

1                   **The conductive cooling of planetesimals with**  
2                   **temperature-dependent properties**

3                   **M. Murphy Quinlan<sup>1</sup>, A. M. Walker<sup>1,2</sup>, C. J. Davies<sup>1</sup>, J. E. Mound<sup>1</sup>, T.**  
4                   **Müller<sup>1,3</sup>, J. Harvey<sup>1</sup>**

5                   <sup>1</sup>School of Earth and Environment, University of Leeds, Leeds, UK

6                   <sup>2</sup>Department of Earth Sciences, University of Oxford, Oxford, UK

7                   <sup>3</sup>Geoscience Center, Georg-August-University Göttingen, Göttingen, Germany

8                   **Key Points:**

- 9                   • Conductivity, heat capacity and density are temperature dependent and control  
10                  the cooling of planetesimals
- 11                  • The estimated depth and timing of meteorite origin changes if temperature-dependent  
12                  properties are used to model the parent body
- 13                  • Temperature-dependent properties in a model of the pallasite parent body delay  
14                  the onset of core solidification by 40 million years

---

Corresponding author: Maeve Murphy Quinlan, School of Earth and Environment, University of  
Leeds, Woodhouse, Leeds LS2 9JT, UK, [eememq@leeds.ac.uk](mailto:eememq@leeds.ac.uk)

**Abstract**

Modelling the planetary heat transport of small bodies in the early Solar System allows us to understand the geological context of meteorite samples. Conductive cooling in planetesimals is controlled by thermal conductivity, heat capacity, and density, which are functions of temperature ( $T$ ). We investigate if the incorporation of the  $T$ -dependence of thermal properties and the introduction of a non-linear term to the heat equation could result in different interpretations of the origin of different classes of meteorites. We have developed a finite difference code to perform numerical models of a conductively cooling planetesimal with  $T$ -dependent properties and find that including  $T$ -dependence produces considerable differences in thermal history, and in turn the estimated timing and depth of meteorite genesis. We interrogate the effects of varying the input parameters to this model and explore the non-linear  $T$ -dependence of conductivity with simple linear functions. Then we apply non-monotonic functions for conductivity, heat capacity and density fitted to published experimental data. For a representative calculation of a 250 km radius pallasite parent body,  $T$ -dependent properties delay the onset of core crystallisation and dynamo activity by  $\sim 40$  Myr, approximately equivalent to increasing the planetary radius by 10%, and extend core crystallisation by  $\sim 3$  Myr. This affects the range of planetesimal radii and core sizes for the pallasite parent body that are compatible with paleomagnetic evidence. This approach can also be used to model the  $T$ -evolution of other differentiated minor planets and primitive meteorite parent bodies and constrain the formation of associated meteorite samples.

**Plain Language Summary**

Meteorites are fragments of the earliest planetary bodies in our Solar System. Meteorite samples record snapshots of the temperatures and cooling rates experienced inside these small rocky bodies before they were broken apart in collisions. By taking the cooling rate recorded in a meteorite and comparing it to the cooling rates expected at different depths inside parent bodies (based on computational modelling), we can estimate what size the parent body might have been and how deep inside it the meteorite formed. Properties like thermal conductivity control how the body cools: these properties are temperature dependent, so their value changes as the body cools down. We find that including this temperature-dependence is important when modelling meteorite parent bodies, and that assuming these properties are constant can result in different interpretations of meteorite samples. As an example, we model the parent body of stony-iron meteorites called pallasites. We find that if you include temperature-dependent properties, the iron core freezes forty million years later than if you use constant thermal properties, which in turn affects in which meteorite samples you expect to find paleomagnetism records of core dynamo activity. This result has implications for the thermal evolution of other meteorite parent bodies and other minor planets in the Solar System, and the code developed can be adapted to investigate these other small bodies.

**1 Introduction**

Planetesimals are small rocky or icy bodies of a few to a few hundred kilometres in diameter that formed by collisional coagulation in the protoplanetary disk, and are considered the building blocks of larger planetary bodies (Weidenschilling, 2000; Kokubo & Ida, 2012). These early planetesimals are hypothesised to be the primary parent bodies of meteorites while the remnants of disrupted planetesimals, preserved as asteroids, are termed the secondary parent bodies (Greenwood et al., 2020). Planetesimals experienced varied thermal histories: differentiated meteorites displaying igneous textures are sourced from planetesimals that underwent melting and segregation of a metallic core and silicate mantle (Baker et al., 2005), while chondritic meteorites contain primitive material including solids that condensed from hot gas in the Solar Nebula (MacPherson,

2014). Understanding the geological context of differentiated meteorites and their parent bodies' thermal evolution allows constraints to be placed on the formation, differentiation and eventual breakup of planetesimals, and on the early evolution of the Solar System. In this context, models of conductive cooling of differentiated primary parent bodies are frequently used to aid the interpretation of meteorite samples. In this study we investigate the importance of including temperature dependent thermal properties in such models. We use a pallasite parent body as an example to illustrate the influence that including  $T$ -dependent properties can have on understanding the origin of meteorite samples.

One approach to understanding the formation of meteorites is to analyse the thermal processing experienced by meteorite samples and to compare this to estimated temperature conditions within the parent body using thermal evolution models. Heat flow in conductively cooling planetesimals is controlled by the material properties of their constituent minerals — thermal conductivity ( $k$ ,  $\text{W m}^{-1} \text{K}^{-1}$ ), density ( $\rho$ ,  $\text{kg m}^{-3}$ ) and heat capacity ( $C$ ,  $\text{J kg}^{-1} \text{K}^{-1}$ ), in addition to the boundary conditions imposed and the geometry of the planetesimal. Large temperature gradients are expected in planetesimals, with typical surface temperatures of  $\sim 250$  K rising to  $\sim 1800$  K at the centre (Bryson et al., 2015; Scheinberg et al., 2016). Planetesimals experience much lower internal pressures than planets: the centre of a 250 km body with an olivine mantle and an iron core would be at  $\sim 300$  MPa, in comparison to Earth's central pressure of 364 GPa (Dziewonski & Anderson, 1981; Scheinberg et al., 2016). If  $k$ ,  $\rho$  and  $C$  are assumed constant, they can be expressed in terms of diffusivity  $\kappa = \frac{k}{\rho C}$ . This is a common approximation made in conductive cooling models of differentiated planetesimals with olivine mantles, despite temperature and pressure dependence (Bryson et al., 2015; Fu et al., 2014; Haack et al., 1990; Tarduno et al., 2012). While the finite difference methods frequently used in these models can be applied to systems involving  $T$ -dependent properties, the heat conduction equation becomes nonlinear and more expensive to solve when  $T$ -dependent  $k$  is included (Özsisik, 1993). Bulk rock conductivity decreases by 40 – 60 % of its value at room temperature in mantle rocks when temperature increases from room temperature to 1273 K, while conductivity increases by approximately 4 % with an increase in pressure of 1 GPa (Hofmeister, 1999; Seipold, 1998; Wen et al., 2015). Due to the weaker dependence of conductivity on pressure, and the low pressure gradients expected in planetesimals, in this paper we will focus on the temperature dependence of material properties.

Previous models of planetesimal thermal evolution take various approaches to the incorporation of  $k$ ,  $\rho$  and  $C$ . These models address different stages of planetesimal evolution, depending on the meteorite group of interest, and can be broadly grouped into two classes. Models focusing on the accretion, early heating and melting of asteroids and planetoids investigate the origin of primitive meteorites (Allan & Jacobs, 1956; Elkins-Tanton et al., 2011; Hevey & Sanders, 2006), while conductive cooling models examine the post-peak- $T$  period following recrystallisation and capture the genesis of extensively differentiated meteorites such as pallasites (Bryson et al., 2015; Ghosh & McSween, 1998; Haack et al., 1990; Nichols et al., 2016; Scheinberg et al., 2016; Tarduno et al., 2012). Models in the first class, for example those investigating the ordinary chondrite parent body, often employ temperature-dependent diffusivity from Yomogida and Matsui (1983):  $\kappa = A+B/T$ , where  $A$  and  $B$  are terms that describe the degree of compaction of the parent body (Akridge et al., 1998; Bennett & McSween, 1996; Harrison & Grimm, 2010). Ghosh and McSween (1999) highlight the importance of incorporating a temperature-dependent specific heat capacity in the modelling of primitive asteroids, recording a decrease in peak temperatures and corresponding change in closure temperatures when  $T$ -dependent  $C$  is used, but  $k$  and  $\rho$  are held constant.

The second class of models, which address conductive cooling in differentiated planetesimals such as the primary pallasite parent body (Bryson et al., 2015; Ghosh & McSween, 1998; Nichols et al., 2016; Scheinberg et al., 2016), generally assume mantle  $k$ ,

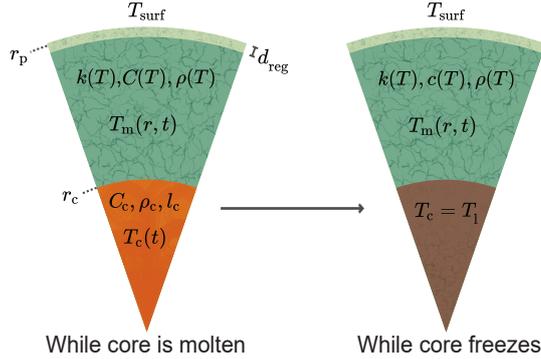
118  $\rho$  and  $C$  are independent of temperature. When experimentally investigating the effect  
 119 of Fe content on olivine conductivity, Zhang et al. (2019) comment on the inclusion of  
 120  $T$ -dependent and composition-dependent  $k$  in their COMSOL<sup>TM</sup> models and note that  
 121 the inclusion of variable properties have a non-negligible effect on the thermal evolution  
 122 of a silicate sphere. However, the focus of the study is olivine forsterite content and the  
 123 impact of olivine composition on the thermal evolution of planetary bodies, and  $T$ -dependence  
 124 is not systematically explored. The implications of neglecting  $T$ -dependent  $k$ ,  $\rho$  and  $C$   
 125 on the interpretation of meteorite parent body models is not understood.

126 Meteorites that display remnant magnetisation can inform us about the magnetic  
 127 field present in the environment of their parent body, which in turn allows us to estimate  
 128 when an internal dynamo may have been active (Scheinberg et al., 2016). The pallasite  
 129 parent body has been chosen as an example for this study as previous research has tied  
 130 paleomagnetism identified in meteorite samples to the period of core crystallisation in  
 131 the parent body (Bryson et al., 2015, 2019; Nichols et al., 2016; Tarduno et al., 2012).  
 132 In order for the metal portion of a pallasite meteorite to record a convective core dy-  
 133 namo, it must cool through the tetraenaite chemical ordering temperature of the metal  
 134 portion while the core is crystallising (Bryson et al., 2015; Scheinberg et al., 2016). Mod-  
 135 ifying the material properties of the body affects whether this condition is met. The geo-  
 136 chemical and petrological heterogeneity exhibited across pallasite meteorites has been  
 137 used to argue for multiple parent bodies or alternatively different environments and depths  
 138 of formation within a single parent body (Boesenberg et al., 2012; McKibbin et al., 2019).  
 139 Paleomagnetism places an easily-testable constraint on models to investigate the impor-  
 140 tance of including  $T$ -dependent properties when deciding parent body geometry, the for-  
 141 mation depth of pallasite meteorites, and the number of parent bodies involved in for-  
 142 mation.

143 Before we address the specific example of the pallasite parent body, we outline the  
 144 approach used to incorporate  $T$ -dependent properties in models of conductive cooling  
 145 of planetesimals and show how, even in simple cases, this can have an important influ-  
 146 ence on their thermal history. We first address the model and numerical scheme in sec-  
 147 tion 2, before exploring the sensitivity of the model to different parameters with man-  
 148 tle  $k$ ,  $C$  and  $\rho$  as independent of  $T$  and investigating the range of parameters used in the  
 149 literature. We then address the incorporation of a non-linear term when  $T$ -dependent  
 150  $k$  is included by using a series of simple linear functions for  $k(T)$  in section 3.2. We im-  
 151 plement  $T$ -dependent functions for  $k$ ,  $C$  and  $\rho$  in section 3.3, and attempt to recreate  
 152 these results by averaging the values for  $k$ ,  $C$  and  $\rho$  radially and through time and then  
 153 using these mean values in the constant model. Finally, we discuss the relevance to mod-  
 154 elling the pallasite parent body.

## 155 2 Methods

156 To investigate the effect of including temperature-dependent properties in the ther-  
 157 mal evolution of planetesimals, we used the 1D in radius  $r$  heat conduction equation with  
 158 a non-linear term to allow for temperature dependence of  $k$ ,  $\rho$  and  $C$  (Carslaw & Jaeger,  
 159 1986; Özisik, 1993). As in Bryson et al. (2015), the layered body is composed of three  
 160 primary materials: a metallic FeS core which is initially molten, a solid olivine mantle  
 161 and an insulating megaregolith layer (see Figure 1). Assuming a purely conductive man-  
 162 tle following magma-ocean solidification, in which convective heat transport is neglected,  
 163 the temperature  $T$  in the mantle satisfies the differential heat conduction equation in spher-  
 164 ical geometry:



**Figure 1.** Not to scale. General model set-up, both before and during core solidification, displaying the functions relevant to different regions. Core radius is defined as a fraction of the total planetary radius, which includes the megaregolith layer. The megaregolith has a constant  $\kappa$ .

$$\frac{\partial T}{\partial t} \rho C = \frac{1}{r^2} \frac{\partial}{\partial r} \left( kr^2 \frac{\partial T}{\partial r} \right) = \overbrace{\frac{dk}{dT} \left( \frac{\partial T}{\partial r} \right)^2}^{\text{non-linear term}} + \underbrace{\frac{2k}{r} \frac{\partial T}{\partial r}}_{\text{geometric term}} + \overbrace{k \frac{\partial^2 T}{\partial r^2}}^{\text{linear term}}, \quad (1)$$

165 where  $t$  is time. The non-linear term arises due to the  $T$ -dependence of  $k$ . The insulat-  
 166 ing megaregolith layer is given a constant diffusivity lower than that of the mantle as  
 167 in Bryson et al. (2015). Pressure and self-gravitation are not incorporated into the cur-  
 168 rent model. The boundary and initial conditions are chosen as follows:

$$T(r_p, t) = T_{\text{surf}}, \quad T(r, t_0) = T_{\text{init}}, \quad T(r_c, t) = T_c(t), \quad (2)$$

169 where  $r_p$  is the planetesimal radius,  $r_c$  is the core radius,  $T_{\text{surf}}$  is the constant surface  
 170 temperature,  $T_c$  is the core temperature and  $T_{\text{init}}$  is the initial temperature, implying  
 171 a homogeneous initial interior temperature distribution at  $t_0$ ; the code can accommo-  
 172 date a heterogeneous initial temperature array but this is not used in this study. A Dirich-  
 173 let boundary condition has been applied to the surface as in Bryson et al. (2015) instead  
 174 of a radiative condition as used by Ghosh and McSween (1998), assuming the temper-  
 175 ature at the surface of the planetesimal is constant and that of the ambient Solar Neb-  
 176 ular. While a radiative boundary condition is a closer approximation to the physical sys-  
 177 tem, a simpler fixed-temperature boundary condition has been found to produce neg-  
 178 ligible difference in inner-Solar System asteroidal models (Hevey & Sanders, 2006; Moskovitz  
 179 & Gaidos, 2011).

180 The boundary condition for the base of the mantle depends on the core temper-  
 181 ature. Because of our focus on the effect of  $T$ -dependent properties of the mantle, we  
 182 follow the previous simplified core models of Bryson et al. (2015) and Tarduno et al. (2012)  
 183 and assume the core is initially entirely liquid and vigorously convecting, and that on  
 184 cooling it behaves as if it were pure iron or as an FeS mixture with eutectic composition.  
 185 We discuss the implications of this simplified core model in section 4. The core temper-  
 186 ature is updated by considering the total energy extracted across the core-mantle bound-  
 187 ary (CMB). The energy transferred during a small time increment  $\delta t$  is

$$E_{\text{CMB}} = -A_c k_{\text{CMB}} \left. \frac{\partial T}{\partial r} \right|_{r=r_c} \delta t, \quad (3)$$

188 where  $A_c$  is the surface area of the core,  $r_c$  is the radius of the core, and  $k_{\text{cmb}}$  is the ther-  
 189 mal conductivity at the base of the mantle at the CMB, i.e.  $k_{\text{CMB}} = k_m(T(r_c, t))$ . As  
 190  $E_{\text{CMB}} = \rho_c V_c C_c \Delta T$  where  $V_c$  is the total volume of the core and  $\Delta T$  is change in tem-  
 191 perature, the change in the core temperature in one time increment ( $\Delta T_c$ ) is:

$$\Delta T_c = \frac{A_c k_{\text{CMB}} \left. \frac{\partial T}{\partial r} \right|_{r=r_c} \delta t}{\rho_c C_c V_c} = \frac{3k_{\text{CMB}} \left. \frac{\partial T}{\partial r} \right|_{r=r_c} \delta t}{\rho_c C_c r_c}. \quad (4)$$

192 The temperature at the base of the mantle is then updated by adding  $\Delta T$  to the tem-  
 193 perature at the previous timestep:

$$T_{\text{CMB}}(r_c, t) = T_{\text{CMB}}(r_c, t - \delta t) + \Delta T_c. \quad (5)$$

194 The core cools as the mantle conducts heat to the surface, and is assumed to solidify when  
 195  $T_c$  reaches the melting temperature of the FeS core ( $T_1$ , in this case  $T_1 = 1200$  K; Bryson  
 196 et al., 2015). Once the core begins to freeze, the temperature is constant at  $T_1$  as latent  
 197 heat is extracted across the CMB. The liquid and solid fraction act identically during  
 198 this process and partitioning of elements is not addressed during freezing. The core so-  
 199 lidifies entirely once the total latent heat associated with crystallisation has been extracted  
 200 — when  $E_{\text{CMB}}$  during the solidification period exceeds  $E_l$ , where the total latent heat  
 201 of the core is:

$$E_l = m_c L_c = \frac{4}{3} \pi r_c^3 \rho_c L_c, \quad (6)$$

202 where  $m_c$  is the mass of the core and  $L_c$  the specific latent heat of fusion of the core (Bryson  
 203 et al., 2015; Tarduno et al., 2012).

## 204 2.1 Numerical Implementation

205 We solve the conduction equation numerically for the mantle using an explicit fi-  
 206 nite difference scheme with first order differences in time and second order in space. Equa-  
 207 tion 1 can be rewritten with the temperature at radius  $r$  and time  $t$  denoted by  $T_r^t$ :

$$T_r^t = T_r^{t-\delta t} + \frac{1}{\rho C} \delta t \times \left( \underbrace{\left. \frac{dk}{dT} \right|_r^{t-\delta t} \frac{(T_{r+\delta r}^{t-\delta t} - T_{r-\delta r}^{t-\delta t})^2}{4\delta r^2}}_{\text{non-linear term}} + \overbrace{\frac{k}{r\delta r} (T_{r+\delta r}^{t-\delta t} - T_{r-\delta r}^{t-\delta t})}^{\text{geometric term}} + \underbrace{\frac{k}{\delta r^2} (T_{r+\delta r}^{t-\delta t} - 2T_r^{t-\delta t} + T_{r-\delta r}^{t-\delta t})}_{\text{linear term}} \right), \quad (7)$$

208 where  $\delta t$  and  $\delta r$  are the constant timestep and radius step, and  $k$  is evaluated at  $T_r^{t-\delta t}$ .  
 209 A consequence of this discretisation is that temperature dependent properties lag if eval-  
 210 uated at  $t - \delta t$ . A more accurate method is to evaluate  $k$  as:

$$k^t = k^{t-\delta t} + \left( \frac{\partial k}{\partial T} \right)^{t-\delta t} (T^{t-\delta t} - T^{t-2\delta t}), \quad (8)$$

211 and similarly for  $C$  and  $\rho$  (Özısık, 1993). To reduce the error associated with variable  
 212  $k$  not being centred in time, we chose a sufficiently small  $\delta t$  such that  $k(T_r^{t-\delta t}) \approx k(T_r^t)$ ,  
 213 within a defined error ( $< 1\%$  of  $k$ ). We compared this with a selection of runs using the  
 214 more accurate but computationally expensive method above for  $k^t$  and  $C\rho^t$ , and the dif-  
 215 ferences in results were negligible.

216 The maximum timestep allowable for stability in the Forward-Time Central-Space  
 217 (FTCS) scheme must satisfy Von Neumann stability criteria in 1D:  $\frac{\kappa\delta t}{\delta r^2} \leq \frac{1}{2}$ , with the  
 218 largest diffusivity of the scheme being chosen for the most restrictive conditions (Crank  
 219 & Nicolson, 1947; Charney et al., 1950). For a constant spatial grid with  $\delta r = 1000$  m,  
 220  $\delta t = 1 \times 10^{11}$  s was sufficient to meet this criterion for the most restrictive cases with  
 221 large  $\kappa$ . An adaptive grid was not used due to the first-order nature of the problem be-  
 222 ing addressed.

223 In order to assess accuracy, this numerical solution, with constant  $k$ ,  $C$  and  $\rho$ , was  
 224 compared to the analytical solution for a sphere given by equation 6.18 in Crank (1979)  
 225 with an initial uniform temperature  $T_i$  and a constant surface temperature  $T_s$ :

$$\frac{T - T_i}{T_s - T_i} = 1 + \frac{2r_p}{\pi r} \sum_{n=1}^{\infty} \frac{(-1)^n}{n} \sin \frac{n\pi r}{r_p} \exp(-\kappa n^2 \pi^2 t / r_p^2) \quad (9)$$

226 where  $r = 0$  at the centre of the sphere and  $\kappa$  is a constant diffusivity, given by  $\kappa =$   
 227  $\frac{k}{\rho C}$  (see supplementary information). We also verified that we can reproduce the results  
 228 of Bryson et al. (2015) when using the same input parameters.

## 229 2.2 Meteorite formation depth

230 The FeNi portion of pallasite meteorites records the cooling rate of the sample at  
 231 800 K (J. Yang, Goldstein, & Scott, 2010). This measurement is intrinsic to the mete-  
 232 orite sample and independent of parent body modelling. For a given cooling model, the  
 233 intersection between the contour that matches the measured cooling rate of the mete-  
 234 orite sample and the 800 K isotherm gives a formation depth for pallasite material within  
 235 the planetesimal. Then, the time when this depth passes through the tetrataenite chem-  
 236 ical ordering temperature (593 K) and is magnetically recording can be compared to the  
 237 timing of core crystallisation to see if it occurs while the core is freezing, thus potentially  
 238 recording core dynamo activity (Bryson et al., 2015). To illustrate the implications of  
 239 this study on the pallasite parent body, we calculate the formation depths of two pal-  
 240 lasite meteorite samples, Imilac and Esquel, which have published cooling rates and rem-  
 241 nant magnetisation (Bryson et al., 2015; J. Yang, Goldstein, & Scott, 2010). We use the  
 242 cooling rates applied by Bryson et al. (2015), calculated from cloudy-zone particle size  
 243 (J. Yang, Goldstein, & Scott, 2010).

## 244 2.3 Parameter choices for the pallasite parent body

245 We selected parameters from previous models of planets, planetesimals and aster-  
 246 oids in the literature and experimental results from geochemistry and mineral physics  
 247 studies as detailed in Table 1. For many of these parameters, we have chosen both a ref-  
 248 erence value relevant to our example case of the pallasite parent body, and a range of  
 249 values used in other models of differentiated planetesimals with different assumptions  
 250 regarding geometry and composition. We have chosen a reference initial temperature that  
 251 ensures a solid mantle that conductively cools, and a reference surface temperature that  
 252 reflects the average mid-plane temperature of the circum-Solar disk at 2.5 AU, 1 Myr  
 253 after Solar System formation (Hevey & Sanders, 2006). Reference values related to the  
 254 megaregolith, the core and the boundary conditions are from Bryson et al. (2015), while  
 255 mantle olivine properties have been chosen from experimental results and other plan-  
 256 etesimal models (Su et al., 2018; Xu et al., 2004, see Table 1 for further citations). We  
 257 have chosen  $r_p = 250$  km as our reference value so that paleomagnetic recording oc-  
 258 curs while the core is crystallising for both samples (sections 2.2 and 3).

259 Initially, we allowed models to run for 400 million years. We increased the run time  
 260 if it did not capture the period of core solidification, for example in cases with larger radii.  
 261 The core reverts to an isothermal state following the solidification period. This simpli-

**Table 1.** *Model Parameters.*

Symbol	Parameter	Value(s)	Units
$r_p$	Planetesimal radius	<b>250</b> , 150 – 600 <sup>b,d,s</sup>	km
$r_c$	Core radius	<b>50</b> <sup>b,s</sup> , 20 – 80 <sup>q</sup>	% of $r_p$
$d_{\text{reg}}$	Megaregolith thickness	<b>8</b> <sup>b</sup> , 0 – 20 <sup>i,t</sup>	km
$k$	Mantle conductivity	<b>3</b> <sup>b</sup> , 1.5 – 4 <sup>e,w,aa</sup>	W m <sup>-1</sup> K <sup>-1</sup>
$C$	Mantle heat capacity	<b>819</b> <sup>r</sup> , 600 – 2000 <sup>h,k,n,o,s</sup>	J kg <sup>-1</sup> K <sup>-1</sup>
$\rho$	Mantle density	<b>3341</b> <sup>r</sup> , 2500 – 3560 <sup>l,m,y</sup>	kg m <sup>-3</sup>
$C_c$	Core heat capacity	<b>850</b> <sup>p,z</sup> , 780 – 850 <sup>c,u</sup>	J kg <sup>-1</sup> K <sup>-1</sup>
$\rho_c$	Core density	<b>7800</b> <sup>o</sup> , 7011 – 7800 <sup>c,l,p,u</sup>	kg m <sup>-3</sup>
$\kappa_{\text{reg}}$	Megaregolith diffusivity	<b>5</b> × 10 <sup>-7</sup> <sup>b</sup>	m <sup>2</sup> s <sup>-1</sup>
$L_c$	Latent heat of fusion of core	<b>2.7</b> × 10 <sup>5</sup> <sup>g,o</sup> , 2.56 × 10 <sup>5</sup> <sup>p</sup>	J kg <sup>-1</sup>
$T_1$	Freezing temperature of core	<b>1200</b> <sup>b</sup> , 1213 <sup>g,o,s</sup>	K
$T_{\text{init}}$	Initial temperature	<b>1600</b> <sup>b</sup> , 1450 – 1820 <sup>o,p</sup>	K
$T_{\text{surf}}$	Surface temperature	<b>250</b> <sup>j,v</sup> , 150 – 300 <sup>a,f,o</sup>	K
$T_{\text{cz}}$	Tetrataenite formation temp.	593 <sup>b</sup>	K
$T_{\text{cr}}$	Cooling-rate temperature	800 <sup>b,x</sup>	K
$\delta t$	Timestep	1 × 10 <sup>11</sup>	s
$\delta r$	Radial step	1000	m

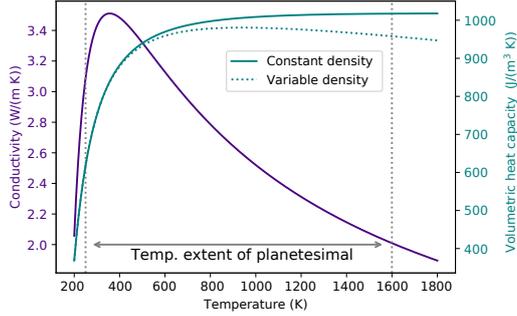
*Note:* Reference values in **bold**. <sup>a</sup> Boss (1998), <sup>b</sup> Bryson et al. (2015), <sup>c</sup> Davies and Pommier (2018), <sup>d</sup> The OSIRIS-REx Team et al. (2019), <sup>e</sup> Elkins-Tanton et al. (2011), <sup>f</sup> Gail et al. (2014), <sup>g</sup> Ghosh and McSween (1998), <sup>h</sup> Ghosh and McSween (1999), <sup>i</sup> Haack et al. (1990), <sup>j</sup> Hevey and Sanders (2006), <sup>k</sup> Hort (1997), <sup>l</sup> Johnson et al. (2019), <sup>m</sup> Miyamoto et al. (1982), <sup>n</sup> Robie et al. (1982), <sup>o</sup> Sahijpal et al. (2007), <sup>p</sup> Scheinberg et al. (2016), <sup>q</sup> Solomon (1979), <sup>r</sup> Su et al. (2018), <sup>s</sup> Tarduno et al. (2012), <sup>t</sup> Warren (2011), <sup>u</sup> Williams and Nimmo (2004), <sup>v</sup> Woolum and Cassen (1999), <sup>w</sup> Xu et al. (2004), <sup>x</sup> C. W. Yang et al. (1997), <sup>y</sup> Yomogida and Matsui (1983), <sup>z</sup> Young (1991), <sup>aa</sup> Zhang et al. (2019).

262 fined approximation of a highly-conductive metallic core is sufficient for the example ap-  
 263 plication in this study, for which the post core-solidification period is not of interest.

#### 264 **2.4 Incorporation of temperature dependent properties**

265 In solids at low temperatures ( $T < \theta_D$ , the Debye temperature), heat capacity  
 266 increases from zero at 0 K as  $C_v \sim AT^3$ , where  $C_v$  is specific heat capacity at a con-  
 267 stant volume and  $A$  is a constant (Debye, 1912). At high temperatures ( $T > \theta_D$ ), heat  
 268 capacity is weakly dependent on temperature and can be approximated with a constant  
 269 value (Petit & Dulong, 1819). This results in approximately 30 % increase in  $C$  in olivine  
 270 over the temperature range commonly modelled for planetesimals (Figure 2).

271 In electrically insulating solids such as mantle silicates, heat is primarily transferred  
 272 through lattice or phonon conduction. As temperature increases, the mean energy per  
 273 phonon also increases due to the change in phonon specific heat. At lower temperatures  
 274 ( $T < \theta_D$ ), the inelastic phonon relaxation time is constant as scattering is primarily  
 275 due to crystal defects or boundaries. This results in  $k \propto T^3$  due to the  $T$ -dependence  
 276 of  $C$  (Hofmeister, 1999; Poirier, 2000). When phonon momentum exceeds a threshold  
 277 at high temperatures, phonon–phonon Umklapp scattering acts to reduce  $k$ , producing



**Figure 2.** Temperature dependent material properties of olivine. Temperature extent shown for the reference case (Table 1). As the temperature dependence of density ( $\rho$ ) is small, heat capacity ( $C$ ) and density are combined as volumetric heat capacity and are shown with a constant and  $T$ -dependent  $\rho$  to highlight the effect; both are divided by the value of the constant density,  $\rho_0 = 3341 \text{ kg m}^{-3}$ . These experimental functions are discussed further in section 2. Data from: Fei (2013); Robie et al. (1982); Su et al. (2018); Suzuki (1975); Xu et al. (2004).

278 a  $k \propto \frac{1}{T}$  dependency (Poirier, 2000). This non-monotonic behaviour is illustrated for  
 279 olivine in Figure 2.

280 A change in density with temperature can be linked to thermal expansion by the  
 281 coefficient of expansivity,  $\alpha$ :  $\rho = \rho_0 - \alpha\rho_0(T - T_0)$ , where  $\rho_0$  is a reference density at  
 282  $T_0$ , commonly room temperature ( $\sim 295 \text{ K}$ ). Density is less temperature dependent than  
 283  $C$  or  $k$ , and is combined with heat capacity in Figure 2 as volumetric heat capacity, both  
 284 as a constant and as a  $T$ -dependent function to illustrate the scale of its effect.

285 In order to fully understand the effect of including temperature dependence in our  
 286 model, we constructed a simple linear function for conductivity before investigating the  
 287 more complex equation based on experimental results (Equation 14):

$$k = k_0 + \beta T, \quad (10)$$

288 where  $k_0$  is a reference conductivity at 0 K and  $\beta$  controls the temperature dependence,  
 289 and can be set as positive or negative.  $\beta$  and  $k_0$  must be chosen such that  $k$  does not  
 290 become negative over the temperatures explored in the body. In order to contrast a  $T$ -  
 291 dependent conductivity with simply setting the average conductivity higher or lower, func-  
 292 tions with both positive and negative  $\beta$  were chosen to approximate the same mean con-  
 293 ductivity over radius and time. Additionally, the cases were run with and without the  
 294 non-linear term. Both  $\rho$  and  $C$  were held constant to isolate the effect of the conduc-  
 295 tivity. The megaregolith layer maintains a constant  $\kappa$  for all model runs including those  
 296 with fully variable  $k$ ,  $\rho$  and  $C$ , as after initial rapid equilibration with the surface tem-  
 297 perature, this layer has a constant temperature. The core properties have also been kept  
 298 constant.

299 For this study, we have chosen the function used for heat capacity in olivine from  
 300 Su et al. (2018), based on lattice vibration theory from Berman and Brown (1985) and  
 301 fit to experimental data from Isaak (1992):

$$C = 995.1 + \frac{1343}{\sqrt{T}} - \frac{2.887 \times 10^7}{T^2} - \frac{6.166 \times 10^2}{T^3}. \quad (11)$$

302 Note that this is valid for the range of temperatures  $T_{\text{surf}} - T_{\text{init}}$ . We do not explore tem-  
 303 peratures close to 0 K. The expression for thermal expansivity is also taken from Su et  
 304 al. (2018) based on the functional fit by Fei (2013) and using experimental data from Suzuki  
 305 (1975):

$$\alpha = 3.304 \times 10^{-5} + 0.742 \times 10^{-8}T - 0.538T^{-2}. \quad (12)$$

306 We then use  $\alpha$  to calculate the change in density with temperature:  $\rho = \rho_0 - \alpha\rho_0(T -$   
 307  $T_0)$ , where  $T_0 = 295$  K and  $\rho_0 = 3341$  kg m $^{-3}$ .

308 As the lower temperatures modelled ( $\sim 250$  K) are rarely of interest in terrestrial  
 309 mineral physics and are less accessible to experimental studies, we constructed a sim-  
 310 ple conductivity function for olivine spanning 250 – 1800 K. As discussed above, con-  
 311 ductivity is controlled by different processes at high and low temperatures, resulting in  
 312 different temperature dependencies. For the high- $T$  region, we used the experimentally-  
 313 derived curve from Xu et al. (2004):

$$k = 4.13 \times \left(\frac{298}{T}\right)^{\frac{1}{2}} \times (1 + aP), \quad (13)$$

314 where  $a = 0.032$  GPa $^{-1}$  (experimentally derived) and  $P = 4$  GPa. As  $T$ -dependence  
 315 of  $k$  at temperatures  $\ll \theta_D$  is similar to that of  $C$ , a function identical in shape to equa-  
 316 tion 11 but normalised such that  $C = 1$  at  $T > \theta_D$  was used for the low- $T$  region. As  
 317 this low- $T$  curve is constant and equal to 1 above  $\theta_D$ , it can be multiplied by equation  
 318 13 to fill in the low- $T$  region without altering the higher- $T$  experimental results. Our re-  
 319 sultant function is differentiable and non-monotonic:

$$k = 80.421 \times \left(1.319 \times T^{-\frac{1}{2}} + 0.978 - \frac{28361.765}{T^2} - \frac{6.057 \times 10^{-5}}{T^3}\right) \times T^{-\frac{1}{2}}, \quad (14)$$

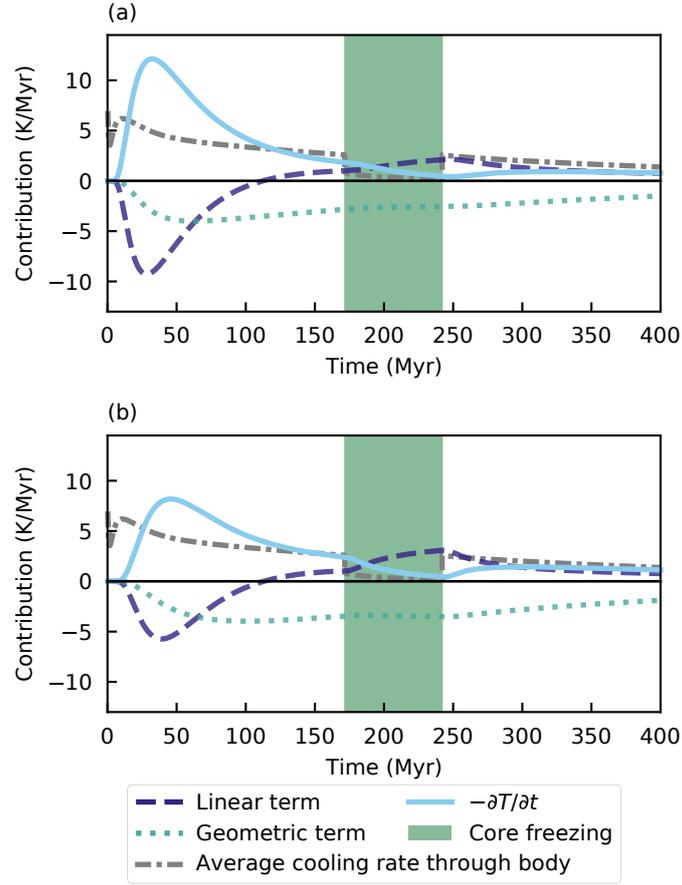
320 While the pressures inside the planetesimal are  $\ll 4$  GPa, changing pressure to  $< 1$  GPa  
 321 in equation (13) increases conductivity in our composite function by  $< 0.3$  W m $^{-1}$  K $^{-1}$  at  
 322 all temperatures. As this is outside of the calibration range of the experiments by Xu  
 323 et al. (2004) we have chosen not to include this adjustment as it may not be physically  
 324 realistic and pressure effects are not the focus of this study, and instead use  $a$  and  $P$  as  
 325 quoted by Xu et al. (2004). These functions are illustrated in Figure 2.

### 326 3 Results

327 The model produces arrays of temperature and cooling rate through time and radi-  
 328 us. For any radius  $r$ , the linear, geometric and non-linear (if applicable) terms of the  
 329 heat conduction equation can be plotted against time. Model outputs that are impor-  
 330 tant to the interpretation of meteorites include the initiation and duration of core crys-  
 331 tallisation, the depth within the parent body from which the meteorite was derived and  
 332 when this occurred, and the peak cooling rates reached. In the specific case of the pal-  
 333 lasite parent body, the calculated depth of formation can then be tracked to see if this  
 334 region of the parent body passes through the temperature where magnetism is recorded  
 335 while the core is solidifying, thus potentially recording core dynamo activity.

#### 336 3.1 Constant $k$ , $\rho$ and $C$

337 The model was run with constant  $k$ ,  $\rho$  and  $C$  for both the reference parameters in  
 338 Table 1 and the end-member values quoted, if applicable. In addition, parameters were  
 339 varied by  $\pm 10$  % of the reference value to gauge the sensitivity of the model to differ-  
 340 ent inputs. The full results of these parameter explorations are tabulated in the supple-  
 341 mentary information.



**Figure 3.** Results for the reference case with constant  $k$ ,  $\rho$  and  $C$ . The components of the heat conduction equation are shown at a depth of (a) 42 km (one third of the thickness of the mantle) and (b) 84 km (two thirds). The cooling rate is multiplied by  $-1$  to illustrate how it balances the other components to add to zero. The shaded green area defines the period of core crystallisation.

**Table 2.** *Model results for constant  $k$ ,  $\rho$  and  $C$* 

Varied parameter	Value	Core starts Myr	Core ends Myr	Duration Myr	Esquel depth km	Imilac depth km
Reference case		172	242	70	64	57
$r_p + 10\%$	275 km	210	296	86	64	56
$r_c + 10\%$	138 km	167	241	74	58	53
$r_{\text{reg}} + 1 \text{ km}^{\text{a}}$	9 km	172	242	71	64	57
$k + 10\%$	$3.3 \text{ W m}^{-1} \text{ K}^{-1}$	157	221	64	68	60
$C + 10\%^{\text{b}}$	$901 \text{ J kg}^{-1} \text{ K}^{-1}$	180	252	72	61	54
$k_{\text{max}}$	$4 \text{ W m}^{-1} \text{ K}^{-1}$	132	185	53	77	67
$k_{\text{min}}$	$1.5 \text{ W m}^{-1} \text{ K}^{-1}$	330	400	70	42	36

*Note:* Model results with parameters varied to  $\pm 10\%$  of the default value, with endmember cases included for  $k$ . References for parameter choices given in Table 1. <sup>a</sup>Megaregolith thickness was increased and decreased by 1 km as 10 % (0.8 km) is smaller than  $\delta r$ .

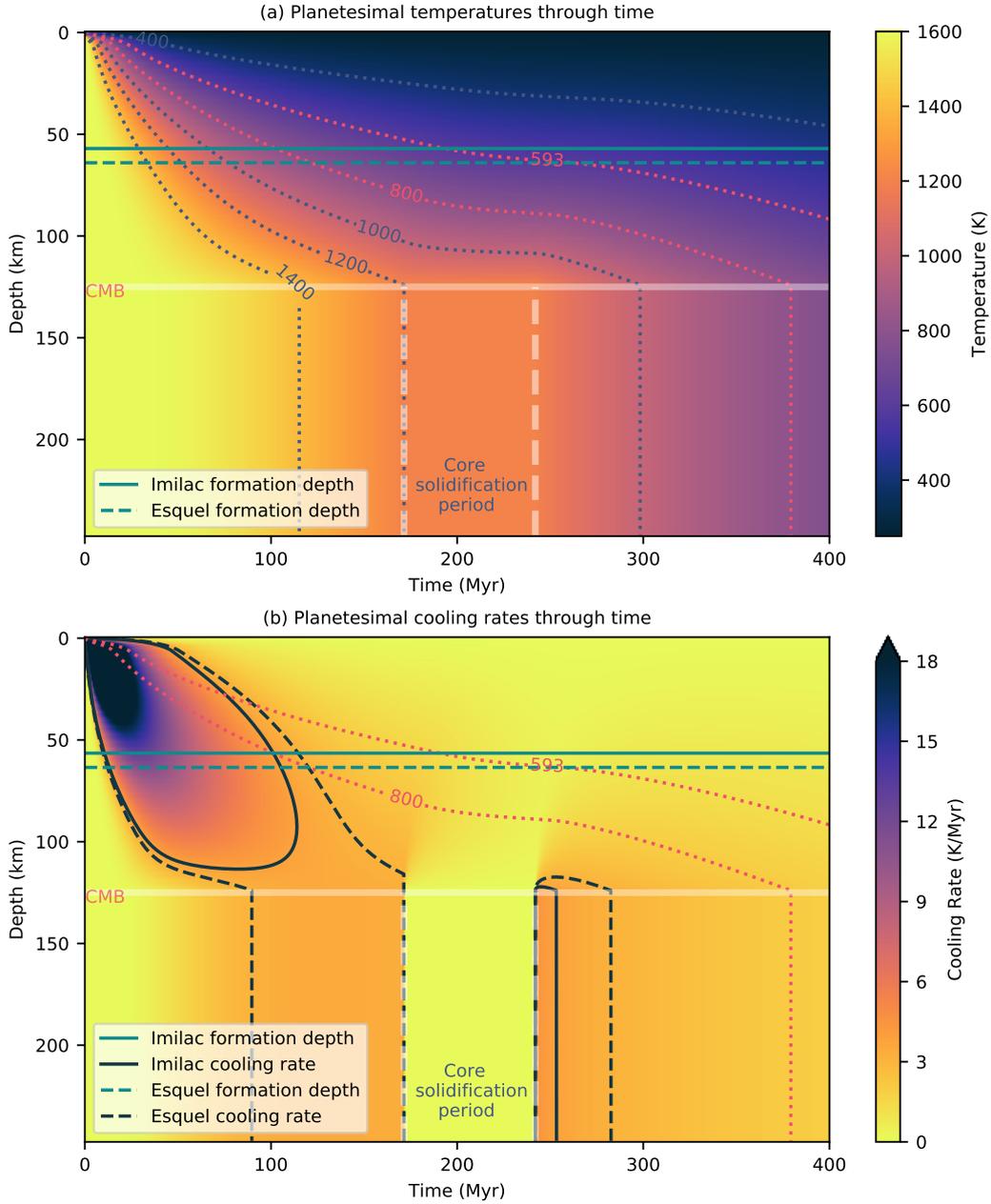
<sup>b</sup>Increasing or decreasing  $C$  or  $\rho$  (not both) by 10 % results in a change in  $\rho C$  by 10 %. Full results in supplementary information.

342 Figure 3 shows the chosen reference case for the constant  $k$ ,  $\rho$  and  $C$ . The linear  
343 term initially dominates the cooling, especially in the shallower regions of the body where  
344 there is lower curvature (Figure 3a); the geometric term that accounts for the body’s spher-  
345 ical geometry is of more relative importance deeper within the body at smaller radii (Fig-  
346 ure 3b). Peak cooling rates are higher and are reached marginally earlier in the shallow  
347 portion of the body, as the near-surface rapidly equilibrates with the boundary held at  
348 250 K while the temperature anomaly propagates through the mantle to deeper regions  
349 with a time delay determined by the diffusion timescale.

350 The slope of  $T(r)$  from the base of the mantle to the surface is negative for the du-  
351 ration of the model run. Initially,  $T(r)$  is convex upwards but flattens over time and be-  
352 comes convex downwards as the linear term changes sign: initially within the body  $\frac{\partial^2 T}{\partial r^2}$   
353 is negative for all radii and increases with time, becoming positive at the boundaries first,  
354 with this change in sign propagating towards the middle of the mantle. When the core  
355 is removed to approximate a solid sphere, this effect is only seen to propagate downwards  
356 from the surface boundary as the breaking effect of the core on the cooling of the man-  
357 tle is not present. The geometric term then drives further cooling after this point (Fig-  
358 ure 3).

359 When the core reaches 1200 K and begins to freeze, the temperature at the CMB  
360 is held constant. The fixed core temperature reduces the cooling rate in the mantle sharply;  
361 in the deeper regions of the mantle  $-\frac{\partial T}{\partial t}$  drops towards zero as the mantle reaches the  
362 same temperature as the core. The effect is less pronounced in the shallow regions as the  
363 cooling rate has already slowed significantly and is approaching zero.

364 The body cools rapidly at the surface, with shallow depths quickly equilibrating  
365 with the constant surface temperature (Figure 4). High temperatures are maintained for  
366 longer deeper within the body due to the overlying insulating mantle. Using the cool-  
367 ing rates applied by Bryson et al. (2015), calculated from cloudy-zone particle size (J. Yang,  
368 Goldstein, & Scott, 2010) we calculated source depths of 64 km for Esquel and 57 km  
369 for Imilac, approximately midway through the mantle (Figure 4 and Table 2).



**Figure 4.** Planetesimal (a) temperatures and (b) cooling rates through time for the default model with constant  $k$ ,  $\rho$  and  $C$ . The calculated source depth of the Imilac and Esquel meteorites for this model set-up are shown in both plots, using the cooling rates applied by Bryson et al. (2015), calculated from cloudy-zone particle size (J. Yang, Goldstein, & Scott, 2010). Temperature contours highlight the tetrataenite formation temperature when paleomagnetism can be recorded (593 K) and the temperature for which the sample’s cooling rates were measured (800 K), while cooling rate contours show the measured cooling rates for both samples.

370 The geometry of the body is a strong controlling factor on the cooling rate and tim-  
 371 ing of core crystallisation (Table 2). The planetary radius has the largest effect: increas-  
 372 ing the total radius by 10 % slows the cooling of the planetesimal at depth and delays  
 373 the onset of core crystallisation by 38 Myr. When the core fraction is increased by 10  
 374 %, the core begins to freeze 5 Myr earlier as there is less insulating mantle, but takes  
 375 4 Myr longer to freeze fully due to its increased size. While the average cooling rate of  
 376 the body drops sharply for all cases on initiation of core solidification, the effect is more  
 377 pronounced when the core fraction is increased as the cooling rate of the core dominates  
 378 the overall cooling rate. Increasing the insulating megaregolith thickness by 1 km while  
 379 maintaining a 250 km total radius does not delay the onset of core crystallisation, but  
 380 does increase the duration of the solidification period by 1 Myr. Increasing the megareg-  
 381 olith thickness further does delay core solidification, with a 20 km thick megaregolith  
 382 causing a 73 Myr delay when compared to the reference case (see supplementary infor-  
 383 mation). The resulting changes in the calculated source region depth for pallasite me-  
 384 teorites is also shown in Table 2.

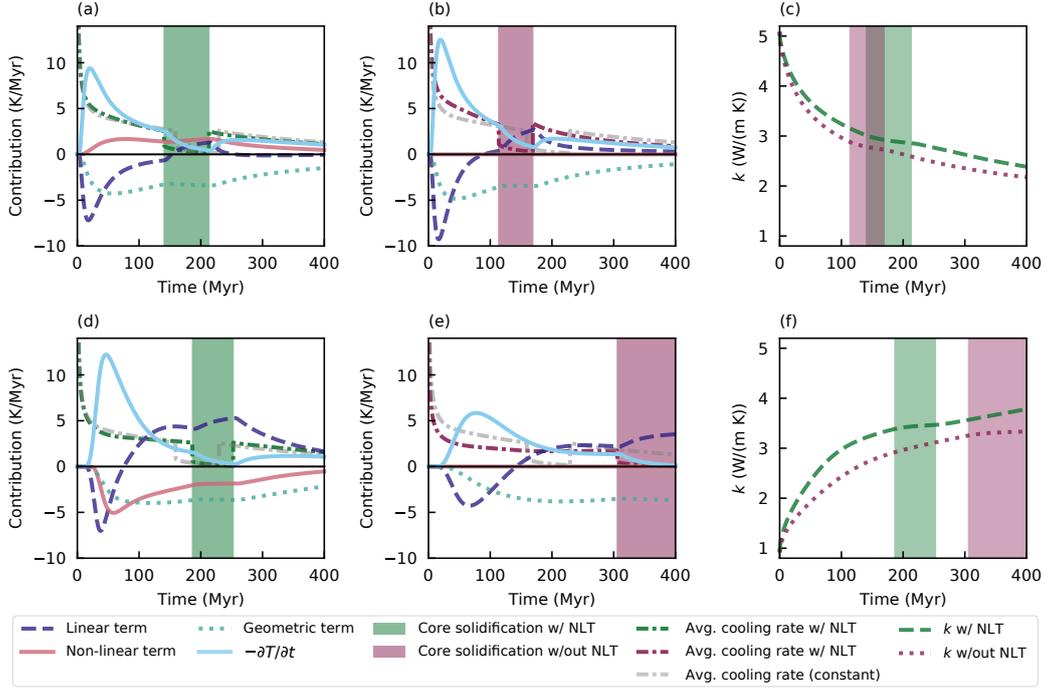
385 Increasing  $k$  by 10 % accelerates the cooling in the body, causing the core to be-  
 386 gin solidifying 15 Myr earlier. Increasing  $\rho$  or  $C$  by 10 % has the opposite effect, and de-  
 387 lays the onset of core crystallisation by 8 Myr. Table 2 also shows the results of setting  
 388  $k = 4 \text{ W m}^{-1} \text{ K}^{-1}$  and  $1 \text{ W m}^{-1} \text{ K}^{-1}$ , which reflect the end-member expected values  
 389 if  $k$  varied with  $T$  (see Figure 2). Between these two cases, there is a 198 Myr difference  
 390 in the timing of the start of core solidification. The core begins to freeze at 132 Myr and  
 391 the freezing period lasts 53 Myr when  $k = 4 \text{ W m}^{-1} \text{ K}^{-1}$ , while the core begins to freeze  
 392 at 330 Myr when  $k = 1 \text{ W m}^{-1} \text{ K}^{-1}$ . An increase in conductivity results in deeper source  
 393 regions for the pallasite meteorites, with the Esquel and Imilac source regions moving  
 394 13 and 10 km deeper respectively when  $k = 4 \text{ W m}^{-1} \text{ K}^{-1}$ , while both move  $\sim 22$  km  
 395 shallower when  $k = 1 \text{ W m}^{-1} \text{ K}^{-1}$ .

### 3.2 Simple linear $T$ -dependent conductivity

396  
 397 In this section we explore  $k(T)$  in the form  $k = k_0 + (\beta T)$  with  $\rho$  and  $C$  held con-  
 398 stant. For the examples shown in Figure 5 and summarised in Table 3, we chose  $\beta =$   
 399  $\pm 0.0025 \text{ W m}^{-1} \text{ K}^{-2}$  and  $k_0$  such that  $k = 3.0 \text{ W m}^{-1} \text{ K}^{-1}$  at the mean temperature  
 400 of the reference case with constant  $k$ ,  $\rho$  and  $C$  (with megaregolith thickness set to 0 km  
 401 - Table 3) to isolate the effect of  $T$ -dependence. The model was run both with and with-  
 402 out the non-linear term in Figures 5a and 5b. When compared to the constant case with  
 403  $k = 3 \text{ W m}^{-1} \text{ K}^{-1}$ , allowing  $k$  to vary with  $T$  changes the timing and duration of the  
 404 core crystallisation period (see Table 3). For  $\beta = 0.0025 \text{ W m}^{-1} \text{ K}^{-2}$  and  $k_0 = 1.1125$   
 405  $\text{ W m}^{-1} \text{ K}^{-1}$  (panel (a), Figure 5), the onset of core crystallisation is 19 Myr earlier than  
 406 for the constant case (table 3); in the early stages of the model run the average cooling  
 407 rate throughout the body is higher than the constant case due to higher initial conduc-  
 408 tivity in the mantle (panel (c) of Figure 5). After  $\sim 80$  Myr (before the core begins to  
 409 freeze), the average cooling rate throughout the body drops below the constant case, re-  
 410 sulting in a 3 Myr longer core-crystallisation period. The duration of core crystallisa-  
 411 tion is close to that of the constant case as, during this time period, the variable con-  
 412 ductivity is similar to the fixed conductivity of the constant case (panel (c), Figure 3).

413 When the non-linear term is neglected (panel (b), Figure 5), core crystallisation  
 414 initiates 46 Myr earlier than in the constant reference case, due to increased cooling rates  
 415 despite a lower average conductivity. The non-linear term is always positive and slows  
 416 cooling if  $\beta > 0$ , reducing the peak cooling rates experienced at this depth and the av-  
 417 erage cooling rates in the mantle.

418 The equivalent results for  $\beta = -0.0025$  are shown in panels (d), (e) and (f) of Fig-  
 419 ure 5 and in Table 3. For  $\beta = -0.0025 \text{ W m}^{-1} \text{ K}^{-2}$  and  $k_0 = 4.8875$ , the onset of core  
 420 solidification is delayed by 27 Myr and the period of core crystallisation is 4 Myr shorter



**Figure 5.** Results for model with a linear function for  $k(T)$  and constant  $\rho C$ . Panels (a), (b) and (c) show results for  $\beta = 0.0025$ . Panels (a) and (b) show the components of the heat equation with and without the non-linear term (NLT), with the cooling rate averaged across all radii included and compared to the reference case with 9 km megaregolith. Panel (c) shows the average conductivity through time for both these cases with the core crystallisation period highlighted. Panels (d), (e) and (f) show the equivalent results for  $\beta = -0.0025$ .

**Table 3.** *Simple linear function for conductivity*

Model	Slope $\beta$	Reference $k_0$	Average	Core starts	Duration of
	$\text{W m}^{-1} \text{K}^{-2}$	$\text{W m}^{-1} \text{K}^{-1}$	mantle $k$	solidifying	solidification
			$\text{W m}^{-1} \text{K}^{-1}$	Myr	Myr
Constant case	0.00	3.00	3.00	159.24 <sup>a</sup>	70.17 <sup>a</sup>
Positive $\beta$	0.0025	1.1125	3.02	140.52	72.79
Positive $\beta$ without non-linear term	0.0025	1.1125	2.77	113.62	55.40
Negative $\beta$	-0.0025	4.8875	3.16	186.37	66.11
Negative $\beta$ without non-linear term	-0.0025	4.8875	2.76	305.73	94.27

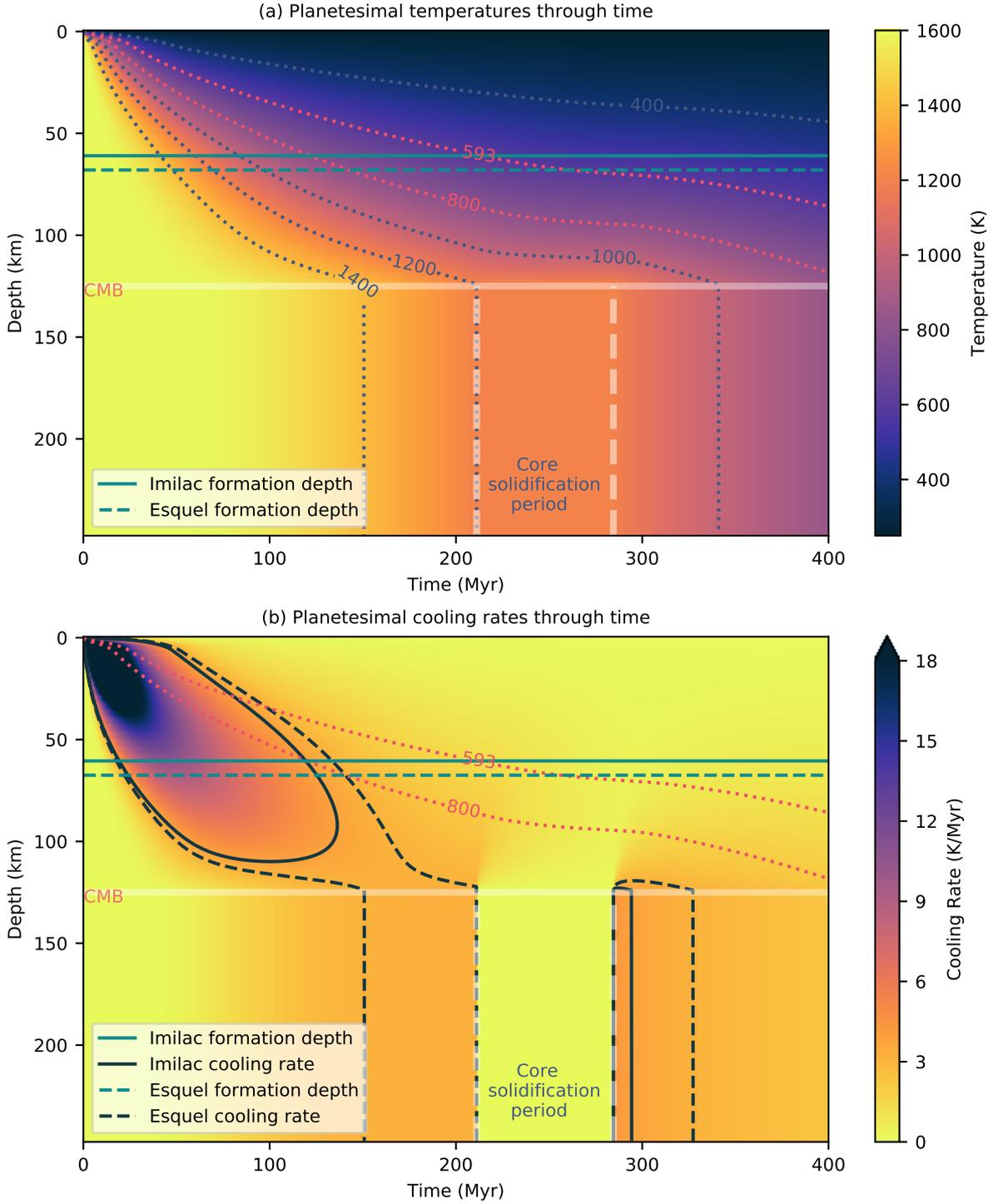
*Note:* Model results with a linear function for  $k$ . Megaregolith thickness is set to 0 km in all cases. <sup>a</sup>As megaregolith is not included, note the earlier solidification than for the reference case with 8 km megaregolith, where the core starts solidifying at 171.58 Myr and the solidification period lasts 70.43 Myr.

421 than for the constant case due to the increasing conductivity of the mantle with time.  
422 The non-linear term in this case is negative, owing to the negative sign of  $\frac{dK}{dt}$ , and it am-  
423 plifies the initial peak cooling rates at the depth examined (panel (d), Figure 5); how-  
424 ever, the overall average cooling rate of the body is initially lower due to the low con-  
425 ductivity (Figure 5f). When the non-linear term is neglected, the core begins to solidify  
426 146 Myr later than in the constant case, and solidification takes 24 Myr longer. As the  
427 core does not freeze at the midpoint between the initial and surface temperatures, the  
428 non-linear terms for positive and negative  $\beta$  are not symmetric.

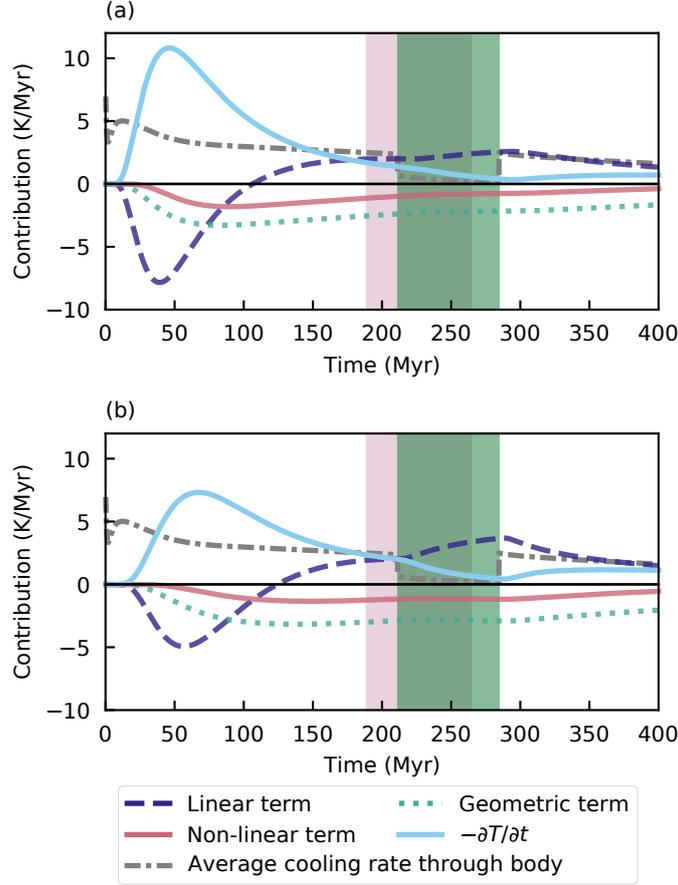
429 In summary, positive  $\beta$  leads to earlier onset of core freezing and a longer duration  
430 of core freezing, while negative  $\beta$  results in later onset of freezing and a shorter freez-  
431 ing period. For both  $\pm\beta$  the change in onset time when compared to the constant case  
432 is much larger than the change in the duration of core freezing, as there is a much greater  
433 difference between constant and variable  $k$  earlier in the model than during core solid-  
434 ification (Figures 5c, 5d). Even for linear conductivity functions with shallow slopes, the  
435 conductivity structure of the mantle is very different to that of the constant case and  
436 the temporal dependence of this structure has implications for the timing of events within  
437 the body that cannot be approximated by changing the value of  $k$  in the constant case.  
438 Inclusion of the non-linear term is essential as neglecting it can result in large over- or  
439 underestimations of core crystallisation onset time (for negative  $\beta$ , neglecting the non-  
440 linear term results in 119 Myr delay in the onset of core crystallisation). The implica-  
441 tions of these results on the pallasite parent body are investigated using the experimen-  
442 tally derived functions in the next section.

### 443 3.3 Temperature-dependent properties: using experimental functions

444 The fully variable case, using the default parameters in Table 1 and the  $k(T)$ ,  $C(T)$   
445 and  $\rho(T)$  functions (equations 11, 12 and 14), resulted in a 40 Myr delay in the onset  
446 of core crystallisation but only 3 Myr longer period of core crystallisation when compared  
447 to the reference case with constant properties (Figure 6). The temperature distribution



**Figure 6.** Planetesimal (a) temperatures and (b) cooling rates through time for a model with  $T$ -dependent  $k$ ,  $\rho$  and  $C$ . The calculated source depth of the Imilac and Esquel meteorites for this model set-up are shown in both plots, using the cooling rates applied by Bryson et al. (2015), calculated from cloudy-zone particle size (J. Yang, Goldstein, & Scott, 2010). Temperature contours highlight the tetrataenite formation temperature when paleomagnetism can be recorded (593 K) and the temperature that corresponds to the sample’s measured cooling rates (800 K), while cooling rate contours show the measured cooling rates for both samples.



**Figure 7.** Results for the reference case with  $T$ -dependent  $k$ ,  $\rho$  and  $C$ . The components of the heat conduction equation are shown at a depth of (a) 42 km (one third of the thickness of the mantle) and (b) 84 km (two thirds). The cooling rate is multiplied by  $-1$  to illustrate how it balances the other components to add to zero. The green area defines the period of core crystallisation when  $T$ -dependent properties are used, while the pink area highlights the period of core crystallisation from the mean constant case for comparison.

448 in the shallow mantle is similar to that of the constant reference case, but the interior  
 449 stays hotter for longer when  $T$ -dependent properties are used (Figure 6). The fully vari-  
 450 able case requires deeper source regions for the pallasite meteorite samples than the refer-  
 451 ence case, with a depth of 61 km calculated for Imilac and 68 km for Esquel (Table  
 452 4).

453 When discussing simple linear functions for  $k(T)$ , we have demonstrated that cases  
 454 with constant and variable properties should be correctly calibrated in order to make mean-  
 455 ingful comparisons. In order to do so, we measured the average temperature in the man-  
 456 tle of the fully variable case and used this to calculate new constant values of  $k$ ,  $C$  and  
 457  $\rho$  using equations 11, 12 and 14. The mean temperature of the mantle over the 400 Myr  
 458 of the model lifetime was 780 K, giving  $k = 2.8 \text{ W m}^{-1} \text{ K}^{-1}$ ,  $\rho = 2945 \text{ kg m}^{-3}$  and  
 459  $C = 996 \text{ J kg}^{-1} \text{ K}^{-1}$ . The model with constant properties was then rerun with these  
 460 updated values for  $k$ ,  $\rho$  and  $C$ , to more closely approximate the results from the fully  
 461 variable model. In this section, this new model using updated constant  $k$ ,  $\rho$  and  $C$  is  
 462 referred to as the constant mean values case, and the results are shown in Table 4.

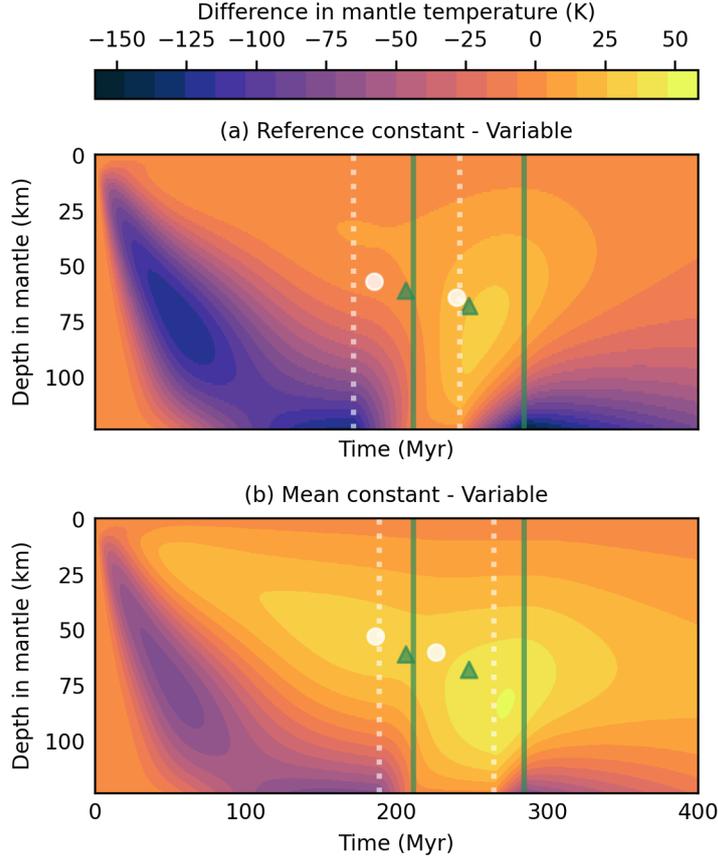
**Table 4.** Variable  $k$ ,  $\rho$  and  $C$ .

Model	Core	Core	Imilac	Esquel	Imilac	Esquel
	Starts	Stops	depth	depth	timing	timing
	Myr	Myr	km	km	Myr	Myr
Reference (constant $k, \rho, c$ ) <sup>a</sup>	172	242	57	64	185	240
Constant (mean $k, \rho, c$ ) <sup>b</sup>	189	265	53	60	186	226
Variable <sup>c</sup>	211	285	61	68	206	248
Variable (non-linear = 0) <sup>d</sup>	245	335	47	54	190	234
Variable conductivity <sup>e</sup>	200	272	64	71	206	260
Variable heat capacity <sup>e</sup>	190	266	53	60	186	226
Variable density <sup>e</sup>	198	276	50	57	185	224

*Note:* Summary of key results. Timing of core crystallisation period given in millions of years after model start (Myr) and formation depth of meteorites given in km. <sup>a</sup>Reference case with constant  $k = 3 \text{ W m}^{-1} \text{ K}^{-1}$ ,  $\rho = 3341 \text{ kg m}^{-3}$  and  $C = 819 \text{ J kg}^{-1} \text{ K}^{-1}$ . <sup>b</sup>Constant case here differs from the reference case: values for  $k$ ,  $\rho$  and  $C$  are calculated at the mean  $T$  in the fully variable case:  $k = 2.8 \text{ W m}^{-1} \text{ K}^{-1}$ ,  $\rho = 2945 \text{ kg m}^{-3}$ , and  $C = 996 \text{ J kg}^{-1} \text{ K}^{-1}$ . <sup>c</sup>Case with  $T$ -dependent  $k$ ,  $\rho$  and  $C$ . <sup>d</sup> $T$ -dependent properties, but with non-linear term neglected. <sup>e</sup>One property allowed to vary with  $T$  with other properties held at mean values as in <sup>b</sup>.

463 In the fully variable case (Figure 7), the non-linear term is negative and enhances  
464 the overall cooling rate at the depths displayed for all times shown (up to 400 Myr), as  
465 the slope of the function for  $k$  is negative for all  $T > 300 \text{ K}$  (Figure 2). A thin insu-  
466 lating layer in the shallow mantle forms where  $T < 300 \text{ K}$  and the non-linear term is  
467 positive. The core begins to freeze 211 Myr after model initiation, and takes 61 Myr to  
468 fully solidify. The constant mean values case does not replicate this result: with constant  
469  $k$ ,  $\rho$  and  $C$ , the core begins to solidify at 189 Myr and takes 53 Myr to fully freeze (Ta-  
470 ble 4). In addition, the constant mean values case requires shallower source regions for  
471 the pallasite meteorites Imilac and Esquel: 53 and 60 km respectively (Table 4). Qual-  
472 itatively, the fully variable case is similar to the case with linear  $k$  and negative  $\beta$  in sec-  
473 tion 3.2: the core begins to freeze later but takes a shorter time to fully crystallise than  
474 the constant mean values case (Tables 3 and 4). However, the insulating layer in the shal-  
475 low mantle with a positive non-linear term cannot be replicated by the simple linear case  
476 and so the fully variable case must be used for quantitative results. When the non-linear  
477 term is set to zero, again the fully variable model behaves similarly to the  $\beta < 0$  lin-  
478 ear case (Table 4).

479 When the different properties are allowed to vary in turn,  $T$ -dependent  $C$  produces  
480 the smallest deviation in core crystallisation timing from the constant mean values case,  
481 as at high  $T$  (temperatures such as those experienced by the planetesimals prior to and  
482 during core crystallisation),  $C$  is approximately constant (Figure 2). Including variable  
483  $\rho$  results in a 9 Myr delay in the onset and 2 Myr longer duration of core crystallisation  
484 in comparison to the constant mean values case, while including only variable  $k$  results  
485 in an 11 Myr delay in the onset and a 4 Myr shorter duration of core crystallisation. Vari-  
486 able  $\rho$  produces the shallowest meteorite source regions of the three properties while vari-  
487 able  $k$  produces the deepest (Table 4). Including just one  $T$ -dependent property cannot  
488 replicate the fully variable model.



**Figure 8.** Difference in temperature distribution between (a) the reference constant model and variable model and (b) the mean constant model and variable model, where average  $k$ ,  $\rho$  and  $C$  through time and radius are equal. Period of core crystallisation is shown in dashed white for the constant cases, and in green for the variable case. Symbols mark the source regions for the Imilac and Esquel meteorites as they pass through the 593 K isotherm; white circles show the results from the constant cases, while green shows the result when variable properties are used. We use the cooling rates applied by Bryson et al. (2015), calculated from cloudy-zone particle size (J. Yang, Goldstein, & Scott, 2010)

489

## 4 Discussion and Conclusion

490

491

492

493

494

495

496

497

498

499

500

Including  $T$ -dependent thermal properties changes the temperature structure in the modelled planetesimal: predictions of mantle temperature can differ by 50 K over tens of millions of years even when the best estimates for constant  $k$ ,  $\rho$  and  $C$  are used (Figure 8). This results in significant changes in the timing and duration of core crystallisation: the onset of core solidification is 22 Myr later, a delay of 12 %, while the core solidified 3 % faster. The delay in onset of core crystallisation is equivalent to increasing the radius of the planetesimal by 10 % with constant parameters, but increasing  $r_p$  extends the period of solidification by 13 % (Table 2). We use the example of a pallasite parent body to illustrate these results: including  $T$ -dependent properties delays the onset of core crystallisation and results in deeper source regions for pallasite meteorites than when constant  $k$ ,  $\rho$  and  $C$  are used (Figure 8). In this example,  $T$ -dependent  $k$ ,  $\rho$

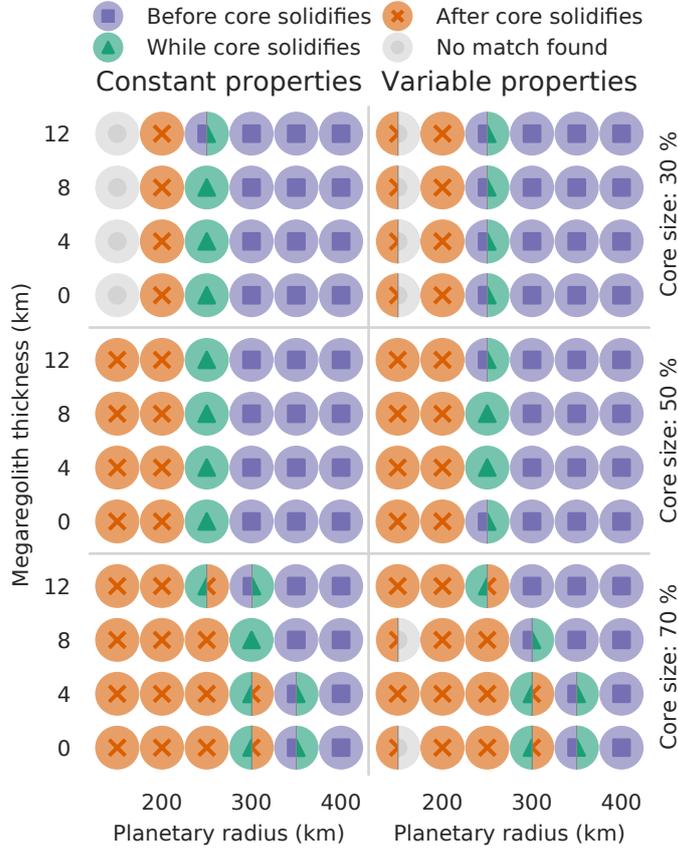
501 and  $C$  result in a hotter deep mantle but cooler shallow mantle, which cannot be repli-  
502 cated by constant values (Figure 8).

503 Including  $T$ -dependent properties also affects whether or not samples are predicted  
504 to preserve remnant magnetisation from a core dynamo: while in the constant reference  
505 case both the Imilac and Esquel meteorite source depths cool through 593 K during core  
506 solidification, the Imilac region cools down below 593 K before core solidification when  
507 variable  $k$ ,  $\rho$  and  $C$  or mean constant values based on the variable case are used (Table  
508 4). While the relative timing of the meteorite source regions' cooling through 593 K and  
509 the core crystallising can be reproduced by the constant mean case for this example, the  
510 input values for  $k$ ,  $\rho$  and  $C$  require the fully variable case to be run initially in order to  
511 be calculated.

512 In our example of a 250 km radius parent body, Imilac forms only  $\sim 5$  Myr before  
513 the core begins to crystallise and so can be accounted for by error in the measurement  
514 of the cooling rate from this sample (Bryson et al., 2015; J. Yang, Goldstein, & Scott,  
515 2010). However, larger discrepancies in timing can be found for different cooling rates,  
516 parent body radii, megaregolith thickness or core fraction (Figure 9). Including  $T$ -dependent  
517 properties narrows the range of input parameters that allow meteorite samples to po-  
518 tentially record paleomagnetic signatures. This provides a simple criteria for testing dif-  
519 ferent parameter combinations: whether the meteorite source region cools through the  
520 tetrataenite chemical ordering temperature during core solidification. As shown in Fig-  
521 ure 9, when constant  $k$ ,  $\rho$  and  $C$  are used, megaregolith thicknesses anywhere between  
522 0–12 km satisfy the above criteria for a planetesimal of 250 km radius and a core that  
523 is 50% of  $r_p$ , while a megaregolith layer of 4–8 km is required when  $T$ -dependent prop-  
524 erties are used. If the core fraction is reduced to 30% of  $r_p$ , a 250 km body with megare-  
525 golith between 0–8 km can accommodate both meteorite samples, whereas no suitable  
526 combination of parameters can be chosen when  $T$ -dependent  $k$ ,  $\rho$  and  $C$  are used. Simi-  
527 larly, no suitable parent body with a 250 km radius and a core fraction of 70%  $r_p$  can  
528 be found if  $T$ -dependent properties are used, whereas if these values are taken as con-  
529 stant, then a planetesimal with a radius of 300 km including an 8 km thick megaregolith  
530 can produce the cooling rates and required timings in both meteorites.

531 Nichols et al. (2016) find that two additional pallasites, Marjalahti and Brenham,  
532 record a small, weak magnetic field and argue that these samples cooled through the tetrataen-  
533 ite formation temperature before the onset of core crystallisation. This timing stipula-  
534 tion could provide an additional constraint on the allowable physical parameters in the  
535 model. However, for the range of parameters explored in Figure 9, Marjalahti and Bren-  
536 ham form before core crystallisation for all cases except a selection already ruled out by  
537 Esquel and Imilac forming after core crystallisation. Therefore, in this case they do not  
538 provide an additional constraint on the timing of core crystallisation, but may be use-  
539 ful for different parameter searches.

540 One limitation of this work comes from the simplified approach to modelling the  
541 core. We assumed a dynamo is generated during bottom-up eutectic solidification and  
542 have neglected  $T$ -dependent properties in this region. In reality, core solidification in plan-  
543 etesimals is likely to be complex and strongly dependent on the bulk sulfur content of  
544 the core. Bulk S content is difficult to estimate from iron meteorite samples due to the  
545 incompatibility of S in solid iron, and the resulting low-S composition of these samples  
546 (Neufeld et al., 2019). Bryson et al. (2019) predict a core dynamo driven by composi-  
547 tional convection at earlier times than suggested by the model we present, while the ini-  
548 tially non-eutectic core composition evolves towards a eutectic composition. They ar-  
549 gue that eutectic solidification would not be expected to generate a core dynamo, as sul-  
550 fur would not be expelled during solidification as the inner core adopts an FeS compo-  
551 sition. Within this framework, Esquel and Imilac are instead predicted to experience a  
552 magnetic field in the period “before core solidification” in Figure 9, but this period of  
553 non-eutectic solidification cannot be easily quantified without a fuller treatment of the



**Figure 9.** Planetary radius, core size and megaregolith thickness investigation for the constant  $k$ ,  $\rho$  and  $C$  case, and the fully variable case. The colour and symbol denote whether or not the Imilac and Esquel meteorite source region cooled through 593 K during core crystallisation  $\pm 10$  Myr: green triangles mark models where this criteria was met. Red crosses denote models where the meteorite cooled through 593 K after core crystallisation, whereas blue squares show where this happened before the core began to crystallise. Grey markers note that no matches for the meteorite cooling rates at 800 K were found, implying the meteorite could not have formed in that body. Where both samples have different results, Imilac is shown on the left and Esquel on the right. We use the cooling rates applied by Bryson et al. (2015), calculated from cloudy-zone particle size (J. Yang, Goldstein, & Scott, 2010)

554 core, which is not warranted by our focus on the importance of temperature dependent  
 555 conductivity on the cooling of the mantle. Furthermore, core solidification fronts may  
 556 initiate at the core-mantle boundary, resulting in top-down solidification through den-  
 557 dritic growth (Scheinberg et al., 2016). Top-down crystallisation would allow a dynamo  
 558 to be generated during eutectic solidification, and both modes of solidification have been  
 559 inferred for differentiated planetesimals based on iron meteorite cooling rates (J. Yang  
 560 et al., 2008; J. Yang, Goldstein, Michael, et al., 2010; Neufeld et al., 2019).

561 Following crystallisation, the core is assumed to return to an isothermal state due  
 562 to the high conductivity of the material. For the pallasite example case, this is an ac-  
 563 ceptable simplification as it is the times preceding and during the core solidification pe-  
 564 riod that are of interest. For other applications it may be required to restart the model  
 565 with the core included in the iterative solution with a Neumann boundary condition at  
 566 the centre, as used for approximating the analytical solution. The effects of pressure and  
 567 gravity have also been neglected due to the low pressure gradient expected within the  
 568 body as discussed in section 1.

569 In conclusion,  $T$ -dependent properties can significantly impact the output of plan-  
 570 etesimal cooling models, even if the model results are being used qualitatively or to judge  
 571 the relative timing of processes within the body, such as whether meteorite formation  
 572 regions cool through specific temperatures before, during or after the period of core crys-  
 573 tallisation. The inclusion of  $T$ -dependent  $k$ ,  $\rho$  and  $C$  results in later crystallisation of the  
 574 core ( $\sim 40$  Myr later than the constant reference case and  $\sim 20$  Myr later than the up-  
 575 dated constant case) and deeper meteorite formation depths due to suppressed cooling  
 576 rates in the mantle. This result cannot be replicated with constant values for  $k$ ,  $\rho$  and  
 577  $C$ , even when these values are chosen to match the mean values of each through time  
 578 and radius in the variable model. If  $T$ -dependent  $\kappa$  is included without a non-linear term,  
 579 the reduction in cooling rates through the body is overestimated, resulting in core so-  
 580 lidification 33 Myr after the variable case and 73 Myr after the constant case. These re-  
 581 sults are shown with relevance to the pallasite parent body. The parameter space which  
 582 satisfies the cooling rate criteria for the material which formed the Imilac and Esquel me-  
 583 teorites shrinks when  $T$ -dependent mantle properties are included; it follows that if more  
 584 samples are investigated the parameter space will shrink further. Future work could use  
 585 this more restrictive parameter space to address the ongoing debate over the number of  
 586 required pallasite parent bodies and potentially place a minimum constraint on the num-  
 587 ber of bodies required.  $T$ -dependent properties should also be addressed for other plan-  
 588 etesimals and meteorite parent bodies where conduction is involved, for example the or-  
 589 dinary chondrite parent body, where peak temperatures and the inferred parent body  
 590 radius may be incorrectly calculated.

## 591 Acknowledgments

592 Data availability: representative model output data are publicly available from the  
 593 National Geoscience Data Centre (NGDC), the Natural Environment Research Coun-  
 594 cil (UK) data centre for geoscience data, under the data ID 138605, available for down-  
 595 load at <http://data.bgs.ac.uk/id/dataHolding/13607679> (Murphy Quinlan, 2020).  
 596 Extended results tables are available for download at [https://github.com/murphyqm/  
 597 pytesimal-test-results](https://github.com/murphyqm/pytesimal-test-results) (Murphy Quinlan, 2021). A simple Python script to down-  
 598 load and plot this data, along with the model source code is available at [https://github  
 599 .com/murphyqm/pytesimal](https://github.com/murphyqm/pytesimal) (Murphy Quinlan & Walker, 2020). The software is writ-  
 600 ten in Python 3 under the MIT license. This paper uses version 1.0.0, archived at DOI:  
 601 [10.5281/zenodo.4321772](https://doi.org/10.5281/zenodo.4321772).

602 MMQ was supported by the Leeds-York Natural Environment Research Council  
 603 Doctoral Training Partnership (NE/L002574/1). CJD was supported by Natural Envi-  
 604 ronment Research Council Independent Research Fellowship (NE/L011328/1). We thank

605 James F. J. Bryson and an anonymous reviewer for providing helpful comments and sug-  
 606 gestions which improved this manuscript. Perceptually uniform colourmaps used in Fig-  
 607 ures 4, 6 and 8 are from the cmocean package for Python (Thyng et al., 2016).

## 608 References

- 609 Akridge, G., Benoit, P. H., & Sears, D. W. (1998). Regolith and megaregolith  
 610 formation of h-chondrites: Thermal constraints on the parent body. *Icarus*,  
 611 *132*(1), 185–195.
- 612 Allan, D., & Jacobs, J. (1956). The melting of asteroids and the origin of meteorites.  
 613 *Geochimica et Cosmochimica Acta*, *9*(5-6), 256–272.
- 614 Baker, J., Bizzarro, M., Wittig, N., Connolly, J., & Haack, H. (2005). Early plan-  
 615 etesimal melting from an age of 4.5662 Gyr for differentiated meteorites. *Na-  
 616 ture*, *436*(7054), 1127–1131.
- 617 Bennett, M. E., & McSween, H. Y. (1996). Revised model calculations for the ther-  
 618 mal histories of ordinary chondrite parent bodies. *Meteoritics & Planetary Sci-  
 619 ence*, *31*(6), 783–792.
- 620 Berman, R. G., & Brown, T. H. (1985). Heat capacity of minerals in the system  
 621 Na<sub>2</sub>O–K<sub>2</sub>O–CaO–MgO–FeO–Fe<sub>2</sub>O<sub>3</sub>–Al<sub>2</sub>O<sub>3</sub>–SiO<sub>2</sub>–TiO<sub>2</sub>–H<sub>2</sub>O–CO<sub>2</sub>: repre-  
 622 sentation, estimation, and high temperature extrapolation. *Contributions to  
 623 Mineralogy and Petrology*, *89*(2), 168–183.
- 624 Boesenberg, J. S., Delaney, J. S., & Hewins, R. H. (2012). A petrological and  
 625 chemical reexamination of Main Group pallasite formation. *Geochimica et  
 626 Cosmochimica Acta*, *89*, 134–158.
- 627 Boss, A. P. (1998). Temperatures in protoplanetary disks. *Annual Review of Earth  
 628 and Planetary Sciences*, *26*(1), 53–80.
- 629 Bryson, J. F. J., Neufeld, J. A., & Nimmo, F. (2019). Constraints on asteroid  
 630 magnetic field evolution and the radii of meteorite parent bodies from thermal  
 631 modelling. *Earth and Planetary Science Letters*, *521*, 68–78.
- 632 Bryson, J. F. J., Nichols, C. I. O., Herrero-Albillos, J., Kronast, F., Kasama,  
 633 T., Alimadadi, H., ... Harrison, R. J. (2015). Long-lived magnetism  
 634 from solidification-driven convection on the pallasite parent body. *Nature*,  
 635 *517*(7535), 472–475.
- 636 Carslaw, H. S., & Jaeger, J. C. (1986). *Conduction of heat in solids* (2nd ed.). Ox-  
 637 ford : New York: Clarendon Press ; Oxford University Press.
- 638 Charney, J. G., Fjörtoft, R., & Neumann, J. (1950). Numerical integration of the  
 639 barotropic vorticity equation. *Tellus*, *2*(4), 237–254.
- 640 Crank, J. (1979). *The mathematics of diffusion*. Clarendon Press.
- 641 Crank, J., & Nicolson, P. (1947). A practical method for numerical evaluation of so-  
 642 lutions of partial differential equations of the heat-conduction type. *Mathemat-  
 643 ical Proceedings of the Cambridge Philosophical Society*, *43*(1), 50–67.
- 644 Davies, C. J., & Pommier, A. (2018). Iron snow in the martian core? *Earth and  
 645 Planetary Science Letters*, *481*, 189–200.
- 646 Debye, P. (1912). Zur Theorie der spezifischen Wärmen. *Annalen der Physik*,  
 647 *344*(14), 789–839.
- 648 Dziewonski, A. M., & Anderson, D. L. (1981). Preliminary reference earth model.  
 649 *Physics of the Earth and Planetary Interiors*, *25*(4), 297 - 356.
- 650 Elkins-Tanton, L. T., Weiss, B. P., & Zuber, M. T. (2011). Chondrites as samples of  
 651 differentiated planetesimals. *Earth and Planetary Science Letters*, *305*(1-2), 1–  
 652 10.
- 653 Fei, Y. (2013). Thermal expansion. In *Mineral physics & crystallography* (p. 29-44).  
 654 American Geophysical Union (AGU).
- 655 Fu, R. R., Hager, B. H., Ermakov, A. I., & Zuber, M. T. (2014). Efficient early  
 656 global relaxation of asteroid vesta. *Icarus*, *240*, 133–145.

- 657 Gail, H.-P., Trieloff, M., Breuer, D., & Spohn, T. (2014). Early thermal evolution of  
658 planetesimals and its impact on processing and dating of meteoritic material.  
659 In *Protostars and planets VI*. University of Arizona Press.
- 660 Ghosh, A., & McSween, H. Y. (1998). A thermal model for the differentiation of as-  
661 teroid 4 vesta, based on radiogenic heating. *Icarus*, *134*(2), 187–206.
- 662 Ghosh, A., & McSween, H. Y. (1999). Temperature dependence of specific heat ca-  
663 pacity and its effect on asteroid thermal models. *Meteoritics & Planetary Sci-*  
664 *ence*, *34*(1), 121–127.
- 665 Greenwood, R. C., Burbine, T. H., & Franchi, I. A. (2020). Linking asteroids and  
666 meteorites to the primordial planetesimal population. *Geochimica et Cos-*  
667 *mochimica Acta*, *277*, 377–406.
- 668 Haack, H., Rasmussen, K. L., & Warren, P. H. (1990). Effects of re-  
669 golith/megaregolith insulation on the cooling histories of differentiated as-  
670 teroids. *Journal of Geophysical Research*, *95*(B4), 5111–5124.
- 671 Harrison, K. P., & Grimm, R. E. (2010). Thermal constraints on the early history of  
672 the h-chondrite parent body reconsidered. *Geochimica et Cosmochimica Acta*,  
673 *74*(18), 5410–5423.
- 674 Hevey, P. J., & Sanders, I. S. (2006). A model for planetesimal meltdown by  $^{26}\text{Al}$   
675 and its implications for meteorite parent bodies. *Meteoritics & Planetary Sci-*  
676 *ence*, *41*(1), 95–106.
- 677 Hofmeister, A. M. (1999). Mantle values of thermal conductivity and the geotherm  
678 from phonon lifetimes. *Science*, *283*(5408), 1699–1706.
- 679 Hort, M. (1997). Cooling and crystallization in sheet-like magma bodies revisited.  
680 *Journal of Volcanology and Geothermal Research*, *76*(3-4), 297–317.
- 681 Isaak, D. G. (1992). High-temperature elasticity of iron-bearing olivines. *Journal of*  
682 *Geophysical Research: Solid Earth*, *97*(B2), 1871–1885.
- 683 Johnson, B. C., Sori, M. M., & Evans, A. J. (2019). Ferrovulcanism on metal worlds  
684 and the origin of pallasites. *Nature Astronomy*, *4*(1), 41–44.
- 685 Kokubo, E., & Ida, S. (2012). Dynamics and accretion of planetesimals. *Progress of*  
686 *Theoretical and Experimental Physics*, *2012*(1).
- 687 MacPherson, G. J. (2014). Calcium–Aluminum-Rich Inclusions in Chondritic Me-  
688 teorites. In A. M. Davis (Ed.), *Volume 1 of treatise on geochemistry (second*  
689 *edition): Meteorites and cosmochemical processes* (p. 139–179). Elsevier-  
690 Pergamon.
- 691 McKibbin, S. J., Pittarello, L., Makarona, C., Hamann, C., Hecht, L., Cher-  
692 nonozhkin, S. M., ... Claeys, P. (2019). Petrogenesis of main group pallasite  
693 meteorites based on relationships among texture, mineralogy, and geochem-  
694 istry. *Meteoritics & Planetary Science*, *54*(11), 2814–2844.
- 695 Miyamoto, M., Fujii, N., & Takeda, H. (1982). Ordinary chondrite parent body - An  
696 internal heating model. *Lunar and Planetary Science Conference Proceedings*,  
697 *12*, 1145-1152.
- 698 Moskovitz, N., & Gaidos, E. (2011). Differentiation of planetesimals and the thermal  
699 consequences of melt migration. *Meteoritics & Planetary Science*, *46*(6), 903–  
700 918.
- 701 Murphy Quinlan, M. (2020). *Temperature and cooling rate data for a conductively*  
702 *cooling 250km radius planetesimal with and without temperature-dependent*  
703 *material properties*. <http://data.bgs.ac.uk/id/dataHolding/13607679>.  
704 British Geological Survey.
- 705 Murphy Quinlan, M. (2021). *The conductive cooling of planetesimals with*  
706 *temperature-dependent properties: tabulated results*. [https://github.com/](https://github.com/murphyqm/pytesimal-test-results)  
707 [murphyqm/pytesimal-test-results](https://github.com/murphyqm/pytesimal-test-results). doi: 10.5281/zenodo.4439180
- 708 Murphy Quinlan, M., & Walker, A. (2020). *Pytesimal: v1.0.0*. [https://github](https://github.com/murphyqm/pytesimal)  
709 [.com/murphyqm/pytesimal](https://github.com/murphyqm/pytesimal). doi: 10.5281/zenodo.4321772
- 710 Neufeld, J. A., Bryson, J. F. J., & Nimmo, F. (2019). The top-down solidification  
711 of iron asteroids driving dynamo evolution. *Journal of Geophysical Research:*

- 712 *Planets*, 124(5), 1331-1356.
- 713 Nichols, C. I. O., Bryson, J. F. J., Herrero-Albillos, J., Kronast, F., Nimmo, F.,  
714 & Harrison, R. J. (2016). Pallasite paleomagnetism: Quiescence of a core  
715 dynamo. *Earth and Planetary Science Letters*, 441, 103–112.
- 716 Özisik, M. (1993). *Heat conduction*. New York: Wiley.
- 717 Petit, A.-T., & Dulong, P.-L. (1819). Recherches sur quelques points importants de  
718 la théorie de la chaleur. *Annales de Chimie et de Physique*, 10, 395–413.
- 719 Poirier, J.-P. (2000). *Introduction to the Physics of the Earth's Interior*. Cambridge:  
720 Cambridge University Press.
- 721 Robie, R. A., Hemingway, B. S., & Takei, H. (1982). Heat capacities and entropies  
722 of  $\text{Mg}_2\text{SiO}_4$ ,  $\text{Mn}_2\text{SiO}_4$ , and  $\text{Co}_2\text{SiO}_4$  between 5 and 380 K. *American Mineralogist*,  
723 67(5-6), 470–482.
- 724 Sahijpal, S., Soni, P., & Gupta, G. (2007). Numerical simulations of the differentiat-  
725 ion of accreting planetesimals with  $^{26}\text{Al}$  and  $^{60}\text{Fe}$  as the heat sources. *Meteo-*  
726 *oritics & Planetary Science*, 42(9), 1529–1548.
- 727 Scheinberg, A., Elkins-Tanton, L. T., Schubert, G., & Bercovici, D. (2016). Core  
728 solidification and dynamo evolution in a mantle-stripped planetesimal. *Journal*  
729 *of Geophysical Research: Planets*, 121(1), 2–20.
- 730 Seipold, U. (1998). Temperature dependence of thermal transport properties of crys-  
731 talline rocks — a general law. *Tectonophysics*, 291(1-4), 161–171.
- 732 Solomon, S. C. (1979). Formation, history and energetics of cores in the terrestrial  
733 planets. *Physics of the Earth and Planetary Interiors*, 19(2), 168–182.
- 734 Su, C., Liu, Y., Song, W., Fan, D., Wang, Z., & Tang, H. (2018). Thermodynamic  
735 properties of San Carlos olivine at high temperature and high pressure. *Acta*  
736 *Geochimica*, 37(2), 171–179.
- 737 Suzuki, I. (1975). Thermal Expansion of Periclase and Olivine, and their Anhar-  
738 monic Properties. *Journal of Physics of the Earth*, 23(2), 145–159.
- 739 Tarduno, J. A., Cottrell, R. D., Nimmo, F., Hopkins, J., Voronov, J., Erickson, A.,  
740 ... McKinley, R. (2012). Evidence for a Dynamo in the Main Group Pallasite  
741 Parent Body. *Science*, 939(315), 1427–1798.
- 742 The OSIRIS-REx Team, DellaGiustina, D. N., Emery, J. P., Golish, D. R., Rozitis,  
743 B., Bennett, C. A., ... Lauretta, D. S. (2019). Properties of rubble-pile aster-  
744 oid (101955) Bennu from OSIRIS-REx imaging and thermal analysis. *Nature*  
745 *Astronomy*, 3(4), 341–351.
- 746 Thyng, K., Greene, C., Hetland, R., Zimmerle, H., & DiMarco, S. (2016, Septem-  
747 ber). True colors of oceanography: Guidelines for effective and accurate col-  
748 ormap selection. *Oceanography*, 29(3), 9–13.
- 749 Warren, P. H. (2011). Ejecta-megaregolith accumulation on planetesimals and large  
750 asteroids. *Meteoritics & Planetary Science*, no–no.
- 751 Weidenschilling, S. J. (2000). Formation of planetesimals and accretion of the terres-  
752 trial planets. *Space Science Reviews*, 92, 295–310.
- 753 Wen, H., hui Lu, J., Xiao, Y., & Deng, J. (2015). Temperature dependence of ther-  
754 mal conductivity, diffusion and specific heat capacity for coal and rocks from  
755 coalfield. *Thermochimica Acta*, 619, 41–47.
- 756 Williams, J.-P., & Nimmo, F. (2004). Thermal evolution of the martian core: Impli-  
757 cations for an early dynamo. *Geology*, 32(2), 97.
- 758 Woolum, D. S., & Cassen, P. (1999). Astronomical constraints on nebular temper-  
759 atures: Implications for planetesimal formation. *Meteoritics & Planetary Sci-*  
760 *ence*, 34(6), 897–907.
- 761 Xu, Y., Shankland, T. J., Linhardt, S., Rubie, D. C., Langenhorst, F., & Klasinski,  
762 K. (2004). Thermal diffusivity and conductivity of olivine, wadsleyite and ring-  
763 woodite to 20 GPa and 1373 K. *Physics of the Earth and Planetary Interiors*,  
764 143-144, 321–336.
- 765 Yang, C. W., Williams, D. B., & Goldstein, J. I. (1997). A new empirical cool-  
766 ing rate indicator for meteorites based on the size of the cloudy zone of the

- 767 metallic phases. *Meteoritics & Planetary Science*, 32(3), 423–429.
- 768 Yang, J., Goldstein, J. I., Michael, J. R., Kotula, P. G., & Scott, E. R. (2010).  
769 Thermal history and origin of the ivb iron meteorites and their parent body.  
770 *Geochimica et Cosmochimica Acta*, 74(15), 4493 - 4506.
- 771 Yang, J., Goldstein, J. I., & Scott, E. R. (2008). Metallographic cooling rates and  
772 origin of IVA iron meteorites. *Geochimica et Cosmochimica Acta*, 72(12),  
773 3043–3061.
- 774 Yang, J., Goldstein, J. I., & Scott, E. R. (2010). Main-group pallasites: Thermal  
775 history, relationship to IIIAB irons, and origin. *Geochimica et Cosmochimica*  
776 *Acta*, 74(15), 4471–4492.
- 777 Yomogida, K., & Matsui, T. (1983). Physical properties of ordinary chondrites.  
778 *Journal of Geophysical Research: Solid Earth*, 88(B11), 9513–9533.
- 779 Young, H. D. (1991). *University physics* (8th ed.). New York: Addison-Wesley.
- 780 Zhang, Y., Yoshino, T., Yoneda, A., & Osako, M. (2019). Effect of iron content on  
781 thermal conductivity of olivine with implications for cooling history of rocky  
782 planets. *Earth and Planetary Science Letters*, 519, 109–119.