

Reducing experimental errors for microwave photonic transversal filter signal processors based on integrated optical microcombs

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Abstract

Microwave photonic (MWP) transversal signal processors offer a compelling solution for realizing versatile high-speed information processing by combining the advantages of reconfigurable electrical digital signal processing and high-bandwidth photonic processing. With the capability of generating a number of discrete wavelengths from micro-scale resonators, optical microcombs are powerful multi-wavelength sources for implementing MWP transversal signal processors with significantly reduced size, power consumption, and complexity. By using microcomb-based MWP transversal signal processors, a diverse range of signal processing functions have been demonstrated recently. In this paper we provide a detailed analysis for the errors induced by experimental imperfections processors. First, we investigate the errors arising from different sources including imperfections in the microcombs, the chirp of electro-optic modulators, chromatic dispersion of the dispersive module, shaping errors of the optical spectral shapers, and noise of the photodetector. Next, we provide a global picture quantifying the impact of error sources on the overall system performance. Finally, we introduce feedback control to compensate the errors caused by experimental imperfections, achieving significantly improved accuracy. These results provide a guide for optimizing the accuracy of microcomb-based MWP transversal signal processors.

Index Terms—Microwave photonics, optical microcombs, optical signal processing.

I. INTRODUCTION

Ever-increasing data capacity in the information age is driving the demand for high-speed information processing. In contrast to conventional microwave signal processing based on electronics, that face intrinsic bandwidth bottlenecks [1, 2], the use of photonic hardware and technologies to process high-bandwidth microwave signals, or microwave photonic (MWP) processing, can provide orders of magnitude faster speeds [3, 4] which is critical for high-speed processing applications [3-6].

In the past two decades, a range of high speed MWP processors have been demonstrated by employing different optical approaches, in both discrete and integrated form, as optical filtering modules to process microwave signals modulated on a single optical carrier [3, 7-16]. While successful, featuring high performance with dynamic tuning, these approaches provided only single processing functions with limited reconfigurability and fixed parameters. In contrast, MWP transversal signal processors, where the microwave signal is modulated onto multiple optical carriers with adjustable delays and weights before summing via photodetection [17, 18], have significant advantages in achieving highly reconfigurable processing [17, 18].

For MWP transversal signal processors, a large number of optical carriers forming discrete taps to sample the input microwave signal are needed to achieve a high accuracy. Despite the use of conventional multi-wavelength sources, such as discrete laser arrays [19-21] and fiber Bragg grating arrays [22-24], to offer the discrete taps, the numbers of available taps they can provide are normally restricted to be < 10 – mainly due to the dramatic increase of the system size, power consumption, and complexity with the tap number. Recent advances in optical microcombs [25, 26] provide an effective way to circumvent such problem by generating a large number of wavelengths equally spaced by large microwave bandwidths from single chip-scale devices. This opens new horizons for implementing MWP transversal signal processors with significantly reduced size, power consumption, and complexity. By using microcomb-based MWP transversal signal processors, a range of signal processing functions have been demonstrated recently, first for basic functions including differentiations [27, 28], integration [29], and Hilbert transforms [30-32], followed by more complex functions such as phase encoding [33], arbitrary waveform generation [34], and computations within the framework of optical neural networks [35-37].

For signal processors, accuracy is a key parameter. Recently [ref JSTQE] we presented an analysis quantifying the performance errors of microcomb based MWP signal processors. That work focused on theoretical errors due to mis-design - it did not take into account experimental errors such as noise etc.. In this paper, we provide a complementary detailed analysis to that work, focusing on performance errors induced by experimental imperfections of microcomb-based MWP transversal signal processors. First, errors arising from imperfect

microcomb characteristics, chirp in the electro-optic modulator, chromatic dispersion in the dispersive module, shaping errors of the optical spectral shaper, and noise of the photodetector are investigated. Next, a global picture is presented to show the influence of different error sources by quantifying their contributions to the overall system performance. Finally, we introduce feedback control to compensate any errors arising from experimental limitations, and in doing so we achieve a significant improvement in accuracy. These results are useful for understanding and optimizing the accuracy of microcomb-based MWP transversal signal processors.

II. MICROCOMB-BASED MWP TRANSVERSAL SIGNAL PROCESSORS

Microwave transversal signal processors are implemented based on the transversal filter structure in digital signal processing that features a finite impulse response [37]. Implementing them with photonic technologies yields a significantly increased processing bandwidth compared to their electronic counterparts [17]. **Fig. 1** shows the schematic diagram and signal processing flow of a typical MWP transversal signal processor. An optical microcomb, serving as a multi-wavelength source, provides a large number of wavelength channels as discrete taps. An input microwave signal is multicast onto each channel via an electro-optic modulator (EOM) to generate multiple microwave signal replicas. Next, time delays between adjacent wavelength channels are introduced by optical delay elements, and the delayed replicas at different wavelength channels are weighted through spectral shaping. Finally, the delayed and weighted replicas are summed via photodetection to generate the final microwave output of the system.

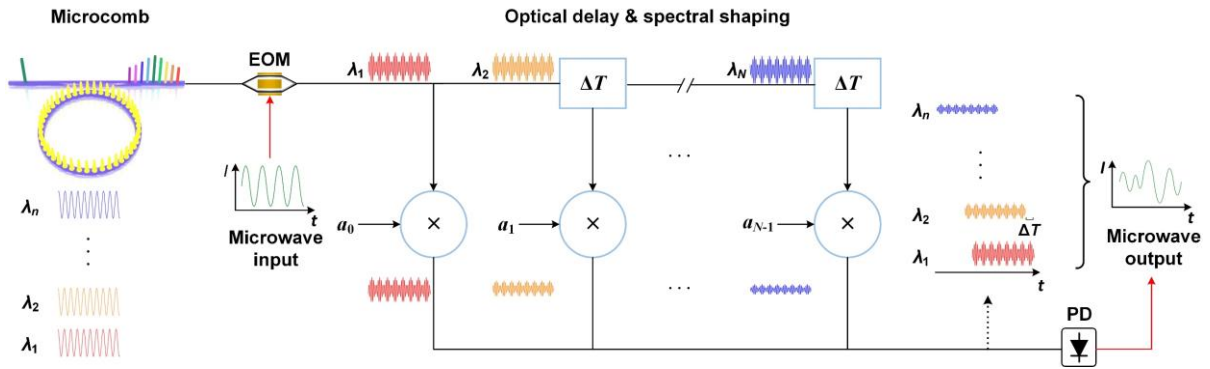


Fig. 1. Schematic diagram and signal processing flow of a MWP transversal signal processor with an optical microcomb source. EOM: electro-optic modulator. PD: photodetector.

For the MWP transversal signal processor in **Fig. 1**, each of the taps can be regarded as a discrete sample of the system's impulse response, i.e., the system's impulse response can be expressed as [17]

$$H(t) = \sum_{n=0}^{M-1} a_n \delta(t - n\Delta T), \quad (1)$$

where M is the tap number, a_n ($n = 0, 1, 2, \dots, M-1$) is the tap weight of the n^{th} tap, and ΔT is the time delay

between adjacent wavelength channels. Therefore, the output microwave signal $s(t)$ can be given by [38]

$$s(t) = f(t) * h(t) = \sum_{n=0}^{M-1} a_n f(t - n\Delta T), \quad (2)$$

where $f(t)$ is the input microwave signal. After Fourier transformation from **Eq. (1)**, the spectral transfer function of the MWP transversal signal processor is

$$H(\omega) = \sum_{n=0}^{M-1} a_n e^{-j\omega n\Delta T}, \quad (3)$$

which shows agreement with the spectral response of a typical microwave transversal filter [38].

As can be seen from **Eqs. (1) – (3)**, by simply altering the tap weights a_n ($n = 0, 1, 2, \dots, M-1$) through comb shaping, different signal processing functions can be achieved without any changes of the hardware [17]. This allows for a high degree of reconfigurability for the MWP transversal signal processor.

Fig. 2 shows a schematic of the experimental implementation of the MWP transversal signal processor in **Fig. 1**, which includes a microcomb generation module and a transversal signal processing module. In the microcomb generation module, a continuous-wave (CW) laser, amplified by an erbium-doped fibre amplifier (EDFA) with a polarization controller (PC) to adjust its polarization, is used to pump a high-Q nonlinear microring resonator (MRR) to generate optical microcombs. The output from this module is sent to the transversal signal processing module that performs the signal processing flow (**Fig. 1**), which involves a PC, EOM, spool of single-mode fibre (SMF) as the optical delay module, optical spectral shaper (OSS) to shape the comb lines, and a balanced photodetector (BPD) for photodetection. The BPD connected to the two complementary output ports of the OSS divides all the wavelength channels into two groups with a phase difference of π , which introduces positive and negative signs onto the tap coefficients a_n ($n = 0, 1, 2, \dots, M-1$) in **Eqs. (1) – (3)**.

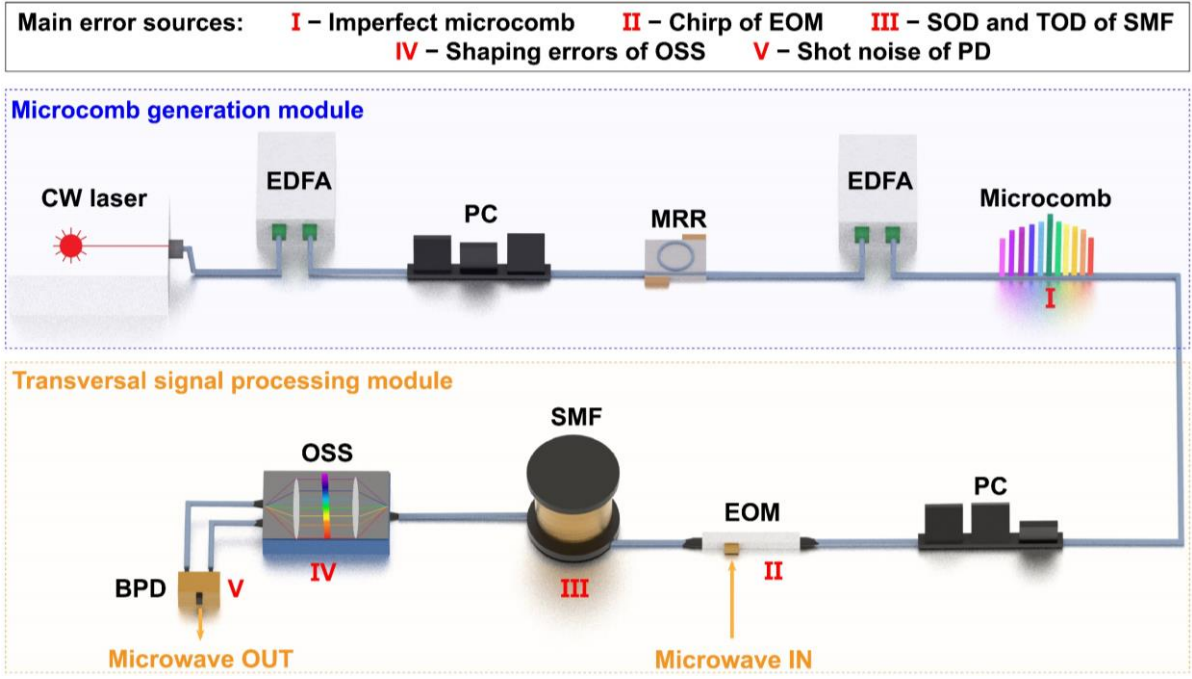


Fig. 2. Schematic of a practical microcomb-based MWP transversal signal processor. The main error sources are labelled as I – V. CW laser: continuous-wave laser. EDFA: erbium-doped fibre amplifier. PC: polarization controller. MRR: microring resonator. EOM: electro-optic modulator. SMF: single-mode fibre. OSS: optical spectral shaper. BPD: balanced photodetector. SOD: second-order dispersion. TOD: third-order dispersion.

For experimentally implemented MWP transversal signal processors in **Fig. 2**, performance errors arise from two sources – theoretical versus experimental limitations. The former refers to the theoretical approximation of a continuous impulse response (which corresponds to infinite tap number M) using a practical system with a finite tap number, and was the subject of our previous paper mentioned above [ref]. The latter refers to errors induced by the imperfect performance of different components, such as the microcomb, chirp of the EOM, second- (SOD) and third-order dispersion (TOD) of the SMF, shaping errors of the OSS, and noise in the PD.

To quantify the performance errors, the root mean square error (RMSE) is normally used to compare the deviation between the processor's output and the ideal result, which is defined as [39]

$$\text{RMSE} = \sqrt{\sum_{i=1}^k \frac{(Y_I - y_i)^2}{k}} \quad (4)$$

where k is the number of sampled points, Y_1, Y_2, \dots, Y_n are the values of the ideal processing result, and y_1, y_2, \dots, y_n are the values of the output of the microcomb-based MWP transversal signal processors.

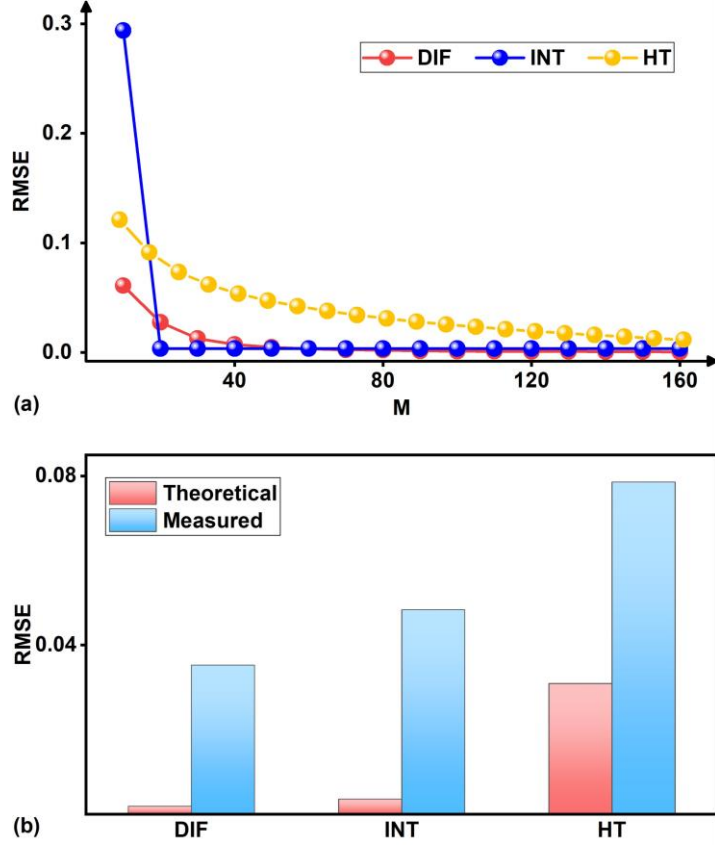


Fig. 3. (a) Root mean square errors (RMSEs) induced by theoretical limitation for differentiation (DIF), integration (INT), and Hilbert transformation (HT) as a function of tap number M . (b) Comparison of RMSEs induced by theoretical limitations and practical measured RMSEs for DIF, INT, and HT when $M = 80$. In (a) – (b), the comb spacing, length of dispersive medium, and second-order dispersion (SOD) parameter are $\Delta\lambda = 0.4$ nm, $L = 4.8$ km, and $D_2 = 17.4$ ps/nm/km, respectively. The input microwave signals are assumed to be Gaussian pulses with a full width at half maximum (FWHM) of ~ 0.17 ns.

Fig. 3(a) shows the RMSEs induced by theoretical limitations [ref our JSTQE] as a function of tap number M for three different signal processing functions, including first-order differentiation (DIF), integration (INT), and Hilbert transform (HT). These theoretical RMSEs were calculated assuming a perfect response for all the components in **Fig. 2**. As can be seen, the theoretical RMSEs are small for a large tap number $M \geq 80$, indicating that the theoretical errors can be greatly reduced by increasing the tap number. **Fig. 3(b)** compares the theoretical and experimentally measured RMSEs for $M = 80$, showing that the former is much lower, reflecting that experimental errors typically dominate the system performance of microcomb-based MWP transversal signal processors. In the following Section III, we provide a detailed analysis of the experimentally induced processing errors and in Section IV provide approaches to reduce these errors.

III. ERRORS INDUCED BY EXPERIMENTAL IMPERFECTIONS

In this section, we provide a detailed analysis of the experimentally induced system errors by the sources outlined in **Fig. 2**. In subsections A – D, we investigate the influence of specific error sources, assuming the other sources are error-free. In subsection E, we compare the contributions of the different errors to the overall system performance.

In the following analysis, we use first-order DIF, INT, and HT as examples to quantify the experimentally induced errors. Their spectral transfer functions are given by [27, 29, 31]

$$H_{DIF}(\omega) = j\omega, \quad (5)$$

$$H_{INT}(\omega) = \frac{1}{j\omega}, \quad (6)$$

$$H_{HT}(\omega) = \begin{cases} e^{j\pi/2}, & 0 \leq \omega < \pi \\ e^{j\pi/2}, & -\pi \leq \omega < 0 \end{cases} \quad (7)$$

where $j = \sqrt{-1}$ and ω is the angular frequency.

For comparison, in our analysis we assume the processors have the same tap number ($M = 80$), comb spacing ($\Delta\lambda = 0.4$ nm), and length and SOD for the SMF ($L = 4.8$ km and $D_2 = 17.4$ ps/nm/km). These parameters are the same as those in our previous papers [27, 29, 31]. The input microwave signal is taken as a Gaussian pulse with a full width at half maximum (FWHM) of ~ 0.17 ns, whose spectral bandwidth (~ 5 GHz) is within the processing bandwidth of the signal processors (i.e., $FSR_{MW} = 1 / (\Delta\lambda \times L \times D_2) = \sim 30$ GHz).

A. Influence of the optical microcombs

In this section, we analyze the influence of microcomb imperfections on the system performance for different processing functions. These imperfections generate intensity and phase noise in the comb channels. The intensity noise includes power fluctuations of the comb lines and the intensity noise floor, which mainly arise from photon shot noise and spontaneous emission beat noise [40]. For MWP transversal signal processors, the microcomb intensity noise results in inaccuracy of the tap coefficients, thereby degrading the overall system accuracy.

To characterize the microcomb intensity noise, the optical signal-to-noise ratio (OSNR) is introduced, which is the ratio of the maximum optical signal to the noise power in each of the comb lines. **Fig. 4(a)** shows the output waveforms from processors that perform DIF, INT, and HT, where flat intensity noise floors are assumed for the microcombs with different OSNRs. The ideal processing output (without errors) and the results for error-free microcombs (with $OSNR = \infty$, and only including theoretical errors) are also shown for comparison. As the OSNR of the comb lines increases from 10 dB to ∞ , the processors' output waveforms match the ideal results better for all three processing functions, reflecting the reduced error achieved by increasing the OSNR. To better reflect the intensity envelop of the microcombs, a sinc-shaped intensity noise floor is introduced. The corresponding results are shown in **Fig. 4(b)**, showing a trend similar to that in **Fig. 4(a)**.

Fig. 4(c) shows the RMSEs between the experimental and ideal results as a function of the OSNR. As expected, for both the flat and sinc-shaped intensity noise floor, the RMSEs decrease with the microcomb OSNR for all three processing functions, showing agreement with the trend in **Figs. 4(a)** and **(b)**. For OSNRs less than

20 dB, the RMSEs decrease more steeply. As the OSNR increases, the decrease in RMSE is more gradual, and there is only a very small reduction in error beyond an OSNR of 20 dB. For DIF and INT functions, the RMSE for microcombs with sinc-shaped intensity noise floors is higher than for flat intensity noise floors, whereas the opposite trend is observed for HTs. This reflects the fact that the impact of the microcomb intensity envelope errors depends on the processing function.

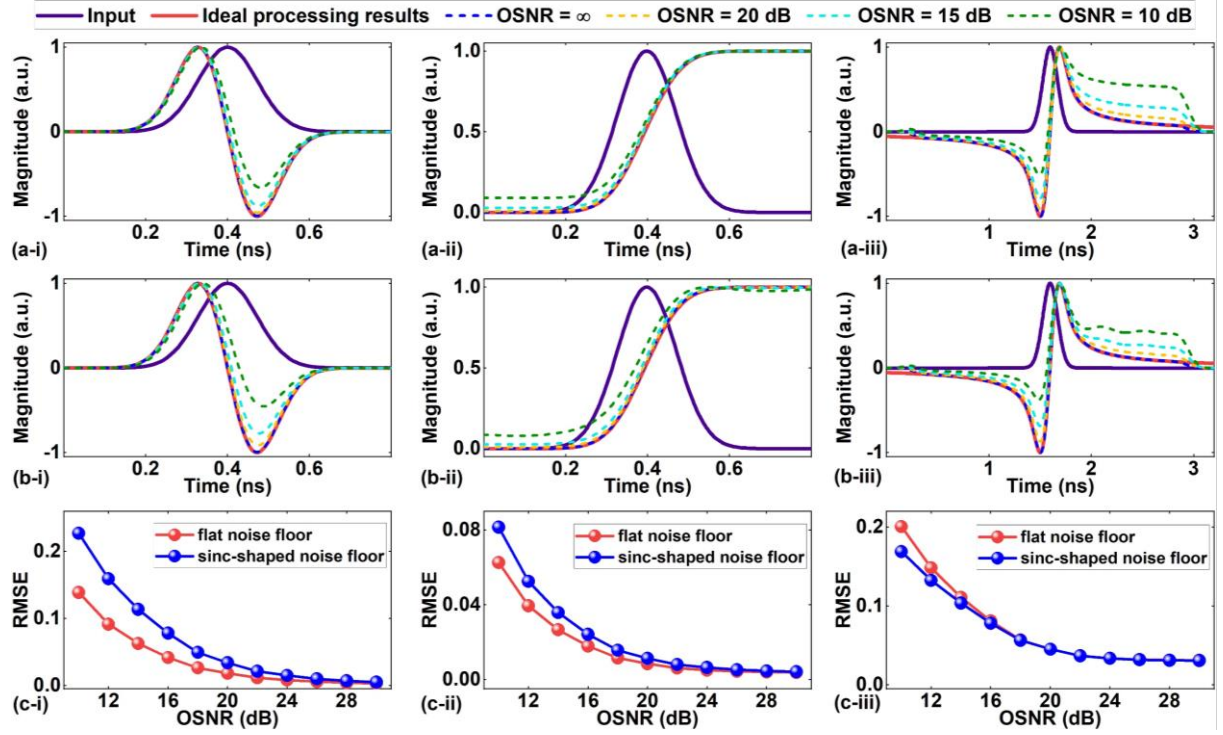


Fig. 4. Influence of microcombs' intensity noise on computing errors of differentiation (DIF), integration (INT), and Hilbert transformation (HT). (a) – (b) Temporal waveform of Gaussian input pulse and output waveforms from the transversal signal processors performing (i) DIF, (ii) INT, and (iii) HT, where the intensity noise floors of the microcombs are (a) flat and (b) sinc-shaped, respectively. Different curves show the results for different optical signal-to-noise ratios (OSNRs) of the comb lines. The ideal processing results are also shown for comparison. (c) Corresponding RMSEs between the ideal computing results and the processors' output waveforms as a function of microcomb's OSNR. In (a) – (c), the Gaussian input pulse has a FWHM of ~ 0.17 ns. The tap number, comb spacing, length of dispersive medium, and SOD parameter are $M = 80$, $\Delta\lambda = 0.4$ nm, $L = 4.8$ km, and $D_2 = 17.4$ ps/nm/km, respectively.

The phase noise of microcombs, which manifests as a broadened linewidth, an appearance of multiple repetition-rate beat notes, and a reduction in temporal coherence [41], is affected by several factors, such as the noise of the CW pump as well as the mechanical and thermal noise of the MRR [42, 43]. These sources of error are difficult to quantitatively analyze. For mode-locked microcombs with extremely low phase noise, the phase noise induced errors are negligible [35, 36]. Therefore, to achieve high performance accuracy over long periods, it is necessary to use microcombs with low phase noise, high coherence, and stable mode locking. A number of mode-locking approaches have been reported [17, 18]. It is worth noting that even with relatively incoherent microcombs, processors can still achieve high performance because the microcomb mainly serves as a multi-wavelength source where the optical powers of different wavelength channels are detected incoherently by a BPD.

B. Influence of the electro-optic modulator

In **Fig. 2**, an electro-optic modulator is used to modulate the input microwave signal onto different wavelength channels. The most commonly used electro-optic modulators are Mach-Zehnder modulators (MZMs), owing to their high modulation efficiency, low insertion loss, and large operation bandwidth [44]. Due to the asymmetry in the electric field overlap at each electrode [45], practical MZMs not only produce intensity modulation, but also give rise to undesired phase modulation, known as modulation chirp. The chirp leads to distortions in the modulated optical signals, thus resulting in the output errors. Here, we analyze the influence of modulator chirp on the performance errors for different processing functions.

The chirp of a MZM can be characterized by the chirp parameter given by [46]

$$\alpha = \frac{\gamma_1 + \gamma_2}{\gamma_1 - \gamma_2} \quad (8)$$

where γ_1 and γ_2 are the voltage-to-phase conversion coefficients for the two arms of the MZM. When $\alpha = 0$ (*i.e.*, $\gamma_1 = -\gamma_2$), pure intensity modulation is achieved. **Figs. 5(a) – (c)** show the output waveforms from microcomb-based MWP transversal signal processors that perform DIF, INT, and HT for different chirp parameters α . The ideal results and the processing results corresponding to a chirp-free MZM ($\alpha = 0$) are also shown for comparison. For all processing functions the output waveform approaches the ideal result as α decreases from 1 to 0, indicating the reduced system error for a lower modulator chirp.

Fig. 5(d) shows the RMSE between the ideal and experimental output waveforms versus modulator chirp α . As expected, the RMSE increases with α for all processing functions, which agrees with the trend in **Figs. 5(a) – (c)**. We also noted that the impact of the modulation chirp on the system performance is more significant for the DIF and INT functions as compared to the HT.

C. Influence of single-mode fibre

In **Fig. 2**, a spool of SMF is employed as the dispersive module of the MWP transversal signal processor, which introduces both amplitude and phase errors due to its chromatic dispersion, including both SOD and TOD. SOD induces a uniform time delay between adjacent taps, which is required for MWP transversal signal processors without alignment errors. However, SOD also introduces a time delay between the modulated sidebands, which leads to a power degradation of the microwave output after photodetection, and hence system errors [47]. On the other hand, the SMF TOD introduces non-uniform time delays between adjacent taps, thus resulting in undesired phase errors. In this section, we analyze the influence of the SMF's SOD and TOD on the performance errors for different processing functions.

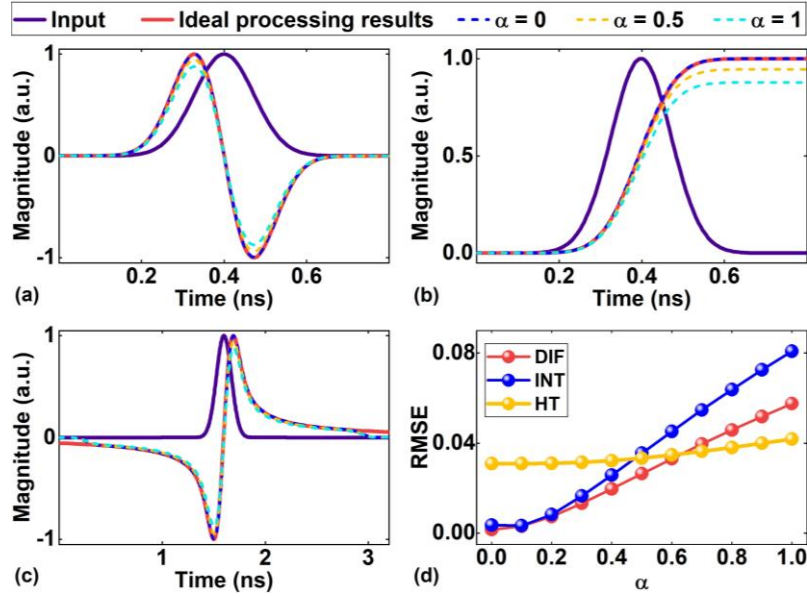


Fig. 5. Influence of the modulator chirp on computing errors of differentiation (DIF), integration (INT), and Hilbert transformation (HT). (a) – (c) Temporal waveform of Gaussian input pulse and output waveforms from the transversal signal processors performing (a) DIF, (b) INT, and (c) HT. Different curves show the results for different chirp parameter α . The ideal processing results are also shown for comparison. (d) Corresponding RMSEs between the ideal computing results and the processors' output waveforms as a function of α . In (a) – (d), the Gaussian input pulse has a FWHM of ~ 0.17 ns. The tap number, comb spacing, length of dispersive medium, and SOD parameter are $M = 80$, $\Delta\lambda = 0.4$ nm, $L = 4.8$ km, and $D_2 = 17.4$ ps/nm/km, respectively.

A MZM generates two modulated sidebands, with the output termed a double-sideband (DSB) signal. The SOD of the SMF generates different phase shifts for the two sidebands resulting in different phase shifts between the carrier and the two beat microwave sidebands. Therefore, the final microwave output after photodetection experiences a power degradation, with its power given approximately by [47]

$$P_{MW} \propto \cos\left(\frac{\pi L D_2}{c} \lambda_c^2 f_{MW}^2\right) \quad (9)$$

where c is the speed of light in vacuum, λ_c is the center wavelength of each channel, and f_{MW} is the frequency of the input microwave signal.

Figs. 6(a) – (c) show the output waveforms from the processors for the DIF, INT, and HT functions, with and without including the power degradation caused by SOD. The ideal processing results are also shown for comparison. The SOD parameter is kept constant at $D_2 = 17.4$ ps/nm/km. For all processing functions, there are only slight differences induced by SOD. **Fig. 6(d)** shows the power degradation P_{MW} as a function of D_2 , which is calculated based on **Eq. (9)**. As can be seen, the power degradation induced by SOD is very small, being $< 10^{-3}$ dB for $D_2 = 17.4$ ps/nm/km in **Figs. 6(a) – (c)**.

Fig. 6(e) shows the RMSE as a function of D_2 , showing that the RMSEs only vary very slightly ($< 10^{-4}$) with D_2 for all processing functions, in agreement with **Figs. 6(a) – (c)**. These results indicate that although the SOD of SMF induces power degradation of the microwave output, its influence is very small.

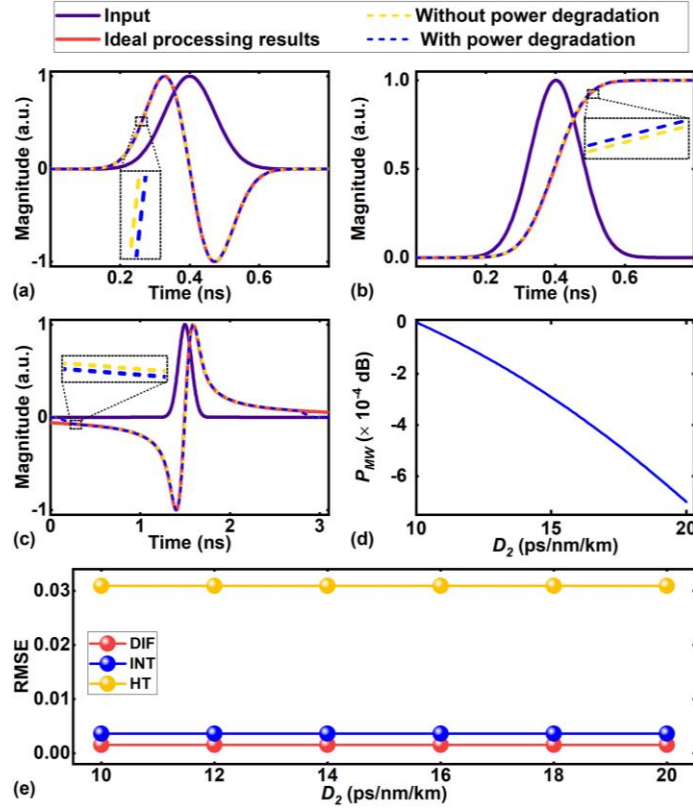


Fig. 6. Influence of SMF's SOD on computing errors of differentiation (DIF), integration (INT), and Hilbert transformation (HT). (a) – (c) Temporal waveform of Gaussian input pulse and output waveforms from the transversal signal processors performing (a) DIF, (b) INT, and (c) HT. Different curves show the results with and without the influence of power degradation induced by SOD. The SOD parameter is $D_2 = 17.4$ ps/nm/km. The ideal processing results are also shown for comparison. (d) Power degradation of the output microwave signal P_{MW} as a function of the SOD parameter D_2 . (e) Corresponding RMSEs between the ideal computing results and the processors' output waveforms as a function of D_2 . In (a) – (e), the Gaussian input pulse has a FWHM of ~ 0.17 ns. The tap number, comb spacing, and length of dispersive medium are $M = 80$, $\Delta\lambda = 0.4$ nm, and $L = 4.8$ km, respectively.

The TOD of the SMF introduces additional non-uniform time delays between the modulated replicas in the wavelength channels, thus resulting in alignment errors in the processing results. The additional time delay of the n^{th} tap is given by [48]

$$\Delta T_{TOD} = D_3 L \Delta\lambda^2 n^2 \quad (10)$$

where D_3 is the TOD parameter.

Figs. 7(a) – (c) show the output waveforms from the processors for all functions, versus the TOD parameter D_3 . The ideal processing results and the processing results corresponding to a TOD-free SMF ($D_3 = 0$) are also shown for comparison. The system output approaches the ideal as D_3 (and the TOD) decreases from 0.5 ps/nm²/km to zero for all processing functions.

Fig. 7(d) shows the RMSE as a function of D_3 , where, as expected, the RMSE increases with increasing D_3 for all functions – agreeing with the trend in **Figs. 7(a) – (c)**. The influence of TOD on the system performance is more significant for the INT function as compared to the DIF and HT functions, reflecting that INT has a more stringent requirement for the accuracy of the phase of the different taps.

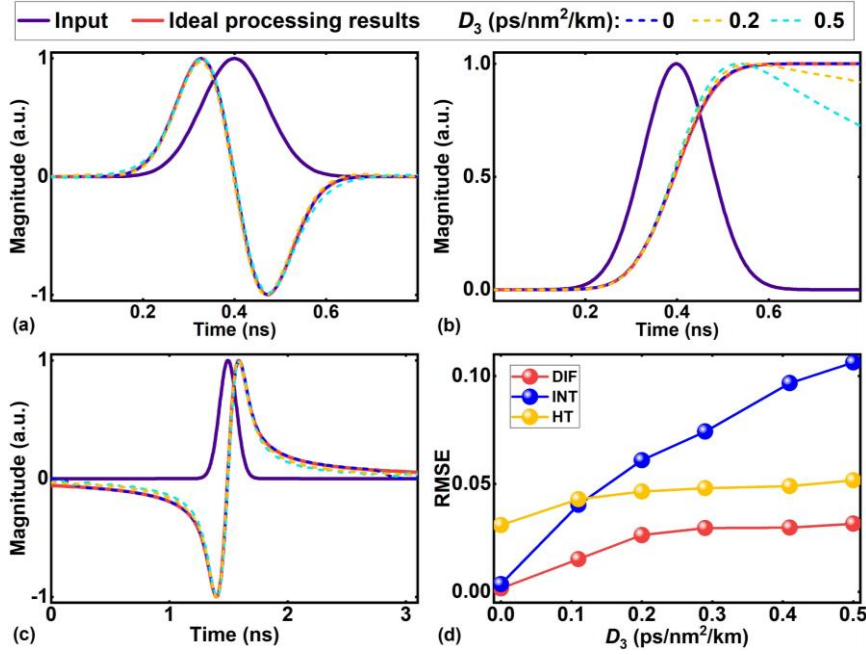


Fig. 7. Influence of SMF's TOD on computing errors of differentiation (DIF), integration (INT), and Hilbert transformation (HT). (a) – (c) Temporal waveform of Gaussian input pulse and output waveforms from the transversal signal processors performing (a) DIF, (b) INT, and (c) HT. Different curves show the results for different TOD parameter D_3 . The ideal processing results are also shown for comparison. (d) Corresponding RMSEs between the ideal computing results and the processors' output waveforms as a function of D_3 . In (a) – (d), the Gaussian input pulse has a FWHM of ~ 0.17 ns. The tap number, comb spacing, length of dispersive medium, and SOD parameter are $M = 80$, $\Delta\lambda = 0.4$ nm, $L = 4.8$ km, and $D_2 = 17.4$ ps/nm/km, respectively.

D. Influence of optical spectral shapers and photodetectors

In **Fig. 2**, an optical spectral shaper is used as a spectral shaping module to weight the delayed signals across different wavelength channels according to the designed tap coefficients. This is followed by a BPD that sums the delayed and weighted signals to generate the microwave output of the processor. The OSS induces shaping errors, which result in inaccurate tap coefficients and hence output errors. On the other hand, noise and an uneven transmission response of the BPD lead to variations of the power of the microwave output. In this section, we analyze the influence of these error sources for the different processing functions.

We introduce random tap coefficient errors (RTCEs) within a certain percentage range of ΔPR to characterize the shaping errors of the OSS. **Figs. 8(a) – (c)** show the output waveforms from the processors for all functions and for the RTCEs in different ranges. The ideal processing results and the processing results without RTCEs ($\Delta PR = 0$) are also shown for comparison. For all the three processing functions, the processors' output waveforms show better agreement with the ideal results for a smaller ΔPR , reflecting an improved computing accuracy associated with reduced RTCEs.

Fig. 8(d) shows the RMSE as a function of ΔPR , showing that the RMSE increases with ΔPR for all functions, agreeing with the trend in **Figs. 8(a) – (c)**. The shaping errors of the OSS have a more obvious impact on the system accuracy for DIF as compared to the other two functions, indicating that DIF has a more stringent requirement for the accuracy of the tap amplitudes.

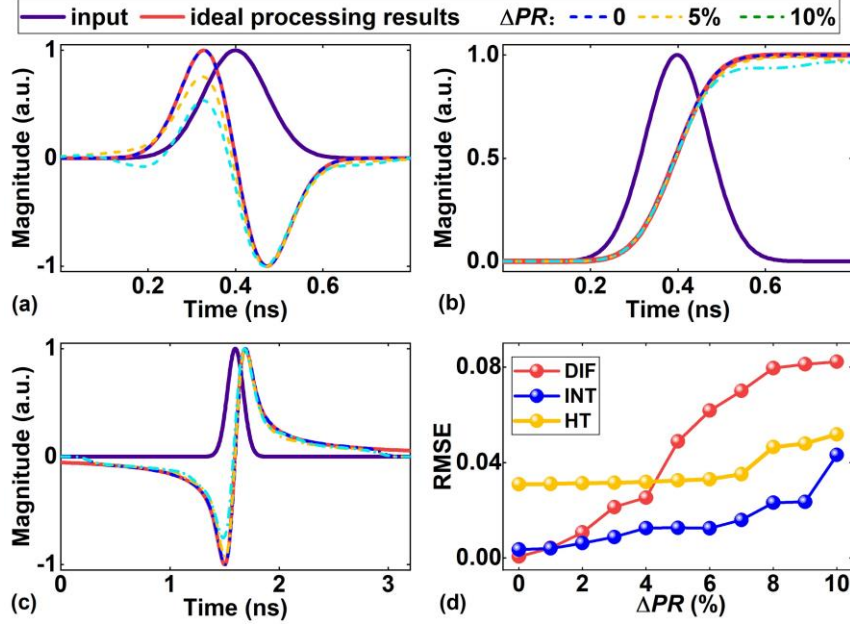


Fig. 8. Influence of shaping errors induced by the OSS on computing accuracy of differentiation (DIF), integration (INT), and Hilbert transformation (HT). (a) – (c) Temporal waveform of Gaussian input pulse and output waveforms from the transversal signal processors performing (a) DIF, (b) INT, and (c) HT. Different curves show the results for different percentage ranges (ΔPR s) of random tap coefficient errors (RTCEs). The ideal processing results are also shown for comparison. (d) Corresponding RMSEs between the ideal computing results and the processors' output waveforms as a function of ΔPR . In (a) – (d), the Gaussian input pulse has a FWHM of ~ 0.17 ns. The tap number, comb spacing, length of dispersive medium, and SOD parameter are $M = 80$, $\Delta\lambda = 0.4$ nm, $L = 4.8$ km, and $D_2 = 17.4$ ps/nm/km, respectively.

In **Fig. 2**, the use of a BPD greatly suppresses the common-mode noise of the optical signal, which largely cancels out the intensity noise caused by the photodetector. Therefore, the errors induced by the BPD mainly come from its limited response bandwidth and uneven transmission response, which introduce additional errors in the tap coefficients after spectral shaping. Similarly, the limited bandwidth and uneven response of the EOM could also introduce additional errors to the tap coefficients before spectral shaping. These errors, together with the shaping errors of the OSS, can be effectively mitigated through feedback control, which will be discussed in section IV. Finally, we note that the BPD shot noise can induce random power fluctuations in the output microwave signal which limits the lowest achievable phase noise floor [49]. The influence of this on the system performance is similar to the microcomb noise, and can be reduced by using a BPD with higher sensitivity [50].

E. Impact of error sources

In this section, we analyze the contribution of the error sources discussed above on the system performance.

Fig. 9(a) shows the simulated output waveforms for all functions, including errors induced by the sources from I to V in **Fig. 2**, with the ideal results shown for comparison. Based on the measurements and parameters of the components in our previous experiments [27, 30, 34], the OSNR of the sinc-shaped microcomb, chirp parameter of the EOM, SOD and TOD parameter of the SMF, and range of RTCEs are set to OSNR = 30 dB, $\alpha = 0.5$, $D_2 = 17.4$ ps/nm/km, $D_3 = 0.083$ ps/nm²/km, and $\Delta PR = 5\%$, respectively. As expected, the overall output waveform errors become larger with the accumulation of errors induced by these sources for all functions.

In order to quantify the contributions of the different sources of error, we calculate the RMSE from **Fig. 9(a)**, shown in **Fig. 9(b)**. The RMSE measured with practical processors are also shown for comparison. In our simulations, we used the input microwave signal waveform measured by a high-bandwidth real-time oscilloscope to calculate the RMSEs, this can minimize the errors induced by the discrepancy between the experimentally generated and ideal Gaussian pulses. The RMSEs of the simulation results increase with the accumulation of errors, which agrees with the trend in **Fig. 9(a)**. There are margins between the RMSEs of the simulation results and the experimental results mainly caused by deviations between the simulation and experiment parameters as well as factors that are not accounted for in our simulation, such as the phase noise of the microcomb, the limited response bandwidth and uneven transmission response of the EOM and BPD, and shot noise of the BPD. According to **Fig. 9(b)**, the system error for the DIF is mainly induced by the microcomb imperfections and EOM chirp. For the INT, function the main error sources are the EOM chirp and the SMF TOD. As compared to the DIF and INT functions, the theoretical errors have a more significant influence on the computing accuracy for HTs.

IV. ERROR COMPENSATION VIA FEEDBACK CONTROL

In this section, feedback control is introduced to compensate for errors induced by the imperfect response of experimental components. The benefit of feedback control is quantitatively analyzed by comparing the system errors with and without feedback.

As shown in **Fig. 10**, we classify the error sources discussed in **Section III** into two categories, depending on whether amplitude or phase errors are introduced in the taps. The amplitude and phase errors refer to errors in the tap coefficients (i.e., a_n in **Eqs. (1) – (3)**) and time delays (i.e., $n\Delta T$ in **Eqs. (1) – (3)**) for different taps, respectively. The sources of amplitude error include the microcomb intensity noise, EOM chirp, TOD and SOD of the SMF, OSS shaping errors, PD shot noise, and the bandwidth response of the EOM and BPD. The sources of phase errors include microcomb phase noise, TOD of the SMF, and BPD shot noise. We note that some of the error sources in **Fig. 10** are static or slow-varying, e.g., chirp of EOM, SOD and TOD of SMF, and shaping errors of OSS. In contrast, the fluctuations in the amplitude and phase caused by microcombs and the BPD are normally faster - on the order of 10 GHz.

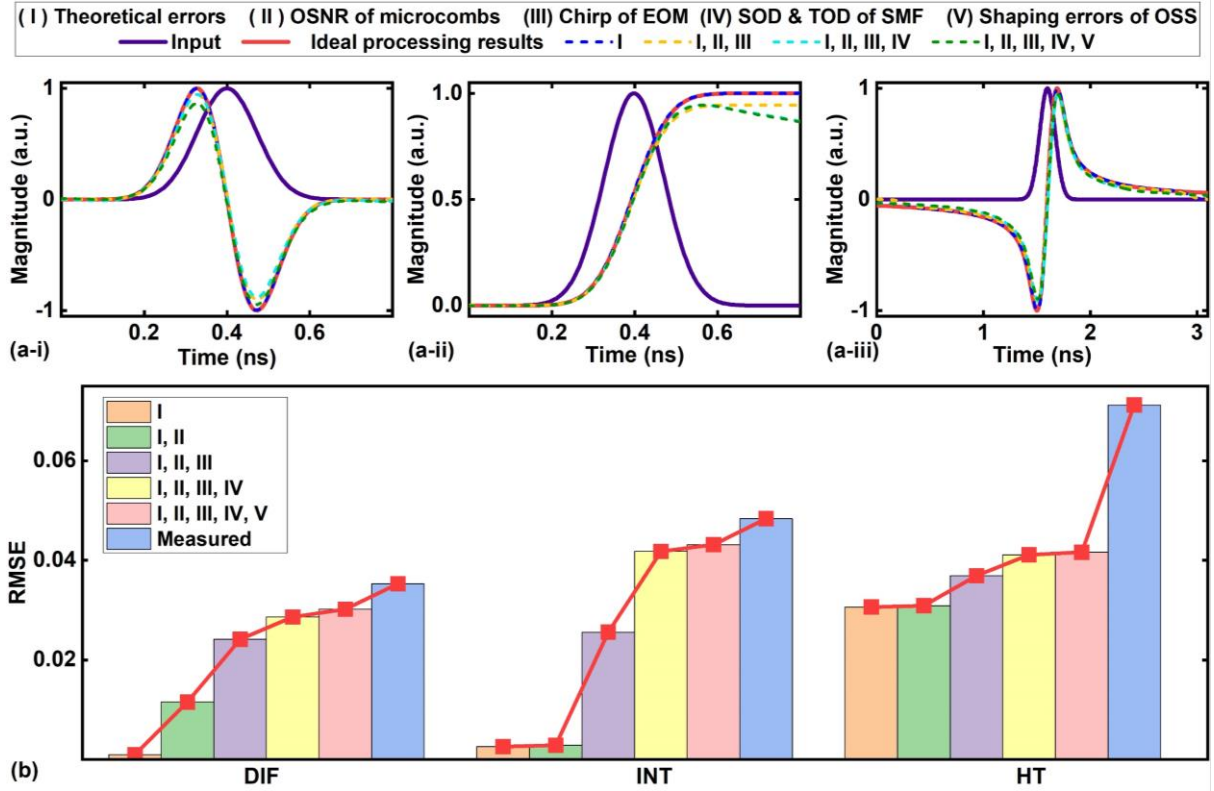


Fig. 9. Contributions of different error sources to the overall computing errors of differentiation (DIF), integration (INT), and Hilbert transformation (HT). (a) Temporal waveform of Gaussian input pulse and output waveforms from the transversal signal processors performing (i) DIF, (ii) INT, and (iii) HT. Different curves show the results after accumulating computing error induced by different sources from I to V. The ideal processing results are also shown for comparison. (b) Corresponding RMSEs between the ideal computing results and the processors' outputs. The practical measured RMSEs are also shown. In (a) and (b), the microcomb has an OSNR of 30 dB. The chirp parameter, SOD parameter, TOD parameter, and tap coefficient fluctuations are $\alpha = 0.5$, $D_2 = 17.4$ ps/nm/km, $D_3 = 0.083$ ps/nm²/km, and $\Delta PR = 5\%$. The Gaussian input pulse has a FWHM of ~ 0.17 ns. The tap number, comb spacing, and length of dispersive medium are $M = 80$, $\Delta\lambda = 0.4$ nm, and $L = 4.8$ km respectively.

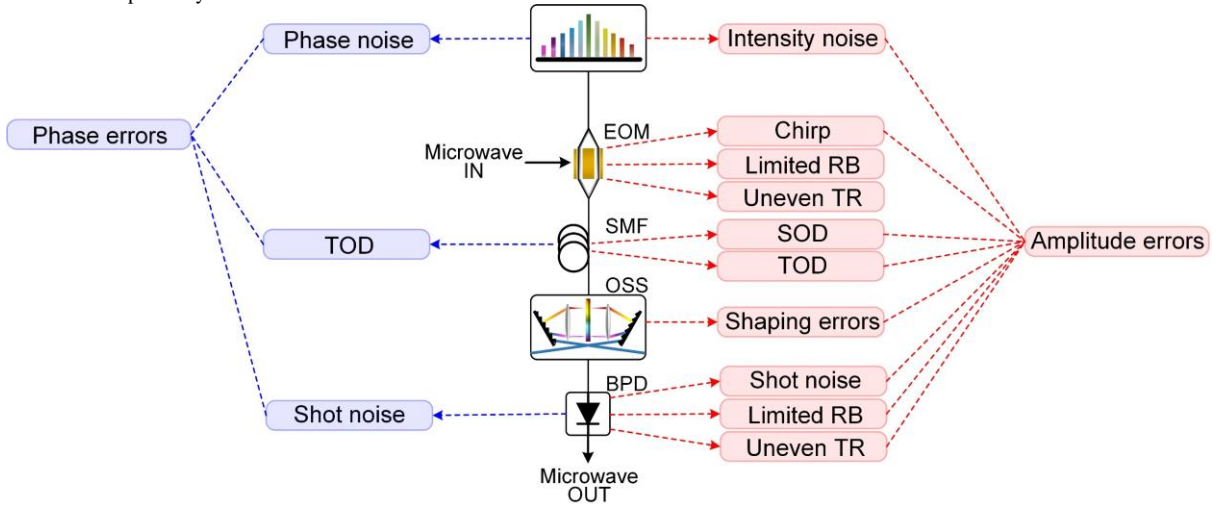


Fig. 10. Amplitude and phase errors induced by different components in microcomb-based MWP transversal signal processors. EOM: electro-optic modulator. SMF: single-mode fibre. OSS: optical spectral shaper. BPD: balanced photodetector. RB: response bandwidth. TR: transmission response. SOD: second-order dispersion. TOD: third-order dispersion.

The static or slow-varying amplitude errors in **Fig. 10** can be compensated for by introducing feedback control to calibrate the designed tap coefficients set for the OSS. **Fig. 11(a)** shows a schematic of a MWP transversal signal processor with feedback control. A feedback control loop including all the components of the signal processor is introduced to calibrate the amplitude of the temporal impulse response of each tap based on the ideal

impulse response. During the calibration process, a microwave signal is employed as the input signal to test the impulse response of the processor channel by channel, where the same input microwave signal is modulated onto the corresponding comb line. The intensities of the microwave signals after photodetection are recorded by an oscilloscope and sent to a computer, where they are subtracted from the designed tap weights to generate error signals. Finally, the generated error signals are sent to the OSS to calibrate the attenuation of comb line intensity. After several iterations of the above process, the amplitude errors caused by the non-ideal impulse response of the system can be effectively reduced. Similarly, the static or slow-varying phase errors can be mitigated by exploiting the programmable phase characteristics of the OSS to compensate the deviation between the measured and desired phase response.

In **Fig. 11(b)**, we compare the RMSEs for all functions with and without feedback control. The RMSEs due to theoretical errors are also shown for comparison. As expected, the measured RMSEs with feedback control are much lower than those measured without calibration and approach the theoretical RMSEs more closely. After calibration, there are still discrepancies between the measured RMSEs and theoretical RMSEs, reflecting that there are still residual errors that cannot be compensated for with feedback control. We infer that these errors are mainly induced by rapidly varying error sources, by deviations between the simulated and experimental parameters, and by the limited resolution of the instruments such as the OSS and oscilloscope.

To further improve the system accuracy, multiple-stage feedback control can be employed. For example, another feedback loop with one more OSS can be introduced in the microcomb generation module to flatten the comb lines of the initially generated microcomb. This allows for uniform wavelength channel link gain and can also reduce the loss control range for the spectral shaping in the transversal signal processing module. Recently, self-calibrating photonic integrated circuits have been demonstrated [51, 52], where the impulse response calibration was achieved by incorporating an optical reference path to establish a Kramers-Kronig relationship and then calculate the amplitude and phase errors based on a Fourier transform. This offers new possibilities to achieve precise feedback control in microcomb-based MWP transversal signal processors. This offers new possibilities to achieve precise feedback control in MWP transversal signal processors, [53-73] based on optical integrated microcombs. [74-129] This type of analysis could potentially be useful for both quantum optical photonic chips [130-142] as well as advanced integrated nonlinear and linear photonic chips. [143-178]

V. CONCLUSIONS

In summary, we analyze the system errors induced by experimental imperfections for microcomb-based MWP transversal signal processors. We first investigate the errors arising from imperfect microcomb characteristics, the electro-optic modulator chirp, chromatic dispersion in the dispersive module, errors in the optical spectral shaper, and photodetector noise. We give a global picture of the quantitative influence of error sources on the overall system performance. Finally, we introduce feedback control to compensate for errors. Our results show that the influence of the error sources varies for the different processing functions studied here, and that these errors can be significantly reduced by introducing feedback control for both static and slowly varying sources of error. This work provides a useful guide for optimizing the performance of microcomb-based MWP transversal signal processors for versatile high-speed information processing applications.

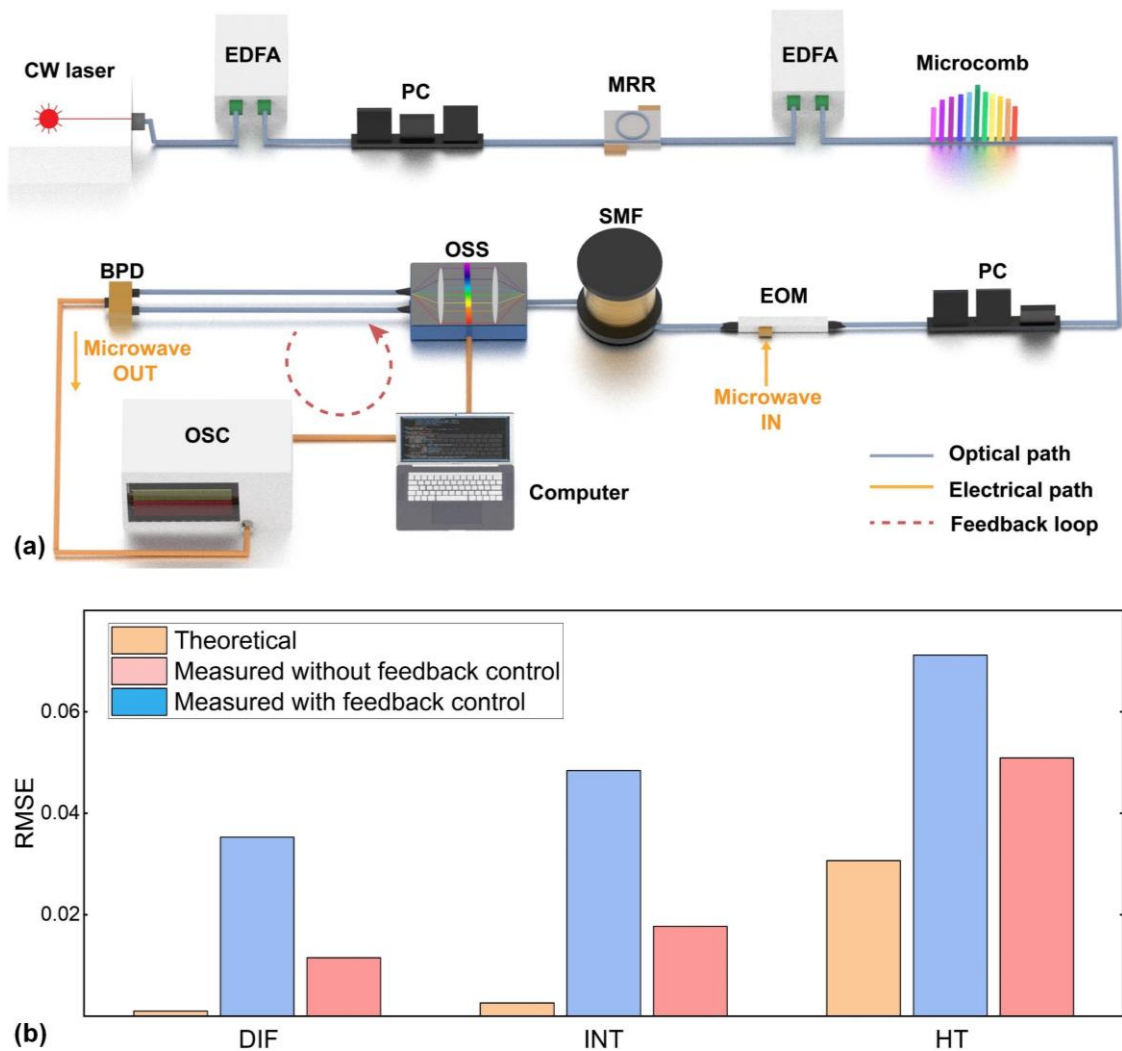


Fig. 11. (a) Schematic of a microcomb-based MWP transversal signal processor with feedback control. CW laser: continuous-wave laser. EDFA: erbium-doped fibre amplifier. PC: polarization controller. MRR: microring resonator. OSS: optical spectral shaper. OSA: optical spectrum analyzer. OC: optical coupler. EOM: electro-optic modulator. SMF: single-mode fibre. BPD: balanced photodetector. OSC: oscilloscope. (b) Comparison of measured RMSEs for DIF, INT, and HT with and without feedback control. The corresponding theoretical RMSEs are also shown for comparison. The tap number, comb spacing, length of dispersive medium, and SOD parameter are $M = 80$, $\Delta\lambda = 0.4$ nm, $L = 4.8$ km, and $D_2 = 17.4$ ps/nm/km, respectively. The input microwave signals are Gaussian pulses with a FWHM of ~ 0.17 ns.

Competing Interests

The authors declare that there are no competing interests.

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