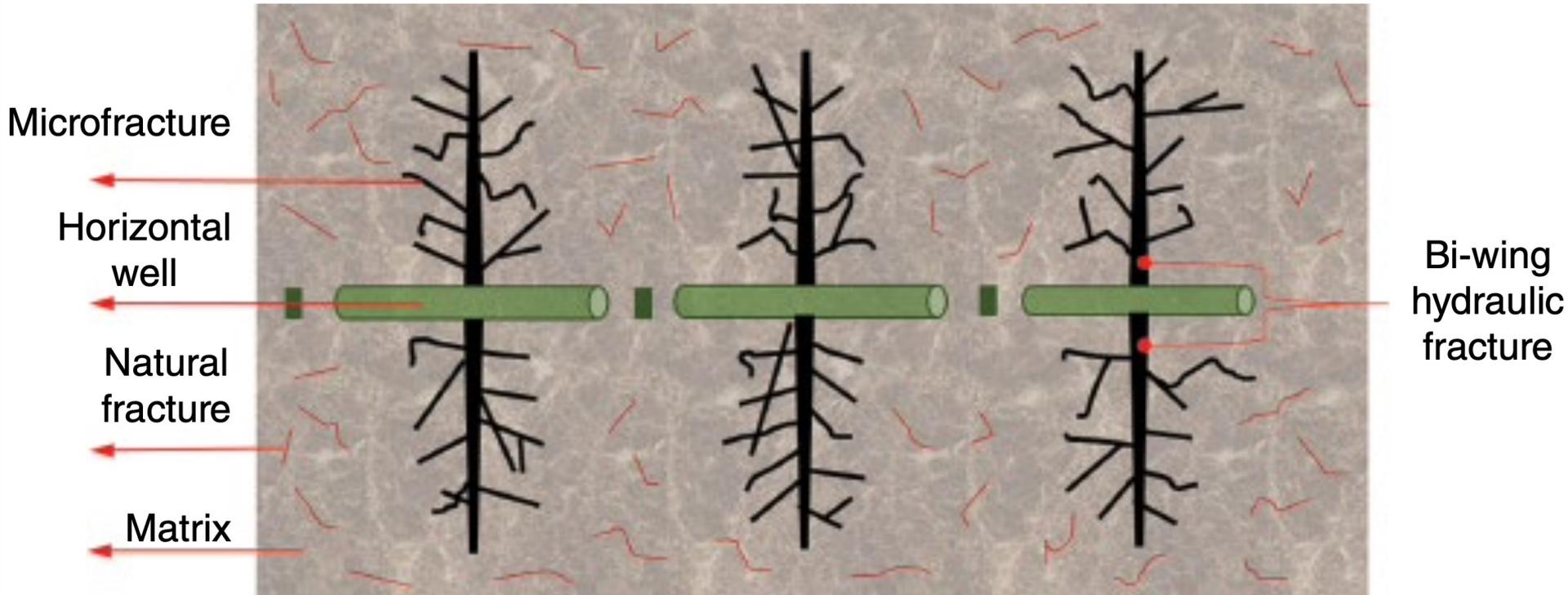


# Using percolation-based effective-medium approximation to determine effective permeability in fractured reservoirs

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Schematic of multi-scale fracture system in the shale gas reservoir after hydraulic fracturing operations. Natural fracture, microfracture, and hydraulic fractures coexist (after Chen et al., 2019).

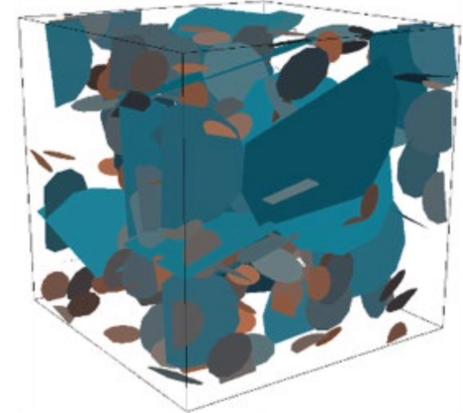
- (1) Developing a theoretical model for effective permeability in matrix-fracture systems**
- (2) Comparing theoretical estimates with 2- and 3-D numerical simulations**

## Matrix-fracture systems

### - Chen et al. (2019)

Discrete fracture-matrix networks were composed of line (2D) and elliptical (3D) fractures.

Generalized lattice Boltzmann (LB) method to simulate fluid flow.

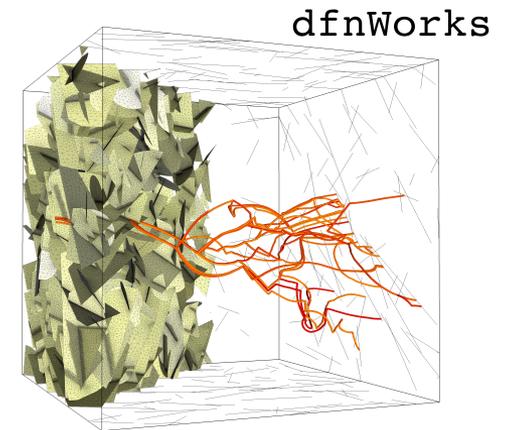


Chen et al. (2019)

### - New 3-D simulations via dfnWorks

Planar discs with a constant radius.

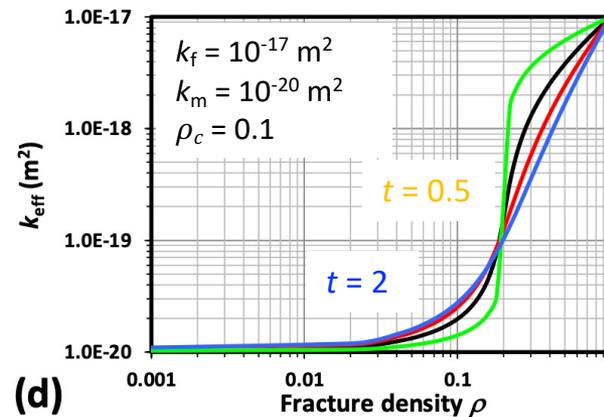
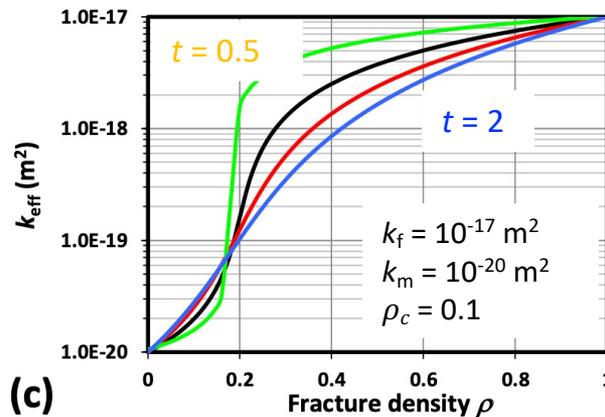
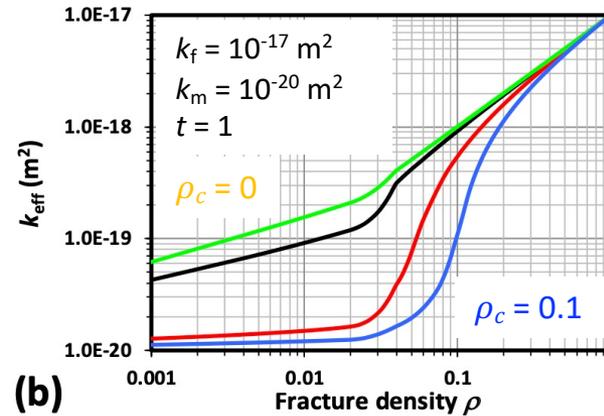
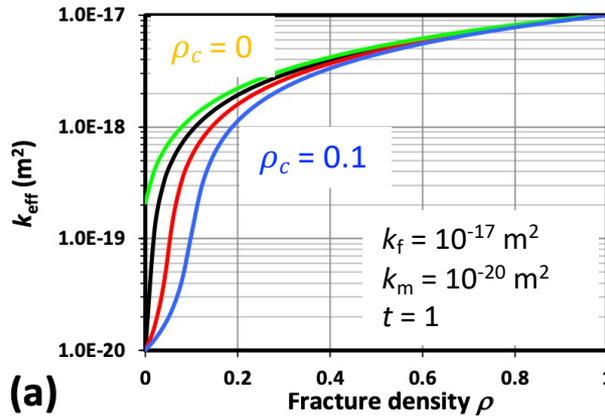
Fluid flow is simulated based on the Reynolds equation.



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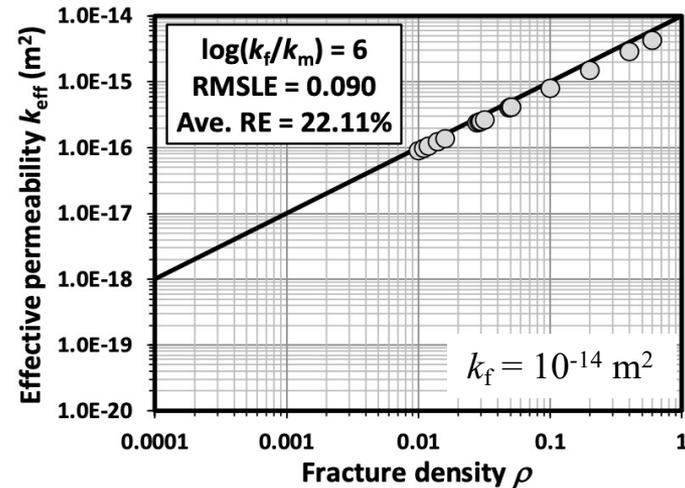
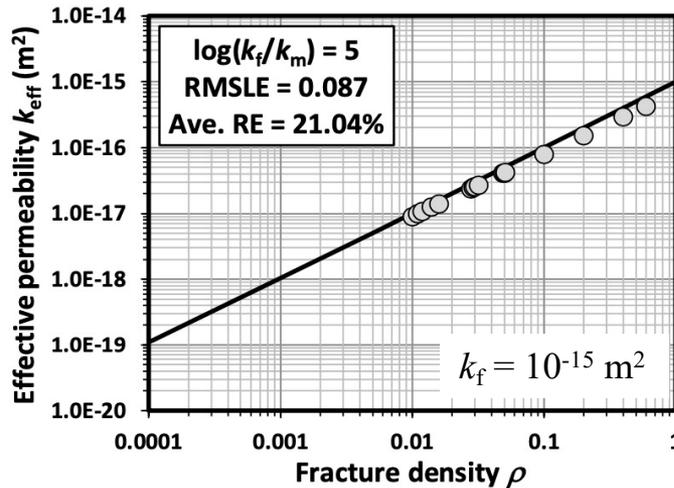
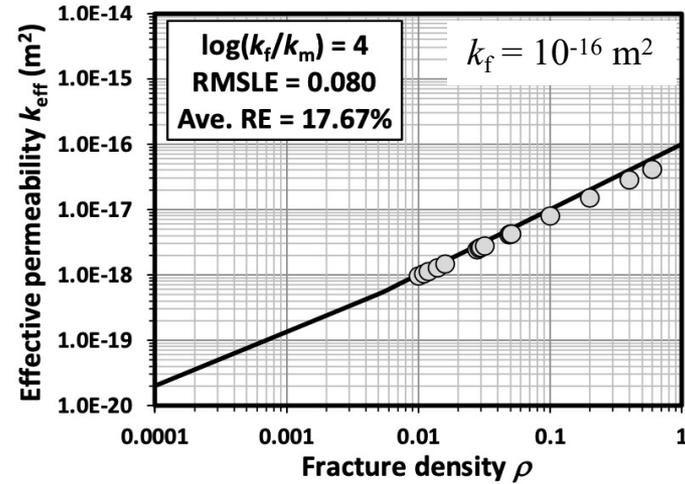
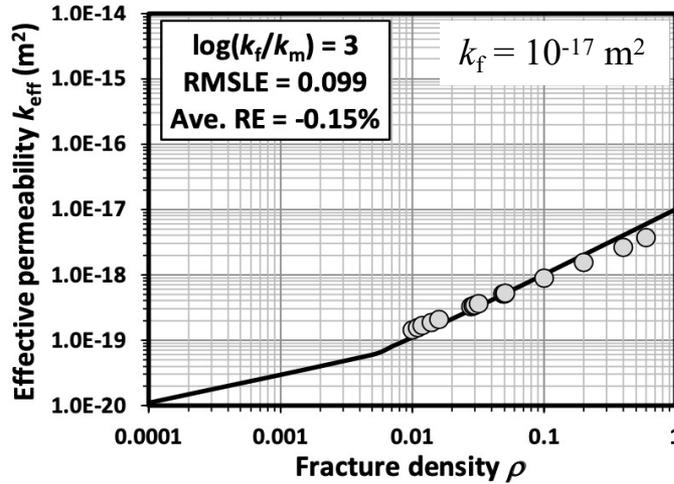
# Percolation-based EMA

$$(1 - \rho) \frac{k_m^t - k_{eff}^t}{k_m^t + \left[ \frac{1 - \rho_c}{\rho_c} \right] k_{eff}^t} + \rho \frac{k_f^t - k_{eff}^t}{k_f^t + \left[ \frac{1 - \rho_c}{\rho_c} \right] k_{eff}^t} = 0$$



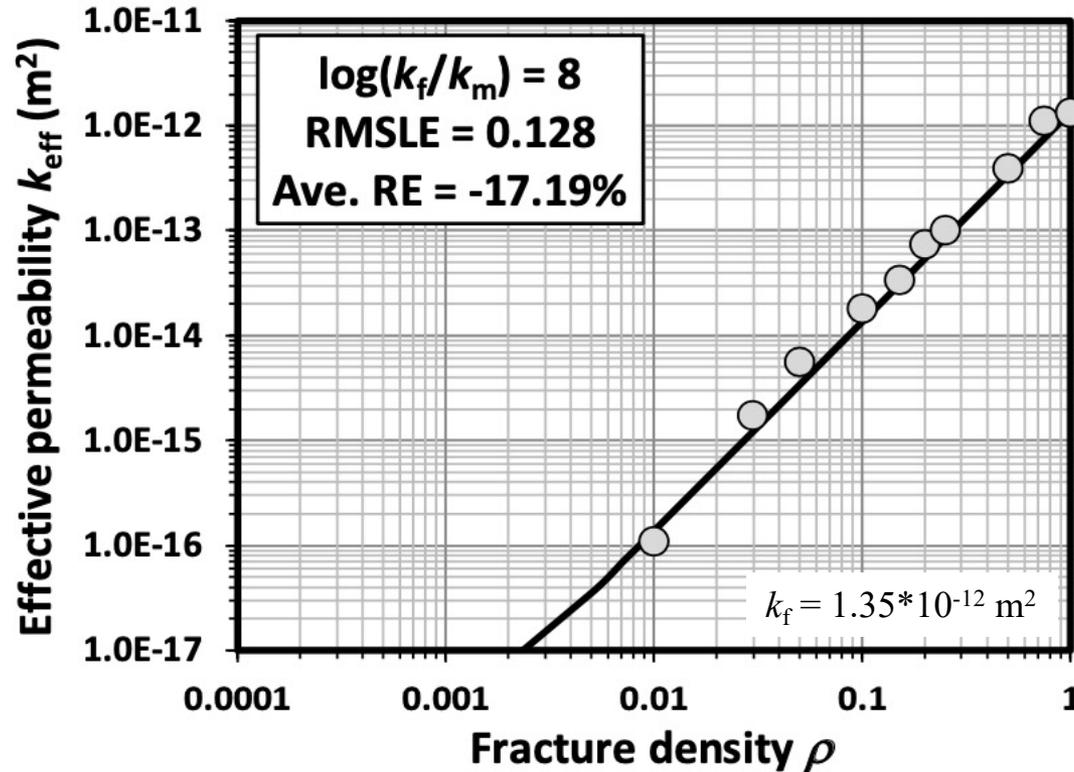
## 2-D simulations (Chen et al., 2019)

$t = 1$   
 $\rho_c = 0$   
 $k_m = 10^{-20} \text{ m}^2$



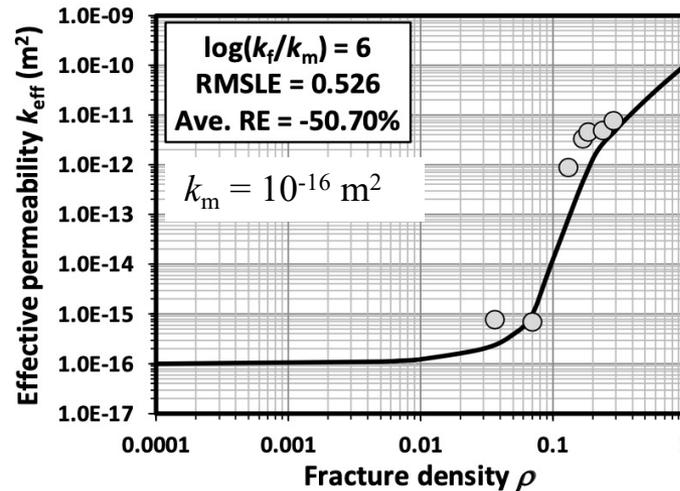
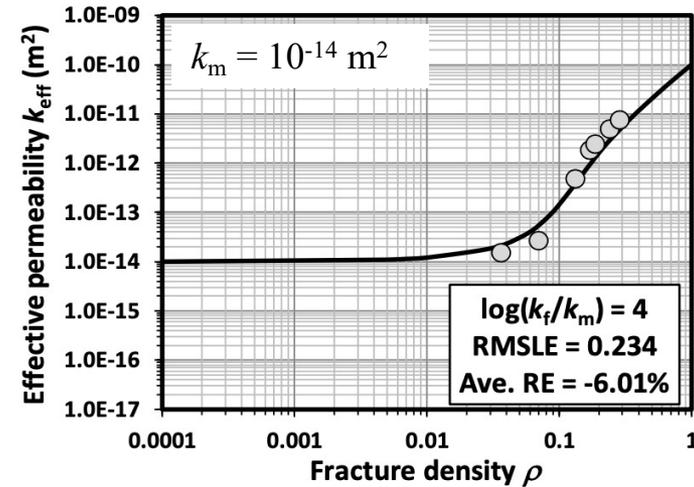
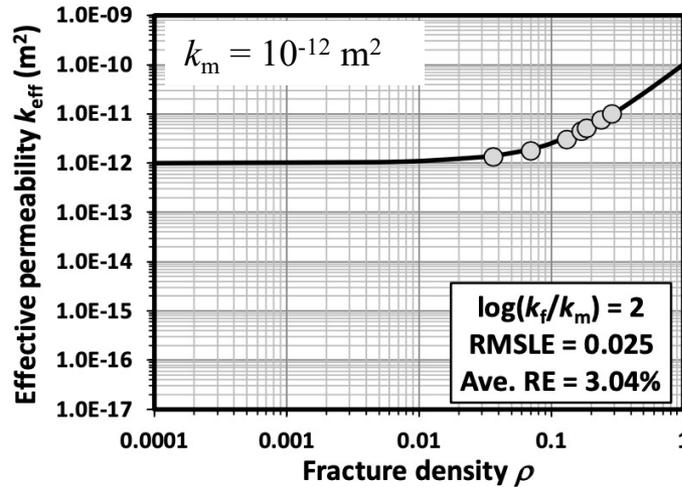
## 3-D simulations (Chen et al., 2019)

$t = 2$   
 $\rho_c = 0$   
 $k_m = 1.35 \cdot 10^{-20} \text{ m}^2$



## 3-D dfnWork simulations

$t = 2$   
 $\rho_c = 0.1$   
 $k_f = 10^{-10} \text{ m}^2$



- The proposed P-EMA model estimated the  $k_{\text{eff}}$  reasonably well.
- We found that the scaling exponent  $t = 1$  resulted in accurate estimations of  $k_{\text{eff}}$  in two dimensions, while  $t = 2$  led to good agreement between the theory and simulations in three dimensions.
- In contrast to other empirical and semi-empirical models, our proposed P-EMA  $k_{\text{eff}}$  model has no ad hoc parameters and is predictive once the parameters  $t$ ,  $\rho_c$ ,  $k_m$ , and  $k_f$  are known for a fractured reservoir.

# Acknowledgement

**Jeffrey D. Hyman**  
Staff Scientist , EES-16  
Los Alamos National Lab





# Questions?

## Matrix-fracture systems

### - Chen et al. (2019): Two dimensions

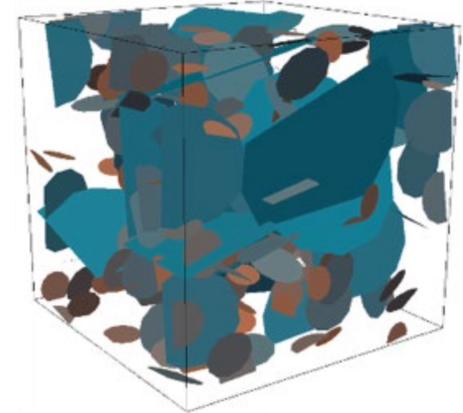
Two random numbers were generated based on a uniform distribution to determine the coordinates of two points in the domain.

A fracture with width of one lattice units and permeability of  $3.33 \times 10^{-9} \text{ m}^2$  ( $3.33 \times 10^3 D$ ; based on the cubic law) was created by connecting the two points via a straight line.

### - Chen et al. (2019): Three dimensions

the fracture network was composed of 855 elliptical fractures.

The radius of fractures followed a truncated power-law distribution with lower and upper cutoffs  $r_{\min} = 0.1 \mu\text{m}$  and  $r_{\max} = 1 \mu\text{m}$  and exponent 2.28.



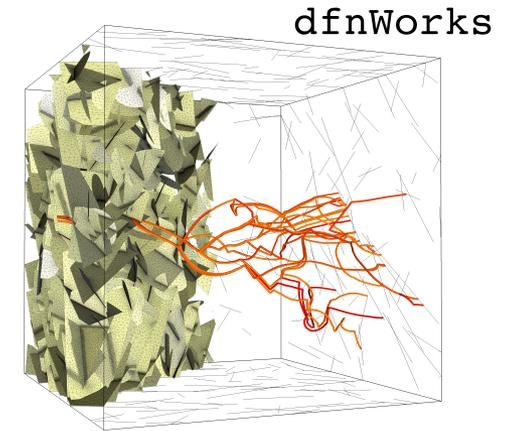
Chen et al. (2019)

## Matrix-fracture systems

### - New 3-D simulations via dfnWorks

planar discs with a constant radii of 5 meters within a 50 m cubic domain.

The orientation of fractures was sampled from a Fisher distribution with intensity parameter of 0.1 that resulted in a uniform covering of the unit sphere and equiprobable random orientations.



<https://dfnworks.lanl.gov/>