

1 **Timelines of plume characteristics of the Hunga Tonga-Hunga Ha'apai**
2 **eruption sequence from 19 December 2021 to 16 January 2022: Himawari-8**
3 **observations**
4

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29 **Preface:**

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31 Hunga Tonga-Hunga Ha'apai eruption on 15 January 2022 recorded as one of the most explosive
32 submarine eruptions in modern times.

33

34 **Abstract:**

35

36 The 15 January 2022 shallow water eruption of Hunga Tonga-Hunga Ha'apai (HTHH) volcano
37 was remarkable, in part, because it produced the highest plume observed in the advanced satellite
38 era. The Himawari-8 geostationary satellite captured this HTHH eruption well and provides a
39 unique opportunity to track the evolution (plume and umbrella cloud height) of a large volcanic
40 eruption through time. The 15 January 2022 eruption was preceded by eruptions in late
41 December 2021 and 13 January 2022, for which we have also assessed plume characteristics. In
42 addition to umbrella cloud height, we use Himawari-8 data to determine the radial expansion of
43 the umbrella clouds and volumetric flow rates (VFR).

44

45 The altitude of umbrella clouds preceding 15 January 2022 reached ~16-18 km, crossing into the
46 stratosphere. On the day of the large climactic eruption (15 January 2022), the umbrella clouds
47 attained a height close to 31 km. We observed two powerful explosive eruptions on 15 January at
48 an interval of four hours, indicated by the minimum 11.2 μ m brightness temperature occurring at
49 04:10 UTC (172 K) and 08:10 UTC (174 K). On 15 January 2022, beyond 05:30 UTC, the
50 strong westward propagation of upper umbrella (U_B) clouds at ~31 km enabled the visibility of
51 lower umbrella (U_A) clouds at ~18 km. We find that U_A is mainly dominant with ash, whereas
52 U_B is dominant with thick ice clouds based on brightness temperature difference analysis. The
53 satellite-derived VFR for 15 January 2022 is around $5.00 \times 10^{11} \text{ m}^3 \text{ s}^{-1}$, nearly two orders of
54 magnitude higher than that estimated on 19 December 2021 and 13 January 2022 eruptions.

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59 **Main Text**

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61 On 15 January 2022, at 04:00 UTC, the shallow water Hunga Tonga-Hunga Ha'apai (referred as,
62 "HTHH") (175.38°W, 20.57°S) volcano, constituted one of the century's most explosive
63 submarine eruptions to our knowledge. The ashfall, tsunamis, and shock waves produced by the
64 eruption severely affected the Kingdom of Tonga and surrounding regions¹. Shock waves
65 produced by the HTHH eruption circled multiple times around the globe² and the overshooting
66 region of the plume reached around 55-58 km^{3,4}. The quantification of the plume height and
67 umbrella cloud height (height of dominant level of radial spreading of umbrella clouds) is
68 essential for understanding the physical processes associated with this explosive eruption and
69 linking plume behavior with other data sets (e.g., seismic, atmospheric, infrasound,
70 hydroacoustic, lightning). We use the Himawari-8 geostationary satellite⁵ (full disk data at 10-
71 min interval) to track the timelines of grid-averaged brightness temperatures of the umbrella
72 clouds measured at the wavelength of 11.2 μ m (BT_{avg}), which we then convert to cloud height,
73 over 19 Dec 2021–16 Jan 2022. We also use minimum brightness temperatures at 11.2 μ m
74 (BT_{min}) to determine when plume overshoot occurs. Because the 15 January 2022 HTHH
75 eruption occurred after an approximately month-long period of eruptive activity that started on
76 19 December 2021, an assessment of this full eruptive sequence is critical for understanding why
77 the preceding HTHH submarine eruptions were not as explosive. We also measure the radial
78 expansion of umbrella clouds as a function of time to calculate volumetric flow rate (VFR, in the
79 atmosphere) for three distinct eruptions during this period. These volumetric flow rates include
80 ash but may be dominated by the volumes of water and gas in the plumes.

81

82 **a. Initial eruption on 19 Dec 2021**

83

84 The recent eruptive phase of HTHH began on 19 Dec 2021 at 20:40 with the creation of a water
85 and ash-rich plume that rose to an altitude of ~17 km (crossing above mean tropopause height at
86 ~16 km; Figure 1e; violet shaded region). This initial eruption subsided on 20 Dec 2021 between
87 04:30-05:00 UTC, as inferred from the pulsed brightness temperature at 11.2 μ m ($BT_{11.2\mu m}$)
88 emanating from the center of the volcano. Umbrella clouds from this event laterally spread in the
89 northeastward direction, due to prevailing westerly (eastward) wind in the upper troposphere (as

90 seen from ERA5), covering an area of around 22 thousand square km within the first 150 min
91 (Figure 1g). Using the umbrella cloud area over the first 150 minutes of the eruption on 19 Dec
92 2021, and assuming spreading at the level of neutral buoyancy^{6,7}, the VFR was found to be ~ 3.91
93 $\times 10^9 \text{ m}^3\text{s}^{-1}$ (Figure 1g).

94

95 We use the brightness temperature difference between thermal infrared bands at $11.2\mu\text{m}$ and 12.4
96 μm ($\text{BTD}_{11.2-12.4\mu\text{m}}$) to assess the plume's composition. On 19 Dec 2021 at 22:50 UTC, $\text{BTD}_{11.2-}$
97 $12.4\mu\text{m}$ is negative for the umbrella clouds spreading in the north-east direction, implying the
98 presence of an ash-dominant plume. But at the edge of the umbrella clouds, the near zero value
99 of $\text{BTD}_{11.2-12.4\mu\text{m}}$ indicates the prevailing thick ice clouds ($\text{BT}_{11.2\mu\text{m}}$ at $\sim 230\text{K}$).

100

101 Between 20th and 31st Dec 2021, we observe intermittent fluctuations in $\text{BT}_{11.2\mu\text{m}}$ around the
102 volcano (within an area of about 3000 km^2) indicative of lower intensity sporadic eruptions.
103 During this period, the plumes moved towards the northeast and the averaged plume top heights
104 within grid-box varied between 8 and 12 km. The presence of meteorological clouds during 01-
105 12 Jan 2022 hindered clear observations of brightness temperature changes related to volcanic
106 activity. However, we do not see evidence for eruptions that surpassed the different
107 meteorological clouds during this time. The ground-based observations would be more useful to
108 assess the weak and sporadic volcanic activity during 01-12 Jan 2022.

109

110 **b. Major eruption on 13 Jan 2022**

111

112 With the clearing of the meteorological clouds, we could use Himawari-8 to observe a major
113 eruption on 13 Jan 2022. We see the major surge and fluctuations in BT_{min} between 13 Jan 2022
114 at 15:30 UTC and 14 Jan 2022 at 14:50 UTC, where its minimum value reaches around 174.5 K
115 at 23:30 UTC (Figure 1f; light-blue shaded region). The plume spreads in the north-eastward
116 direction following the upper tropospheric eastward moving wind, and the umbrella clouds
117 covered an area of about 30 thousand square km within the first 150 min (Figure 1g). The
118 altitude of umbrella clouds reached $\sim 18.5 \text{ km}$, crossing the tropopause height (Figure 1f; light-
119 blue shaded region). For the initial 150 min of eruption on 13 Jan 2022, our estimation of VFR

120 was found to be $\sim 5.13 \times 10^9 \text{ m}^3 \text{ s}^{-1}$. The VFR on 13 Jan 2022 is almost 30% higher than the
121 corresponding value on 19 Dec 2021.

122

123 **c. Climactic eruption on 15 Jan 2022**

124

125 The climactic stage of the eruption began on 15 January 2022, at 04:00 UTC, was observed in
126 $11.2\mu\text{m}$ brightness temperature (Figure 1f; orange shaded region). This timing of the initial
127 eruption at 04:00 UTC was also confirmed with the true color imagery. Within forty minutes (for
128 instance, at 04:50 UTC, Fig. 1c), the umbrella cloud had expanded around the volcano in a near-
129 circular pattern. We find that the umbrella cloud had an initial height of ~ 31.5 km, which is less
130 than the overshoot height around 55-58 km^{3,4} [sky-blue dot in Fig. 1f]. The average umbrella
131 cloud height declines to ~ 18 km over a period of ~ 11 hours (Fig. 1f). As stated above, plume
132 overshoot can be identified using BT_{min} values. For example, the BT_{min} value at eruption
133 initiation (04:00 UTC) was 172K, which is colder than any point in the atmosphere (Figure 1g,f).
134 We identify a second instance of plume overshoot between 08:10-08:30 UTC as shown by a
135 second dip in BT_{min} and that we confirm with GOES data (indicated by the grey line in the
136 orange shaded region in Figure 1f). We interpret the second overshoot to indicate a second
137 eruptive pulse.

138

139 **Two umbrella-clouds**

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141 We identify a second lower-altitude (~ 18.5 km, 1-1.5 km above the tropopause) umbrella cloud
142 that becomes visible at 05:30 UTC as the upper umbrella cloud moves westward, presumably
143 due to advection by stratospheric winds (Figure 1d). The lower umbrella cloud, U_A , has a distinct
144 brightness temperature relative to the upper umbrella cloud: U_A ($BT < 210$ K) and U_B ($215\text{K} <$
145 $BT < 235\text{K}$) (Figure 1d; indicated by two contour labels). This is further established based on the
146 probability distribution function (PDF) of $BT_{11.2\mu\text{m}}$ on 15 Jan 2022 at 08:40 UTC in Figure 1j,
147 which shows the two peaks at around 210 K and 220K, representing the umbrella clouds U_A and
148 U_B .

149

150 On 15 Jan 2022, between 04:10-04:30 UTC, we observed that significant ash is present in the
151 initial plume based on the negative value of $\text{BTD}_{11.2-12.4\mu\text{m}}$. As time progresses, $\text{BTD}_{11.2-12.4\mu\text{m}}$ of
152 the upper and westward spreading umbrella cloud (U_B) evolves to be near-zero or slightly
153 positive indicating a thick ice dominant U_B . However, the eastward umbrella (U_A), especially
154 near the edge, has a negative value indicating the ash dominance. The U_B covered an area of
155 about 175 thousand square km within the initial 150 min (Figure 1i).

156
157 The satellite-based VFR for the upper umbrella cloud, U_B (contour levels between 215 and 235
158 K), is estimated to be $5.00 \times 10^{11} \text{ m}^3\text{s}^{-1}$ for the initial 50 min of eruption. Note that the model fit
159 to the data is poor, which brings into question the assumption of gravitationally driven spread at
160 the level of neutral buoyancy. Still, the VFR on 15 Jan 2022 is around two orders of magnitude
161 higher than the corresponding VFR on 19 Dec 2021 and 13 Jan 2022.

162

163 **Concluding remarks:**

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165 The 15 January 2022 eruption of HTHH was preceded by approximately a month of volcanic
166 activity including two eruptions that produced stratospheric plumes. The major findings are
167 summarized below:

168

169 1. The initial eruption occurred on 19 Dec at around 20:40 UTC for about 9 hours until 20
170 Dec 2021 between 04:30-05:00 UTC; the umbrella clouds reached an altitude of ~ 17 km
171 and crossed into the stratosphere. The satellite-based VFR for the Dec 19 event is $\sim 3.91 \times$
172 $10^9 \text{ m}^3\text{s}^{-1}$. Between Dec 20 and 31 Dec 2021, we find the production of weak plumes that
173 reached 8-12 km. During 01-12 Jan 2022, we did not observe volcanic
174 plumes. However, meteorological clouds may have hindered the ability to interpret small
175 plumes.

176

177 2. A major eruption occurred on 13 Jan 2022 at 15:30 UTC and where the minimum value
178 of $\text{BT}_{11.2\mu\text{m}}$ reached approximately 174 K. The umbrella clouds reached an altitude of
179 ~ 17.5 - 18.5 km (above tropopause height). The VFR attained a value of $\sim 5.1 \times 10^9 \text{ m}^3\text{s}^{-1}$.

180

- 181 3. On 15 Jan 2022 at 04:00 UTC, we observe the large climactic eruption. The altitude of
182 umbrella clouds was stratospheric in nature, attaining an altitude around ~ 31 km. The
183 satellite-derived VFR for 15 Jan 2022 is $5.00 \times 10^{11} \text{ m}^3\text{s}^{-1}$, nearly two orders of magnitude
184 higher than that estimated on 19 Dec 2021 and 13 Jan 2022 eruptions. We observe a
185 second eruptive pulse at $\sim 08:10$ UTC, four hours after the start of the eruption, that
186 produces plume overshoot. This is inferred from the coldest $BT_{11.2\mu\text{m}}$ occurring at $\sim 08:10$
187 UTC with a value of 174 K.
- 188
- 189 4. We identify two distinct umbrella clouds within the 15 Jan 2022 plume. The upper cloud,
190 U_B , is at an altitude of ~ 31 km. The lower cloud, U_A , spreads approximately at the level
191 of the tropopause (~ 18 km) and only becomes visible at 05:30 UTC as the upper umbrella
192 cloud is advected westward, presumably due to the easterly wind in the stratosphere near
193 30 hPa. We find that U_A is mainly composed of ash as indicated by negative value
194 $BTD_{11.2-12.4\mu\text{m}}$, whereas U_B is composed of thick ice clouds as revealed from near-zero or
195 a slightly positive value of $BTD_{11.2-12.4\mu\text{m}}$.
- 196

197 Results on the timelines of overshooting volcanic plumes (based on BT_{min}) and umbrella heights
198 (based on BT_{avg}) during HTHH eruption suggest that the high spatial and temporal resolution
199 satellite data play an important role in advancing our understanding of eruption history and their
200 implementation in plume modeling. Observations reveal two explosive eruptions observed on 15
201 Jan 2022 at the interval of four hours – an aspect of the eruption sequence not yet recognized.
202 These observations lead to the fundamental question about what causes multiple eruptive pulses,
203 a topic warrants investigation. In this context, a future direction could be comparing the
204 occurrence of these two strong explosive eruptions against other data sets (e.g., seismic). During
205 the eruption, we also find the formation of two distinct umbrella clouds, a lower one dominated
206 by ash that spreads at the tropopause, and an upper cloud that is dominated by ice (as inferred
207 from $BTD_{11.2-12.4\mu\text{m}}$). An idealized simulation of this submarine eruption using a plume dynamic
208 model^{8,9} might help in understanding the series of processes controlling the dynamics of thick
209 ice-rich and ash-rich umbrella clouds with an overshooting plume height at ~ 58 km^{3,4}.

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261

262 **Author contributions:**

263

264 AG analyzed the data and developed it with RB, KEF and TM. AG, RB, KEF, TM contributed to
265 conceptual development of this work. KEF, RB, TM supervised this research. KEF and RB
266 obtained NASA funding. AG drafted the original manuscript. The manuscript was reviewed and
267 edited by KEF, TM and RB.

268

269 **Competing interests:** Authors declare that they have no competing interests.

270

271 **Data and materials availability:**

272 The Himawari-8 data used in this study are available in public domain and it can be also
273 obtained from <https://registry.opendata.aws/noaa-himawari/>. Two supplementary movies of
274 BT_{11.2μm} and BT_{D11.2-12.4μm} and .csv related to Figures 1e,f (BT_{min}, BT_{avg}, Plume/Umbrella
275 height) can be accessed using this link <https://zenodo.org/record/6331115#collapseCitations>.

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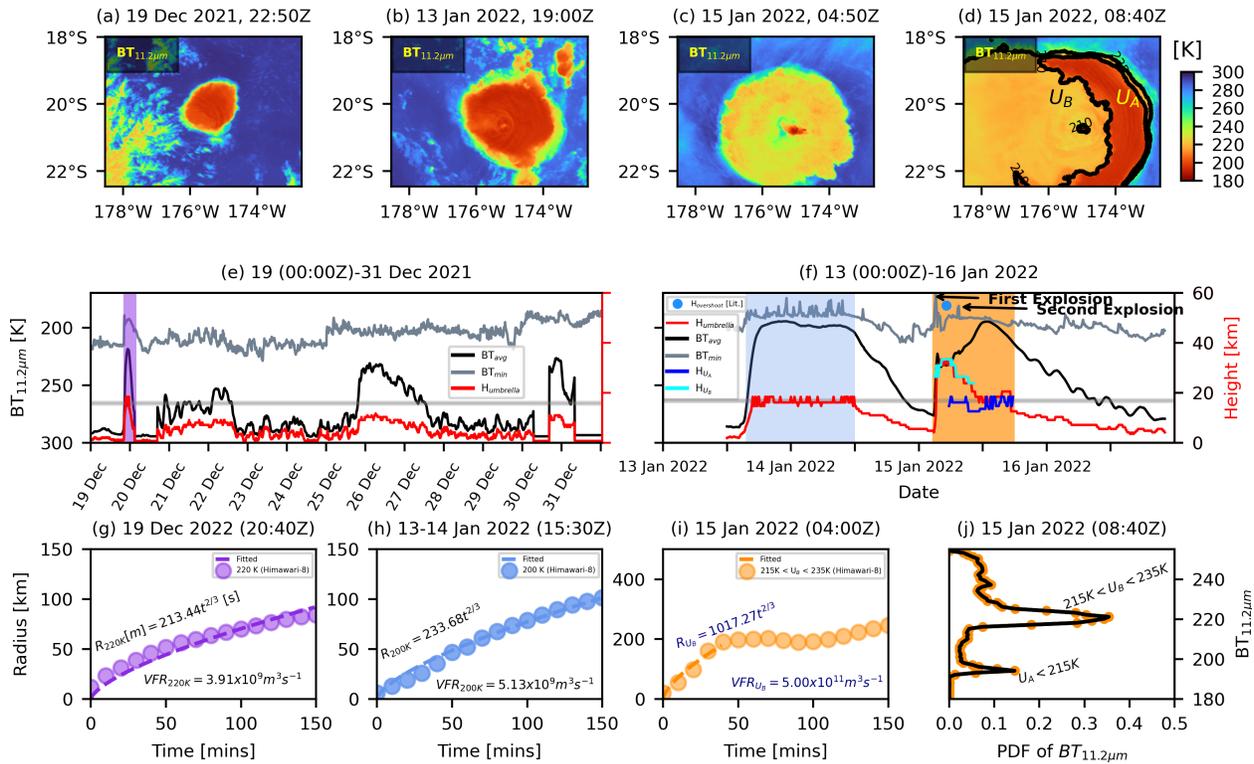
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282 **Figure:**



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285 **Figure 1: Upper panels:** (a) Himawari-8 observed brightness temperature at 11.2 microns
 286 (BT_{11.2μm}) centered around Hunga Tonga-Hunga Ha'apai (HTHH) (175.38°W, 20.57°S)
 287 submarine volcano on 19 December (Dec) 2021 at 22:50 UTC. Panel (b), (c) and (d) are similar
 288 to panel (a) but for 13 January (Jan) 2022 at 19:00 UTC, 15 Jan 2022 at 04:50 UTC, 15 Jan 2022
 289 at 08:40 UTC, respectively. The colorbar represents the brightness temperature measured in
 290 Kelvin [K].

291

292 **Middle panels:** (e) the black line (BT_{avg}) indicates the timelines of the domain averaged
 293 (174.953°W–175.842°W; 20.6005°S–20.247°S) BT_{11.2μm}. The redline (H_{umbrella}) indicates the
 294 satellite-derived umbrella height based on the BT_{avg} value and ERA5 data above. The grey line
 295 represents the minimum BT_{11.2μm} (BT_{min}) covering 400 by 300 pixels centered over HTHH
 296 volcano during 19-31 Dec 2021. The light grey horizontal bar around ~16 km is for the mean
 297 tropopause height during 19-31 Dec 2021 estimated using ERA5. (f) The black, red, and grey
 298 lines represent the same quantities as in panel e. The blue and cyan lines indicate contour U_A and
 299 contour U_B umbrella heights (depicted in panel d) for the eruption on 15 January 2022. The

300 contour U_A is outlined for $BT_{11.2\mu m} < 215K$, and contour U_B is outlined for $BT_{11.2\mu m} < 215K$ and
301 $BT_{11.2\mu m} > 235K$. Skyblue dot indicates the overshooting plume height as shown by preprints
302 online^{3,4}. The light grey horizontal bar line is again the same as (e). Both the first and second
303 explosions on 15 January at the interval of four hours are highlighted by the black arrows
304 (represented by the coldest $BT_{11.2\mu m}$ value).

305

306 **Bottom panels:** (g) on 19 December 2021 (initial eruption starts around 20:40 UTC), the radial
307 change of umbrella height as a function of the initial 150 minutes is described by violet dots
308 (representing the highlighted violet shaded region in panel e). The dashed brown line in panel (g)
309 indicates the polynomial fitting for the initial 150 min contour labeled at 220K. The R (in meter)
310 and t (in sec) relations and volumetric flow rate (VFR) values are described by the inset text at
311 different $BT_{11.2\mu m}$ contour level. (h) Same as (g) but for light sky-blue shaded regions in panel (f)
312 depicting the 13-14 January 2021 eruption time (starting around 15:30 UTC). In this case, the
313 polynomial fitting is performed for the 200K $BT_{11.2\mu m}$ value. The R and VFR represent the same
314 as in (g). (i) Same as (g) but for an orange shaded region in panel (f) of the greatest explosive
315 eruption on 15 January 2022 starting at 04:00 UTC. (j) The probability distribution function of
316 $BT_{11.2\mu m}$ on 15 January 2022 at 08:40 UTC, when two umbrella clouds are quite distinctly
317 appearing (as seen in Fig. 1d).

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330 **Materials and Methods**

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332 **Umbrella Cloud heights**

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334 We use atmospheric window channels (11.2 μm and 12.4 μm) observations from Himawari-8
335 geostationary satellite to determine the average altitude of HTHH plumes and umbrella clouds
336 from 19 Dec 2021 to 16 Jan 2022 (red lines in Fig. 1e and 1f). We take domain average
337 (174.953°W–175.842°W; 20.6005°S–20.247°S, $\sim 3000 \text{ km}^2$ centered over HTHH) brightness
338 temperature at 11.2 μm (BT_{avg}) and convert the BT_{avg} into the height based ERA5 data¹⁰. This
339 method allows us to determine the altitude of the cloud tops associated with volcano eruption
340 provided that the averaging domain is devoid of meteorological clouds contamination as it can
341 influence the BT_{avg} values.

342

343 For some overpasses of CALIPSO datasets¹¹, we also compare the plume height estimations with
344 observations from space-borne active sensors to validate our method and results (Figure not
345 shown).

346

347 To identify when plume overshoot happens, we estimate the minimum $\text{BT}_{11.2\mu\text{m}}$ (BT_{min}) values
348 within a domain of 400 x 300 pixels enclosing the vent site. Each pixel of full disk Himawari-8
349 data has a 2 km resolution. In this BT_{min} analysis, the cold pixels indicate that a portion of the
350 plume rose higher and are consistent with the occurrence of overshoot (grey line in Figure 1e,f).

351

352 **Differentiating U_A and U_B**

353

354 We identified two umbrella clouds on 15 Jan 2022 using brightness temperature contour levels
355 fixed at $\text{BT}_{11.2\mu\text{m}} < 215 \text{ K}$ (tropospheric umbrella; U_A) and $215\text{K} < \text{BT}_{11.2\mu\text{m}} < 235\text{K}$ (stratospheric
356 umbrella; U_B) within a domain of 400 x 300 pixels. We also evaluate the normalized probability
357 distribution function (PDF) of $\text{BT}_{11.2\mu\text{m}}$ as a function of time for the above domain to characterize
358 the peak $\text{BT}_{11.2\mu\text{m}}$ for U_A and U_B . If PDF is zero for the condition of U_A , then it is likely that U_B is
359 dominant (as observed from cyan color in Fig. 1f) and vice-versa. Two peaks in Fig. 1j depict
360 two umbrella clouds at 08:40 UTC on 15 Jan 2022. Estimation of umbrella clouds in this fashion

361 is useful to characterize the composition of plumes. Based on $BTD_{11.2-12.4\mu m}$ estimation, we show
362 above that the U_A is mostly ash rich (especially near the edge) and U_B is dominant with thick ice
363 clouds.

364

365 **Volumetric Flow Rate Estimates**

366

367 We use a 3D distribution of brightness temperature data to assign each pixel value with a unique
368 index of zero and nonzero value for a given threshold condition of brightness temperature, and
369 we then apply histogram to estimate the time-series of areal extents of umbrella clouds. The
370 threshold condition of brightness temperature is given based on the maximum PDF of $BT_{11.2\mu m}$.
371 The time-series of areal extents (A) of umbrella clouds is then converted into radial extent (R),

372 using $R = \sqrt{A/\pi}$ as the umbrella was elongated in one direction (eastward on 19 Dec 2021 and

373 westward during other three events) due to prevailing wind in the upper troposphere and

374 stratosphere. For estimating volumetric flow rate (VFR), we use the parameterization equation^{6,12}

375 $R = \left(3\lambda QN/2\pi\right)^{1/3} t^{2/3}$ (where λ is a constant that is approximately 0.2, Q is the volume flux

376 and N is the brunt-Vaisala frequency, and t is time) to fit with our measurements of spherical-

377 equivalent plume top radius through time for the initial 50-150 min (Figure 1g-h). Also, the brunt

378 Vaisala frequency (N) is taken as 0.026 near tropopause and 0.022 at around 30 km in the

379 stratospheric region as evaluated using ERA5 reanalysis data.