

1 **Finding Magnetopause Standoff Distance using a Soft**
2 **X-ray Imager – Part 1: Magnetospheric masking**

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9 **Key Points:**

- 10 • The SMILE mission will carry Soft X-ray Imager onboard
11 • Magnetospheric masking methods separate the magnetosphere from the magne-
12 tosheath and cusps

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Abstract

The magnetopause standoff distance characterizes global magnetospheric compression and deformation in response to changes in the solar wind dynamic pressure and interplanetary magnetic field orientation. We cannot derive this parameter from in-situ spacecraft measurements. However, time-series of the magnetopause standoff distance can be obtained in the near future using observations by soft X-ray imagers. In two companion papers, we describe methods of finding the standoff distance from X-ray images. In Part 1, we present the results of MHD simulations which we use for the calculation of the X-ray emissivity in the magnetosheath and cusps. Some MHD models predict relatively high density in the magnetosphere, larger than observed in the data. Correcting this, we develop magnetospheric masking methods to separate the magnetosphere from the magnetosheath and cusps. We simulate the X-ray emissivity in the magnetosheath for different solar wind conditions and dipole tilts.

Plain Language Summary

The highly dynamic solar wind continuously bombards the Earth's magnetosphere, which changes shape in response. The magnetopause is the outer boundary of the magnetosphere, which is known to move. We are limited in our knowledge of the overall shape of the magnetopause, as current in situ measurements can only tell us about any change in the magnetopause at one specific location. Spacecraft carrying soft X-ray imagers, however, will soon revolutionise our understanding by monitoring large areas of the magnetopause as the solar wind varies. In this first of a series of two papers, we simulate X-ray emissions in the vicinity of the Earth using two magnetohydrodynamic models, and for two case studies with vastly different incoming solar wind conditions. In a subsequent paper, we examine methods how to extract the magnetopause shape from the simulated X-ray images.

1 Introduction

The Earth's magnetopause is the boundary between the geomagnetic and interplanetary magnetic fields. The magnetopause standoff distance, i.e. the distance from the Earth to the subsolar magnetopause, implicitly characterizes the magnetospheric activity. A more compressed magnetosphere results in stronger magnetospheric-ionospheric currents and correspondingly higher magnetospheric activity. When the magnetopause crosses geosynchronous orbit, spacecraft that rely upon observations of the Earth's magnetic field to determine their orientation may lose this information. Therefore we would like better predict the magnetopause position for variable solar wind conditions.

The magnetopause standoff distance is usually determined by the pressure balance condition. Up to now, we have been able to find the magnetopause position for a given solar wind condition by three methods. First, we can use direct in-situ measurements. This method gives us the exact magnetopause position, but only in one or several local points and at the time when the spacecraft crosses the magnetopause. Second, we can apply empirical magnetopause models (e.g., Dmitriev et al., 2016; Lin et al., 2010; Petrinec & Russell, 1996; Shue et al., 1998; Sibeck et al., 1991; Wang et al., 2013). Empirical models are usually based on large datasets of magnetopause crossings and use predefined functional forms to describe an expected magnetopause shape. However, any fixed function may not perfectly reproduce the real magnetopause shape. Besides, we do not know exactly the list of input parameters which may influence the magnetopause position since this list could possibly include characteristics of the magnetospheric currents (e.g. the ring current, magnetospheric-ionospheric region 1 and 2 currents, the cross-tail current) in addition to the upstream solar wind conditions. Moreover, some solar wind parameters (e.g., the interplanetary magnetic field (IMF) Bx component) may change the total pressure upstream of the magnetopause (e.g., Archer et al., 2015; Samsonov et al.,

2017), but they are not included in the empirical models. Third, the magnetopause position can be found from results of global magnetohydrodynamic (MHD) as well as hybrid or kinetic simulations. However, numerical models have some limitations, for example MHD models do not simulate self-consistently some magnetospheric currents (e.g. the ring current) and often rely upon a possibly unphysical numerical resistivity. Therefore each of the three methods is not perfect for finding the magnetopause standoff distance and shape. This is especially true for extreme solar wind conditions because we have a very limited number of observations at these times and models may be less accurate.

Gordeev et al. (2015); Samsonov et al. (2016) showed that the simulated magnetopause positions obtained for typical solar wind conditions differ between several global MHD models. For example, the magnetopause standoff distance predicted by the Lyon-Fedder-Mobarry (LFM) and Open Geospace General Circulation Model (Open GGCM) models is 0.5-1.5 R_E less (i.e., closer to the Earth) than that in the Space Weather Modeling Framework (SWMF) model for the same solar wind conditions. There are several reasons for the difference. Firstly, the magnetopause position is determined by the pressure balance condition. The total pressure on the inner side of magnetopause is mostly the magnetic pressure which consists of the dipole field and the superposition of magnetic fields of the magnetospheric currents, like the Chapman-Ferraro current, the ring current, the magnetospheric-ionospheric region 1 current, and to a lesser extent the cross-tail current (Tsyganenko & Sibeck, 1994). Although the magnetospheric thermal pressure is generally insignificant compared to the magnetic pressure, it can also make some input in the pressure balance. Different MHD models use different boundary conditions at the inner numerical boundary (usually at radial distance of about 2-3 R_E from the Earth) which result in different magnetospheric densities and thermal pressure, in particular in the dayside magnetosphere. Beside that, some models try to include the ring current, and some do not. As a result, the total magnetospheric pressure varies between the models.

The total pressure on the outer side of magnetopause is often supposed to be equal to the solar wind dynamic pressure but this assumption is not very accurate. Samsonov et al. (2012) using MHD simulations calculated the variations of the total pressure (i.e., the sum of the dynamic, thermal and magnetic pressures) through the subsolar magnetosheath. Since the magnetosheath in the subsolar region is a layer with a width great than 1 R_E (typically about 3 R_E), the total pressure changes through the magnetosheath and these changes depend on the IMF orientation. Therefore differences in the inner boundary conditions and in the numerical methods between the MHD models may result in a different total pressure at the magnetopause which in turn influences the magnetopause position.

Moreover, the magnitudes of the magnetopause electric currents may depend on the numerical resolution of MHD models as well as on the type of diffusion term applied in the models (e.g., the total variation diminishing (TVD) slope limiter) and on the order of accuracy of the numerical scheme. The stronger the magnetopause currents near the subsolar point, the smaller the magnetopause standoff distance (Tsyganenko & Sibeck, 1994). This might be another reason which explains the differences between the models.

Empirical magnetopause models do not agree well with each other in predicting the magnetopause standoff distance either (Samsonov et al., 2016). Axisymmetric magnetopause models cannot reproduce the cusp indentations or the changes related to the dipole tilt effect, and most of them predict the subsolar magnetopause to be closer to the Earth than non-axisymmetric models for typical solar wind conditions and zero tilt angle. Case and Wild (2013) compared predictions of the axisymmetric and non-axisymmetric empirical models with Cluster magnetopause crossings (mostly in the high-latitude region) and found that, on average, the Petrinec and Russell (1996) and Shue et al. (1998)

116 models overestimate the radial distance to the magnetopause by $1 R_E$, while the Dmitriev
 117 and Suvorova (2000) and Lin et al. (2010) models underestimate it by $0.5 R_E$ and 0.25
 118 R_E , respectively. Moreover, two non-axisymmetric models (Lin et al., 2010; Wang et al.,
 119 2013) predicted different magnetopause positions on the Sun–Earth line and in the ter-
 120 minator plane (Samsonov et al., 2016). In general, the scattering of predictions of the
 121 magnetopause standoff distance for typical solar wind conditions between empirical and
 122 MHD models may be about $2 R_E$ (Samsonov et al., 2016).

123 Recent studies show that the Earth’s magnetosheath and cusps are sources of soft
 124 X-rays with energies from 0.05 to 2.0 keV (e.g., Carter et al., 2010; Cravens et al., 2001;
 125 Kuntz et al., 2015; Robertson et al., 2006). The soft X-rays result from the interaction
 126 between heavy solar wind ions (e.g. O^{7+}) and exospheric neutrals (hydrogen). Using a
 127 soft X-ray detector, we can produce two-dimensional (2-D) images of the X-rays around
 128 the magnetosphere. By processing these images we can find the magnetopause position
 129 (Branduardi-Raymont et al., 2012; Collier et al., 2012; Collier & Connor, 2018; Sibeck
 130 et al., 2018; Sun et al., 2019; Walsh et al., 2016). The Soft X-ray Imager (SXI) will travel
 131 onboard a joint space mission of the European Space Agency and the Chinese Academy
 132 of Sciences. The name of the mission is Solar wind Magnetosphere Ionosphere Link Ex-
 133 plorer (SMILE) (Branduardi-Raymont et al., 2018). Besides the SXI, SMILE carries the
 134 Ultra Violet Imager (UVI), a magnetometer, and a plasma instrument for in-situ mea-
 135 surements of the solar wind and magnetosheath parameters. SMILE is due to launch in
 136 early 2025 into a highly elliptical orbit with apogee of about $19 R_E$, inclination angle
 137 of 70 or 98 degrees depending on launcher, and orbital period of about 50 hours. Using
 138 the SXI, we can obtain continuous time-series of the magnetopause standoff distance for
 139 variable solar wind conditions.

140 In the two companion papers, we simulate the expected output of the SXI and present
 141 the methods of finding the magnetopause standoff distance from X-ray images. We use
 142 the results of global MHD simulations to calculate the X-ray emissivity in geospace. In
 143 Part 1, we present the results of simulations for two events, using two numerical mod-
 144 els. We discuss finding the magnetopause position in the simulations and explain pos-
 145 sible reasons for differences between the models. Some MHD models predict the density
 146 in the magnetosphere to be higher than has been observed, and we, therefore, introduce
 147 several methods of magnetospheric masking by highlighting grid points located in the
 148 magnetosphere. In Part 2, we will discuss the simulation and processing of X-ray images
 149 and show how we can find the magnetopause position from them.

150 2 Models and Boundary Conditions

151 We use the SWMF global MHD model (Tóth et al., 2005, 2012) version 20180525
 152 and the Lyon-Fedder-Mobarry magnetosphere–ionosphere model (LFM-MIX) (Lyon et
 153 al., 2004; Merkin & Lyon, 2010) version LTR-2_1_5 available through the runs on request
 154 from the Community Coordinated Modeling Center at Goddard Space Flight Center.
 155 The SWMF model uses an adaptive structured Cartesian grid with highest resolution
 156 in the inner magnetosphere (Powell et al., 1999). In this study, we use runs with the best
 157 spatial resolution of $0.125 R_E$ in the whole dayside magnetosphere and magnetosheath.
 158 The resolution in the nightside magnetosphere ($x < -4 R_E$), upstream of the bow shock,
 159 and on the flanks near the terminator plane is $0.25 R_E$ or worse. The LFM model uses
 160 a distorted spherical grid with spatial resolution along the x axis in the subsolar mag-
 161 netosphere close to that in the SWMF model. In both models, the low-altitude numer-
 162 ical boundary is located at a radial distance of $R \simeq 2-3 R_E$. The density at this bound-
 163 ary in the SWMF model is usually fixed and equal to 28 cm^{-3} . In the LFM model, the
 164 radial gradient of the density at the inner boundary is fixed to be equal to zero (Xi et
 165 al., 2015). The solar wind enters into the numerical region through another boundary
 166 located relatively far upstream of the bow shock, e.g. at $x = 30 R_E$ (LFM) or $33 R_E$
 167 (SWMF).

168 We simulate two cases in this study. The first case is an artificial case with con-
 169 stant solar wind conditions: the ion density $N_{SW} = 12.25 \text{ cm}^{-3}$, the velocity along Sun-
 170 Earth line 400 km/s , $B_X = B_Y = 0$, $B_Z = 5 \text{ nT}$. These velocity and magnetic field
 171 modulus values are close to the average, while the density is moderately higher than av-
 172 erage. As a result, the magnetosphere is slightly compressed in this case. The ionospheric
 173 Pedersen conductance is constant and equal to 5 mho .

174 In the second case, we use solar wind conditions from the Wind spacecraft on June
 175 16-17, 2012. This event consists of a large interplanetary coronal mass ejection (ICME)
 176 simulated in the heliosphere by Shen et al. (2014) and characterized by a large solar wind
 177 density with a brief interval of extremely high values up to 100 cm^{-3} during a long north-
 178 ward IMF interval. The auroral emission, ionospheric currents and convection in this event
 179 have been studied by Carter et al. (2020). In this case, we employ a statistical auroral
 180 ionosphere conductance model driven by the solar irradiation index (F10.7) and by the
 181 FAC patterns (Ridley et al., 2004).

182 The solar wind conditions in the second case are shown in Figure 1. The whole time
 183 interval from 17:00 UT on 16 June to 12:00 UT on 17 June 2012 has been simulated, but
 184 only several selected times, i.e., 20:00, 22:25, and 23:10 on 16 June and 00:00 UT on 17
 185 June, are analyzed in detail below. The solar wind parameters in Figure 1 are time-shifted
 186 from the Wind position near Lagrangian point L1 to the upstream numerical boundary
 187 ($x = 33 R_E$ for the SWMF model). However, we should also take into account the prop-
 188 agation time from this boundary to the subsolar magnetopause if studying the variations
 189 of the standoff distance. If we estimated the time lag using the solar wind velocity ob-
 190 served by Wind, we would underestimate this lag because the velocity in the magnetosheath
 191 is on average a few times less than in the supersonic solar wind upstream of the bow shock.
 192 Samsonov et al. (2017, 2018) showed that the average propagation time of directional
 193 discontinuities across the magnetosheath for typical solar wind conditions is about 14
 194 min, and this time lag depends on how strongly the velocity drops down in the magnetic
 195 barrier ahead of the magnetopause. In the case presented here, the solar wind speed changes
 196 and remains higher than a typical one after 20:22 UT when the interplanetary shock ar-
 197 rives at the upstream boundary, therefore we estimate the propagation time between the
 198 solar wind boundary and magnetopause to be equal to 10 min. We use this time lag for
 199 the SWMF model, while by checking temporal variations of MHD parameters upstream
 200 of the bow shock we conclude that a more appropriate time lag for the LFM model is
 201 5 min. In Table 1, we provide the solar wind conditions at 19:50, 22:15, 23:00, and 23:50
 202 UT (i.e. 10 min before the times of magnetospheric response mentioned above) as well
 203 as the dipole tilt and magnetopause standoff distance in the empirical and MHD mod-
 204 els. We compare the magnetopause positions obtained in MHD simulations with the two
 205 empirical magnetopause models (Shue et al., 1998; Lin et al., 2010).

206 The soft X-ray emissivity P_x is found to be proportional to the ion density N_{SW}
 207 in the solar wind and magnetosheath, the exospheric neutral density N_H , and the rel-
 208 ative velocity V_{rel} .

$$P_x = \alpha N_{SW} N_H V_{rel}, \quad \text{here} \quad \alpha = 10^{-15} \text{ eV cm}^2 \quad (1)$$

209 The interaction efficiency factor α depends on the charge transfer cross section, the frac-
 210 tion of high charge state ion species in the solar wind, transition energy and other fac-
 211 tors. This estimate of α agrees with previous studies (e.g., Cravens, 2000; Pepino et al.,
 212 2004; Sun et al., 2019; Wegmann et al., 1998).

213 The exospheric neutral density N_H falls off with R^{-3} where R is a geocentric dis-
 214 tance (Cravens et al., 2001). According to this model, the neutral density at the radial
 215 distance of $10 R_E$, i.e. near the subsolar magnetopause for typical solar wind conditions,
 216 is equal to 25 cm^{-3} .

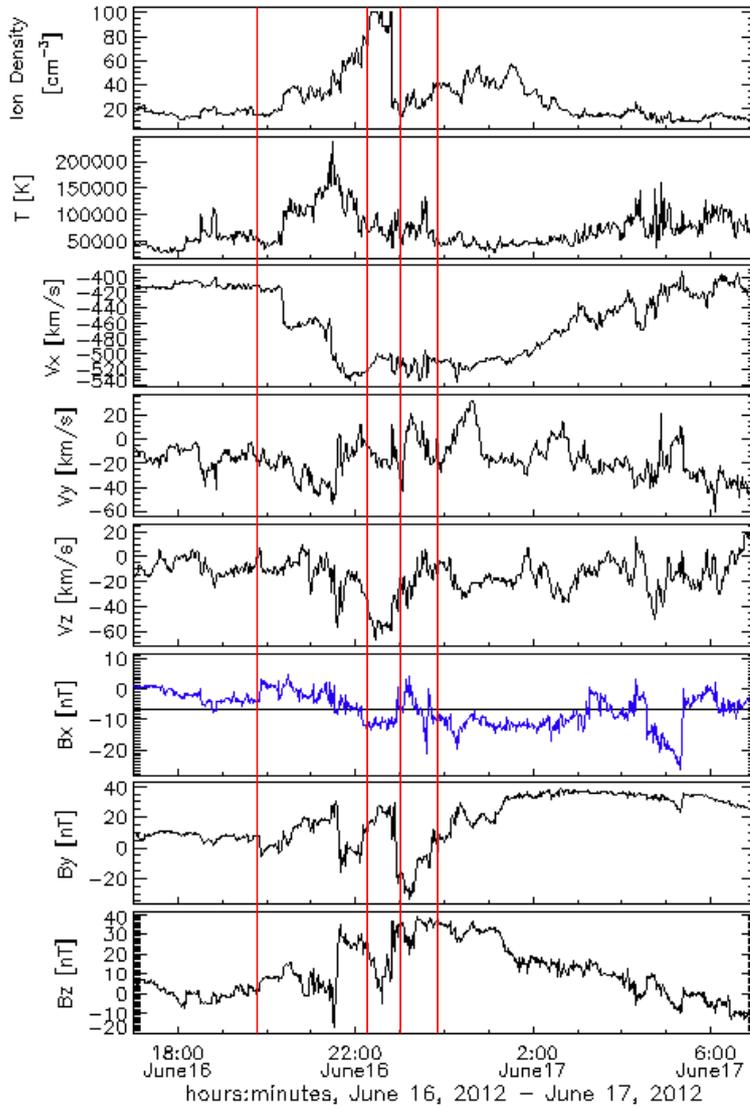


Figure 1. Solar wind parameters observed by Wind on June 16-17, 2012. Vertical red lines mark the four selected times (19:50, 22:15, 23:00, and 23:50 UT) used for the following analysis taking into account the 10 min time lag between the solar wind boundary and magnetopause (see details in text).

Table 1. Solar wind parameters (top rows 1-3) at selected times on June 16, 2012. Bottom part shows: the Earth dipole tilt (row 1), the magnetopause standoff distance predicted by the empirical Shue et al. (1998) (row 2) and Lin et al. (2010) (row 3) models, the standoff distance in the SWMF (row 4) and LFM (row 5) simulations. We apply the time lags of 5 and 10 min to the LFM and SWMF simulations respectively to take into account the propagation time from the inflow boundary to the subsolar magnetopause.

UT	19:50	22:15	23:00	23:50
Density, cm^{-3}	14.9	74.6	14.7	39.1
Velocity, km/s	411	523	519	513
B_Z , nT	1.1	23.3	34.4	36.5
Tilt, degr.	29.8	24.1	22.2	20.1
R_{SHUE}, R_E	9.2	6.7	8.6	7.5
R_{LIN}, R_E	9.0	6.1	8.2	6.9
R_{SWMF}, R_E	8.4	5.8	7.4	6.6
R_{LFM}, R_E	9.0	6.1	7.4	7.0

217 3 MHD simulations

218 3.1 Case 1

219 We exploit the SWMF and LFM models to reproduce the magnetospheric config-
 220 uration and obtain input conditions for the following simulations of SXI images. Using
 221 this stationary case with a purely northward IMF, we display several differences between
 222 the models which may result in different magnetopause standoff distances. One such dif-
 223 ference is related to the boundary conditions at the inner numerical boundary. Figure
 224 2 displays the density obtained in the equatorial plane for the SWMF (left) and LFM
 225 (right) models. The magnetospheric density in the SWMF model is nearly one order of
 226 magnitude higher than that in the LFM model. Therefore, while the magnetopause po-
 227 sition can be clearly identified using the density distribution in the LFM model, the den-
 228 sity changes through the subsolar magnetopause might vary too smoothly for unambigu-
 229 ous determination of the magnetopause standoff distance in the SWMF results.

230 The inner boundary conditions seem to play a minor role in differences of the mag-
 231 netopause standoff distance. Since the standoff distance is controlled by the pressure bal-
 232 ance condition, we show profiles of the pressure components and total pressures along
 233 the Sun-Earth line in Figure 3. In the solar wind upstream of the bow shock, the dy-
 234 namic pressure is about two orders of magnitude higher than either thermal or magnetic
 235 pressures. At the bow shock, the dynamic pressure decreases while both the thermal and
 236 magnetic pressures increase. In general, the total pressure (i.e. the sum of dynamic, ther-
 237 mal, and magnetic pressures) is supposed to be conserved through the bow shock accord-
 238 ing to the Rankine-Hugoniot conditions. However, the total pressure can change through
 239 the magnetosheath since the magnetosheath is a thick layer several R_E wide (Samsonov
 240 et al., 2012). Further, the total pressure does not change through the magnetopause be-
 241 cause the magnetopause is a tangential discontinuity in the northward IMF case.

242 Since the bow shock in MHD simulations is always a layer (with a width of sev-
 243 eral grid spacings) rather than a discontinuity due to the numerical dissipation, we do
 244 not expect that the total pressure stays exactly the same on both sides of the bow shock.
 245 Indeed, Figure 3 shows that the total pressure changes in a different way through the
 246 bow shock in the SWMF and LFM models. The SWMF model predicts a small ($\sim 3\%$)
 247 decrease in the total pressure which may be a precursor of the following decreasing trend

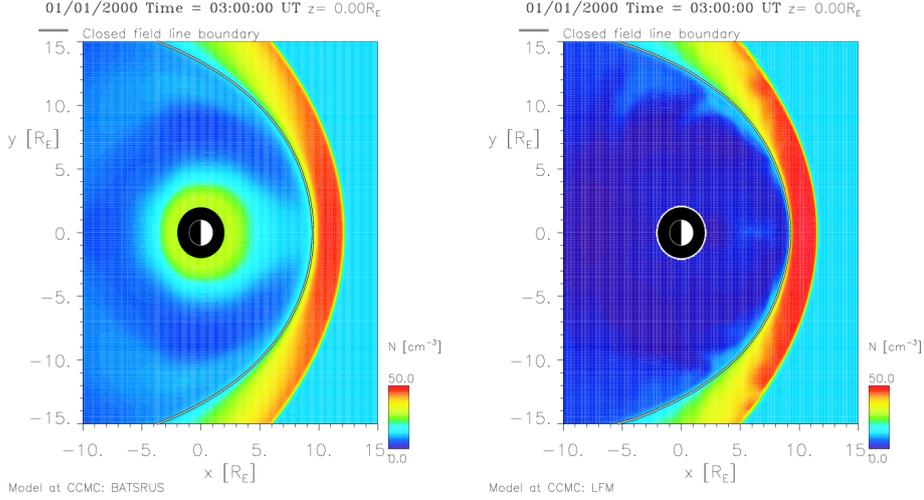


Figure 2. Density in the equatorial plane in the SWMF (left) and LFM (right) models in Case 1. The grey line indicates the position of the open-close field line boundary (magnetopause on the dayside).

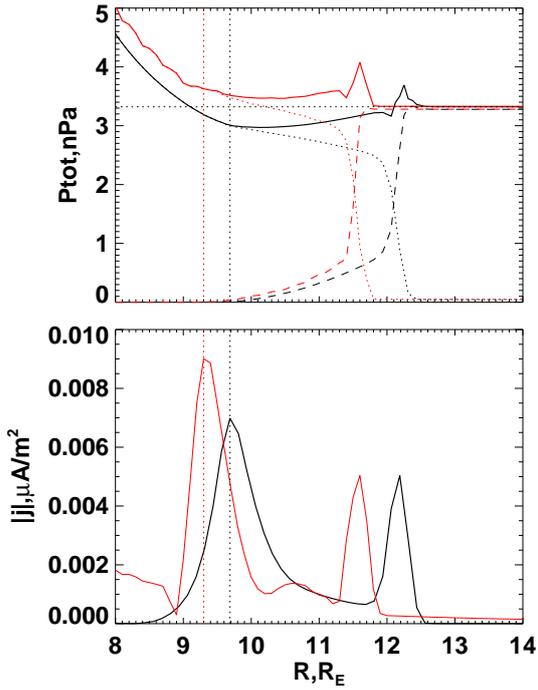


Figure 3. Top: dashed lines indicate dynamic pressure, dotted lines – the sum of thermal and magnetic pressures, solid lines – the sum of dynamic, thermal, and magnetic pressures along the Sun-Earth line. Dotted horizontal line points out the total pressure upstream of the bow shock (the same for both models). Bottom: electric current density. The peaks in electric current density on the left-hand side of the bottom plot correspond to the magnetopause position and are marked with dotted vertical lines. The peaks on the right-hand side correspond to the bow shock. Black (red) lines show results of the SWMF (LFM) models.

248 down in the magnetosheath. On the contrary, the LFM model predicts a $\sim 8\%$ increase
 249 in the total pressure. Then, the total pressure in both models slightly decreases through
 250 the magnetosheath. The dotted vertical lines mark the maxima of the electric current
 251 density which usually indicate the magnetopause position. In the SWMF model, the $|j|$
 252 maximum is located at $x = 9.7 R_E$ while it is shifted $0.4 R_E$ Earthward in the LFM
 253 model. For comparison, the empirical models predict the magnetopause at $x = 9.6 R_E$
 254 (Shue et al., 1998) and $x = 9.5 R_E$ (Lin et al., 2010) in this particular case, in good
 255 agreement with the MHD simulations.

256 We only point out the difference in the magnetopause position between the mod-
 257 els in this paper, but we do not study in detail the reasons for this difference. We sup-
 258 pose that the possible explanation might reside in the different numerical methods in the
 259 two models or different simulations in the inner magnetosphere and different inner bound-
 260 ary conditions.

261 3.2 Case 2

262 We present the MHD results in the four selected times in this case. Table 1 dis-
 263 plays the key solar wind parameters (top panel) at 19:50, 22:15, 23:00, and 23:50 UT,
 264 the magnetospheric dipole tilt, and the magnetopause standoff distances in the empir-
 265 ical (Shue et al., 1998; Lin et al., 2010) and MHD SWMF and LFM models (bottom panel)
 266 taking into account the corresponding time lags between the solar wind boundary and
 267 magnetopause for the MHD models (5 min for the LFM model and 10 min for the SWMF
 268 model).

269 The solar wind density is higher than the average at 19:50 UT, while the velocity
 270 and magnetic field magnitude are close to typical values. Therefore the magnetosphere
 271 is only moderately compressed. Next, at $t=22:15$ UT, the solar wind density becomes
 272 extremely high and the magnetosphere is tremendously compressed, therefore the empir-
 273 ical Lin et al. (2010) model and both MHD models predict the standoff distance well
 274 inside geostationary orbit, at 6.1 or $5.8 R_E$, even for the northward IMF. The Shue et
 275 al. (1998) model, however, predicts the standoff distance of $6.7 R_E$, i.e. slightly higher
 276 than geostationary orbit at $6.6 R_E$.

277 The solar wind density abruptly drops between 22:48 and 22:50 UT resulting in
 278 the magnetospheric expansion from $5.8 R_E$ at 22:50 UT to $7.4 R_E$ at 23:05 UT in the
 279 SWMF simulation. However, even at 23:00 and 23:50 UT all the solar wind parameters
 280 presented in Table 1 (density, velocity, IMF B_Z) are higher than those in the ordinary
 281 conditions, therefore the magnetosphere stays significantly compressed.

282 The empirical and MHD models predict different standoff distances and the dif-
 283 ferences between the models change in time. Although both empirical magnetopause mod-
 284 els depend on the same solar wind conditions, they apply different power laws between
 285 the solar wind dynamic pressure and the standoff distance so that the variations of the
 286 standoff distance during magnetospheric compression are larger in the Lin et al. (2010)
 287 model than in the Shue et al. (1998) model. Besides, the Lin et al. (2010) model takes
 288 into account the dipole tilt, while the Shue et al. (1998) model does not. Moreover, the
 289 magnetopause standoff distance in the Lin et al. (2010) model depends on the sum of
 290 the solar wind dynamic and magnetic pressures while it depends only on the dynamic
 291 pressure in the Shue et al. (1998) model (but note that the magnetic pressure is usually
 292 one order of magnitude less than the dynamic pressure).

293 The SWMF model predicts the magnetopause to be closer to the Earth than both
 294 the empirical models for the compressed magnetospheric conditions. We refer to the pa-
 295 per of Samsonov et al. (2016) in which reasons for the differences between empirical and
 296 MHD models were discussed. Both empirical and MHD models might be inaccurate. Since
 297 empirical models are statistical, they may smooth standoff distance variations both for

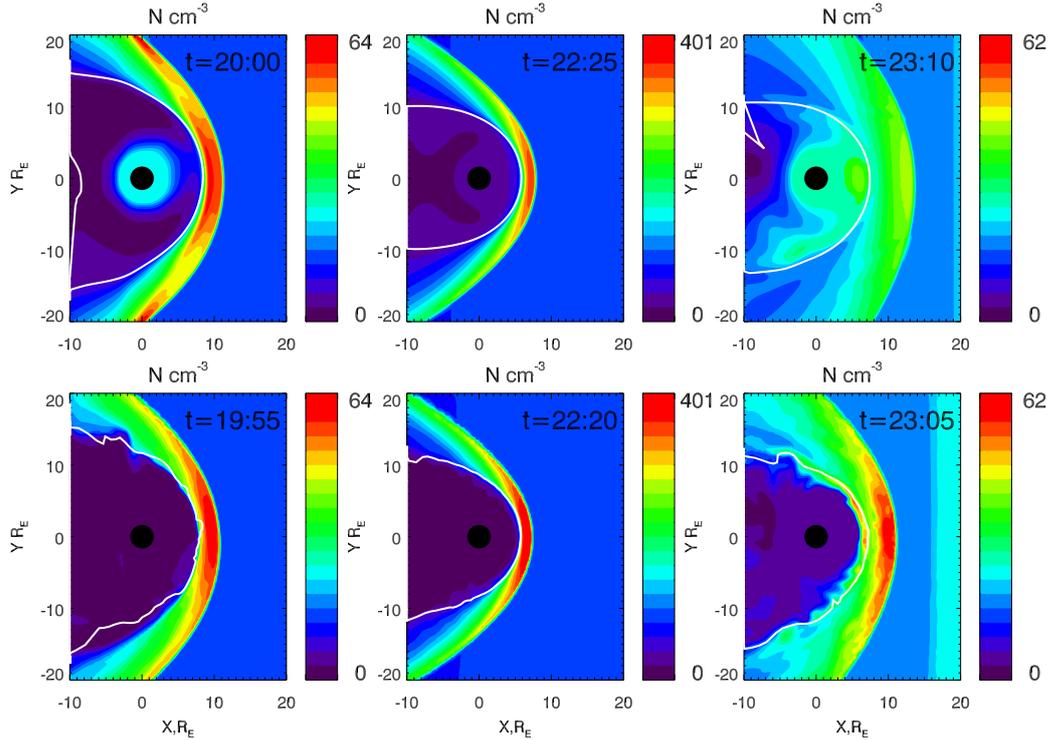


Figure 4. Density in the equatorial plane in the SWMF (top) and LFM (bottom) models in Case 2 at different times. The thick grey line indicates the open-closed field line boundary.

298 strong compressions and expansions. Besides, the empirical models depend only on present
 299 solar wind conditions, while the standoff distance in the MHD models smoothly evolves
 300 and therefore depends on the present and past conditions. On the other hand, MHD mod-
 301 els may not accurately reproduce some magnetospheric currents, e.g., the ring current
 302 or the magnetospheric-ionospheric currents. Moreover, the present case occurs at a large
 303 dipole tilt, which exacerbates the differences between the models.

304 Figure 4 compares the density distribution in the equatorial plane at three times
 305 calculated by either the SWMF (top row) and LFM (bottom row) models. As mentioned
 306 above, we apply the additional time lag of 5 min between the SWMF and LFM simu-
 307 lations to obtain a better match of the density distribution in the magnetosheath and
 308 solar wind. Since the LFM model is less diffusive it can better reproduce some sharp
 309 density peaks observed by Wind and respectively the density maxima in the magnetosheath
 310 are sometimes higher (e.g., in the subsolar region downstream of the bow shock at t=23:05
 311 UT).

312 At 20:00 (19:55 for LFM) UT, the magnetosphere is moderately compressed. The
 313 solar wind plasma parameters vary slowly, the IMF B_z is weak and positive, therefore
 314 the magnetopause position is stable. As well as in Case 1, the LFM model predicts a mag-
 315 netospheric density lower than that in the magnetosheath and solar wind, while the SWMF
 316 model predicts a magnetospheric density close to or even higher than that in the solar
 317 wind and on the magnetosheath flanks. The density gradually decreases from 64 cm^{-3}
 318 in the subsolar magnetosheath at $x = 9.4 R_E$ to 9.3 cm^{-3} in the magnetosphere at $x =$
 319 $7.5 R_E$ in the SWMF model. The LFM models predicts nearly the same density in the
 320 magnetosheath, but the density falls below 0.1 cm^{-3} in the subsolar magnetosphere at
 321 $x < 7 R_E$.

322 The magnetosphere is extremely compressed at 22:25 (22:20 in the LFM model)
 323 UT with maximum densities of $\sim 400 \text{ cm}^{-3}$ in the magnetosheath and corresponding so-
 324 lar wind densities of $\sim 100 \text{ cm}^{-3}$. The density in the outer magnetosphere in the SWMF
 325 simulation is also higher than that in quieter conditions even if it keeps the same at the
 326 inner boundary of the MHD domain. However, the density significantly drops through
 327 the magnetopause, e.g., from 340 cm^{-3} at $x=6.6 R_E$ to 73 cm^{-3} at $x=5.4 R_E$, which
 328 forms a sharp boundary in Figure 4. In the LFM model, the density still stays fairly low
 329 in the magnetosphere varying from several cm^{-3} near the magnetopause to about 0.1
 330 cm^{-3} near the inner boundary despite the huge magnetosheath density.

331 The density distribution at 23:10 (23:05) UT is essentially different from that we
 332 usually obtain in MHD simulations. The thick grey line that indicates the open-closed
 333 boundary (OCB) usually nearly coincides with the maximal density gradient at the mag-
 334 netopause, except in this particular case. Interestingly, the SWMF model predicts an
 335 increase in the density through the inward OCB crossing, in particular from 27 cm^{-3}
 336 at $x=8.0 R_E$ in the magnetosheath to 40 cm^{-3} at $x=6.5 R_E$ in the outer magnetosphere.
 337 The magnetospheric density distribution is asymmetric with a higher density on the dawn
 338 side. In the LFM model, the sharp density gradient is located about $1 R_E$ Earthward
 339 of the OCB which demonstrates specifics of the density distribution at this time as well.
 340 Nevertheless, the magnetospheric density in the LFM simulation gradually decreases to-
 341 ward the Earth and stays below 1 cm^{-3} for $x < 5.5 R_E$.

342 Summarizing the comparison between the two MHD models, we conclude that the
 343 density in the magnetosphere predicted by the SWMF model is significantly higher than
 344 that predicted by the LFM model. Spacecraft observations mostly agree with the pre-
 345 dictions of the LFM model, i.e. the density is low, e.g. about 1 cm^{-3} , in the dayside mag-
 346 netosphere outside the plasmasphere (but it might be possible that particle detectors un-
 347 derestimate the cold ion density under certain conditions (Toledo-Redondo et al., 2019)).
 348 Consequently, we should reduce the density in the magnetosphere predicted by the SWMF
 349 model to zero or to very small values while simulating X-ray images. In the next section,
 350 we describe methods of magnetospheric masking which help us separate the magneto-
 351 spheric and magnetosheath regions. On the other hand, we can simulate X-ray images
 352 for the LFM model without magnetospheric masking. We discuss this topic in detail be-
 353 low.

354 4 Magnetopause position and magnetospheric masking

355 4.1 Magnetopause position indicated by maximum of electric current 356 density

357 The magnetopause is by definition a boundary between the magnetospheric and
 358 magnetosheath (i.e. solar wind connected) magnetic fields and consequently should co-
 359 incide with a current layer which separates those fields. Samsonov et al. (2016) presented
 360 MHD simulations for stationary solar wind conditions with typical plasma and magnetic
 361 field parameters which illustrate that the maximum of electric current density J well in-
 362 dicates the magnetopause position in the dayside region. Figure 5 displays the electric
 363 current density in the equatorial and noon-meridional planes in Case 1. Although this
 364 is a stationary case with the purely northward IMF, the position of the subsolar mag-
 365 netopause nearly coincides with the maximum of the electric current density as it oc-
 366 curs for other IMF orientations too. More precisely, the maximum of the current den-
 367 sity is slightly farther from the Earth than the OCB indicated by thick white lines in Fig-
 368 ure 5. Anyway, the electric current density can be used as a good indicator of the mag-
 369 netopause position in the dayside region. The picture becomes more complicated near
 370 the cusps where simultaneously as many as three local maxima of the electric current
 371 density at different radial distances may appear (see right panel of Figure 5). Finding
 372 the magnetopause position becomes ambiguous in this case.

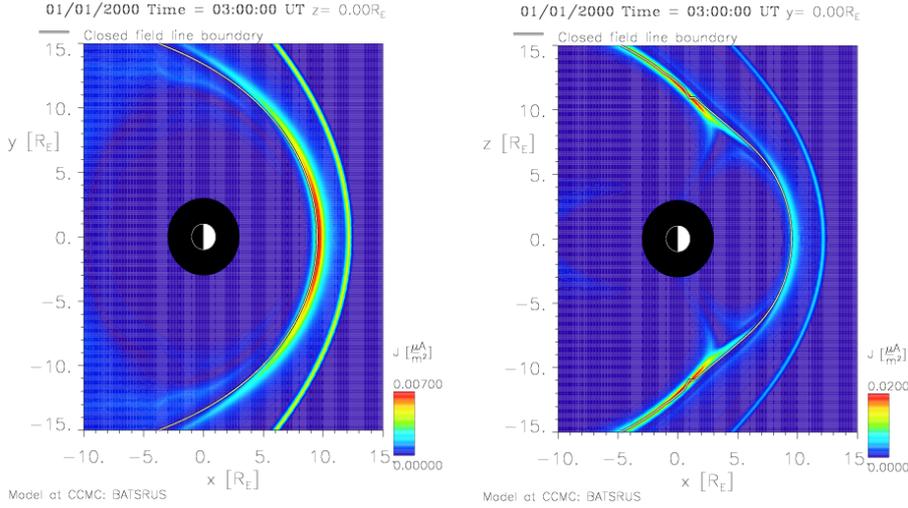


Figure 5. Electric current density in the equatorial (left) and noon-meridional(right) planes in the SWMF model in Case 1. Thick white line indicates the OCB.

373 While the electric current density in stationary MHD solutions usually has only two
 374 maxima in the subsolar region, one corresponding to the magnetopause and another one,
 375 farther from the Earth, indicating the bow shock, the picture may become more confusing
 376 in some non-stationary solutions. If a directional discontinuity (whether rotational
 377 or tangential, but with significant changes in the IMF orientation) or an interplanetary
 378 shock propagates through the magnetosheath, this results in another maximum of the
 379 electric current density which might be confused with the maximum at the magnetopause.
 380 An example of such temporal variations of J at $t=23:00$ UT in Case 2 is presented in
 381 Figure 6. The electric current layer in the middle of the magnetosheath, between the mag-
 382 netopause and bow shock, corresponds to the tangential discontinuity with decreases in
 383 the density and IMF B_y and increase in the IMF B_z imposed at the upstream numeri-
 384 cal boundary at about 22:49 UT. Such transient structures may cause problems for auto-
 385 matic identification of the magnetopause position in MHD simulations using electric
 386 current distributions. Fortunately, events with such strong directional discontinuities or
 387 interplanetary shocks are rare.

388 The inner local maximum of the electric current density along the Sun-Earth line
 389 always corresponds to the magnetopause even if more than two maxima of J between
 390 the magnetosphere and bow shock occur (as an exception a weak electric current layer
 391 might rapidly move through the dayside magnetosphere after impact of interplanetary
 392 shocks (Samsonov & Sibeck, 2013)). Figure 7 shows profiles of J along the Sun-Earth
 393 line in Case 1 and at several times in Case 2. The inner maximum at the magnetopause
 394 is highest in Case 1 and at 20:00 and 22:25 in Case 2. The maxima at the bow shock are
 395 highest at the three other times, so even at 23:00 the maximum in the middle of the mag-
 396 netosheath does not exceed that at the bow shock. The inner maximum coincides with
 397 the magnetopause position in all cases.

398 4.2 Magnetospheric masking using threshold conditions

399 Usually MHD parameters in the dayside magnetosphere noticeably differ from those
 400 in the dayside magnetosheath. For example, the magnetospheric density and thermal
 401 pressure are lower, the flow velocity is lower as well, the magnetic field magnitude in the
 402 magnetosphere is typically larger but this depends on the IMF orientation since for a

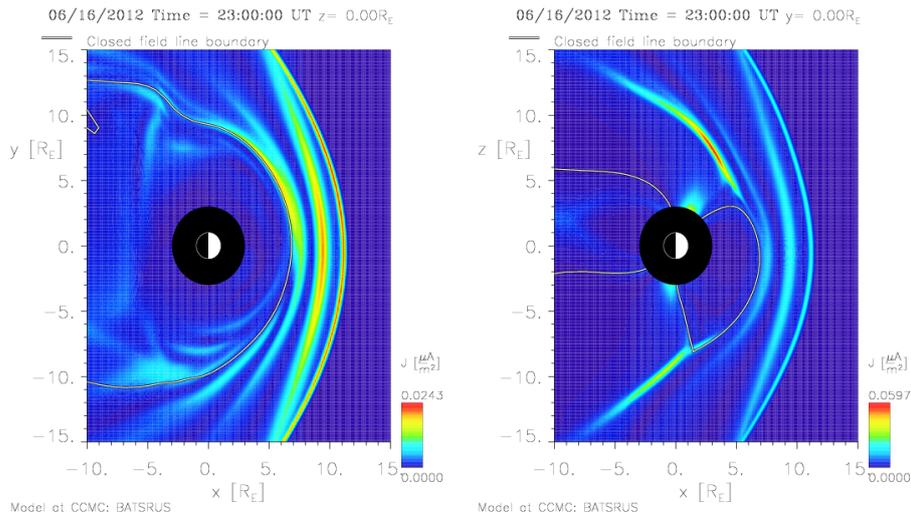


Figure 6. Electric current density in the equatorial (left) and noon-meridional(right) planes in the SWMF model at $t=23:00$ UT in Case 2. Thick white line indicates the OCB.

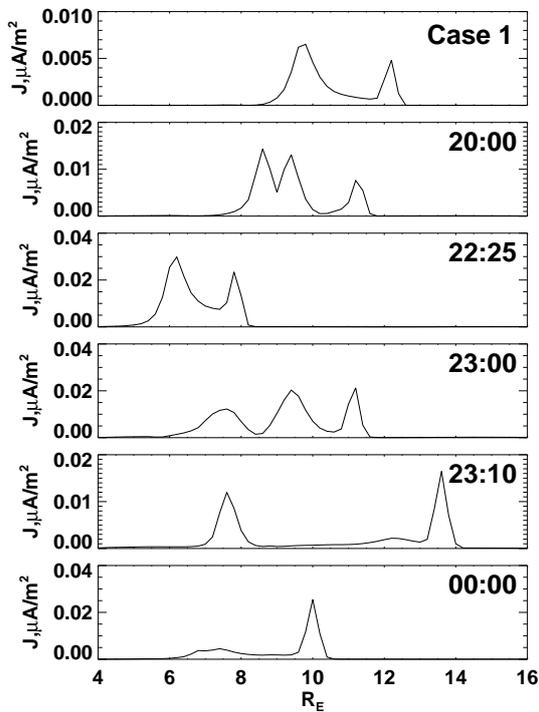


Figure 7. Electric current density along the Sun-Earth line in Case 1 and at different times in Case 2.

northward IMF the difference through the subsolar magnetopause may be small. However, the boundary layer between the magnetospheric and magnetosheath parameters is usually diffuse in MHD simulations and the magnetopause position sometimes can not be accurately determined. For example, the velocity decreases to zero at the stagnation point near the stationary subsolar magnetopause (Spreiter et al., 1966), however, the velocity may considerably increase both in the magnetosheath and in the outer magnetosphere on the flanks, near and behind the terminator plane (since the flowpause, the boundary between different streams, may not coincide with the magnetopause there). Therefore the velocity distribution alone cannot be used as a confident magnetopause indicator in the whole dayside region. Instead, we try several combinations of the different MHD parameters and describe a more reliable method below.

In Figure 8 a-b, we show that the thermal pressure is usually higher in the dayside magnetosheath and cusps than in both the magnetosphere and solar wind. However, the difference is blurred on the magnetosheath flanks, and therefore we apply additionally the second condition on velocity in the whole numerical box. We begin by finding the subsolar magnetopause position (e.g., using the electric current density profile at the Sun–Earth line), move $\sim 0.5 R_E$ inward from it, and use the thermal pressure from this point for the first threshold condition. This point is supposed to be inside the magnetosphere, but close to the magnetopause. The threshold for the velocity is obtained far upstream of the bow shock, e.g. near the upstream numerical boundary. Thus we impose the following conditions to determine the magnetospheric area

$$\begin{aligned} p &< p(msp) + \Delta p, \\ V_X &> V_X(sw) * k_v. \end{aligned} \quad (2)$$

Here, $p(msp)$ and $V_X(sw)$ are the thresholds of the thermal pressure in the magnetosphere and the x component of the velocity in the solar wind respectively. Note that the latter is negative in the solar wind therefore V_X can be either small negative or positive in the magnetosphere. We set $\Delta p = 0.2$ nPa, and $k_v = 0.15$. If both conditions (2) are matched, the location is taken to be in the magnetosphere. We have tested more than ten MHD solutions with different solar wind conditions and this method mostly works well, however it may fail in some cases with highly variable solar wind conditions. We present both successful and failed examples below.

Figure 8 shows the thermal pressure (a,b) and X-ray emissivity (c,d) (see equation (1)) in the equatorial and noon-meridional planes in case 1 calculated by using the SWMF model and applying the magnetospheric mask. Note that we use the logarithmic scale for the emissivity plots in this figure and below. The magnetosheath and cusps are evident in the 2-D slices of thermal pressure. The region of highest pressure is the subsolar magnetosheath. The thermal pressure in the cusps and on the magnetosheath flanks is lower, but still larger than that in the magnetosphere. Such pressure distribution is typical for MHD simulations (particularly for those cases with steady or slowly changing solar wind conditions) and the magnetospheric masking method using conditions (2) well separates the magnetosheath and cusps from the solar wind and magnetosphere in such cases. We obtain that the emissivity in the cusps is several times higher than that in the subsolar magnetosheath, e.g. the maximum P_X in the cusp in the noon-meridional plane reaches $9.8 \cdot 10^{-5}$ eV cm $^{-3}$ s $^{-1}$ while the maximum P_X in the subsolar magnetosheath in the equatorial plane is only $2.5 \cdot 10^{-5}$ eV cm $^{-3}$ s $^{-1}$. We use logarithmic color scales for the following emissivity plots to better illustrate this difference. Figure 8 (e,f) shows the emissivity in the same case calculated without the magnetospheric mask. We can not confidently determine the magnetopause position in this case.

However, MHD models sometimes predict a relatively high thermal pressure in the magnetosphere, nearly the same or higher than that in the cusps and magnetosheath.

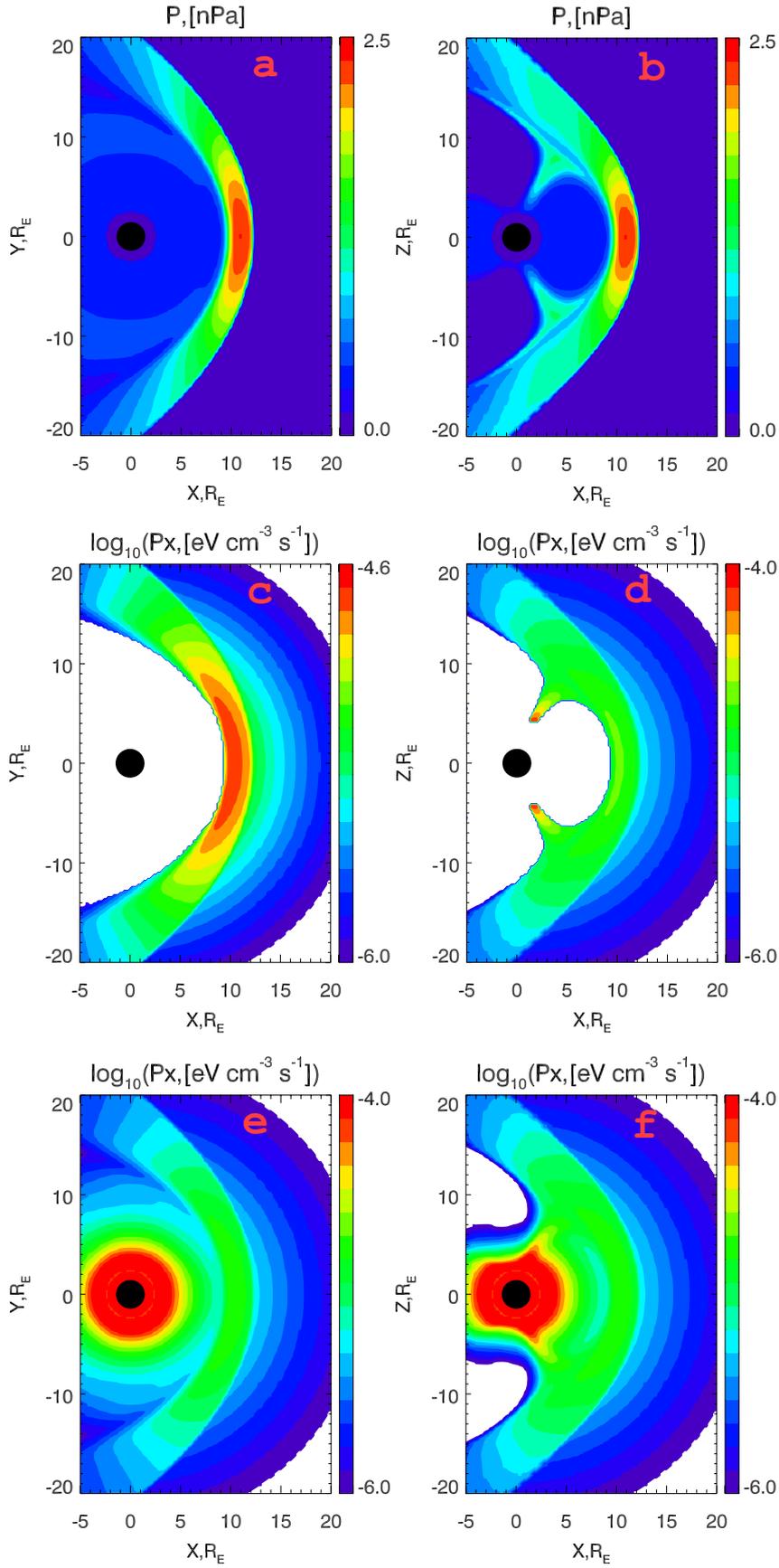


Figure 8. Thermal pressure (a,b) and X-ray emissivity calculated with the masking based on conditions (2) (c,d) in the equatorial (a,c) and noon-meridional (b,d) planes in Case 1. Panels (e,f) show the emissivity for the same case without magnetospheric mask.

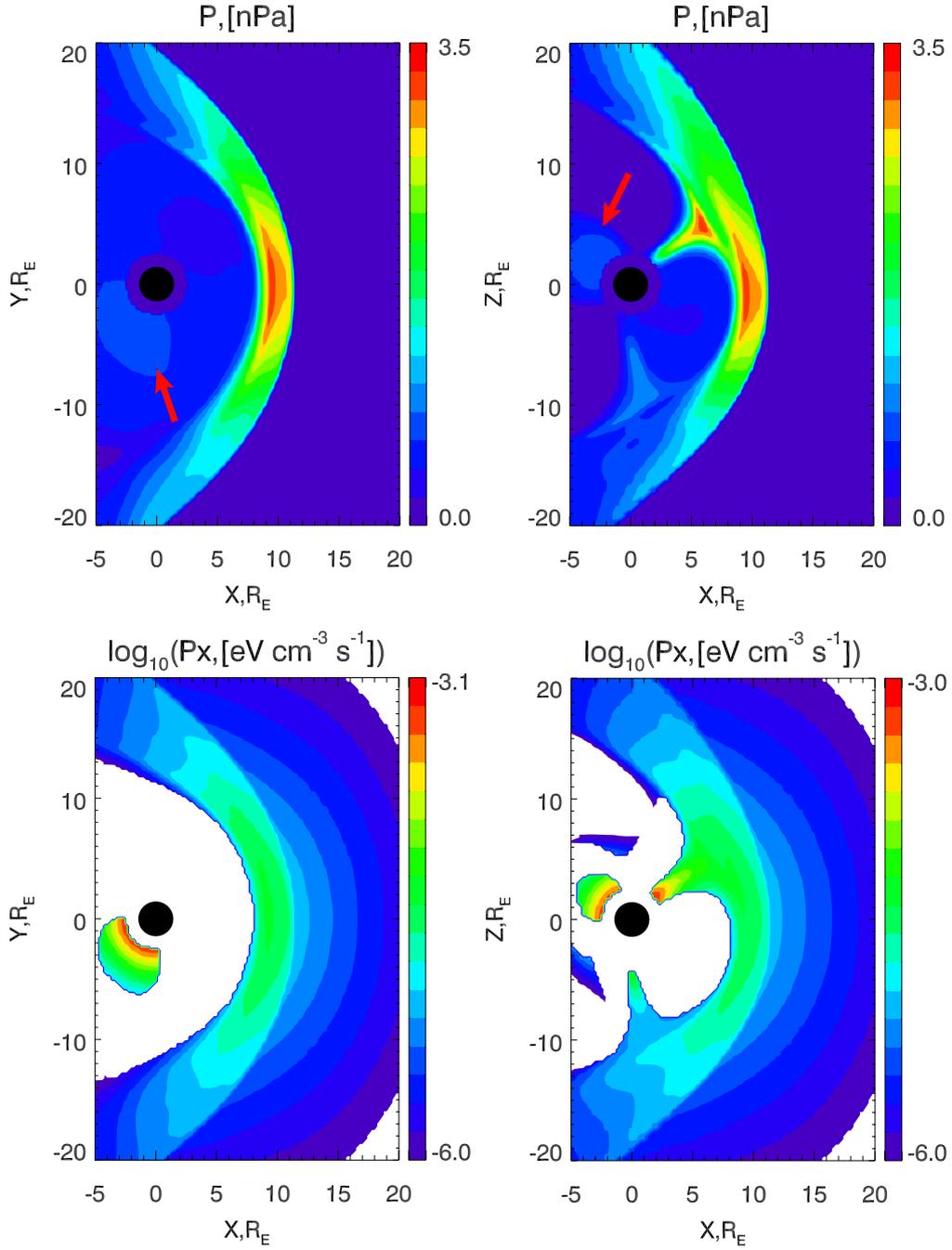


Figure 9. Thermal pressure (top) and emissivity (bottom) in the equatorial and noon-meridional planes in Case 2 at 20:00 UT (16 July) for the non-coupled SWMF model. Red arrows indicate the region in which the thermal pressure is higher than the average in the magnetosphere and close to that in the southern cusp and flank magnetosheath.

451 We have found several such examples in the simulations of Case 2. Figure 9 shows the
 452 thermal pressure and X-ray emissivity in the same format as in Figure 8 (a-d), but at
 453 20:00 UT on 16 June, 2012. At first glance, the thermal pressure in the magnetosphere
 454 seems to be lower than that in the magnetosheath. However, the dipole is strongly tilted
 455 in this case which results in a large north-south asymmetry. The pressure in the north-
 456 ern cusp is several times higher than that in the southern cusp. Moreover, the magne-
 457 topause shape and pressure distribution in the magnetosheath is also asymmetric. At
 458 the same time, there are regions in the magnetosphere where the pressure is higher than
 459 the average and reaches about the same values as in the southern cusp and flank mag-
 460 netosheath. This occurs in the nightside region on closed field lines near the Earth and
 461 is visible in the noon-midnight plane as well as on the dawn side in the equatorial plane
 462 (the two regions indicated by red arrows in Figure 9). As a result, the masking method
 463 with pressure thresholds is not able to separate the whole magnetospheric domain from
 464 the cusps and flank magnetosheath. In this case, we obtain that some regions in the night-
 465 side magnetosphere do not match the masking condition (2). This results in a high X-
 466 ray emissivity in several spots in the inner magnetospheric region which we do not ex-
 467 pect to be a source of X-rays in reality. However, this will not be a problem in our study
 468 because we concentrate on the emissivity in the dayside region.

469 Note that the pressure distribution in the magnetosphere may change while using
 470 a global MHD model coupled with kinetic models developed for the inner magnetosphere,
 471 like the Rice Convection Model (RCM). The results shown in Figure 9 were obtained for
 472 the non-coupled SWMF code. Figure 10 shows the simulations at the same time for the
 473 SWMF coupled with RCM. In this case, the growth of the thermal pressure in the in-
 474 ner magnetosphere is larger than in the simulations by the non-coupled SWMF model,
 475 and the size of the regions of the enhanced pressure is also bigger. This displays the way
 476 in which the RCM influences the results of MHD simulations, namely it changes the pres-
 477 sure distribution in the magnetosphere. As a result, the pressure threshold condition fails
 478 even in a larger magnetospheric zone therefore the size of the high X-ray emissivity re-
 479 gion in the inner magnetosphere is larger there than for the non-coupled SWMF model.
 480 We believe that this is a flaw of our masking method because we do not expect that high-
 481 charge state solar wind ions can penetrate into the inner magnetosphere.

482 4.3 Magnetospheric masking using flowlines

483 We find that the method of magnetospheric masking using thermal pressure thresh-
 484 olds can fail in cases with high pressure zones in the magnetosphere, therefore another
 485 method is presented in this subsection. In this method, every grid point in the simula-
 486 tion box is traced back along its flowline until the flowline reaches the supersonic solar
 487 wind. If the flowline does not reach the supersonic solar wind in a reasonable time, then
 488 this point is taken to be in the magnetosphere. Sun et al. (2019) also used the flowline
 489 method for magnetospheric masking, but their algorithm was different and implied us-
 490 ing a numerical code to solve the continuity equation. In our method, we need only a
 491 3-D velocity distribution and a relatively simple code to calculate the motion along flow-
 492 lines. We further reduce the computational time by making a preliminary separation of
 493 grid points, i.e. points with $|V| > 0.65V_{SW}$ are assumed to be related to the solar wind
 494 (they could be in the supersonic solar wind, magnetosheath, or far magnetotail) and points
 495 with $|V| < 0.01V_{SW}$ are assumed to be in the magnetosphere. Then we trace the re-
 496 maining points until one of the two conditions above is fulfilled.

497 The flowlines traced back to the solar wind outline the dayside magnetosphere, but
 498 they do not mark the cusps. It means that the cusps are determined as magnetospheric
 499 regions despite the fact that the solar wind plasma fills the cusps in observations. We
 500 apply the method suggested by Sun et al. (2019) to mark the cusps. In this method, we
 501 make two local spherical grids separately for the northern and southern hemispheres for
 502 the interval of radial distances which cover the expected cusp locations. The grid spac-

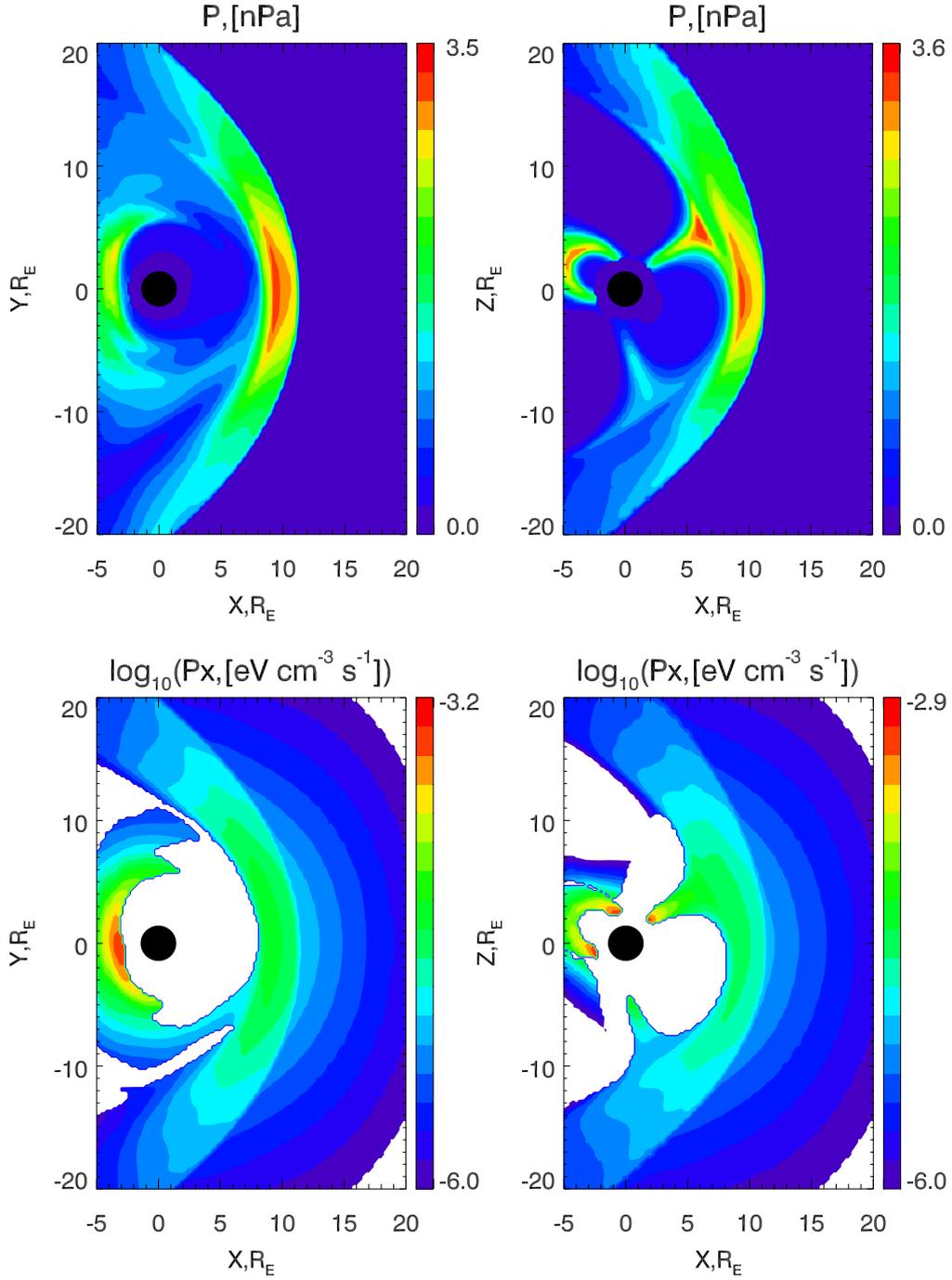


Figure 10. Thermal pressure (top) and emissivity (bottom) in the equatorial and noon-meridional planes in Case 2 at 20:00 UT for the SWMF coupled with RCM. The region of high thermal pressure is located in the nightside magnetosphere. Correspondingly, the magnetospheric mask does not cover this region, and we obtain a large X-ray emissivity there.

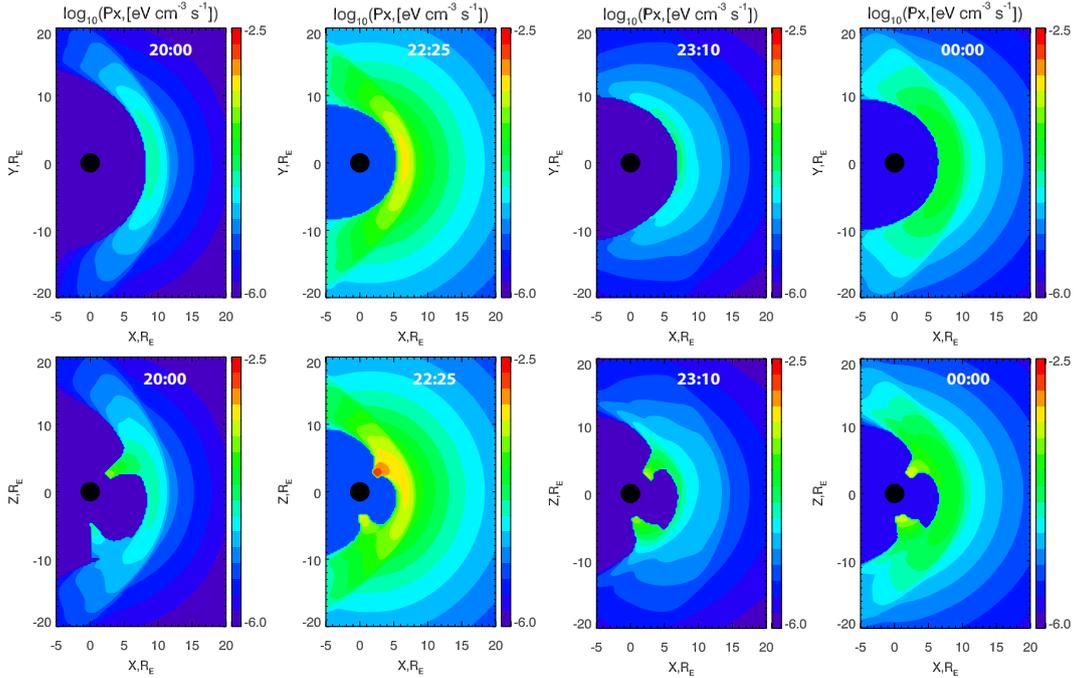


Figure 11. Emissivity in the equatorial and noon-meridional planes in Case 2 at 20:00, 22:25, and 23:10 UT on 16 June and at 00:00 on 17 June calculated by the masking method with flowlines.

503 ing in radial direction is $0.125 R_E$. For each radial shell, we find the maximum of the
 504 plasma pressure p_{max} and select a surrounding zone of the high pressure using condi-
 505 tion $p > k_p p_{max}$ where $k_p = 0.7$. We inspected several k_p values and found that the
 506 difference in the selected area for different k_p is negligible for stationary cases without
 507 a dipole tilt, such as case 1, but it might become significant for real events with a large
 508 dipole tilt, such as case 2. We choose a value of k_p which provides a smoothest transi-
 509 tion at the outer boundary of the cusps.

510 Figure 11 shows the X-ray emissivity at 20:00, 22:25, and 23:10 UT on 16 June and
 511 at 00:00 on 17 June in case 2 calculated by using the magnetospheric masking method
 512 with flowlines. The dipole tilt results in the north-south asymmetry in all cases. The emis-
 513 sivity is generally higher in the northern cusp where the solar wind density is higher too.
 514 The flowline masking method provides a smooth boundary which clearly separates the
 515 magnetosphere from the cusps and magnetosheath. The outer boundary of the magne-
 516 tosphere in the subsolar region determined by the flowline masking method generally nearly
 517 coincides with the open-closed field line boundary except in several extreme cases.

518 In Figure 12, we show profiles of the emissivity, density, and electric current den-
 519 sity along the Sun-Earth line at four times for Case 2. Firstly, the figure illustrates that
 520 the maximum of the emissivity near the subsolar magnetopause differs by more than one
 521 order of magnitude at different times depending on the magnetospheric compression (Px
 522 maximum located in the northern cusp is weakest at 20:00 UT and strongest at 22:25
 523 UT). Secondly, positions of the maximum of emissivity, the maximum density gradient,
 524 and the maximum of the electric current density change relative to each other at differ-
 525 ent times. At 20:00 and 22:25 UT, when the solar wind conditions are relatively stable,
 526 the positions of the maximum of density gradient and the maximum of electric current
 527 density nearly coincide with each other. Note that the grid spacing is $0.25 R_E$ in this
 528 run. The density and electric current density are taken at the centers of the numerical

529 grid cells, while the density gradient is taken at the boundaries between the cells which
 530 results in the $0.125 R_E$ difference. The position of the emissivity maximum is located
 531 $0.25\text{-}0.5 R_E$ sunward of the electric current (or density gradient) maximum. At 23:10
 532 UT, immediately after a significant drop of the solar wind density, the magnetosphere
 533 rapidly expands and the simulation predicts density in the closed field line region (i.e.
 534 in the magnetosphere) larger than that in the inner part of the magnetosheath. There-
 535 fore the maximum of the density gradient $grad(N)$ is shifted about $2 R_E$ earthward of
 536 the maximum of electric current density j which indicates the magnetopause current layer.
 537 The emissivity maximum and the flowline boundary (i.e., a sharp drop of the emissiv-
 538 ity) are located between the maxima of $grad(N)$ and $|j|$. At 00:00 UT, the solar wind
 539 conditions are relatively stable but the magnetospheric density remains rather high. There-
 540 fore the emissivity maximum again nearly coincides with the flowline boundary and is
 541 located earthward of the maxima of $grad(N)$ and $|j|$.

542 4.4 Emissivity in LFM model

543 As noted above, the LFM model predicts a small magnetospheric density, below
 544 1 cm^{-3} , therefore we can use the X-ray emissivity without magnetospheric masks for sim-
 545 ulation of SXI images. In Figure 13, we compare the emissivity obtained without (left
 546 panels) and with (right panels) magnetospheric masking at 20:00 and 22:25 UT. The mag-
 547 netospheric mask has been constructed using the threshold conditions in equation (2).
 548 As in the case of the SWMF model, the emissivity close to the Earth in the simulation
 549 without masking may be significantly larger than in the magnetosheath because of the
 550 extremely high neutral density (since the neutral density is proportional to R^{-3}). How-
 551 ever, contrary to the results obtained from the SWMF model, the LFM model predicts
 552 the emissivity in the dayside magnetosphere to be smaller than that in the magnetosheath
 553 and therefore we can distinguish the magnetopause position (e.g., see upper left panel
 554 at 20:00 UT). In the case of extreme magnetospheric compression at 22:25 UT, the mag-
 555 netopause position in the simulation without a mask cannot be precisely determined be-
 556 cause the decrease in the solar wind density through the magnetopause in the MHD re-
 557 sults is mostly compensated by the large increase in the neutral density. In most other
 558 cases, the predicted emissivity in the LFM model looks similar to the results at 20:00
 559 UT and therefore the simulations of SXI images can proceed without magnetospheric
 560 masks.

561 5 Conclusions

562 The energy transfer rate from the solar wind into the magnetosphere can be char-
 563 acterized by combinations of the solar wind parameters (e.g., Perreault & Akasofu, 1978;
 564 Vasyliunas et al., 1982; Newell et al., 2007, and references therein). The magnetospheric
 565 state can also be presented by combinations of several global parameters, e.g. by the au-
 566 roral indices SML/SMU (from the SUPERMAG network (Gjerloev, 2012)) or the tra-
 567 ditional AL/AU, the ring current index SMR or Dst, the cross polar cap potential, the
 568 size of the polar cap, and so on. The magnetopause standoff distance may also be in-
 569 cluded in this list because it characterizes global magnetospheric compressions and ex-
 570 pansions. The magnetopause location and motion provide crucial information concern-
 571 ing the state of the solar wind magnetosphere interaction, in particular the reconnection
 572 rate and the amount of flux transferred from the dayside to the magnetotail and vice-
 573 versa. Up to now, we have been unable to measure the standoff distance directly. In-situ
 574 spacecraft observations provide magnetopause crossings at some distance from the sub-
 575 solar point and reveal a momentary magnetopause distance or distances during brief in-
 576 tervals in the case of multiple magnetopause crossings. The standoff distance is often in-
 577 cluded in empirical magnetopause models, but these models are averaged over many events
 578 and solar wind conditions without taking into account time dependence and often as-
 579 sume a predefined functional form to describe the magnetopause shape. The new space

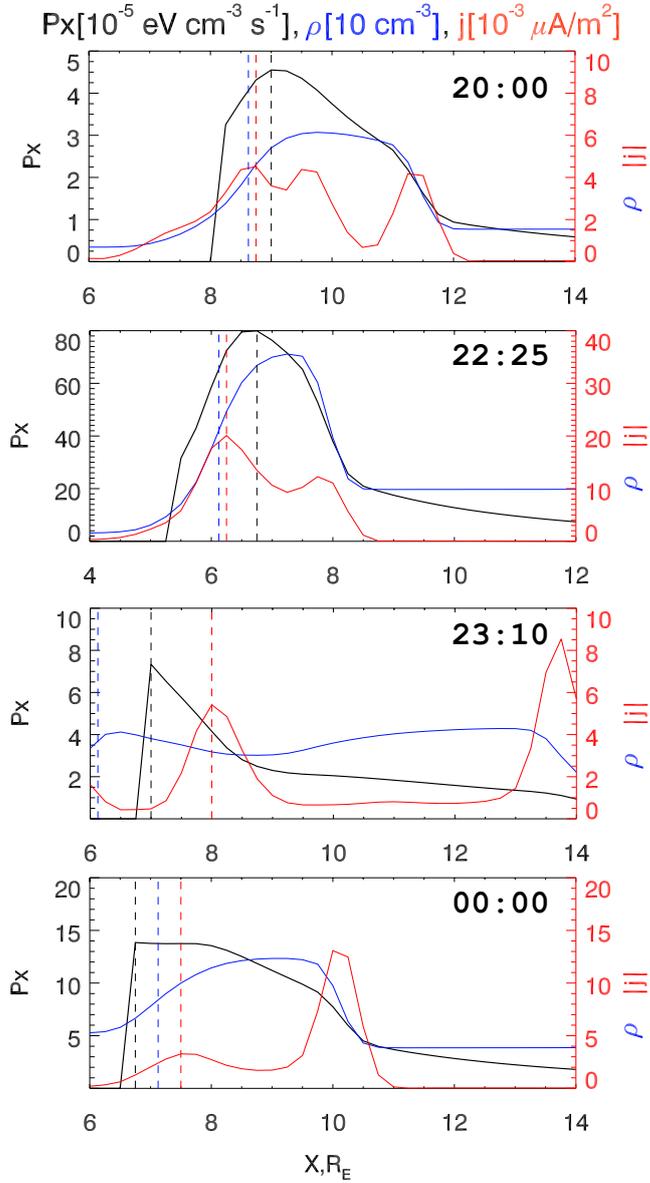


Figure 12. Emissivity (black), density (blue), and electric current density (red) along the Sun-Earth line at different times (20:00, 22:25, 23:10, and 00:00 UT). Dashed vertical lines indicate maxima of the emissivity (black), maxima of the density gradient (blue), and maxima of the electric current density at the magnetopause (red).

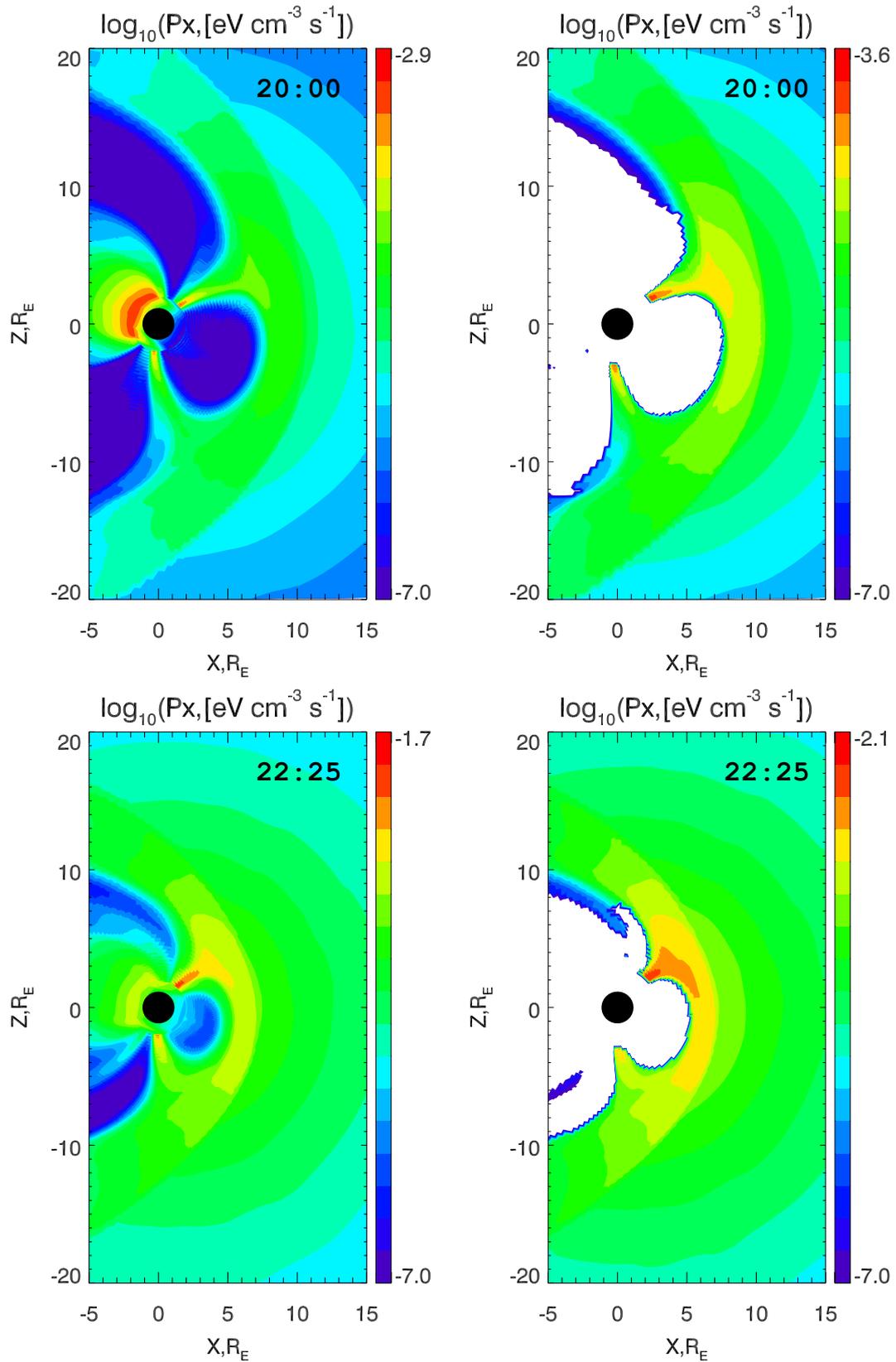


Figure 13. Emissivity in the noon-meridional planes in Case 2 at 20:00 and 22:25 UT without a magnetospheric mask (left) and with the mask obtained from threshold conditions (right) for numerical results of the LFM model.

580 mission SMILE will observe X-rays emitted in the magnetosheath and cusps capturing
 581 temporal variations of the magnetopause standoff distance in response to solar wind vari-
 582 ations.

583 This paper is the first of two companion papers in which we discuss the methods
 584 of finding the magnetopause positions using soft X-ray images. We use the two global
 585 MHD models, SWMF and LFM, and simulate one artificial and one real event. We briefly
 586 discuss the reasons why the numerical models predict different magnetopause positions
 587 for the same solar wind conditions. We illustrate how significantly the density distribu-
 588 tion in the magnetosphere and magnetopause position may change in response to large
 589 variations of the solar wind plasma parameters and magnetic field. We compare predic-
 590 tions of the MHD and empirical magnetopause models. We emphasize that the maxi-
 591 mum electric current density is a good indicator of the magnetopause location even in
 592 a northward IMF case.

593 The density in the outer dayside magnetosphere predicted by the LFM model varies
 594 between 0.1 and 10 cm⁻³ depending on the magnetospheric compression. This gener-
 595 ally agrees with observations. The SWMF model predicts the magnetospheric density
 596 between 10 and 50 cm⁻³ (the last in the case of strong compression). If we calculate the
 597 X-ray emissivity in this case, we cannot clearly distinguish the magnetopause position
 598 because the difference in the emissivity between the dayside magnetosphere and mag-
 599 netosheath is too small. On the contrary, the magnetopause location can be found by
 600 using the emissivity distribution calculated by the LFM model, except for some specific
 601 cases with a fast magnetospheric expansion. We present the two methods of magneto-
 602 spheric masking which separate the points located in the magnetosphere from those lo-
 603 cated in the magnetosheath, cusps, and solar wind. The first method uses threshold con-
 604 ditions for the thermal pressure and velocity, and the second method applies tracing along
 605 flowlines. Using these methods, we can calculate the X-ray emissivity localized in the
 606 magnetosheath and cusps. The results of the calculations are used in the second paper
 607 for simulation of 2-D X-ray images and SXI counts maps.

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 611 ionosphere model developed at Dartmouth College/High Altitude Observatory/Johns
 612 Hopkins University Applied Physics Laboratory/Center for Integrated Space Weather
 613 Modeling available through the NASA Community Coordinated Modeling Center
 614 (<http://ccmc.gsfc.nasa.gov>). In particular, we used results of the runs *Andrei_Samsonov_080818_2*,
 615 *Andrei_Samsonov_083118_1*, *Andrei_Samsonov_021819_1*, *Andrey_Samsonov_070519_1*,
 616 and *Andrey_Samsonov_073119_1*.

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