

1 **Electrical Conductivity Inversion Method of Saline Soil based on**

2 **Sentinel-2 MSI data**

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6 **Abstract:** Electrical conductivity (EC) is not only an important index to evaluate the degree of
7 soil salinization, but also an essential basis for judging whether saline soil can be improved and
8 assess the effect of improvement efforts. Satellite remote sensing provides much information for
9 large scale EC inversion of saline soil, which enables the possibility for evaluating the degree and
10 distribution of soil salinization. Taking the salinized region of western Jilin Province as the study
11 area, 328 salinized soil samples were collected, and the EC was measured in June 2019. The
12 construction of the optimal spectral parameters was based on the correlation between the
13 conductivity and the spectral reflectivity of Sentinel-2 MSI data; after satisfying the normal
14 distribution for the Box-Cox transformation of EC, the inversion model of EC was established by
15 using linear regression model, support vector machine (SVM), regression tree (RT), Gaussian
16 process regression (GPR), and ensemble tree (ET). The verification results of the model on the
17 validation set showed that the performance of GPR was optimal ($R^2 = 0.66$, RMSE = 0.48 mS/cm,
18 MAE=0.52 mS/cm), which increased R^2 by 29.04% compared with the traditional linear
19 regression model. Finally, according to the GPR model, the EC results of pixel-level resolution
20 (10 m \times 10 m) of saline soil in western Jilin Province were inversed, which provided a scientific
21 basis for the study of the distribution characteristics and improvement scheme of saline soil.

22 **Keywords:** Sentinel-2 MSI; Spectral characteristics; Electrical Conductivity retrieval; Saline soil;
23 Machine learning

24 **1 Introduction**

25 Soil salinization and secondary salinization are significant problems faced by China and the
26 whole world. A characteristic of salinized soil is electrical conductivity (EC), wherein higher
27 levels of salt content are strongly correlated with more excellent conductivity; therefore, EC is an
28 important index to judge the degree of soil salinization(Lian et al., 2010).

29 Over the past 20 years, remote sensing has become the most common method for detecting
30 soil EC because of its reliable real-time results and low cost (Csillag et al., 1993; Eldeiry and
31 Garcia, 2008). In many remote sensing methods, large-scale salinized soil monitoring is based on
32 spectral response characteristics. For the spectral characteristic response band of saline soil, many
33 scholars have studied different remote sensing satellites and have their conclusions. The optimum
34 band combination of saline soil monitoring was studied by Dwivedi et al. (1992), and the results
35 show that the 1, 3, and 5 band combinations of TM data contain the most significant amount of
36 salinization information. Wu Yunzhao et al. (2003) found that the visible (0.55-0.77 μm), near-
37 infrared (0.9-1.03 μm , 1.27-1.52 μm), and short-wave infrared (1.94-2.15 μm , 2.15-2.31 μm , 2.33-
38 2.4 μm) are the critical bands for identifying the saline soil. Based on the eight bands of ETM+,
39 Shrestha(2006) established a salt prediction model of normalized vegetation index (NDVI)
40 containing multiple spectral variables and the normalized salt index (NSI) and salt data. It was
41 found that band 7 (middle infrared) and band 4 (near-infrared) had the highest correlation with soil
42 conductivity. Srivastava et al. (2015) found that the spectra between 1390 nm and 2400 nm are
43 very sensitive to salinity changes based on the information of visible-near infrared reflectance

44 spectra. Meti et al. (2019) found that the combination of short-wave infrared and visible bands of
45 Sentinel-2 and Landsat-8 significantly improved the correlation of saline soil pH and EC in the
46 arid regions of northern India. Davis et al. (2019) used Landsat OLI and Sentinel-2 MSI to reverse
47 the conductivity of saline soil, and the result showed that MSI was superior to OLI and that the
48 visible light band was more sensitive to soil salinity.

49 On this basis, many others have studied the model algorithm of the quantitative relationship
50 between soil salinity and spectral characteristics. To sum up, the main modeling methods include
51 linear regression, least squares, and random forest. Allbed et al. (2014a) established the correlation
52 between the spectral index and conductivity based on IKONOS images. They used linear
53 regression to predict the spatial change of soil salt in the Hassa oasis. Nawar et al. (2015) used
54 multivariate adaptive regression splines to construct a soil spectrum and EC prediction model.
55 Besides, Gorji et al. (2017) obtained the spatial distribution of saline soil around Lake Tuz in
56 Turkey based on SI regression analysis. Zhang Suming et al. (2018) used the Kenli area of the
57 Yellow River Delta as their research area. They combined the measured and multi-time phase
58 remote sensing data to analyze and construct their salt inversion model. Farifthe et al. (2007)
59 predicted the salt content of soil utilizing the partial least square regression and artificial neural
60 network. Fan et al. (2016) carried out soil salt inversion and mapping in the Yellow River Delta
61 region based on the PLSAR model using 30 years of multi-source Landsat data. Wang et al.
62 (2019a) used partial least squares regression and random forest inversion to develop a salinity map
63 of the Ebinur Lake area in northwest China, based on the extraction of conductivity and multi-
64 band spectral indexes of saline soil from 116 sampling points. Li et al. (2019) extracted ten
65 sensitive variables of EC from Landsat using random forest to establish a soil salinity prediction

66 model. Wang et al. (2019b) combined soil salinity data with spectral data in order to achieve soil
67 salinity estimation through constructing a random forest model in arid and semiarid regions. The
68 above studies show the feasibility of quantitative analysis of soil salt. However, hyperspectral data
69 are still obtained by data, and the application of hyperspectral data in regional soil salinization
70 monitoring is limited by some practical factors, such as small image coverage area and others.

71 To sum up, in previous studies, the quantitative estimation of the soil salinity by spectrum
72 analysis is realized by screening the sensitive wavebands or the known spectral indexes as the
73 modeling factors. However, this method only takes into account the relationship between the soil
74 salinity and the sensitive waveband or the sensitive spectral index, and then construct the optimal
75 linear and nonlinear models. However, they forgot considering whether the distribution of
76 variables will affect the accuracy of models before modeling.

77 Based on Sentinel-2 MSI spectral data and measured EC of saline soil, the Box-Cox
78 transformation of the conductivity which does not satisfy the normal distribution was performed,
79 the relationship between different spectral parameters and transformed EC data of saline soil is
80 explored, and the optimization of modeling variables is performed. On this basis, the nonlinear
81 estimation model of EC is constructed by using a machine learning algorithm, and we get an
82 inversion method that is matched with EC of carbonated (soda) saline soil in the western Jilin
83 Province. In order to improve the inversion accuracy of EC of saline soil in the western Jilin
84 Province, and to provide data support for accurate monitoring, evaluation, improvement, and
85 utilization of saline soil.

86 **2 Materials and Methods**

87 **2.1 Site descriptions and soil sampling**

88 The western part of Jilin is part of the Songnen Plain, with the range of 121°38'-126°11'E,

89 43°59'-46°18'N, as shown in Figure 1, the total area is approximately 43360 square kilometers,
90 and the terrain is flat. This area belongs to temperate continental monsoon climate; the average
91 annual precipitation and annual evaporation are present as 400-500 mm and 1000-2000mm. (Liu
92 et al., 2015; Xu et al., 2018). Soil evaporation is intense, which makes it easy for salt to
93 accumulate at the surface. This severely imbalanced evaporation-precipitation ratio, coupled with
94 the influence of local topography, hydrogeological conditions, and human activities, makes the
95 degree of salinization in this area grave. The EC results of pixel-level resolution (10 m × 10 m) of
96 saline soil in western Jilin Province were inversed.

97 Carried out the field experiment from June 20–28, 2019, and selected 328 experimental sites.
98 In order to reduce the influence of mixed pixels, taken three points near each sampling point, and
99 collected the soil samples by ring knife. After each soil sample was dried and sifted through 1 mm
100 mesh, three soil samples from each sampling site were uniformly mixed into 10 g samples to
101 prepare soil suspensions with a soil/water ratio of 1:5, the soil suspension was set aside for about 3
102 hours, and EC was measured using a conductivity meter (LEICI, Model DDS-307A).

103 In order to construct and verify the EC inversion model with pixel-level resolution (10 m ×
104 10 m) of saline soil in western Jilin Province, 328 sample points were randomly grouped, of which
105 randomly used two-thirds total 219 points for modeling, which was called the training dataset, and
106 used the remaining one-third total 109 points for validation of the model, which were called
107 validation dataset.

108 **2.2 Sentinel-2 MSI spectral information extraction and feature construction**

109 In order to coincide with the field sampling time, the Sentinel-2 MSI L1C multispectral data
110 of the study area on June 23, 2019 was selected, as shown on the right side of Figure 1(false-color

composite), and extracted the reflectivity of each band corresponding to the sampling points after atmospheric correction. The band parameters are shown in table 1.

Table 1 Spectral bands of Sentinel-2 MSI sensor

| Acronym | Band | Band center /nm | Band width/nm | Spatial resolution/m |
|---------|---------------------|-----------------|---------------|----------------------|
| B1 | Coastal | 443 | 45 | 60 |
| B2 | Blue | 492 | 98 | 10 |
| B3 | Green | 560 | 46 | 10 |
| B4 | Red | 665 | 39 | 10 |
| B5 | Vegetation Red Edge | 703 | 20 | 20 |
| B6 | Vegetation Red Edge | 739 | 18 | 20 |
| B7 | Vegetation Red Edge | 779 | 28 | 20 |
| B8 | NIR | 833 | 133 | 10 |
| B8A | Vegetation Red Edge | 864 | 32 | 20 |
| B9 | Water vapour | 943 | 27 | 60 |
| B10 | SWIR- Cirrus | 1376 | 76 | 60 |
| B11 | SWIR | 1610 | 141 | 20 |
| B12 | SWIR | 2186 | 238 | 20 |

The construction of spectral parameters includes two methods; one is generated by sensitive band combination operation (addition, multiplication), the other is to evaluate the degree of soil salinization by using the existing spectral indexes. Combined these results with the existing research results, and selected the following spectral indexes for correlation analysis with EC (formula (1)), including soil salt index SI1, SI2, SI3 (Allbed et al., 2014a; Douaoui et al., 2017; KHAN et al., 2005), SI4, SI5, NDSI, and ratio salt index (SI-T). The calculation formula for each index shown in Table 2. Calculation formula of correlation coefficient present as follows:

$$R = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2} \sqrt{\sum_{i=1}^n (y_i - \bar{y})^2}} \quad (1)$$

122

Table 2 Spectral Index Construction

| Spectral Index | Formula |
|----------------------------------|-------------------------------------|
| Soil salinity index SI1 | $SI\ 1 = \sqrt{G \times R}$ |
| Soil salinity index SI2 | $SI\ 2 = \sqrt{G^2 + R^2 + NIR^2}$ |
| Soil salinity index SI3 | $SI\ 2 = \sqrt{G^2 + R^2}$ |
| Soil salinity index SI4 | $SI\ 4 = (SWIR \times R) / G$ |
| Soil salinity index SI5 | $SI\ 5 = (B - SWIR2) / (B + SWIR2)$ |
| Normalized salinity index (NDSI) | $NDSI = (R - NIR) / (R + NIR)$ |
| Ratio salt index (SI-T) | $SI - T = R / NIR$ |

123 **2.3 Modeling methods and evaluation index**

124 Our study showed a modeling flow chart of remote sensing inversion with EC in figure 2.

125 Firstly, a training set and single-band reflectance from Sentinel-2 MSI data were analyzed to

126 screen out the sensitive bands. Then the spectral parameters were constructed based on the

127 sensitive band and screened the optimal spectral parameters. We performed a pre-modeling test

128 dataset distribution that satisfies the Gauss-Markov normality hypothesis. We found the optimal

129 transformation for the data that does not satisfy the condition, thus improving the formality,

130 symmetry, and homogeneity of variance of the data distribution. Finally, using the sensitive band

131 and the optimal spectral parameters as the independent variables, the measured EC was used as the

132 response variables to construct the inversion model and obtain more accurate modeling results, as

133 shown in Figure 2.

134 **2.3.1 Box-Cox Transform**

135 In practical applications, the response variables are often not following the normal

136 distribution, so it is not suitable for data analysis directly. Box-Cox transform was proposed by

137 Box and Cox(1964) for the nonlinear transformation of response variables. By determining an

138 optimal parameter λ , the non-normal data is transformed into approximately normal data, and

139 then, the transformed data is regressed. The Box-Cox transformation of y ($y > 0$) can be
 140 represented by formula (2).

$$141 \quad y^{(\lambda)} = \begin{cases} \frac{y^\lambda - 1}{\lambda}, & \lambda \neq 0 \\ \ln y, & \lambda = 0 \end{cases} \quad (2)$$

142 where y is the raw data, λ is the parameter of the change to be determined.

143 Box-Cox transform determines the optimal λ value by finding the maximum $L_{max}(\lambda)$ of the
 144 likelihood function. In order to calculate the pure logarithm on both sides of the likelihood
 145 function, the term A-independent constant is omitted. Formulas (3) and (4).

$$146 \quad \ln L \quad (3)$$

$$147 \quad J(\lambda, y) = \prod_{i=1}^n \left| \frac{d y_i^{(\lambda)}}{d y_i} \right| \quad (4)$$

148 Where MSE is the mean square error, n is the data quantity.

149 2.3.2 Linear regression model

150 The traditional linear regression model is as follows:

$$151 \quad y = \varepsilon + \beta_1 x_1 + \beta_2 x_2 + \cdots + \beta_k x_k \quad (5)$$

152 Where y is the response variable of the model, $x_1 - x_k$ are independent variables, ε is a constant,
 153 and $\beta_0, \beta_1, \dots, \beta_k$ are undetermined coefficients. In this paper, x is the spectral index of Sentinel-2
 154 MSI data, y is the Box-Cox transform result of the measured EC.

155 2.3.3 Machine learning models

156 Because of the influence of mixed pixels and atmospheric radiation, the relationship between
 157 spectral parameters and EC of saline soil may be nonlinear, so the machine learning algorithm
 158 model is considered to invert the EC of saline soil. At present, common machine learning models

159 include the following:

160 1) Support Vector Machine

161 V. Vapnik and Cortes proposed a support vector machine (SVM) (Cortes and Vapnik, 1995).

162 For regression problems that are not suitable for linear models, SVM can improve the accuracy of

163 regression prediction by mapping the low-dimensional training dataset to the high-dimensional

164 space construction model, and it has good generalization ability for small sample data sets.

165 2) Regression Tree

166 The regression tree(RT) is a binary decision tree for regression analysis (Mingers, 1989). The

167 feature selection is carried out recursively, and the given input variable predicts the probability

168 distribution of the output variable, and then, the binary regression tree is generated. The regression

169 tree is unstable with big data sets, and the weak change of the training dataset may lead to a

170 change in the tree structure.

171 3) Gaussian Process Regression

172 Gaussian process regression (GPR) is a new machine learning algorithm, which is a non-

173 parametric regression probability model based on Bayesian and statistical learning theory. It is

174 assumed that the input of the model is x , and the output is $f(x)$. A set of input sets

175 $\{x_i \vee i=1,2,\dots,n\}$ obtains an output set $f(x)$ through a Gaussian process regression model.

176 Under the assumption of the mean of zero, the distribution form of $f(x)$ can be expressed as

177 follows: $f(x) \sim N(0, K(\theta, x, x')), K(\theta, x, x')$ is a covariance matrix with super parameters

178 (some parameters of kernel functions).

179 4) Ensemble Tree

The ensemble tree (ET) is a regression-lifting algorithm based on the regression tree and using the forward distribution and adding. This ensemble learning method constructs a prediction model by weighting several regression tree results when the instance is predicted. Compared with the regression tree, better results may be obtained for some datasets, thus improving prediction performance.

2.3.4 Evaluation indicators

In order to evaluate the accuracy of the inversion model, the method of V fold cross verification (VFCV)(Geisser, 1975) is used to model the data, and the determination coefficient R^2 , root mean square error (RMSE) and mean absolute error (MAE) are used to evaluate the model. The calculation method is shown in the formulas (6), (7), and (8).

$$R^2 = \frac{\sum_{i=1}^N (f_i - \bar{y})^2}{\sum_{i=1}^N (y_i - \bar{y})^2} \quad (6)$$

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (y_i - f_i)^2} \quad (7)$$

$$MAE = \frac{1}{N} \sum_{i=1}^N |y_i - f_i| \quad (8)$$

Where y_i represents a true value, f_i represents a predicted value, \bar{y} represents a mean value, and N represents a sample size.

The principle of the VFCV method is to divide the data set into V parts, one from V parts as verification, the remaining V-1 as training, repeat V times, and take the mean value of each verification result as the final result to find the optimal model. VFCV can improve the generalization ability of the model to a certain extent. In this study, the V value is 10. According to

research experience, it is found that tenfold cross-verification can balance deviation and variance, which is the best choice to obtain model error estimation. The closer the R^2 is to 1 in the evaluation parameter, the higher the fitting accuracy of the model; The closer the RMSE is to 0, the better the performance of the model, the smaller the difference is between the measured value and the predicted value; compared with RMSE, MAE has better robustness to outliers in the dataset and does not reduce the accuracy of the model as a whole.

3 Results

3.1 EC Measurement results

The statistical results of the measured EC for the 328 samples collected in the field are shown in Table 3. It can be seen from the table that the range of EC is 0.66 mS/cm, the standard deviation ranges from 0.06 to 5.87 mS/cm, and the coefficient of variation is significant, which indicates that the sample points have very high spatial heterogeneity.

Table 3 EC (mS/cm) Statistical Table

| | Maximum | Minimum | Mean | Standard deviation | Coefficient of variation (%) |
|-----------------------------|---------|---------|------|--------------------|------------------------------|
| All data N=328 | 5.87 | 0.06 | 0.66 | 0.91 | 138 |
| Training dataset N=219 | 5.87 | 0.06 | 0.72 | 0.98 | 136 |
| Validation dataset N=109 | 5.79 | 0.08 | 0.53 | 0.73 | 137 |

3.2 Selection of sensitive bands

In this paper, the correlation between the measured EC data and the single-band spectral reflectance from the Sentinel-2 MSI was analyzed ($p < 0.01$). The correlation coefficient R values were obtained, as shown in Table 4 below ($p < 0.01$). The results show that the B2, B3, B4, and B8 bands were sensitive bands.

Table 4 Correlation between EC and spectral reflectance of Sentinel-2 MSI

| Band | B2 | B3 | B4 | B5 | B6 | B7 | B8 | B8A | B11 | B12 |
|------|----|----|----|----|----|----|----|-----|-----|-----|
|------|----|----|----|----|----|----|----|-----|-----|-----|

| | | | | | | | | | | |
|---|------|------|------|------|------|------|------|------|------|------|
| R | 0.42 | 0.43 | 0.41 | 0.34 | 0.29 | 0.28 | 0.42 | 0.24 | 0.15 | 0.20 |
|---|------|------|------|------|------|------|------|------|------|------|

N=219, N is number of samples

3.3 Construction of optimal spectral parameters

In order to consider the spectral characteristics synthetically, the spectral parameters of the inversion model combined B2, B3, B4 and B8 bands and spectral index SI1, SI2, SI3, SI4, SI5, NDSI, and SI-T by multiplication. Table 5 shows the correlation coefficient R ($p < 0.01$) between the different spectral parameters based on the Sentinel-2 MSI data and the saline soil EC. Comparing Tables 3 and 4, the correlation between EC and spectral parameters of saline soil was higher than that of a single band reflectivity, and the band combination of $R > 0.40$ was selected as the spectral parameter of the estimation model. Thus $B2 \times B3 \times B4$, $B2 \times B3 \times B8$, $B3 \times B8$, $B3 \times B4 \times B8$, $B2 \times B3$, $B2 \times B8$, SI2, SI1 and SI3 were chosen as the optimal spectral parameters.

Table 5 EC correlation analysis with spectral parameter reflectance

| | | | | | | | |
|---------------------|--------------------------|--------------------------|----------------|--------------------------|----------------|----------------|------|
| Spectral parameters | $B2 \times B3 \times B4$ | $B2 \times B3 \times B8$ | $B3 \times B8$ | $B3 \times B4 \times B8$ | $B2 \times B3$ | $B2 \times B8$ | SI2 |
| R | 0.52 | 0.51 | 0.48 | 0.48 | 0.47 | 0.43 | 0.42 |
| Spectral parameters | SI1 | SI3 | $B2 \times B4$ | NDSI | SI_T | SI5 | SI4 |
| R | 0.41 | 0.41 | 0.38 | 0.32 | 0.33 | 0.23 | 0.14 |

N=219, N is number of samples

3.4 Box-Cox parameter λ estimation results

By testing the data of response variables and independent variables involved in modeling, we can see that the response variable EC does not conform to the normal distribution, as shown in Figure 3. The maximum likelihood estimation method proposed by Box-Cox was used to determine the parameter λ value. For different λ values ($-2 \leq \lambda \leq 2$), the maximum value $L_{max}(\lambda)$ of the likelihood function was calculated by the least square estimation of the linear regression model, which is expressed as $\text{Log-Likelihood} = \ln(L_{max}(\lambda))$, with λ as the horizontal axis and

Log-Likelihood as the longitudinal axis. The results are shown in Figure 4 and Table 6. It can be seen from the results that when $\lambda = 0$, Log-Likelihood was the largest. According to formula (1), the $EC = \ln(EC)$ after the Box-Cox transform was calculated as EC_{bc} , and the data are close to a normal distribution, as shown in Figure 3b).

Table 6 Maximum value of likelihood function and λ statistical table

| | | | | | | | |
|----------------|----------------|---------|---------|---------|---------|---------|---------|
| λ | -2.00 | 1.75 | -1.50 | -1.25 | -1.00 | -0.90 | -0.80 |
| Log-Likelihood | -507.38 | -449.76 | -396.97 | -349.42 | -307.68 | -292.79 | -279.01 |
| λ | -0.70 | -0.60 | -0.50 | -0.40 | -0.30 | -0.20 | -0.10 |
| Log-Likelihood | -266.44 | -255.15 | -245.28 | -236.93 | -230.29 | -225.53 | -222.87 |
| λ | 0.00 | 0.10 | 0.20 | 0.30 | 0.40 | 0.50 | 0.60 |
| Log-Likelihood | -222.57 | -224.90 | -230.16 | -238.62 | -250.53 | -266.02 | -285.13 |
| Λ | 0.70 | 0.80 | 0.90 | 1.00 | 1.25 | 1.50 | 1.75 |
| Log-Likelihood | -307.78 | -333.75 | -362.77 | -394.49 | -483.33 | -582.14 | -687.60 |

3.5 Linear regression models for the EC retrieval

Using EC and EC_{bc} data as dependent variables of linear regression model in 2.3.2, respectively. The regression model and verification accuracy were obtained, as shown in Table 7 and Table 8. It can be seen from the table that the regression model with single band and spectral parameters as independent variables and EC_{bc} as dependent variables had the highest accuracy, and the R^2 of the verification accuracy was 0.51. Therefore, EC_{bc} was used to participate in the modeling. The regression model and verification accuracy were obtained, as shown in Table 7 and Table 8.

Table 7 Linear inversion model before and after soil conductivity transformation

| Variable | Regression model | Model accuracy R^2 | Verification accuracy R^2 |
|---------------------|---|-------------------------|--------------------------------|
| Single band | $EC = -1.266 + 0.001 \times B2 + 0.002 \times B3 - 0.001 \times B4 + 0.003 \times B8$ | 0.21 | 0.21 |
| | $EC_{bc} = -3.078 + 0.001 \times B2 + 0.001 \times B3 - 0.001 \times B4 + 7.90 \times 10^{-5} \times B8$ | 0.32 | 0.39 |
| Spectral parameters | $EC = 1.962 + 1.673 \times 10^{-8} \times (B2 \times B3) - 1.160 \times 10^{-7} \times (B2 \times B8) + 2.008 \times 10^{-7} \times (B3 \times B8) + 2.109 \times 10^{-11} \times (B2 \times B3 \times B4) + 5.073 \times 10^{-11} \times (B2 \times B3 \times B8) + 1.178 \times 10^{-11} \times (B3 \times B4 \times B8)$ | 0.37 | 0.37 |

| | | | |
|--|--|------|------|
| | $^{11} \times (B3 \times B4 \times B8) + 0.001 \times SI2 - 0.001 \times SI3$ | | |
| | EC_bc = $-0.434 + 4.586 \times 10^{-8} \times (B2 \times B3) - 1.862 \times 10^{-7} \times$ $(B2 \times B8) + 1.711 \times 10^{-7} \times (B3 \times B8) + 2.839 \times 10^{-11} \times$ $(B2 \times B3 \times B4) + 3.724 \times 10^{-11} \times (B2 \times B3 \times B8) + 1.658 \times 10^{-11} \times$ $(B3 \times B4 \times B8) + 0.001 \times SI2 - 0.011 \times SI3$ | 0.46 | 0.46 |
| Single band and Spectral parameters | EC = $0.543 + 0.001 \times B2 + 0.002 \times B3 + 0.001 \times B4 + 0.003 \times B8 + 3.790$ $\times 10^{-8} \times (B2 \times B3) - 4.196 \times 10^{-7} \times (B2 \times B8) + 2.246 \times 10^{-7} \times$ $(B3 \times B8) + 1.448 \times 10^{-11} \times (B2 \times B3 \times B4) + 4.789 \times 10^{-11} \times$ $(B2 \times B3 \times B8) + 3.191 \times 10^{-11} \times (B3 \times B4 \times B8) - 0.004 \times SI2$ | 0.42 | 0.45 |
| | EC_bc = $1.489 + 0.001 \times B2 + 0.001 \times B3 + 0.001 \times B4 + 0.003 \times B8 +$ $7.403 \times 10^{-8} \times (B2 \times B3) - 4.354 \times 10^{-7} \times (B2 \times B8) + 1.962 \times 10^{-7} \times$ $(B3 \times B8) + 1.731 \times 10^{-11} \times (B2 \times B3 \times B4) + 3.464 \times 10^{-11} \times$ $(B2 \times B3 \times B8) + 3.900 \times 10^{-11} \times (B3 \times B4 \times B8) - 0.004 \times SI2$ | 0.49 | 0.51 |

N=219, N is number of samples

Table 8 Evaluation Indexes of linear inversion models of EC_{bc}

| Variable | Training dataset | | | Validation dataset | | |
|--|------------------|----------------|-------------|--------------------|----------------|-------------|
| | RMSE | R ² | MAE | RMSE | R ² | MAE |
| | /(mS/cm) | | /(mS/cm) | /(mS/cm) | | /(mS/cm) |
| Single band | 0.55 | 0.32 | 0.50 | 0.56 | 0.39 | 0.51 |
| Spectral parameters | 0.52 | 0.46 | 0.48 | 0.55 | 0.46 | 0.49 |
| Single-band and Spectral parameters | 0.53 | 0.49 | 0.44 | 0.56 | 0.51 | 0.44 |

3.6 Machine learning models for the EC retrieval

The optimal spectral parameters selected from 3.3 were used as the input, and the EC_{bc} was used as the output to build the model with five algorithms of SVM, RT, GPR, and ET, respectively. The inversion results of each model to the validation dataset are shown in Figure 5. In order to quantitatively describe the inversion accuracy of the model, the evaluation index results of the five models are shown in Table 9.

Table 9 Evaluation Indexes of five models

| Model | Training dataset | | | Validation dataset | | |
|------------|------------------|----------------|-------------|--------------------|----------------|-------------|
| | RMSE/(mS/cm) | R ² | MAE/(mS/cm) | RMSE/(mS/cm) | R ² | MAE/(mS/cm) |
| LINEAR | 0.53 | 0.49 | 0.44 | 0.56 | 0.51 | 0.44 |
| SVM | 0.43 | 0.58 | 0.48 | 0.44 | 0.65 | 0.53 |
| RT | 0.50 | 0.58 | 0.57 | 0.52 | 0.57 | 0.53 |
| GPR | 0.42 | 0.61 | 0.58 | 0.48 | 0.66 | 0.52 |

| ET | 0.51 | 0.61 | 0.53 | 0.49 | 0.62 | 0.54 |
|----|------|------|------|------|------|------|
|----|------|------|------|------|------|------|

As can be seen from Table 9, the traditional linear regression model had the worst results among the evaluation indexes of the five models. Among the four machine learning models, the R^2 of the GPR model was 0.66, the RMSE was 0.48, and the MAE was 0.52. The prediction performance of the GPR model was the best, SVM was the second, and RT was the lowest. In the comprehensive view, the accuracy of the five models for the inversion of the saline soil EC was GPR> SVM> ET> RT> LINEAR. Figure 6 shows the comparison between the measured values and the predicted values of 109 points in the data set verified by the GPR model.

3.7 The inversion results of saline soil EC in the west of Jilin Province

In order to reflect the EC of the large-area of saline soil in the west of Jilin, according to the most accurate GPR model in 3.6, based on the Sentinel-2 MSI data of June 23, 2019, EC of the pixel-level resolution of the saline soil in the western part of Jilin Province was obtained by inversion in 2019. The results are shown in Figure 7.

In order to quantify the degree of soil salinization in this study area, according to the classification criterion of Kissell and Sonon (2008), the degree of salinization of inversion EC was graded and mapped. The results are shown in Figure 8. It can be seen from the results that the soil salinization in the study area tends to increase gradually from east to west. Mild saline soil was mainly distributed in Qianguo County, Changling County, and Fuyu City. Moderate and severe saline soil was mainly distributed in Zhenlai County, the junction of Da'an City, Qianan County, and Tongyu County, and a small area of extremely saline soil was distributed in Da'an City, Qianan County, and Zhenlai County.

In order to quantitatively describe the area of the soil with different degrees of salinization, the areas of several salinized soils in Figure 8 were counted, and the results are shown in Table 10.

According to the statistical data, after many years of improvement, the degree of soil salinization in the western part of Jilin Province in 2019 was mainly mild, accounting for 54.48% of the total area, moderate and severe salinization covered 33.29% of the area, and the extremely heavy salinization was 2.26% of the study area.

Table 10 Statistics of soil salinity grades in western Jilin Province in 2019

| Soil Salinity Level(mS/cm) | Non-Saline Soil (0-0.15) | Low Salinity (0.16-0.50) | Medium Salinity (0.51-1.25) | Strongly Salinity (1.26-1.75) | Very High Salinity (1.76-2.0) | Excessively High Salinity (>2.0) |
|----------------------------|--------------------------|--------------------------|-----------------------------|-------------------------------|-------------------------------|----------------------------------|
| Area (km ²) | 653.72 | 3572.07 | 1975.91 | 206.71 | 79.68 | 68.06 |
| Percent (%) | 9.97 | 54.48 | 30.14 | 3.15 | 1.22 | 1.04 |

4. Discussion

When the spectral index is selected, it is an important prerequisite that invalid information generated by the superimposed spectrum can be compressed, and the practical information of saline soil characteristics can be highlighted in order to improve the accuracy of the model. At present, the commonly used spectral indices are the NDVI, the NDSI, and the others mentioned above. We believe that on the one hand, these indices did not use the sensitive band to superimpose useful spectral information to delve into the spectral characteristics of saline soil; on the other hand, the presence of alkali-resistant crops such as soda can lead to the error of using NDVI to retrieve soil salinization. Allbed et al. (2014b) expressed a similar view that salt recognition based on vegetation index would not work in bare land. Therefore, the index of NDVI was avoided in this paper.

We performed a Box-Cox transformation on the EC data of the original saline soil to determine an optimal λ , thereby transforming the non-normal data into approximately normal data. Subsequently, the single-band and spectral parameters were used as independent variables, and the

302 regression model was obtained after the Box-Cox transformation. After verification, the accuracy
303 was $R^2 = 0.51$, which is a particular improvement over the accuracy of 0.45 without conversion
304 (Section 3.5 Table 6). Besides, the spectral parameters were constructed by multiplying the
305 sensitive band by Box-Cox transforming the EC data of the original saline soil and combining the
306 single band as the modeling factor, the selectivity of the modeling was increased, and the synergy
307 between the spectral segments was enhanced.

308 In existing studies, researchers (Atman et al., 2018; Bannari et al., 2018) have found that the
309 short-wave infrared band of Sentinel-2 MSI, which can distinguish different grades of saline soils
310 by combined with visible light bands, is more sensitive to saline soils in arid regions. Meti et al.
311 (2019) once again demonstrated that the combination of visible light bands of Sentinel-2 MSI and
312 short-wave infrared could significantly improve the correlation with soil EC ($R=0.60-0.70$). Also,
313 several studies have demonstrated the potential of the short-wave infrared band of Sentinel-2 MSI
314 in distinguishing saline soils (Bannari et al., 2016; Bannari et al., 2008; FARIFTEH et al., 2007).
315 Researchers (Bannari et al., 2018) have found that light with short-wavelength infrared
316 wavelengths can easily detect soils that are predominantly rich in sulfate minerals, chlorides, and
317 small amounts of bicarbonate. According to this, we constructed a spectral index composed of
318 short-wave infrared and visible light bands (Section 2.2 Table 1 SI4, SI5). $R_{SI4}=0.14$, $R_{SI5}=0.23$.
319 However, the results show a poor correlation, indicating that the above conclusions do not apply to
320 saline soils in western Jilin. We speculate that the western part of Jilin belongs to the Songnen
321 plain, and the type of saline soil is inland soda saline soil, which main salt composition is NaHCO_3
322 and Na_2CO_3 with containing a small amount of sulfate and chloride, thus has present strong
323 alkalinity. We know that saline soils in the arid area, which mainly contain chloride-sulfate saline

and sulfated soils, belong to slightly alkaline soils. Due to the differences in the chemical composition, the characteristic bands of different types of saline soils are different.

At the same time, because of the different driving factors and formation mechanism of saline soil, there are many factors affecting salt, which lead to the complex nonlinear relationship between salt and spectrum. Therefore, the linear regression model is not a good reflection of this relationship; the machine learning algorithm solves the nonlinear problem of the model, which can effectively improve the accuracy of saline soil conductivity inversion. In the machine learning algorithm, the GPR model performs better (Boedecker et al., 2014; Rasmussen et al., 2005) in calculating the probability of the super-parameter acquisition and the variable output compared with the common SVM, the neural network, and RT. The model uses a Gaussian process to deduce the function distribution of the training dataset, obtains the super optimal parameters based on the kernel function, and uses the training dataset to train the super parameters to realize the prediction output; the model works better for high-dimensional small samples and non-linear regression.

5 Conclusion

In this study, according to the correlation of electrical conductivity characteristics and spectral reflectance of each band of Sentinel-2 MSI, the sensitive band was screened, and the optimal spectral parameters were constructed by mathematical operations such as multiplying the sensitive band. The EC_{bc} was obtained by the Box-Cox transformation of EC data, which did not satisfy the normal distribution, and we constructed the linear regression models of EC with spectral parameters and a model of EC_{bc} with spectral parameters, respectively. The verification results showed that the accuracy of the model R^2 after EC transformation was improved from 0.45 to 0.51. Therefore, we established the nonlinear inversion models of GPR, ET, SVM, and RT of

EC_{bc}. Then using validation set, the inversion accuracy of salt soil EC_{bc} was as follows: GPR > ET > SVM > RT > LINEAR. The most accurate GPR model for the validation dataset inversion R² was 0.66, proving the validity of the model. Finally, according to the model, the pixel resolution results of saline soil EC were inversed in western Jilin Province in 2019, which provides necessary data support for evaluating the salinization degree of soil and the effectiveness of the improvement scheme.

Acknowledgments

This research was funded by the National Natural Science Foundation of China (No.41671350).

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