PRIME-SH: A Data-Driven Probabilistic Model of Earth's Magnetosheath

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Key Points:

- PRIME-SH is an algorithm that predicts plasma and magnetic field in Earth's magnetosheath using inputs from in-situ monitors at L1.
- PRIME-SH accurately predicts the magnetosheath conditions in a statistical sense and its predictions obey conservation laws at the shock.
- PRIME-SH can be used to easily assemble continuous maps of the magnetosheath, addressing spatial limitations of in-situ data.

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Abstract

A data-driven model of Earth's magnetosheath is developed by training a Bayesian recurrent neural network to reproduce Magnetospheric MultiScale (MMS) measurements of the magnetosheath plasma and magnetic field using measurements from the Wind spacecraft upstream of Earth at the first Earth-Sun Lagrange point (L1). This model, called PRIME-SH in reference to its progenitor algorithm PRIME (Probabilistic Regressor for Input to the Magnetosphere Estimation), is shown to predict spacecraft observations of magnetosheath conditions accurately in a statistical sense with a continuous rank probability score (CRPS) of 0.227σ (dimensionless standard deviation units). PRIME-SH is shown to be more accurate than many current analytical models of the magnetosheath. Furthermore, PRIME-SH is shown to reproduce physics not explicitly enforced during training, such as field line draping, the dayside plasma depletion layer, the magnetosheath flow stagnation point, and the Rankine-Hugoniot MHD shock jump conditions. PRIME-SH has the additional benefits of being computationally inexpensive relative to global MHD simulations, being capable of reproducing difficult-to-model physics such as temperature anisotropy, and being capable of reliably estimating its own uncertainty to within 3.5%.

Plain Language Summary

As the solar wind encounters Earth's magnetosphere and diverts around it, a shock is formed that heats and compresses the plasma and warps the magnetic field frozen into it. This shocked plasma and magnetic field, known as the magnetosheath, is what drives energy transfer at the magnetopause. Due to orbital constraints there is no continuous in-situ monitor of magnetosheath conditions. Studies of solar wind magnetosphere interaction typically rely on solar wind conditions measured at L1 propagated to Earth by some algorithm, which are then either used directly or used to drive some model of the magnetosheath. This process has numerous points of uncertainty, from the choice of propagation algorithm to the choice of magnetosheath model (or lack thereof). To address these concerns with the traditional approach, this study develops a data-driven model of the magnetosheath that uses data from L1 as its input. This new model, called PRIME-SH, adapts a Bayesian recurrent neural network architecture that is capable of estimating uncertainties for its predictions. This new model is verified to be accurate in a statistical sense, and is also capable of representing physics that is not explicitly incorporated in the model during training.

1 Introduction

The region of turbulent, shocked solar wind plasma downstream of Earth's bow shock is known as the magnetosheath. The magnetosheath plasma and magnetic field transfer energy to Earth's magnetosphere via magnetic reconnection and viscous interaction (Dungey, 1961; Axford, 1964). Despite this, the solar wind conditions upstream of the bow shock are frequently taken as the input to the system in studies of solar wind-magnetosphere interaction. This is largely because of the absence of any continuous in-situ magnetosheath monitor due to orbital constraints. Continuous records of the magnetosheath conditions therefore require modeling the magnetosheath by some method.

Early models of the magnetosheath used gas dynamics as their basis, incorporating some physical assumptions and including limited consideration of the magnetic field outside the magnetopause (Spreiter et al., 1966; Spreiter & Alksne, 1969). These models have matured through the inclusion of additional physics into modern MHD codes (e.g. Powell et al. (1999); Lyon et al. (2004)), that offer spatially and temporally complete model magnetosheaths at the cost of some physical assumptions and increased computational expense. In situations where the computational expense of MHD modeling

is prohibitive, some magnetosheath modeling efforts fit analytical expressions derived from physical assumptions to spacecraft measurements of the magnetosheath (Kobel & Flückiger, 1994; Soucek & Escoubet, 2012; Tsyganenko et al., 2023). Others, such as the recent Mshpy23 model (Jung et al., 2024), parameterize the outputs of MHD models to reduce their computational cost but retain some of their accuracy. A shared feature of these approaches is that they all include physical assumptions. While they may often be valid, there remains differences between their outputs and the actual magnetosheath that can limit their representational power. This issue could be addressed by reducing the number of assumptions used to construct the model; for example, hybrid-Vlasov codes capable of simulating the entire magnetosheath have recently come online (Von Alfthan et al., 2014; Hoilijoki et al., 2016) but come with an even higher computational cost than MHD codes.

One possible way of addressing this limitation is the use of neural network codes that do not assume a functional form or simplified physics. Neural networks have been used to assemble models of geophysical quantities for the past few decades since the early relativistic electron flux model of Koons and Gorney (1991), and have continued to be regularly utilized for space physics tasks. These algorithms do not require physical assumptions to construct tractable or analytical descriptions of the magnetosheath plasma and magnetic field, and are also computationally inexpensive. In particular, new Bayesian recurrent neural network architectures have shown good performance in spatio-temporal inversion tasks such as electron density in the inner magnetosphere (Huang et al., 2022).

A crucial aspect of any prediction algorithm that is typically lacking in magnetospheric physics (and that is addressed by Bayesian neural networks) is uncertainty quantification (Borovsky, 2021). There is growing evidence that uncertainty in solar wind data affects correlation studies of the cross polar cap potential (Sivadas et al., 2022), development of solar wind-magnetosphere coupling functions (Lockwood et al., 2019), and global MHD simulation outputs (Al Shidi et al., 2023); the solar wind data uncertainty and the magnetosheath model uncertainty compound. Since it is the shocked solar wind at the magnetopause rather than the solar wind upstream of the bow shock that interacts with the magnetosphere, this uncertainty has the potential to affect any study that tries to associate solar wind conditions with magnetospheric response in a way that is difficult to account for without a magnetosheath model that estimates this uncertainty.

Another challenge with traditional models aside from their physical assumptions is the fact that they typically use solar wind data that has been propagated from in-situ monitors far from Earth as input. Much like the magnetosheath, there is no continuous in-situ monitor of the solar wind near Earth due to orbital constraints. In order to obtain inputs for each of the previously mentioned models, data from monitors at the L1 position $235R_E$ (1,500,000 km) ahead of Earth need to be propagated to Earth to account for the travel time of the solar wind plasma and interplanetary magnetic field (generally 30-60 minutes). This propagation task is made difficult by the structure and dynamics of the solar wind (Borovsky, 2018), and a variety of algorithms have been developed in order to propagate measurements between L1 and Earth accurately. One such algorithm, the Probabilistic Regressor for Input to the Magnetosphere Estimation (PRIME) (O'Brien et al., 2023) was recently developed to address some of these difficulties with traditional propagation algorithms, and its Bayesian recurrent neural network architecture is well suited to be adapted to the problem of magnetosheath prediction from L1 inputs (since the physics of solar wind propagation is the first "step" of that task).

Motivated by the limitations of traditional algorithms outlined above, a new algorithm capable of predicting magnetosheath plasma and magnetic field conditions given measurements made by an in-situ monitor at L1 is developed. This algorithm, named PRIME-SH after its progenitor algorithm PRIME (O'Brien et al., 2023), requires a dataset of in-situ magnetosheath measurements and associated solar wind inputs at L1 (Section 2), a network architecture adapted from PRIME and optimized for the magnetosheath (Section 3). Outputs from PRIME-SH are validated statistically on a holdout dataset.

PRIME-SH is subjected to additional validation verifying that it reproduces some expected physics (Section 4), after which the results can be summarized and discussed (Section 5).

2 Data

2.1 MMS Target Dataset

Plasma and magnetic field data from the Magnetospheric Multi Scale 1 (MMS-1) spacecraft's (Burch et al., 2016) Fast Plasma Investigation (FPI) (Pollock et al., 2016) and Fluxgate Magnetometer (FGM) (Russell et al., 2016) instruments are utilized as targets for the algorithm to be optimized against. MMS is a constellation of four spacecraft designed to study magnetic reconnection at Earth's magnetopause and neutral sheet. It therefore spends considerable time in Earth's magnetosheath and carries instruments particularly designed to measure the plasma and magnetic field there, making data it collects highly suitable for use as targets to optimize PRIME-SH. The large volume of data produced by MMS-1's instruments have motivated the development of automated classification, identification, and segmentation tools for MMS data that allow rapid selection of large amounts of data with particular features or from particular plasma regimes.

To assemble a solar wind dataset using MMS, an automatic tool developed by Olshevsky et al. (2021) is used to classify all MMS-1 FPI 3D ion distributions from September 2nd 2015 to January 1st 2023. The classifier is capable of discriminating between magnetospheric, magnetosheath, non-foreshock solar wind, and foreshock plasma using the shape of the ion distribution function, and outputs a normalized probability that a given distribution belongs to each class. Periods of time where MMS-1 is in the magnetosheath with probability $p > 0.7$ are found using the classifier; all other time periods are removed thereby removing the magnetosphere, solar wind, foreshock, and ambiguous classifications from the dataset. Remaining FGM magnetic field and FPI ion moments are averaged in 100 second bins. Since the classifier is trained only on data from dayside orbits, any data on the nightside (GSE $X < 0$) are removed. The full spatial distribution of the magnetosheath data are shown in Figure 1.

2.2 Wind Input Dataset

The input solar wind data at L1 comes from the Magnetic Field Investigation (MFI) (Lepping et al., 1995) and Solar Wind Experiment (SWE) (Ogilvie et al., 1995) aboard the Wind spacecraft. Wind was selected for this study because it had the best coverage over the time period of the MMS-1 dataset used here (September 2nd 2015 to January 1st 2023). Key parameter (KP) moments data are utilized, resulting in time series of plasma flow velocity $\vec{v}$ (GSE coordinates), ion density n_{ion}, ion thermal speed $v_{\perp th}$, and IMF $\vec{B}$ (GSM coordinates) at a 100 second cadence. Due to the difficulty involved with spacecraft intercalibration data from other L1 monitors are not included in this study (King, 2005). To give PRIME-SH information about the spatial separation of the input and target spacecraft and the location in the sheath at which the prediction is being made, the positions of Wind and MMS-1 in GSE coordinates are included in the input data. Missing data are linearly interpolated and flagged so they can be excluded if necessary. The precise windows of time in the Wind dataset used as input to predict each MMS target heavily influence the performance of the optimized algorithm; these and other parameters pertaining to the exact construction of the dataset therefore must be optimized through hyperparameter search (see Section 3.2).

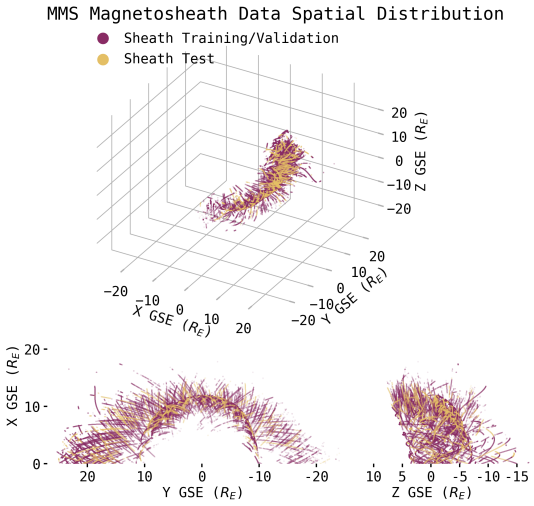

Figure 1. 3D spatial distribution of the 117,427 magnetosheath MMS-1 data points split into 80% training/validation (purple) and 20% test (yellow) subsets. Data consists of $\vec{B}_{GSM}$, $\vec{V}_{GSE}$, n_i, $T_{i\parallel}$, and $T_{i\perp}$ from September 2nd 2015 to January 1st 2023. Train/validation/test split is as used in the optimized dataset (see Section 3.2).

3 Algorithm Methodology

3.1 Network Architecture

The overall architecture selected for the algorithm is similar to that utilized to construct PRIME (Probabilistic Regressor for Input to the Magnetosphere Estimation), an algorithm that predicts the solar wind near Earth using data from the Wind spacecraft at L1 (O'Brien et al., 2023). The Bayesian recurrent neural network architecture developed for PRIME is well suited to be adapted to the task of magnetosheath prediction for several reasons. First, it is capable of incorporating information about the time history of solar wind at L1 into its predictions which is important for predicting the solar wind and the evolution of the magnetosheath. Second, it is capable of assigning uncertainties to its predictions which is crucial in the frequently turbulent environment in the magnetosheath. Third, it has proven to be accurate when applied to the task of solar wind propagation, which is essentially the first step of the task undertaken by PRIME-SH.

The overall form of PRIME-SH is shown in Figure 2. Like PRIME, PRIME-SH utilizes a Gated Recurrent Unit (GRU) sequence (See Cho et al. (2014)) that is fed into fully connected neural network (FCNN) layers (See Bebis and Georgiopoulos (1994)). The last layer of neurons are taken to be the mean and variance of a Gaussian probability distribution for each parameter rather than single scalar values (Nix & Weigend, 1994; Lakshminarayanan et al., 2017). The input feature size is 14, and the output feature size is 9. The algorithm is implemented in the Keras high-level API for tensorflow (`https://keras.io/api/`). Details of the architecture such as the length of the input time series and the size of each layer do not have optimal values that can be determined a priori. Instead, they are chosen via hyperparameter tuning (See Section 3.2).

The loss criterion used to optimize the algorithm during training is chosen to be the continuous rank probability score (CRPS) (Matheson & Winkler, 1976; Hersbach, 2000). The CRPS is a common scoring metric used to compare probabilistic forecasts for weather prediction (Zamo & Naveau, 2018). For a detailed description of the CRPS

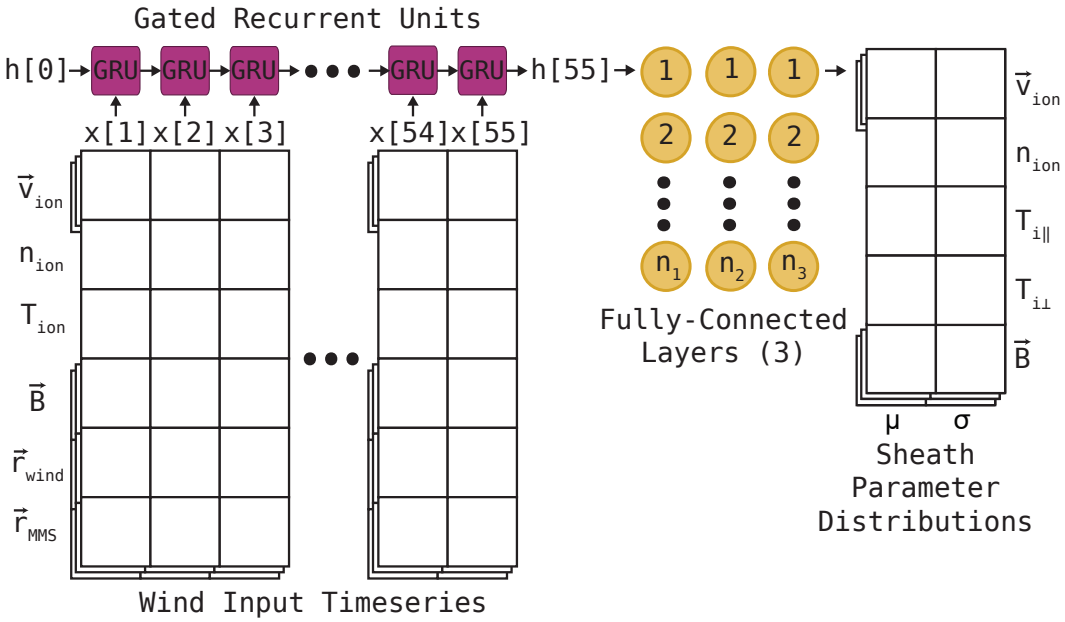

Figure 2. Schematic of PRIME-SH's neural network architecture, based on the architecture of PRIME (O'Brien et al., 2023). Note that the Gated Recurrent Unit (GRU) sequence feeds into a Fully Connected Neural Network (FCNN) in order to output a mean and variance for each desired parameter instead of a single value. Vector quantities such as magnetic field, flow velocity, and spacecraft position are stacked to show that they constitute three units in the input/output but describe one physical vector quantity. Exact layer size and additional regularization features (see Table 1) chosen via hyperparameter search.

see Section 2 of Camporeale and Carè (2021) or Section 3.1 of O'Brien et al. (2023). Briefly, the continuous rank probability score is given by

$$CRPS = \int_{-\infty}^{\infty} [F(y) - H(y - y_{obs})]^2 dy \tag{1}$$

where $F(y)$ is the cumulative distribution function of a probabilistic prediction for some observation y_{obs} and $H(y)$ is the Heaviside step function (Wilks, 2011). The continuous rank probability score is desirable as a loss function because it more symmetrically punishes over and under confident predictions than the negative log probability density (the most commonly used score for probabilistic predictions) (Camporeale & Carè, 2021). A side benefit is that the CRPS has the same unit as the variable of interest, making it more intuitively human-readable. In the case of Gaussian predictions with mean μ and variance σ^2 the CRPS is given by

$$CRPS(y_{obs}, \mu, \sigma) = \sigma \left[\frac{y_{obs} - \mu}{\sigma} erf\left(\frac{y_{obs} - \mu}{\sqrt{2}\sigma} \right) + \sqrt{\frac{2}{\pi}} e^{-\frac{(y_{obs}-\mu)^2}{2\sigma^2}} - \frac{1}{\sqrt{\pi}} \right] \tag{2}$$

(Gneiting et al., 2005). Since PRIME-SH outputs Gaussian probability distributions, and since CRPS is negatively oriented, Equation 2 is used as a loss function during training. The 18 output units in PRIME-SH's last layer are taken to be the means (μs) and variances (σs) defining a Gaussian probability distribution for each parameter. During training the CRPS over all nine parameters in the target dataset are averaged with equal weight assigned to all parameters.

The primary limitation of the CRPS as a loss function training probabilistic algorithms is the fact that it does not explicitly enforce reliability of the algorithm's predicted uncertainties (Camporeale et al., 2019). Reliability is measure of the degree to which a probabilistic forecast's uncertainties are statistically consistent with the observed probabilities of the events the forecast seeks to predict (Anderson, 1996). It has been shown that accuracy and reliability are competing metrics that must be balanced, and that simply minimizing the CRPS does not necessarily mean that the resulting model is reliable (Camporeale & Carè, 2021). Since reliability is not explicitly enforced, the reliability of PRIME-SH's uncertainties must be verified after training (See Section 4.1) (Tasistro-Hart et al., 2021).

3.2 Algorithm Optimization

Optimization of PRIME-SH follows a three step process. First, the optimal length, lead time, and composition of the input timeseries dataset is determined (the dataset hyperparameter search). Then the algorithm hyperparameters are systematically varied in order to find the optimal algorithm, then finally the optimal algorithm is instantiated and trained. This algorithm then becomes the canonical version of PRIME-SH.

Given a particular time when a prediction of the magnetosheath conditions is desired, it is difficult to say a priori what time period of Wind data from L1 contains the necessary information to make that prediction (especially given the flexible nature of neural network algorithms). Since the solar wind typically takes 30 to 60 minutes to get from L1 to Earth, there is likely only so much time history that can be incorporated before including more yields diminishing returns in terms of accuracy. Similarly, it is likely that including conditions at L1 right up until the time the sheath prediction is desired is not necessary, since the solar wind at that time has not had sufficient time to get to Earth. To find the optimal start and stop times of the timeseries used to make each prediction, a range of start and stop times are tested by optimizing a test version of PRIME-SH using different input time series lengths (windows) and lead times before each prediction (strides). It is also likely that large data gaps that are filled with interpolated data can affect the algorithm's performance, therefore a range of permissible data gap sizes are

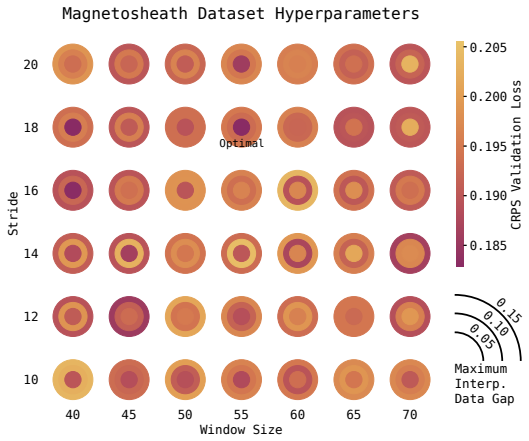

Figure 3. Results from dataset optimization trials over timeseries window (length), stride (lead time), and permitted fraction of interpolated data. Units for window and stride are 100s (the Wind KP data cadence). The optimal set (window 55, stride 18, largest interp. fraction $\leq$ 5%) is shown in darkest green and labelled "optimal". Loss is given in dimensionless units of parameter interquartile range to ensure comparability of CRPS for each parameter.

also tested (expressed in terms of fractions of the window size). Whichever parameters produce a model that can achieve the best results on the validation dataset before overfitting are taken as optimal. When training these test models and for any time a model is trained, the input/target datasets are split into 60% training, 20% validation, and 20% test subsets. Since temporally adjacent entries in the input dataset are almost entirely overlapping, randomly assigning input/target pairs to each subset results in significant data leakage. To avoid this, the full dataset is split into independent blocks four times the length of the timeseries window used as input (i.e. for a window size of 55 measurements/ ~1 hour 32 minutes, the dataset is split into chunks of length 220 measurements/ ~6 hours 8 minutes) and those blocks are then assigned to each subset in order to achieve a 60%-20%-20% train-validation-test split. To ensure that no parameter dominates others due to their absolute relative values, each subset is rescaled to the interquartile range of the training set in order to account for outliers without leaking information about the validation/test sets during training. Results on the validation dataset from the search are shown in Figure 3.

Whichever set from Figure 3 has the lowest CRPS is taken to be optimal. The optimal window size is 55 measurements ($\sim$ 5,500 seconds, ~1 hour 32 minutes), the optimal stride/lead time is 18 measurements ($\sim$1,800 seconds, ~30 minutes). That is to say, for an MMS measurement at time t, the input timeseries from Wind runs from time $t - 5,500s - 1,800s \approx t - 122min$ to time $t - 1,800s \approx t - 30min$. The largest data gap that can be interpolated over is 4.6 minutes ($\leq$ 5% of the input window).

Once the optimal dataset structure is found, the optimal model configuration can be determined via hyperparameter search. The nine hyperparameters that are optimized are listed in Table 1, along with the values used for determining the optimal dataset, the optimal values used for the canonical version of PRIME-SH, and the search range for each hyperparameter. The hyperparameter search is conducted using the Hyperband tournament bracket style algorithm (Li et al., 2018) implemented in the KerasTuner API (O'Malley et al., 2019). The meaning of each hyperparameter is described in the following paragraph. After the optimal model configuration is determined, the canonical version of PRIME-

	Dataset HP Test	Canonical Algorithm	HP Range
GRU Layer	192	416	128-640
FCNN Layer 1	352	352	128-640
FCNN Layer 2	48	32	16-128
FCNN Layer 3	N/A	64	16-128
Normalization	Last Layer	Last Layer	Any Combination
Dropout Location	Last Layer	Last Layer	Any Combination
Dropout Rate	20%	35%	20%-50%
Optimizer	Adamax	Adam	Adam, Adamax, Adagrad
Learning Rate	10^{-4}	10^{-4}	10^{-3}, 10^{-4}, 10^{-5}

Table 1. Detailed layer sizes and architecture parameters for the test version of PRIME-SH used to optimize the dataset parameters (left column), the canonical version of PRIME-SH determined by hyperparameter search (middle column), and the range of each parameter for which the hyperparameter search was conducted (right column).

SH is optimized on the training dataset for 20 epochs (the maximum before the loss on the validation dataset starts to increase).

The nine hyperparameters are as follows (see also Table 1). The first four are the node sizes of the GRU layer and the following three fully-connected layers. The fifth is where in the algorithm sequence to perform a layer normalization step, which stabilizes neural networks during optimization to reduce the time it takes to optimize them (Ba et al., 2016). Layer normalization normalizes a given layer's output vector before passing it to the next layer, which speeds up the convergence of the algorithm used to optimize the weights and biases of the algorithm by reducing the extent to which the gradients with respect to the weights in one layer covary with the outputs of the previous layer. The sixth and seventh hyperparameters are the dropout locations and rate used during training. Dropout is a technique to mitigate overfitting that involves randomly removing some percentage of the units from the network every training epoch. This prevents units from co-adapting which can lead to overfitting (Srivastava et al., 2014). The eighth and ninth hyperparameters are the optimization algorithm used to update the weights and biases in the network and that algorithm's learning rate. Included in the search are the adaptive gradient descent algorithms Adam, Adamax, and Adagrad. An adaptive gradient descent algorithm changes the step size it uses to update parameter weights during optimization to avoid getting stuck in local minima or skipping over minima. Adam updates parameters according to estimates of first order and second moments and has been shown to be suitable for optimizing large algorithms (Kingma & Ba, 2017), Adamax updates parameters according to first order moments and the infinity norm and has been shown to be suitable for recurrent networks (Kingma & Ba, 2017), and Adagrad updates its gradient descent step size per parameter based on the number of updates the parameter receives during training making it suitable for sparse gradients (Duchi et al., 2011). Since each of these conditions could apply to PRIME-SH and the dataset used to optimize it, these three algorithms were included.

4 Results

4.1 Statistical Performance

PRIME-SH's performance is evaluated on the test dataset (not seen by the algorithm at any point during training) by calculating the CRPS between its predictions and the test dataset. Additionally, the mean absolute error (MAE) and Pearson's r correlation coefficient are calculated between the means of PRIME-SH's predicted probabil-

Parameter	PRIME-SH CRPS	PRIME-SH MAE	PRIME-SH r
B_x GSM	2.65nT (0.296σ)	3.61nT (0.403σ)	0.800
B_y GSM	4.18nT (0.245σ)	5.65nT (0.331σ)	0.864
B_z GSM	5.19nT (0.323σ)	7.08nT (0.440σ)	0.779
V_x GSE	14.03km/s (0.182σ)	19.25km/s (0.250σ)	0.945
V_y GSE	13.22km/s (0.127σ)	17.95km/s (0.173σ)	0.969
V_z GSE	15.35km/s (0.291σ)	21.04km/s (0.399σ)	0.838
n_i	$3.63cm^{-3}$ (0.169σ)	$4.96cm^{-3}$ (0.231σ)	0.929
$T_{i\perp}$	23.76eV (0.158σ)	32.58eV (0.216σ)	0.936
$T_{i\parallel}$	22.67eV (0.198σ)	30.70eV (0.268σ)	0.881
P_{dyn}	0.255nPa (0.224σ)	0.353nPa (0.311σ)	0.859

Table 2. Performance of PRIME-SH on the MMS test dataset across continuous rank probability score (CRPS, Equation 1), mean absolute error (MAE), and Pearson's r correlation coefficient (also shown in Figure 4). CRPS is given in the units of each parameter as well as dimensionless units of standard deviations of each parameter in the MMS training dataset to facilitate comparison between each parameter.

ity distributions and the MMS test set thereby ignoring the uncertainty information. To gain a better sense of the accuracy of PRIME-SH's predictions in a statistical sense, its outputs are compared to several analytical models and a parameterization of a popular MHD code for the same MMS-1 test dataset (Figure 4, Table 2). For magnetic field, the model derived in Cooling et al. (2001) is utilized. The Cooling et al. (2001) model essentially "drapes" the interplanetary magnetic field over the Shue et al. (1998) axisymmetric conic section magnetosheath model (based on Kobel and Flückiger (1994)). For magnetosheath flow, the model derived in Soucek and Escoubet (2012) is utilized. The Soucek and Escoubet (2012) model is partially based on Génot et al. (2011) and Kobel and Flückiger (1994), but extends those works to additional magnetopause and bow shock shapes. For density and temperature, the model derived in Spreiter et al. (1966) is utilized. The Spreiter et al. (1966) model is a gas dynamic model that assumes a nondissipative, ideal, compressible, steady flow. Additionally, PRIME-SH is compared to a parameterization of the OpenGGCM MHD code (Raeder et al., 2001, 2008) developed in Jung et al. (2024). This parameterization cannot capture small-scale structure in the MHD code's outputs, but has been shown to be accurate when compared to observations and is importantly computationally inexpensive enough to enable the statistical comparison in this study. The Soucek and Escoubet (2012) and Spreiter et al. (1966) models are implemented in the Mshpy23 package (Jung et al., 2024) and accept one minute resolution OMNI data as input (King & Papitashvili, 2020). The Spreiter et al. (1966) and OpenGGCM models produce isotropic temperatures, therefore their temperatures are compared to the average temperature measured by MMS $T_{iAV} = (2T_{i\perp} + T_{i\parallel})/3$. None of the models PRIME-SH is compared to have uncertainty information, therefore the MAE and CRPS reduce to the same form and number (Hersbach, 2000); both metrics are provided for PRIME-SH's outputs so that all comparisons can be made.

On average, PRIME-SH predicts plasma parameters ($\vec{v}$, n_i, $T_{i\perp}$, and $T_{i\parallel}$) slightly more accurately than magnetic field parameters. This is possibly due to the fact that fluctuations in magnetic field happen more quickly than those in the plasma, and neural networks tend to have more difficulty representing smaller scale variations than larger scale ones whether temporal or spatial in nature. PRIME-SH has a Pearson's r higher than 0.75 for every parameter. There are no strong biases or systematic errors visible in Figure 4, only some amount of regression to the mean in the most extreme values of V_X and n_i (and therefore in P_{dyn} as well). Interestingly, PRIME-SH predicts magnetosheath

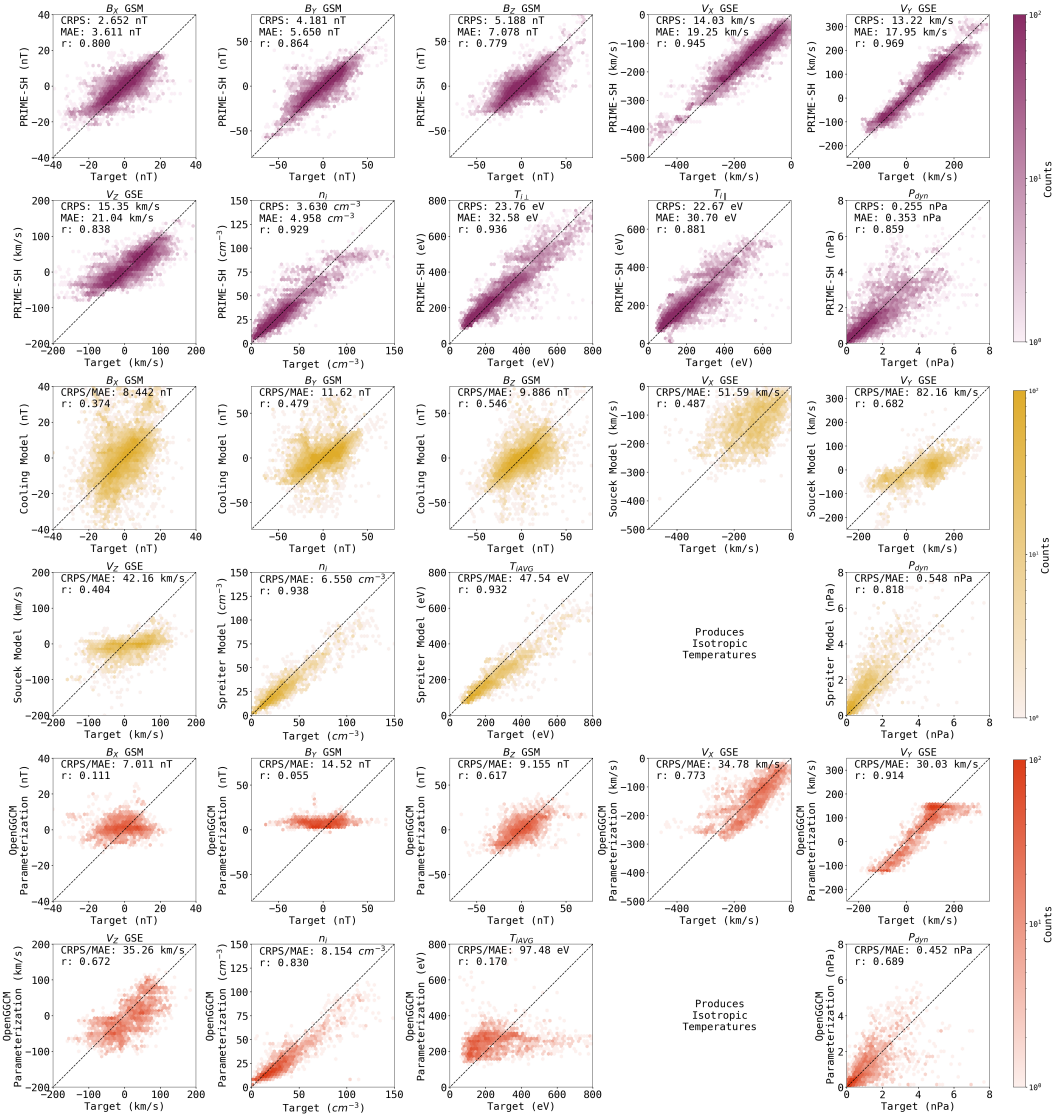

Figure 4. Joint distributions of MMS-1 data (x axis) with predicted parameters from PRIME-SH (purple, top), three analytical magnetosheath models (yellow, middle), and a parameterization of the OpenGGCM MHD code (orange, bottom). CRPS, the mean absolute error (MAE), and Pearson's r correlation coefficient for each parameter shown in the top left of each distribution. The MAE is calculated between the peaks of PRIME-SH's predicted distributions and each MMS observation (thereby throwing away uncertainty information). A perfect prediction corresponds to the line $y = x$, plotted overtop of each distribution for convenience.

conditions almost as accurately as its progenitor algorithm PRIME predicts solar wind conditions given the same type of input data from L1 (PRIME-SH's average CRPS of 0.221σ and PRIME's average CRPS of 0.214σ), despite that it has to represent not only the physics of the solar wind's propagation from L1 to Earth but the physics of the bow shock as well.

For all parameters PRIME-SH outperforms all of the analytical models considered here with respect to MAE and CRPS. For each component in the magnetic field, PRIME-SH predicts MMS-1 observations more accurately than the Cooling et al. (2001) model. Specifically, PRIME-SH's CRPS and MAE are both lower than the Cooling et al. (2001) model's MAE, and PRIME-SH's Pearson's r is higher than the Cooling et al. (2001) model's Pearson's r. There appears to be some systematic overprediction in the Cooling et al. (2001) model's outputs for B_X. This means that PRIME-SH reproduces the actual magnetic field in the magnetosheath given upstream conditions more accurately than the Cooling et al. (2001) model, but whether it produces a physically accurate draped field must be separately validated in Section 4.2.1. The Soucek and Escoubet (2012) model has a large variance in V_X and does not reproduce fast flows ($> 300km/s$) as accurately as PRIME-SH does. It also underpredicts V_Y and V_Z, all of which could be regression effects due to model outputs being too "smooth". The Spreiter et al. (1966) comes the closest to outperforming PRIME-SH of any model considered here, but still does not predict n_i or T_{iAVG} more accurately than PRIME-SH.

Compared to the parameterized MHD model, PRIME-SH has higher representational power and therefore higher accuracy across the parameters. For B_X and B_Y the parameterized MHD model does not vary by much (both have Pearson's $r < 0.12$), which could be consistent with the results presented in Jung et al. (2024) Figures 2, 3, and 4. For plasma flow velocity, the parameterized MHD model clearly reaches the bounds of its parameterization (most visible for $V_Y < -120km/s$ and $V_Y > 160km/s$). The shape of the distribution for T_{iAVG} is also consistent with results presented in Jung et al. (2024) Figure 2. The MHD model is more accurate than the associated analytical model for all parameters except B_Y, n_i, T_{iAVG}, and P_{dyn}, but is not more accurate than PRIME-SH for any of the parameters it is capable of predicting.

PRIME-SH is a 3D model, and its outputs are valid over any regions covered by MMS-1's orbit on the dayside (GSE $X > 0R_E$, GSE $|Y| < 5R_E$). Since the magnetosheath conditions vary significantly across its extent, PRIME-SH's accuracy evaluated against the test set is displayed in GSE coordinates in Figure 5. In general, PRIME-SH's outputs are generally less accurate on predictions closer to the Earth than on those further from the Earth. This suggests that PRIME-SH is less accurate during periods where the magnetosheath is highly compressed or when it makes predictions close to the magnetopause. These periods are rare relative to nominal conditions in the training dataset, so PRIME-SH being somewhat less accurate under these conditions is expected and should be taken into account when using PRIME-SH. It is worth noting that PRIME-SH has not been trained outside of the areas shown in Figure 5 and thus its predictions outside of those areas are likely to be inaccurate or unphysical due to its nature as a neural network algorithm.

Since reliability is not enforced by the CRPS loss function during training, PRIME-SH's output uncertainties must be validated quantitatively through the use of a reliability diagram (Hamill, 1997, 2001). Following the procedure in Camporeale et al. (2019) and Camporeale and Carè (2021), the standardized errors associated with prediction μ_i, σ_i with $i = 1, ..., N$ are defined as $\eta_i = (y_{obs,i} - \mu_i)/(\sqrt{2}\sigma_i)$. The probability density of a given Gaussian forecast is therefore $\Phi_i = \frac{1}{2}[erf(\eta_i) + 1]$, allowing the reliability diagram to be constructed from the empirical cumulative distribution of Φ_i given by $C(\phi) = \frac{1}{N}\sum_{i=1}^{N} H(\phi - \Phi_i)$ (with H being the Heaviside step function). $C(\phi)$ is the observed frequency as a function of the predicted frequency, the same as reliability diagrams of forecasts of discrete events (e.g. those in Hamill (1997)). This method has the benefit

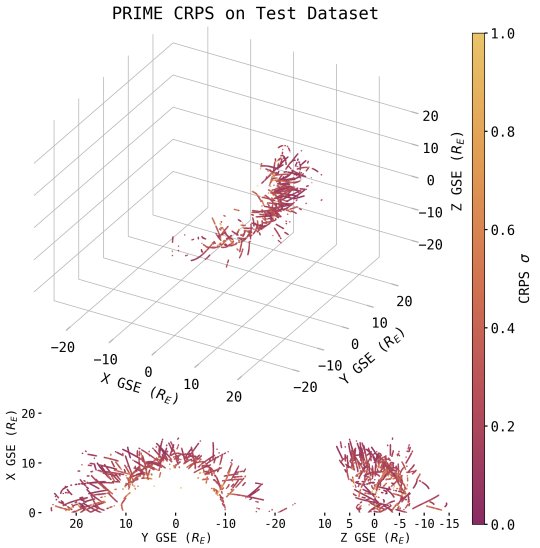

Figure 5. PRIME-SH's accuracy on the test dataset averaged across all nine target parameters in dimensionless standard deviation units (σ). Targets arranged spatially in 3D (top), the GSE X-Y plane (bottom left), and the GSE X-Z plane (bottom right).

of not requiring binning, which has been shown to affect the results of reliability diagrams of discrete events (Bröcker & Smith, 2007). $C(\phi)$ is calculated for all observations in the test dataset for each parameter and presented in Figure 6.

PRIME-SH is not perfectly reliable (its reliability diagram does not exactly follow the dashed line in Figure 6); it generally tends to overestimate the likelihood of unlikely events, and underestimate the likelihood of likely events. With the exception of V_Z, B_X, and $T_\parallel$, PRIME-SH tends to be conservative. This is not unexpected, as even models perfectly calibrated on training data can suffer calibration loss on the test dataset (Kull & Flach, 2015). The largest departures from perfect calibration are observed in V_Y GSE (predicts events that occur with $p = 0.221$ as occurring with $p = 0.320$), B_X GSM (predicts events that occur with $p = 0.754$ as occurring with $p = 0.657$), and $T_\parallel$ (predicts events that occur with $p = 0.674$ as occurring with $p = 0.586$). On average PRIME-SH is reliable to within 3.5% with a maximum difference 10% (calculated $p_{obs} - p_{pred}$). This is roughly as reliable as its progenitor algorithm PRIME and other probabilistic prediction algorithms for space weather tasks (e.g. Tasistro-Hart et al. (2021)), but less reliable than those that use loss functions that enforce reliability explicitly (e.g. Hu et al. (2022)).

4.2 Physical Validation

While a model's accuracy and reliability are important to quantify statistically, it is also important to verify that a model can reproduce expected physics. This is especially important for neural network models that can relatively easily overfit and reproduce a dataset's noise rather than the underlying data representation or physics. In the following sections PRIME-SH's outputs for synthetic data are investigated to ensure that it can reproduce magnetic field and plasma physics in the magnetosheath.

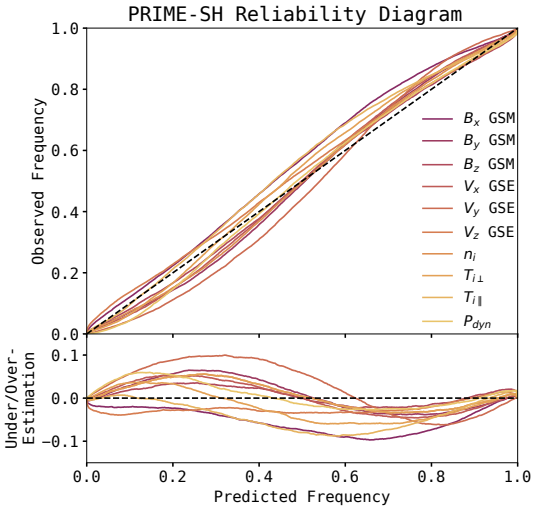

Figure 6. Reliability diagram constructed from PRIME-SH's outputs on the test dataset for each parameter. Shown versus the predicted frequency of the observation from PRIME-SH are the value of the observed frequency (top) and the deviation from perfect reliability (bottom). For the bottom plot, a given parameter being over (under) the line by an amount corresponds to PRIME-SH over (under) predicting the frequency by that amount.

4.2.1 Field Line Draping and Uncertainty

Since the interplanetary magnetic field is frozen into the solar wind plasma, as the plasma is shocked and diverted around the magnetopause the magnetic field "drapes" over the obstacle forming a tangential discontinuity at the magnetopause (Crooker et al., 1985). In order to verify that PRIME-SH captures this feature of the magnetosheath, outputs are generated on a grid of points for the same input data. The grid is chosen to lie in the GSE X-Y or GSE X-Z plane (depending on IMF orientation) with a grid scale of $0.1R_E$. All grid cells inside the Shue et al. (1998) or outside the Jelínek et al. (2012) bow shock (calculated using the conditions at L1 used as inputs for PRIME-SH) are left unused. Only grid cells in regions well sampled by the MMS training data are included, hence the Z extent is restricted to $\pm 5R_E$ away from the ecliptic and the nightside is not included (see Figure 1). The input data are chosen to be a $400km/s$ solar wind only in the GSE X direction with otherwise average solar wind conditions from the Wind L1 dataset: $|B| = 5.34nT$, $V_X = -400km/s$, $V_Y = 0km/s$, $V_Z = 0km/s$, $n_i = 7.12cm^{-3}$, and $v_{th} = 34.9km/s$. In order to investigate whether PRIME-SH is capable of draping, conditions on the grid are calculated for six different IMF orientations: one radial toward Earth (cone angle 0°), one dawnward (cone angle −90°), one duskward (cone angle +90°) one radial away from Earth (cone angle 180°), one purely northward (clock angle 0°), and one purely southward (clock angle 180°). Shown in Figure 7 are these six grids, with the sheath magnetic field streamlines plotted in black arrows and the magnitude of B in each cell in color.

As can be seen in Figure 7, PRIME-SH reproduces the draping of the magnetic field in the magnetosheath well despite the frozen in condition not being enforced during training. For cone angles of ±90° the magnetic field piles up at the nose of the magnetopause, much more than it does for radial IMF. This can be seen in the magnitude of the magnetic field, which is higher at the nose than the flanks for cone angles of ±90°. For cone angles of 0° or 180°, the flanks have a relatively higher magnetic field than the nose (though it is not as strong as the field at the nose in the cone angle ±90° case). For northward

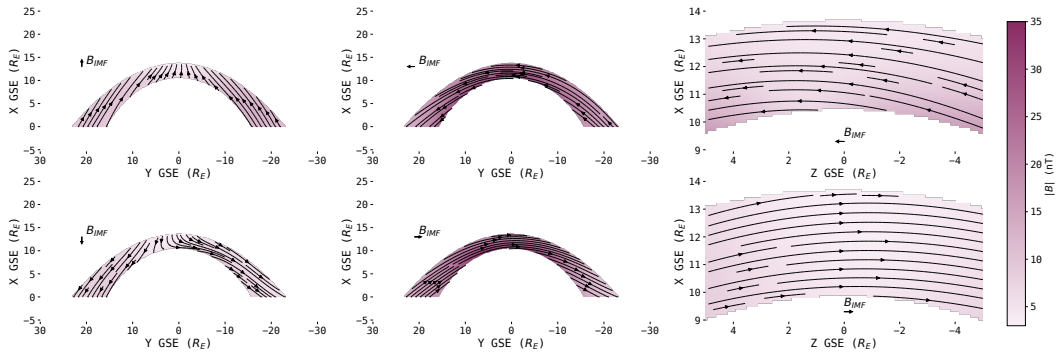

Figure 7. Magnetosheath conditions output by PRIME-SH using synthetic data for six different IMF orientations (Shown with arrows in top left or bottom). Plasma conditions are average conditions from the input dataset, magnetic field magnitude is $5.34nT$ (the average magnitude from the input dataset). Shown in color is the magnitude of B, and the arrows are B_X and B_Y GSM field lines (for the left four plots) or the B_X and B_Z GSM field lines (for the right two plots).

IMF, somewhat more magnetic field pileup pileup is observed at the northern and southern flanks than for the southern IMF case. The magnetic field magnitude is also slightly higher overall in the northward IMF case than in the southward IMF case. These maps suggest that a lower reconnection rate for northward IMF at the nose causes magnetic field pileup and rearrangement in the sheath as many studies have predicted.

4.2.2 Stagnation Point

As the solar wind plasma diverts and is slowed around the magnetopause, a region known as the stagnation point develops where there is very little to no plasma flow (Spreiter et al., 1966). For radial flow and typical Parker spiral magnetic field orientation, this point is thought to be roughly located at the nose of the magnetopause (with slight aberration from Earth's $\approx$ 30km/s motion in the negative GSE Y direction). MHD theory predicts that for a Parker spiral IMF, the stagnation point should deflect dawnward for solar wind flows with low Alfvén Mach numbers (Russell et al., 1981). Here PRIME-SH is used to assemble predictions on more $0.1R_E$ grids of the same configuration as Section 4.2.1, however this time the Alfvén Mach number of the synthetic dataset is varied from $M_A = 4$ to $M_A = 16$ (the solar wind typically has $M_A \approx 10$). The density and velocity are held the same ($n_i = 7.12$, $V_X = -400km/s$) and the magnetic field is kept at a 45° Parker spiral as its magnitude is decreased in steps from $12nT$ to $2.4nT$ to yield the four Alfvén Mach numbers. Shown in Figure 8 are these four grids, with the X and Y GSE plasma flow velocity depicted with black arrows and the Z GSE flow velocity in color. Also depicted is the stagnation point, marked with a purple X.

As can be seen in Figure 7, PRIME-SH produces continuous flow maps that divert around the magnetopause for all four Alfvén mach numbers. Additionally, as the Alfvén Mach number decreases the stagnation point is observed to move dawnward as predicted by MHD theory and simulations. This feature is hard to observe using in-situ instruments, but here through what is essentially a spatio-temporal inversion the feature is shown to occur in reality.

One interesting feature is that there appears to be some weak dawn-dusk asymmetry in the flow velocity maps produced by PRIME-SH. This could be due to biases in MMS-1's orbit showing up in PRIME-SH' outputs, as the asymmetry does not ap-

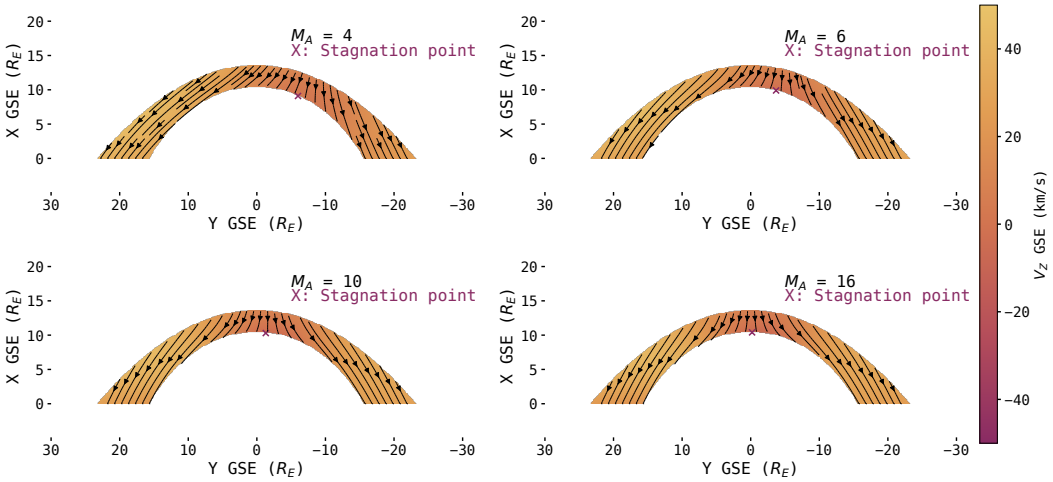

Figure 8. Magnetosheath conditions output by PRIME-SH using synthetic data at four different Alfvén Mach numbers ($M_A = 4, 6, 10, 16$). Flow velocity is $400 km/s$ with $V_Y = V_Z = 0$, magnetic field is a Parker spiral orientation whose magnitude is varied for each case to result in the four Alfvén Mach numbers. Shown in color is the Z GSE velocity, and the arrows are the X and Y GSE velocity. The point of minimum velocity in the sheath (the stagnation point) is marked with the purple X.

pear in MHD simulations of the magnetosheath. However, other experimental work has also found dawn-dusk asymmetries in the magnetosheath properties (Walsh et al., 2012; Dimmock & Nykyri, 2013).

4.2.3 Shock Jump Conditions

Shocks, whether they are collisional or collisionless, conserve mass, momentum and energy. The Rankine-Hugoniot shock jump conditions are formulations of each of these conservation laws in terms of the conditions upstream and downstream of the shock. For an MHD shock, define the shock normal direction to be $\hat{n}$, the plasma flow velocity to be $\vec{v}$, the plasma mass density to be ρ, the thermal pressure to be P, the specific heat ratio to be γ, and the magnetic field to be $\vec{B}$. For some quantity $\vec{X}$ upstream and downstream of the shock, define the notation $\vec{X}_{up} - \vec{X}_{down} = [\vec{X}]$. Mass conservation upstream and downstream of the shock can then be written:

$$[\rho \vec{u} \cdot \hat{n}] = 0 \tag{3}$$

Momentum conservation (with magnetic pressure included) can be written:

$$[\rho \vec{u}(\vec{u} \cdot \hat{n}) + (P + \frac{\vec{B}^2}{2\mu_0})\hat{n} - \frac{(\vec{B} \cdot \hat{n})\vec{B}}{\mu_0}] = 0 \tag{4}$$

Energy conservation can be written:

$$[\vec{u} \cdot \hat{n}(\frac{\rho \vec{u}^2}{2} + \frac{\gamma}{\gamma - 1}P + \frac{\vec{B}^2}{\mu_0}) - \frac{(\vec{B} \cdot \hat{n})(\vec{B} \cdot \vec{u})}{\mu_0}] = 0 \tag{5}$$

(Kallenrode, 2010).

None of these conditions are explicitly enforced during training, but they are part of the underlying physics PRIME-SH should be representing. To validate that PRIME-SH reproduces these conservation laws, a range of synthetic solar wind conditions with

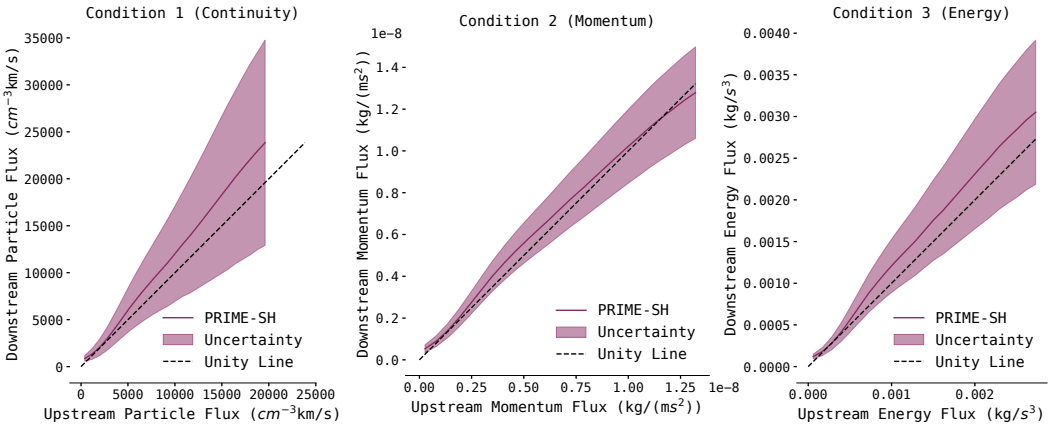

Figure 9. Particle, momentum, and energy fluxes calculated across a range of synthetic input conditions roughly corresponding to the range of the training dataset. Fluxes are calculated just upstream of the bow shock nose (using the input data) and just downstream (using PRIME-SH's outputs), and uncertainties are calculated by propagating PRIME-SH's predicted uncertainties through the MHD shock jump condition equations. Within PRIME-SH's predicted uncertainties the three Rankine-Hugoniot MHD jump conditions are obeyed.

densities ranging from $1cm^{-3}$ to $50cm^{-3}$ with $V_{GSE} = -400km/s$, $\vec{B} = (-4nT)\hat{x} + (-4nT)\hat{y}$, and $v_{th} = 30km/s$ are initialized and used to generate predictions just behind the Jelínek et al. (2012) bow shock nose along the Sun-Earth line. This range was chosen to reflect the full range of densities from the input dataset, which results in better coverage of the range of the three upstream fluxes observed than varying other conditions such as velocity. Equations 3, 4, and 5 are used to calculate the particle, momentum, and energy flux from the synthetic input data (upstream) and from PRIME-SH's outputs (downstream). The uncertainties predicted by PRIME-SH can be propagated through Equations 3, 4, and 5 to obtain uncertainties for the downstream fluxes as well. Only magnetosheath conditions on the Sun-Earth line just behind the Jelínek et al. (2012) bow shock nose are included so it can be assumed that $\hat{n} = \hat{x}$. The downstream fluxes are plotted as a function of upstream fluxes in Figure 9.

Perfect conservation of each flux is represented by the dashed lines in Figure 9. As can be seen, while the quantities predicted by PRIME-SH do not perfectly conserve mass/particles, momentum, and energy, it does conserve them within the the 1σ uncertainty bounds for each quantity. One contribution to this uncertainty is an experimental one. Although the instruments on Wind and MMS have been carefully calibrated, they were not calibrated together. Previous studies have found mismatches when comparing plasma and magnetic field parameters from different missions, even those with very similar instruments (King, 2005; Roberts et al., 2021). The points of largest *fractional* difference between upstream and downstream fluxes occur for the smallest fluxes (when $n_{up} = 1cm^{-3}$), which happens relatively infrequently in the input dataset. Despite the fact that mass/particle conservation, momentum conservation, and energy conservation were not explicitly enforced during training, PRIME-SH has been optimized such that it successfully represents the underlying physics to a degree that the three quantities are conserved.

4.2.4 Plasma Depletion Layer

The plasma depletion layer is a transient region of the subsolar magnetosheath characterized by decreased density and increased magnetic field strength. This layer exists

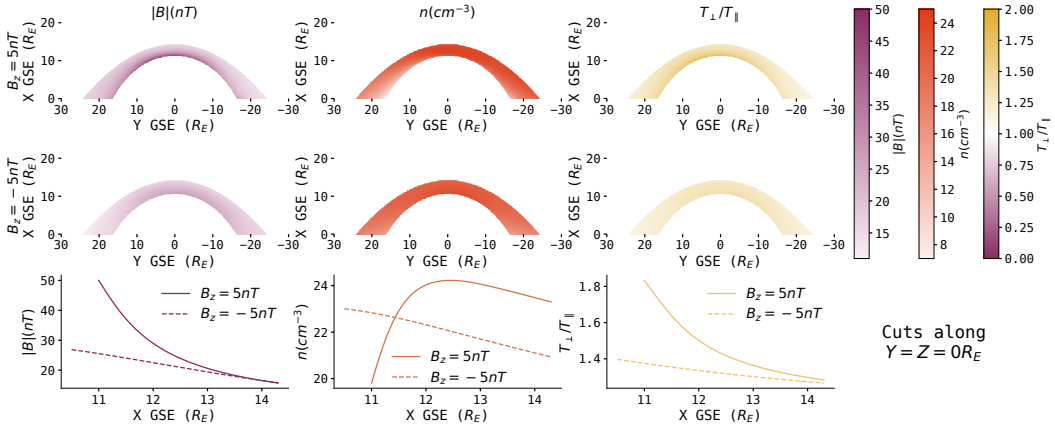

Figure 10. Magnetosheath conditions output by PRIME-SH for synthetic input conditions with IMF purely northward ($B_Z = 5nT$) and purely southward ($B_Z = -5nT$). Average plasma conditions from the input dataset are used. Top row shows $|B|$, n_i, and $T_\perp/T_\parallel$ for $B_Z = 5nT$, middle row shows the same for $B_Z = -5nT$, and bottom row shows cuts along $Y = Z = 0R_E$ for both magnetic field orientations for each parameter for ease of comparison.

when the reconnection rate at the magnetopause is insufficient to prevent "pile-up" of magnetic flux, and as such is typically observed during periods of northward IMF (although it can sometimes be observed during periods of southward IMF). This "pile-up" can modify the local reconnection rate, and could even enable reconnection at the subsolar magnetopause for northward IMF (Anderson, 1996). It has also been shown that the plasma depletion layer has stronger temperature anisotropy than the rest of the magnetosheath, although it is currently unclear whether this is a formation mechanism of the region or simply a consequence of the flux pile-up (Phan & Paschmann, 1996). Despite the fact that the plasma depletion layer has been observed by in-situ spacecraft for many years (Cummings & Coleman, 1968), the dynamics and global geometry of the region is difficult to determine from observations due to their spatio-temporal ambiguity (Wang et al., 2004).

Both to verify PRIME-SH has been properly trained to replicate solar wind flow around the magnetosphere and to overcome the spatio-temporal ambiguity of in-situ observations, PRIME-SH is used to assemble predictions on more grids of the same configuration as Section 4.2.1 for northward ($\vec{B} = 5nT\hat{z}$) and southward ($\vec{B} = -5nT\hat{z}$) IMF. Plasma conditions are the same between each run ($V_{GSE} = -400km/s$, $n = 5cm^{-3}$, and $v_{th} = 30km/s$, Alfvén Mach number 8). The magnetic field magnitude, density, and temperature anisotropy ($T_\perp/T_\parallel$) are shown for each configuration in Figure 10 in the ecliptic and in cuts along the Sun-Earth line.

The plasma depletion layer can be identified in Figure 10 as the region of high $|B|$, $T_\perp/T_\parallel$ and low n close to the subsolar point in the northward IMF case that is not apparent in the southward IMF case. In the cuts along the Sun-Earth line, the density can be more readily observed to begin falling off about $1R_E$ from the magnetopause, while at the same time $|B|$ and $T_\perp/T_\parallel$ begin to increase. This is contrasted with the southward case, in which all three parameters increase across the sheath somewhat linearly. This thickness is consistent with reported thicknesses from the literature which range from $0.3R_E$ to $1R_E$ for $M_A = 8$, depending on identification criteria (Wang et al., 2004). This validates that PRIME-SH has been trained to reproduce magnetic flux pile-up and its effects in the magnetosheath, which are indirect measurements of the dayside magnetic reconnection rate. Unlike numerical simulations, PRIME-SH can generate spatial

map of the plasma depletion layer based directly on observations rather than physical assumptions, which can cause deviation between predicted and observed global depletion layer configurations (Zwan & Wolf, 1976; Southwood & Kivelson, 1995).

5 Conclusions

A Bayesian recurrent neural network is trained to predict MMS-1 observations of Earth's magnetosheath given timeseries input measured by the Wind spacecraft at L1. This algorithm, called PRIME-SH in reference to its progenitor algorithm PRIME, incorporates the time history of the solar wind at L1 to generate probability distributions for magnetosheath plasma and magnetic field parameters. These probability distributions can be used to determine the uncertainty associated with PRIME-SH's predictions.

PRIME-SH is shown to have good performance in a statistical sense across a test dataset of MMS-1 data not used during training (Average CRPS 0.221σ). The uncertainties predicted by PRIME-SH are shown to be reliable to within 3.5% with a maximum difference 10% through a comparison to the test dataset. Additionally, PRIME-SH predicts magnetosheath conditions more accurately than several popular analytical models (Spreiter et al., 1966; Kobel & Flückiger, 1994; Cooling et al., 2001; Soucek & Escoubet, 2012) and a parameterization of the OpenGGCM MHD code (Jung et al., 2024). While statistical validation is important, it is also important to validate that a model is indeed producing physical results. It is verified that the magnetic field values produced by PRIME-SH across a grid of points in the magnetosheath "drape" across the magnetopause in 3D for several different orientations of the upstream magnetic field. Plasma flow velocities output by PRIME-SH across a grid of magnetosheath points divert around the magnetopause as expected, and the point at which the flow stagnates moves dawnward with decreasing Alfvén Mach number as predicted by MHD theory (Russell et al., 1981). PRIME-SH is shown to conserve particle/mass flux, momentum flux, and energy flux within 1σ uncertainty across the bow shock for the range of input parameters it is trained on. PRIME-SH is also capable of reproducing the plasma depletion layer given input conditions for which the depletion layer is expected to form. From this it may be concluded that PRIME-SH has indeed been optimized to represent the physics of solar wind flow from L1, through the bow shock, and around the magnetopause.

PRIME-SH is not only more accurate in a statistical sense than current analytical models and MHD simulation parameterizations, but it also has additional functionality these other models do not. First, PRIME-SH outputs $T_\perp$ and $T_\parallel$ separately. While it is possible to have anisotropic temperatures in MHD simulations using a few assumptions (Erkaev et al., 1999), most MHD and analytical models currently assume isotropic temperatures. Additionally, PRIME-SH outputs uncertainties for with its outputs. These uncertainties were used in this study to assign confidence intervals to fluxes calculated to verify that PRIME-SH conserves particles, mass, and energy. They could additionally be used to in more advanced techniques such as regression recalibration or ensemble modeling. In short, PRIME-SH is an accurate and computationally inexpensive magnetosheath prediction algorithm that offers functionality no other magnetosheath prediction algorithm does, and enables new statistical and event-based studies of the magnetosheath.

Appendix A Open Research

Magnetospheric Multiscale, Wind, and OMNI data are available through the Coordinated Data Analysis Web (CDAWeb) online portal at `https://cdaweb.gsfc.nasa.gov/istp_public/`. Codes for dataset preparation, algorithm development, and analysis presented in this paper are available at `https://github.com/connor-obrien888/primesh`.

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