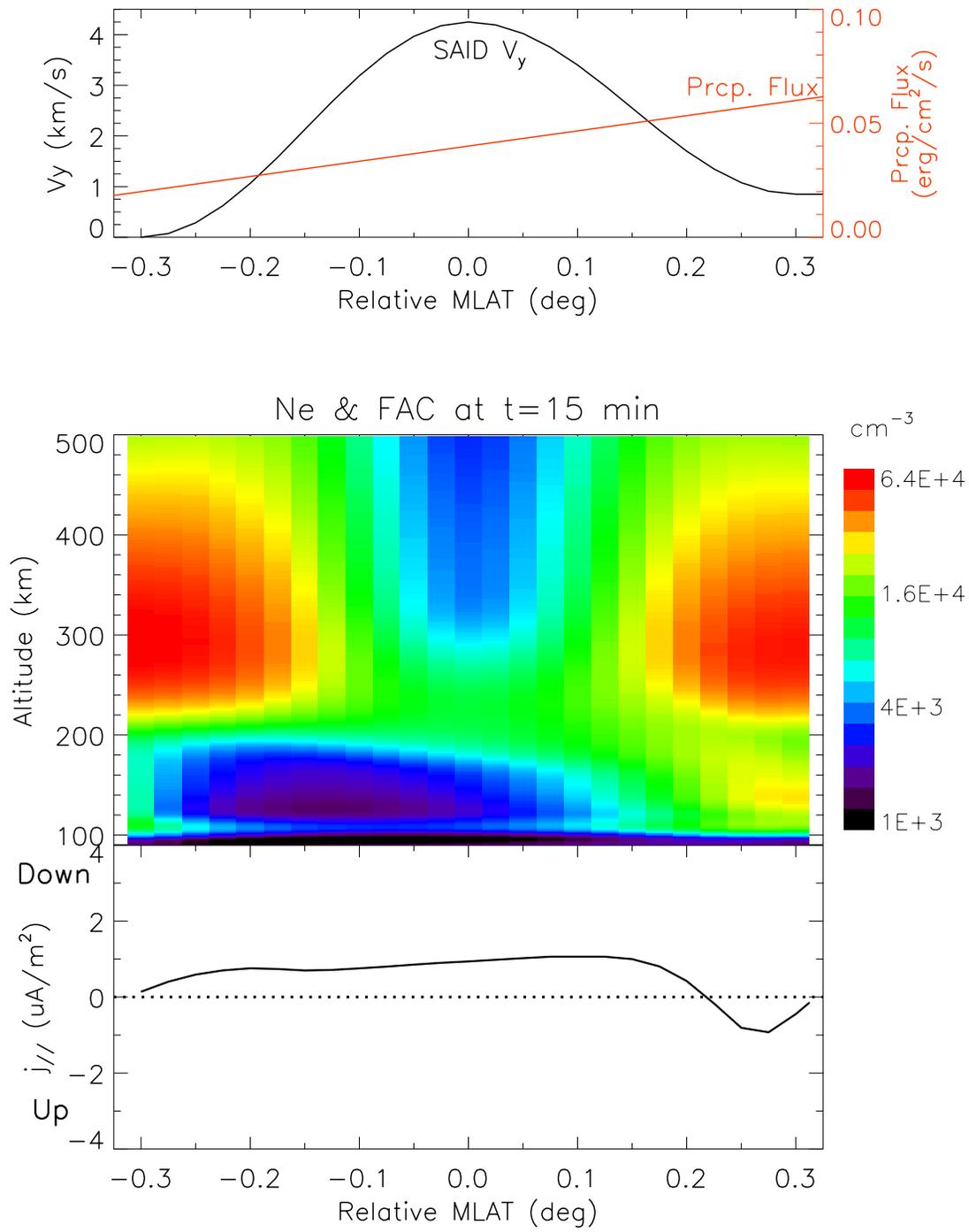


Figure 9. Latitude-altitude profile of Ne, and the latitudinal profile of FAC at t=15 min for a new run with higher flow poleward of SAID. The latitudinal profiles of SAID and the background precipitation are plotted on top for reference

Figure 10

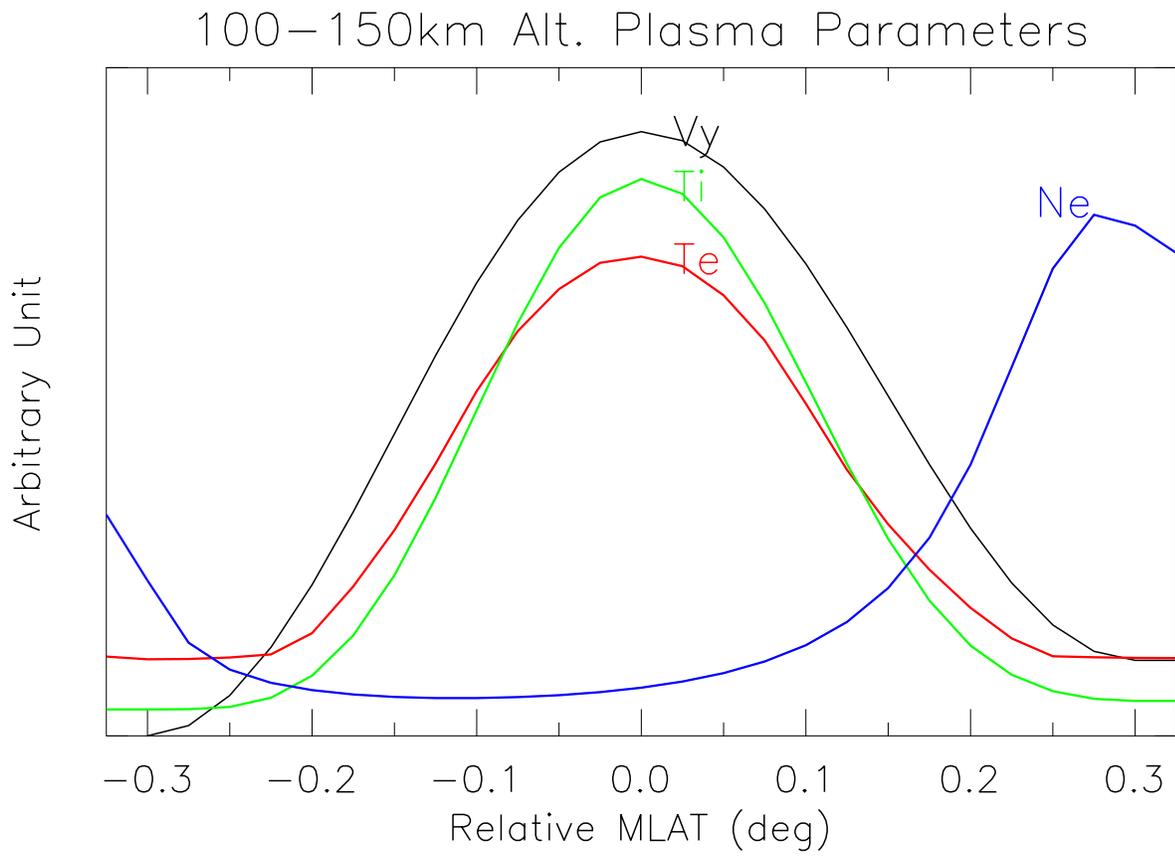


Figure 10. Latitudinal profiles of plasma flows, Te, Ti, and Ne, averaged over 100-150 km altitudes.