

Wetting-phase relative permeability in multi-scale porous media

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BACKGROUND

Factors affecting wetting-phase relative permeability

- Connectivity
- Pore-throat size distribution
- Tortuosity
- Porosity
- Pore shape geometry
- ...

Theoretical upscaling techniques

- Bundle of capillary tubes approach
- Effective-medium approximation (EMA)
- Critical path analysis (CPA)
- Perturbation theory
- Volume averaging method
- ...

PURPOSES AND ASSUMPTIONS

Objectives

- ✓ To apply concepts from CPA to dual-porosity media by revisiting the Hunt et al. (2013) model.
- ✓ To evaluate k_{rw} estimation from accurately characterized S_w - P_c curve using a database including 26 samples.
- ✓ To compare the accuracy of the bi-modal CPA model with that of the bi-modal vG-M model.

Assumptions

- Pores are cylindrical.
- k_{rw} is mainly controlled by pores with sizes greater than some critical pore size.
- ϕ_1 and ϕ_2 are porosities corresponding to the structural and textural pores, respectively.

MATERIALS AND METHODS

Hydraulic flow in a tube of radius R

$$g_h = \frac{\pi R^4}{8\mu l}$$

Samples

The database used in this study is from Schwen et al. (2015) and includes 26 samples. The S_w - P_c and S_w - k_{rw} curves, each of which includes 500 measured data points determined using the evaporation method with extended range of measurements.

Critical path analysis

Concepts of critical path analysis (CPA) from percolation theory have been successfully used to model hydraulic properties of porous media (Hunt et al., 2014; Hunt, 2001). Based on CPA, transport in a network of pores is dominated by those pores whose sizes are greater than some critical size (Fig. 1). Accordingly, pores smaller than the critical pore size make trivial contribution to the overall transport.

Bimodal capillary pressure curve model

For dual-porosity media the capillary pressure curve model is

$$S_w = \begin{cases} 1, & P_c < P_{d1} \\ 1 - \frac{\beta_1}{\phi} \left[1 - \left(\frac{P_c}{P_{d1}} \right)^{D_1-3} \right], & P_{d1} < P_c < P_x \\ S_{wx}, & P_x < P_c < P_{d2} \\ \frac{\phi_2}{\phi} - \frac{\beta_2}{\phi} \left[1 - \left(\frac{P_c}{P_{d2}} \right)^{D_2-3} \right], & P_c > P_{d2} \end{cases}$$

Wetting-phase relative permeability model

Hunt et al. (2013) proposed the following bi-modal model for k_{rw} :

$$k_{rw} = \begin{cases} \left[\frac{\beta_1 - \phi + \phi S_w}{\beta_1} \right]^{\frac{3}{3-D_1}}, & S_w > \phi_2/\phi \\ \left(\frac{\beta_1 - \phi_1}{\beta_1} \right)^{\frac{3}{3-D_1}} \left[\frac{\beta_2 - \phi_2 + \phi S_w}{\beta_2} \right]^{\frac{3}{3-D_2}}, & S_w < \phi_2/\phi \end{cases}$$

RESULTS

Sample	ϕ	D_1	β_1	P_{d1} (cm)	D_2	β_2	P_{d2} (cm)	P_x (cm)	ϕ_1	ϕ_2
CT_1	0.50	2.875	0.47	1.8	2.571	0.22	1418	679	0.25	0.22
CT_2	0.49	2.871	0.44	1.3	2.511	0.17	3508	2590	0.27	0.19
CT_3	0.56	2.235	0.30	6.6	2.687	0.22	1105	373	0.28	0.22
CT_4	0.56	2.511	0.31	3.9	2.637	0.22	1696	469	0.28	0.22
CT_5	0.51	2.489	0.24	5.0	2.601	0.24	1527	373	0.22	0.24
CT_6	0.49	2.573	0.24	4.2	2.606	0.25	1423	340	0.20	0.25
CT_7	0.55	2.194	0.30	6.8	2.636	0.22	1564	373	0.29	0.22
CT_8	0.55	2.535	0.30	2.6	2.631	0.23	1245	310	0.27	0.23
CT_9	0.56	2.595	0.31	2.0	2.638	0.21	1048	296	0.27	0.21
CT_10	0.60	2.347	0.30	6.6	2.690	0.22	501.1	224	0.26	0.22
CT_11	0.53	2.852	0.49	4.5	2.511	0.16	2863	2360	0.29	0.18
CT_12	0.54	2.935	0.58	1.1	2.620	0.25	835.6	195	0.16	0.25
CT_13	0.54	2.551	0.32	3.0	2.645	0.22	1340	340	0.28	0.22
NT_1	0.40	2.958	0.74	16.0	2.447	0.25	2293	1080	0.12	0.28
NT_2	0.45	2.945	0.70	13.9	2.408	0.29	1730	816	0.14	0.31
NT_3	0.41	2.928	0.34	26.2	2.561	0.30	904.8	539	0.07	0.32
NT_4	0.47	2.970	0.86	2.3	2.550	0.25	1106	679	0.14	0.28
NT_5	0.49	2.662	0.20	8.8	2.646	0.31	1412	409	0.15	0.30
NT_6	0.46	2.951	0.91	16.3	2.458	0.26	1575	1420	0.18	0.28
NT_7	0.44	2.951	0.61	3.8	2.515	0.24	1556	1080	0.15	0.26
NT_8	0.44	2.962	1.00	21.3	2.515	0.25	2050	2050	0.16	0.28
NT_9	0.45	2.959	1.00	9.8	2.526	0.25	1677	1290	0.18	0.27
NT_10	0.45	2.974	1.00	3.5	2.512	0.32	1734	282	0.11	0.33
NT_11	0.41	2.968	1.00	10.2	2.518	0.23	1964	1490	0.15	0.26
NT_12	0.42	2.965	1.00	9.7	2.545	0.24	1614	1560	0.16	0.26
NT_13	0.46	1.875	0.13	55.5	2.605	0.27	1743	428	0.12	0.27

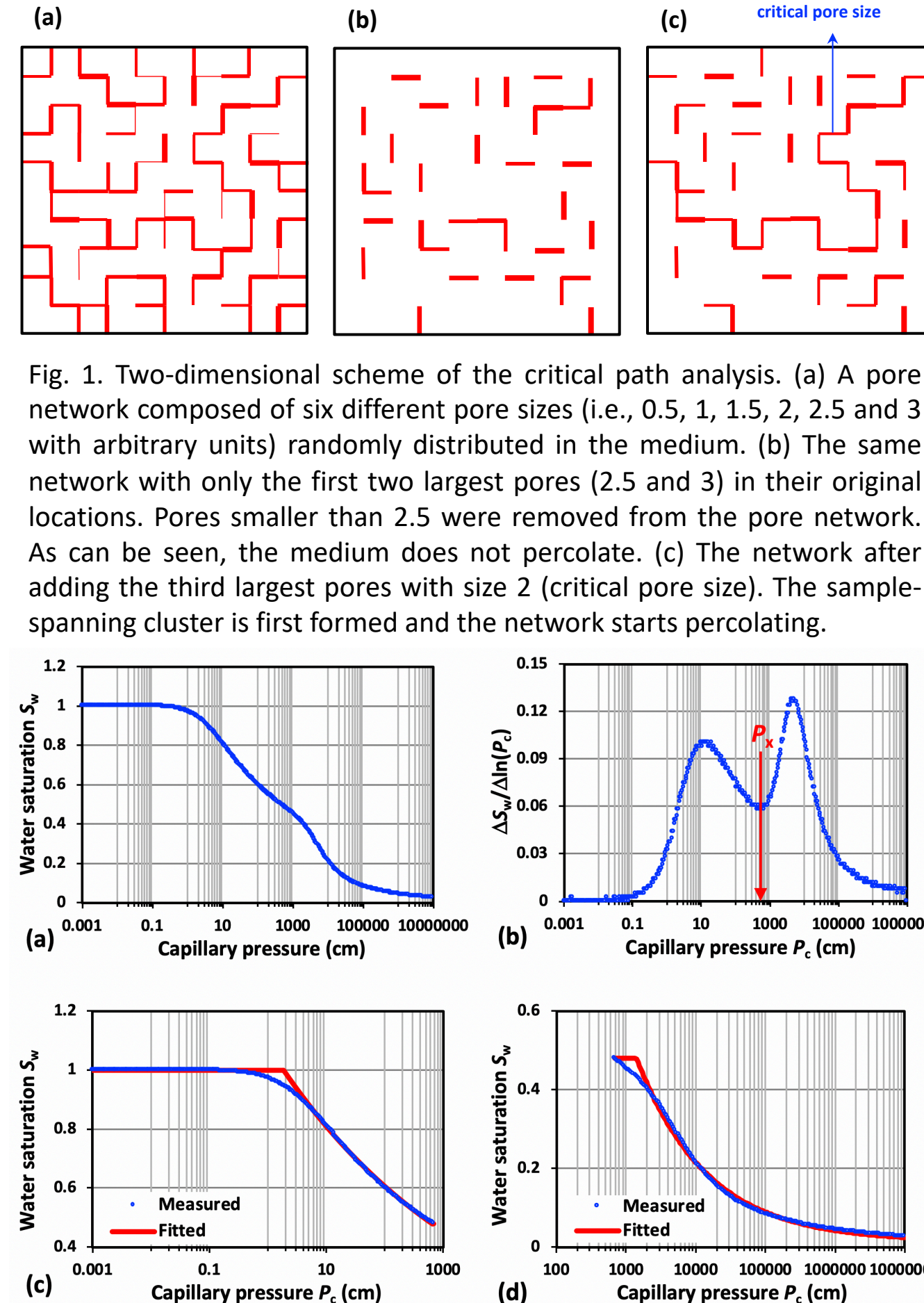


Fig. 2. (a) Measured capillary pressure curve, (b) derived bi-modal pore size distribution, (c) fitted bimodal capillary pressure curve model to the data at higher water saturations, and (d) fitted bimodal capillary pressure curve model to the data at lower water saturations for sample CT_1.

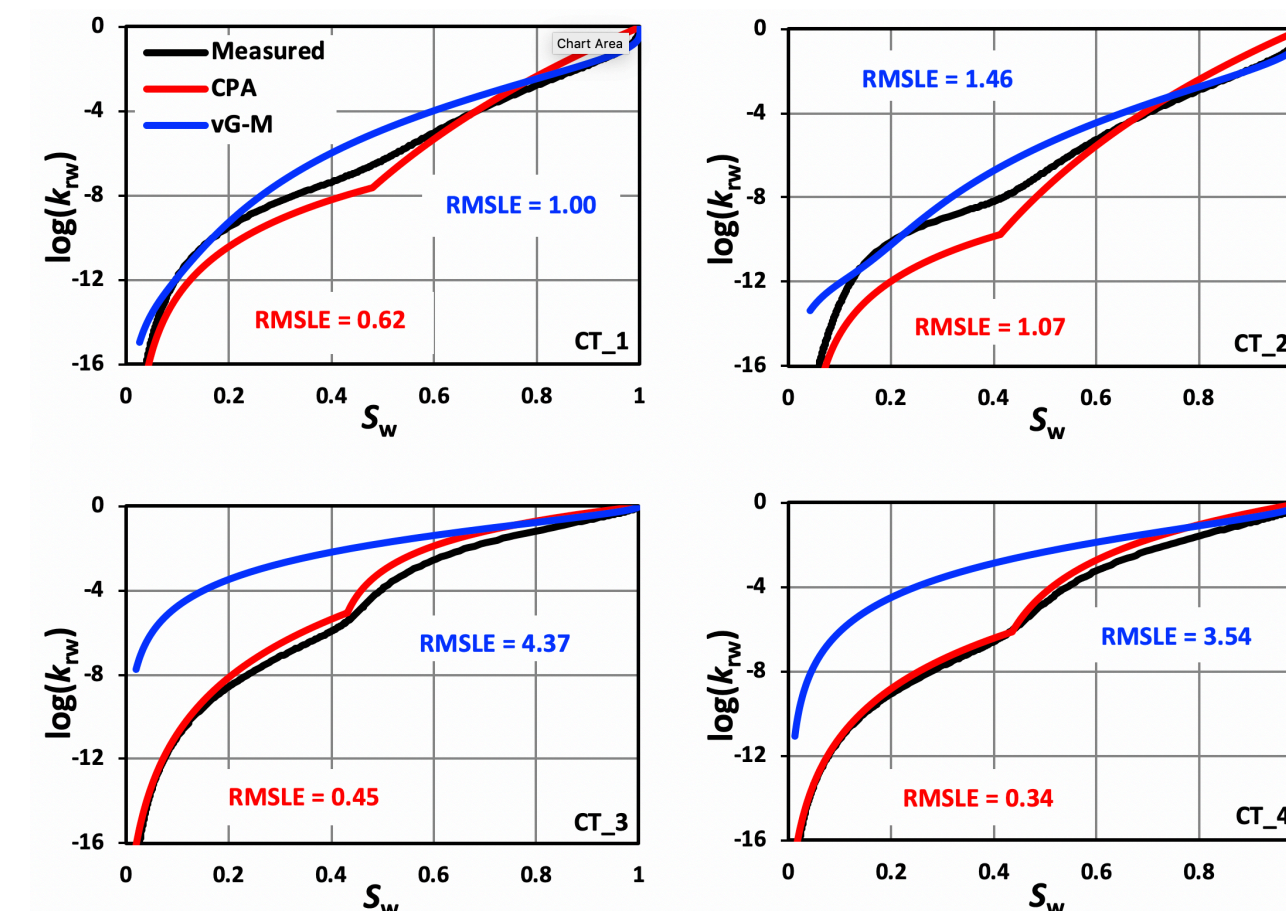
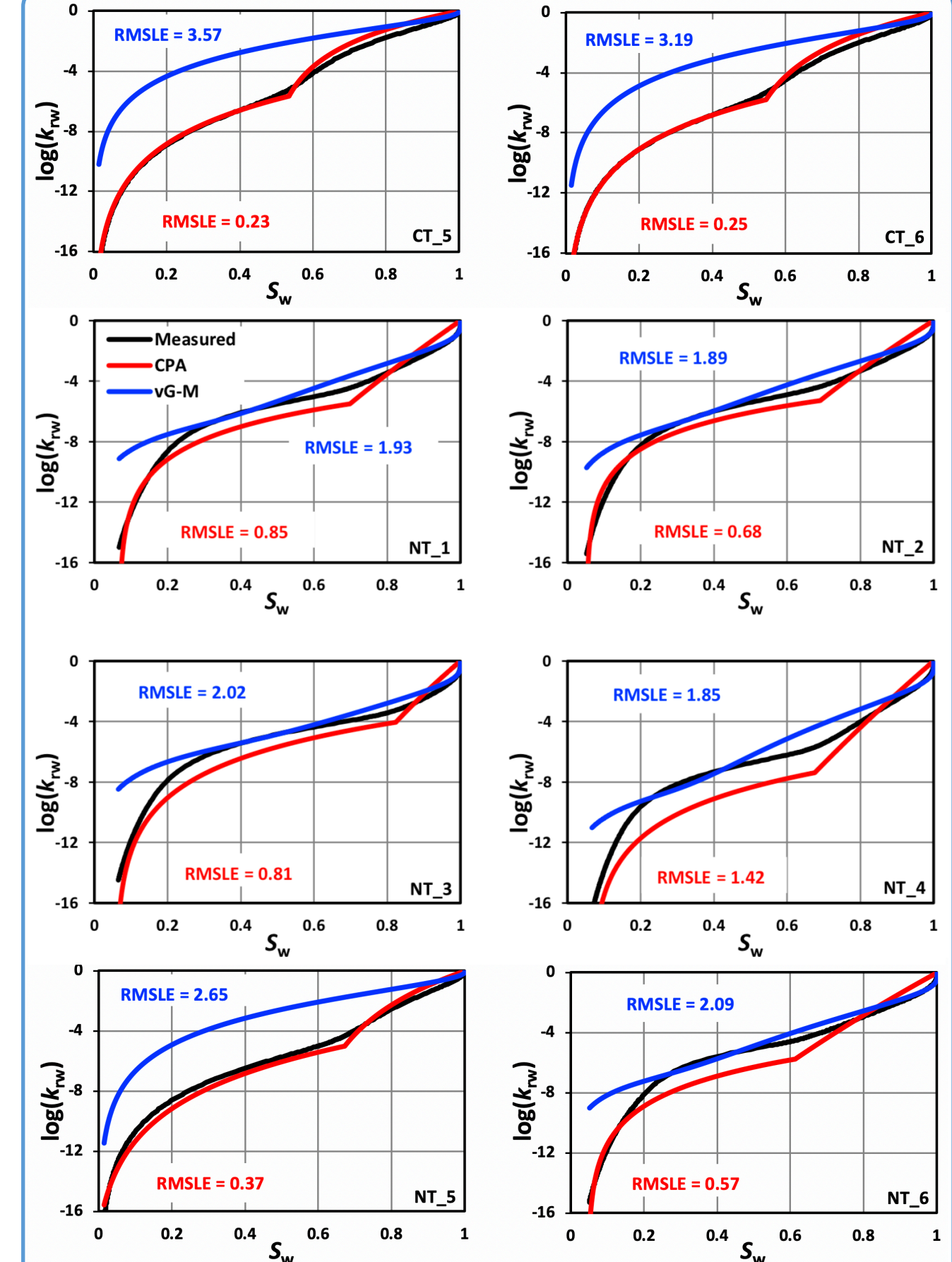


Fig. 3. The measured k_{rw} and the estimated k_{rw} using the bi-modal CPA model and the bi-modal van Genuchten-Mualem.



CONCLUSION

- We estimated the wetting-phase relative permeability from the measured capillary pressure curve.
- Results showed that the bi-modal CPA model estimated k_{rw} more accurately than the bi-modal vG-M model for CT and NT samples.
- We also found that accurate estimation of k_{rw} via CPA requires precise characterization of capillary pressure curve as well as the crossover point separating the structure domain from the texture one.

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