

# Radar Attenuation for Subsurface Sounding on Enceladus: Effects of a Porous Ice Layer

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## Abstract

The presence of a global ocean, the water-rock interface at the base of the ocean, and the inferred ocean composition derived from sampling the active plume at the south pole of Enceladus, make Saturn's moon a promising location for habitable conditions in the Solar System. Due to its thin (<35 km) and cold ice shell, Enceladus is expected to exhibit favourable conditions for direct detection of the ice-ocean interface using low-frequency radar sounder instruments. Here we investigate the two-way radar attenuation in the Enceladus ice shell, focusing on the effect of a porous icy layer generated by Enceladus' jet activity. Our results show that as little as 2% of the ice shell can be penetrated in regions covered by thick and strongly insulating porous layers. However, the high subsurface temperatures in these regions could promote the formation of brines at shallow depth that can be detected by future radar measurements.

# Radar Attenuation for Subsurface Sounding on Enceladus: Effects of a Porous Ice Layer

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## Key Points:

- We calculate the two-way radar attenuation on Enceladus considering a porous thermally insulating surface layer.
- For regions covered by a thick, insulating porous layer the detection of the ice-ocean interface is unlikely.
- For the same regions the high subsurface temperatures increase the likelihood that shallow brines are present and can be detected by radar.

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## 17 **Abstract**

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 19 the inferred ocean composition derived from sampling the active plume at the south pole  
 20 of Enceladus, make Saturn’s moon a promising location for habitable conditions in the  
 21 Solar System. Due to its thin (<35 km) and cold ice shell, Enceladus is expected to ex-  
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 27 face temperatures in these regions could promote the formation of brines at shallow depth  
 28 that can be detected by future radar measurements.

## 29 **Plain Language Summary**

30 Saturn’s moon Enceladus is a prime target for planetary exploration and for the  
 31 search of habitable conditions beyond Earth. Beneath its icy surface, this small moon  
 32 is thought to harbor a global ocean, presumably sampled by active water jets which have  
 33 been observed at Enceladus’ south pole. Moreover, shallow brines may exist within the  
 34 ice shell. The detection of subsurface water reservoirs (either the ocean or shallow brines)  
 35 that can be achieved by radar is fundamental in characterizing Enceladus’ subsurface  
 36 environment and its habitability potential. In this study we calculate the attenuation  
 37 of radar signals through the ice shell in the presence of snow deposits that are believed  
 38 to exist on the surface of Enceladus due to its water jets activity. We find that the ice-  
 39 ocean interface may not be reached in regions covered by thick snow deposits that act  
 40 as a blanket and keep the subsurface warm. However, in these regions, due to the high  
 41 subsurface temperatures, shallow water bodies are likely to exist and could be detected  
 42 by future radar observations.

## 43 **1 Introduction**

44 Saturn’s moon, Enceladus is considered a priority target for future planetary mis-  
 45 sions due to its high astrobiological potential (Choblet et al., 2021; Cable et al., 2021).  
 46 Water jets presumably originating from a subsurface ocean have been observed at the  
 47 south pole of Enceladus by NASA’s Cassini mission (e.g., Porco et al., 2006; Hansen et  
 48 al., 2006), and their analysis provides a direct window into the ocean composition (Postberg  
 49 et al., 2009) that, in turn, can help to understand the nature and amount of impurities  
 50 that may exist within the ice shell. The most direct access to the ice shell structure could  
 51 be provided by future radar measurements. Radar instruments are widely used to char-  
 52 acterize polar ice sheets on the Earth (e.g., Schroeder et al., 2020) and Mars (Plaut et  
 53 al., 2007; Phillips et al., 2008), and are part of the instrument suites of JUICE and Eu-  
 54 ropa Clipper to investigate the ice shells of icy moons in the Jupiter system (Bruzzone  
 55 et al., 2013; Blankenship et al., 2009).

56 The ice shell thickness of Enceladus is thought to vary gradually depending on lat-  
 57 itude and longitude (Čadek et al., 2019; Hemingway & Mittal, 2019). It is expected to  
 58 be thinnest at the south-polar region and thickest at the equatorial sub- and anti-Saturn  
 59 points. Depending on the chosen shape model (Nimmo et al., 2011; Tajeddine et al., 2017)  
 60 and assumed density contrast between the ice shell and the ocean, ice shell thickness mod-  
 61 els suggest strong variations, with values as low as 5 km at the south pole and as high  
 62 as 35 km in equatorial regions, or a more homogeneous ice shell thickness distribution  
 63 with less than 15 km differences (Hemingway & Mittal, 2019).

64 Enceladus’ jet activity likely leads to the formation of a highly porous layer at the  
 65 top of the ice shell due to the material fall-back from the plume eruptions at the south

66 pole (Kempf et al., 2010). If present, such a porous layer could be stable on most of Ence-  
 67 ladius’s surface due to the low temperatures (Gundlach et al., 2018). The thickness of  
 68 this porous layer and its distribution are poorly constrained, but local thicknesses of up  
 69 to 700 m have been reported from the analysis of pit chains on the surface of Enceladus  
 70 (Martin et al., 2023). Such a thick porous layer may strongly affect the thermal state  
 71 of the ice shell, leading to higher signal attenuation (Souček et al., 2023), but its effects  
 72 have not been investigated so far.

73 Another aspect that can affect the subsurface temperature and hence the two-way  
 74 attenuation is the way heat is currently transported through Enceladus’s ice shell. Heat  
 75 transport through the ice shell could occur either by conduction or by convection and  
 76 can affect the thermal state of the ice shell with typically lower temperatures for a con-  
 77 ductive scenario. Here we focus on conductive cases. This scenario is very likely given  
 78 the thin ice shell (<35 km) and high viscosity at the conditions relevant for Enceladus’s  
 79 ice shell (Barr & McKinnon, 2007). High viscosities are expected based on the grain sizes  
 80 observed in polar ice sheets on the Earth (between 1 and 5 mm, (Montagnat & Duval,  
 81 2000)) that are considered to be good analogues for the icy shells in the outer Solar Sys-  
 82 tem.

## 83 2 Methods

### 84 2.1 Thermal State of Enceladus’s Ice Shell

85 To study how ice shell properties impact radar attenuation, we use 1-D steady-state,  
 86 conductive thermal models of Enceladus’s interior. The model is solved numerically us-  
 87 ing the stationary heat-conduction equation for a spherical shell with an outer radius  $R_{\text{top}}$   
 88 of 252 km and an inner radius  $R_{\text{bot}}$ , which is varied to account for surface fluctuations  
 89 on Enceladus. The steady-state heat conduction equation reads:

$$\frac{1}{r^2} \frac{\partial}{\partial r} \left( kr^2 \frac{\partial T}{\partial r} \right) = 0, \quad (1)$$

90 where  $r$  is the radius,  $k$  the thermal conductivity of ice, and  $T$  the temperature. The ther-  
 91 mal conductivity of ice is temperature-dependent and follows the parametrization of Petrenko  
 92 and Whitworth (1999):

$$k(T) = \frac{651}{T}. \quad (2)$$

93 We solve Eq. 1 numerically and use as boundary conditions the surface temperature of  
 94 Enceladus at the top and the melting temperature of water-ice at the ice-ocean inter-  
 95 face. For the surface temperature we use a value of 60 K, but additional tests with val-  
 96 ues of 70 and 85 K are shown in the Supplementary Information (Fig. S2.1)

97 In contrast to previous studies that calculated the two-way radar attenuation in  
 98 icy shells, we consider the effects of a porous ice layer. On Enceladus, the main process  
 99 responsible for the formation of such a layer is the deposition of material from the ac-  
 100 tive plume at the south pole (Kempf et al., 2010; Southworth et al., 2019). This porous  
 101 ice layer may considerably affect the thermal state of the ice shell due to its low ther-  
 102 mal conductivity. Thermal conductivity values have been measured for porous icy lay-  
 103 ers in laboratory experiments (Seiferlin et al., 1996) and derived from thermophysical  
 104 modeling (Ferrari et al., 2021). Such measurements have provided wide ranges in results  
 105 (between  $0.001$  and  $0.025 \text{ Wm}^{-1}\text{K}^{-1}$ ). Therefore, in order to cover a wide parameter space,  
 106 we vary the thermal conductivity of this porous layer between  $0.1$  and  $0.001 \text{ Wm}^{-1}\text{K}^{-1}$ .

107 The thickness and spatial distribution of a porous icy layer on Enceladus is poorly  
 108 constrained. A recent study by Martin et al. (2023) proposed porous layer thicknesses  
 109 of up to 700 m (mean of 250 m) based on the analysis of tectonic pit chains. We test a  
 110 variety of porous layer thicknesses up to 700 m and employ different spatial distributions  
 111 to account for uncertainties related to the porous layer on Enceladus.

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## 2.2 Radar Attenuation

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Radar attenuation in ice is caused by dielectric absorption losses as well as scattering losses. A common assumption in low-frequency radar sounding is that scattering losses are negligible due to the long wavelengths with respect to the scattering structures (e.g., ice grains) within the ice. Hence, attenuation purely driven by absorption losses is assumed here. Following the work of Kalousová et al. (2017) and Souček et al. (2023), we calculate the two-way attenuation along the propagation path at depth  $d$ , which was subdivided into  $N$  layers, as:

$$A_2(d) = \sum_{i=0}^N 2A_1(d_i)\Delta d \quad (3)$$

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where  $d_0$  represents the surface layer,  $d_N$  is the final layer,  $A_1(d_i)$  is the one-way attenuation at depth  $d_i$ , and  $\Delta d$  the thickness of each layer used in calculating  $A_1$ .

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The one-way attenuation  $A_1$  (in dB/km) of a radar signal is proportional to the electrical conductivity of ice ( $\sigma$ ) within the range of High Frequency (HF) and Very High Frequency (VHF) (Matsuoka et al., 2012), and can be approximated as follows:

$$A_1 \approx 0.914\sigma. \quad (4)$$

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The electrical conductivity of ice in terrestrial sounding experiments depends on the ice temperature along with the presence of chemical impurities within the ice, and can be written as follows (Corr et al., 1993):

$$\sigma = \sum_{i=0}^1 \sigma_i^0 C_i \exp \left[ -\frac{E_i}{k_B} \left( \frac{1}{T} - \frac{1}{T_r} \right) \right], \quad (5)$$

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with each contribution representing one component that affects the electrical conductivity. Each summand requires the material molar electrical conductivity  $\sigma_i$  at reference temperature  $T_r = 251$  K, molar concentration  $C_i$ , activation energy  $E_i$ , local ice temperature  $T$ , and the Boltzmann constant  $k_B$ . In this study we use the same values as in Table 1 of Souček et al. (2023). The index 0 indicates a scenario of a pure water-ice shell, while  $i = 1$  adds the effects of the maximum theoretical chloride concentration in pure water-ice (Souček et al., 2023).

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Similar to Kalousová et al. (2017) and Souček et al. (2023), we calculate the plausible attenuation ranges within Enceladus's ice shell. We use "low-loss" to indicate that the attenuation model considers only pure water ice, while the "high-loss" model is characterized by a homogeneous mixture of pure water ice and  $300 \mu\text{M}$  of chloride. The chloride concentration has been chosen based on plume material sampled during NASA's Cassini mission. Although carbonate salts, chloride, silica, and ammonia/ammonium have been detected, only chloride is expected to exist within the ice shell with significant concentrations (of up to  $300 \mu\text{M}$ ) to impact an orbital radar sounder (Souček et al., 2023).

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## 3 Results

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First, we investigate the difference between the "high" and "low" loss attenuation models in multiple 1-dimensional scenarios of Enceladus's internal structure. To this end, we calculate temperature profiles and corresponding two-way attenuation for various ice shell thicknesses, thicknesses of the porous layer, and porous layer thermal conductivities (Fig. 1).

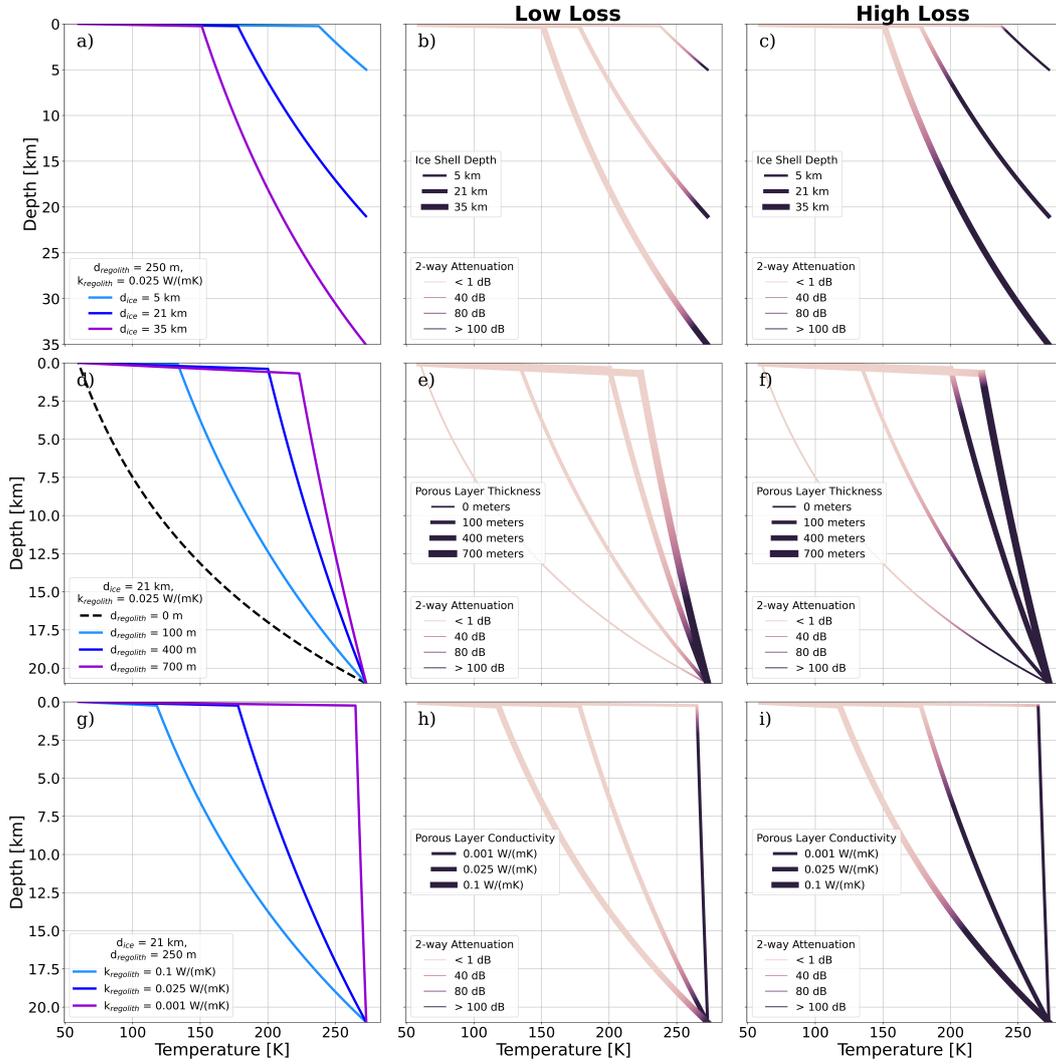
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We define a penetration depth, which is the depth at which the two-way attenuation reaches a 100 dB. The relative penetration depth is the penetration depth divided by the total ice shell thickness of the respective scenario. The relative penetration depth strongly depends on temperature, as the latter affects the electrical conductivity. For a



**Figure 1.** The two-way attenuation ( $A_2$ ) for various: a) ice shell depths (5 – 35 km), b) porous layer thicknesses (0 – 700 m), and c) porous layer thermal conductivities (0.1 – 0.001  $\text{Wm}^{-1}\text{K}^{-1}$ ). Panels d-f) show the low-loss scenarios, while panels g-i) show the high-loss cases.

153 conductive ice shell, the temperature itself depends on the thickness of the ice shell, and  
 154 to a first order on the presence of a porous layer. The porous layer leads to a high thermal  
 155 gradient near the surface due to its insulating effect caused by its low thermal conductivity.  
 156 The relative penetration depth in a low-loss scenario is 91%, 94%, and 95%,  
 157 for ice shell thicknesses of 5 km, 21 km, and 35 km, respectively. The penetration depths  
 158 relative to the total depth in the high-loss case are 16%, 33%, and 48%, for the same  
 159 ice shell thicknesses of 5 km, 21 km, and 35 km, respectively.

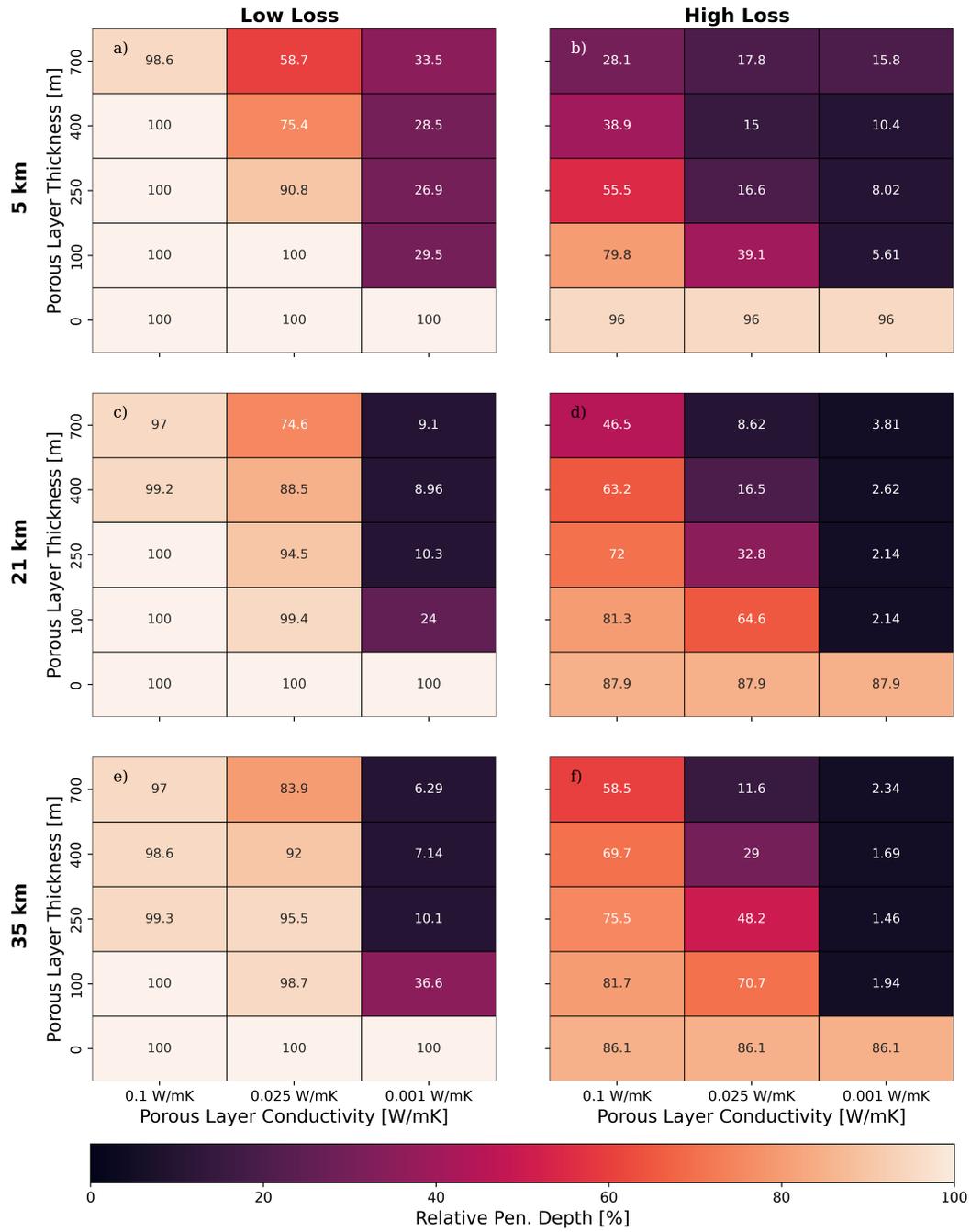
160 We can clearly observe in Fig. 1 that the attenuation dramatically increases with  
 161 increasing porous layer thickness. This can be again attributed to the insulating effect  
 162 of the porous layer, an effect that becomes more pronounced with increasing porous layer  
 163 thickness. As observed on Fig. 1d, the difference between the temperature profiles with  
 164 and without a porous layer of 700 m is as large as 150 K at shallow depth. The low-loss  
 165 scenario with no porous layer only reaches 53.4 dB at the ice-ocean interface, which was  
 166 set here to 21 km. In the low-loss scenario, the presence of a 100 m porous layer increases  
 167 the 2-way attenuation to 100 dB or higher at 99% of the ice shell depth. The relative pen-  
 168 etration depth associated with the 100 dB limit is 88% for a 400 m and 74% for a 700 m  
 169 porous layer. For the high-loss scenario, the radar attenuation increases to more than  
 170 100 dB before reaching the ice-ocean interface even when no porous layer is considered.  
 171 Thus, the relative penetration depth is 88% of the total ice shell for the no porous layer  
 172 case, 64% for the 100 m porous layer case, 16% for the 400 m case, and 8% for the 700 m  
 173 porous layer.

174 The thermal conductivity of the porous layer can significantly impact the thermal  
 175 profile within the ice shell. A highly insulating porous layer (i.e., thermal conductivity  
 176 of  $0.001 \text{ Wm}^{-1}\text{K}^{-1}$ ) with a thickness of 250 m, leads to a warm ice shell, only a few de-  
 177 grees colder than the ice-ocean interface. In the low-loss scenario, the 2-way attenuation  
 178 for the case with the highest thermal conductivity of the porous layer (i.e.,  $0.1 \text{ Wm}^{-1}\text{K}^{-1}$ )  
 179 reaches 95 dB at the ice-ocean interface. For a thermal conductivity of  $0.025 \text{ Wm}^{-1}\text{K}^{-1}$   
 180 of the porous layer, the 2-way attenuation reaches the 100 dB limit at about  $\sim 80\%$  of  
 181 the ice shell in both high- and low-loss scenarios. In the case with the most insulating  
 182 porous layer (i.e., regolith thermal conductivity of  $0.001 \text{ Wm}^{-1}\text{K}^{-1}$ ), the 2-way atten-  
 183 uation reaches 100 dB before 10% of the ice shell is penetrated in both the high and low-  
 184 loss scenarios.

185 In Fig. 2 we explore a large set of parameter combinations. Each cell represents  
 186 a single simulation (equivalent to one line graph in Fig. 1). The value inside each cell  
 187 represents the relative penetration depth. The simulations cover ice shell thicknesses of  
 188 5 km, 21 km, and 35 km, as well as the low-loss and high-loss attenuation models.

189 None of the high-loss models reach 100% relative depth penetration, even with a  
 190 5 km ice shell with no porous layer. Most simulations using a highly insulating porous  
 191 layer with a thermal conductivity of  $0.001 \text{ Wm}^{-1}\text{K}^{-1}$  reach less than 10% relative pen-  
 192 etration depth. Of the total of 90 simulations, 16 models penetrate the whole ice shell,  
 193 with those models generally having porous layers with small thicknesses and high ther-  
 194 mal conductivities.

195 As expected, every combination of parameters has a lower relative penetration depth  
 196 in the high-loss attenuation model compared to low-loss. Secondly, the relative penetra-  
 197 tion depth decreases with increasing porous layer thickness and decreasing thermal con-  
 198 ductivity. However, a trend reversal occurs (i.e., penetration depth increases) in highly  
 199 insulating porous layers (apart from the the 35 km low-loss scenarios). Such a reversal  
 200 only occurs in scenarios with both a highly conductive and very deep porous layer. This  
 201 behavior can be explained by the fact that with increasing porous layer thickness, the  
 202 thermal state of the ice shell starts to approach that of a conductive ice shell character-  
 203 ized by a single thermal conductivity. If the porous layer makes up the entire ice shell,



**Figure 2.** The relative penetration depth of a radar signal for ice shell thicknesses of 5 km (a, d), 21 km (b, e), and 35 km (c, f) and various porous layer thicknesses and thermal conductivities for low-loss (left column) and high-loss (right column) scenarios.

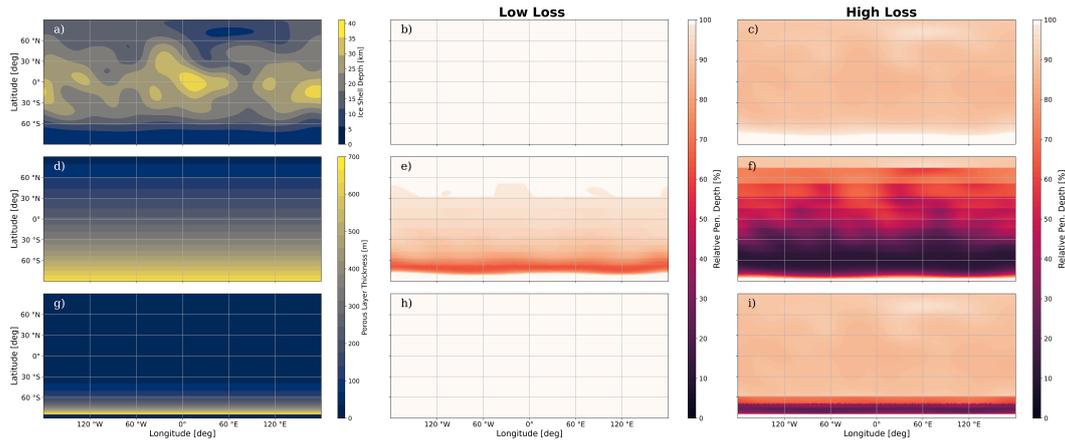
204 the steady-state thermal state will be similar to that of a homogeneous ice shell with a  
 205 thermal conductivity of pure water-ice.

206 Beyond 1-D analysis, we generate attenuation maps (Fig. 3 a)) using a global ice  
 207 shell thickness map from Hemingway and Mittal (2019), based on a shape model of Nimmo  
 208 et al. (2011), gravitational data, and assuming a density contrast between the ice shell  
 209 and the subsurface ocean of  $95 \text{ kg m}^{-3}$  similar to some of the models of (Hemingway &  
 210 Mittal, 2019). Additional attenuation maps using a different ice shell thickness, shape  
 211 model and ice-ocean density contrast are available in the Supporting Information (SI),  
 212 Section S3.

213 The attenuation was calculated by treating each data point as a single tempera-  
 214 ture profile using the corresponding ice shell thickness at the respective location. We con-  
 215 structed two distribution models for the porous layer under the assumption that the thick-  
 216 ness of the porous layer varies only with latitude and: 1) exponentially decreases from  
 217 a 700-m-thick layer at the south pole to 10-m-thick layer at the north pole of Enceladus,  
 218 which we denote as the "exponential-global distribution" (Fig. 3 b) while 2) the porous  
 219 layer is absent within the  $5^\circ$  of the south pole and then exponentially decreases from 255 m  
 220 to 0 m at equator (Fig. 3 c), which we will call "exponential-hemispheric distribu-  
 221 tion". In all cases the conductivity of the porous layer is  $0.025 \text{ W m}^{-1} \text{ K}^{-1}$ .

222 In the low-loss attenuation maps (Fig. 3 d, e, and f), a majority of the surface has  
 223 more than 90% relative penetration depth, with both the no-porous-layer and the exponential-  
 224 hemispheric distribution cases having 100% global radar penetration down to the ice-  
 225 ocean interface. In all three high-loss scenarios, we observe a small band of 100% rela-  
 226 tive penetration depth roughly  $5^\circ$  in latitude away from the south pole. The thin ice shell  
 227 at the south pole allows for the signal to reach the ice-ocean interface even in the pres-  
 228 ence of a thick porous layer (i.e., 700 m in the exponential-global distribution case).

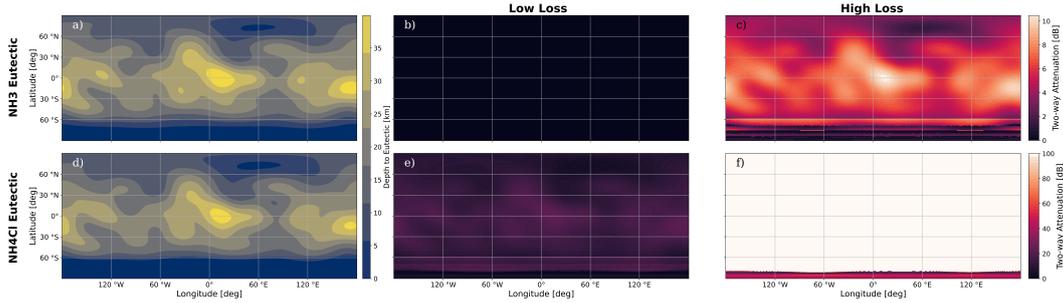
229 We note that in all cases besides the high-loss exponential-global distribution case,  
 230 the penetration depth reaches more than 80% of the ice shell for most locations.



**Figure 3.** Maps of the: a) ice shell thickness (Hemingway & Mittal, 2019) and porous layer distribution for b) the "exponential-global scenario" and c) the "exponential-hemispheric scenario" (see text). The radar penetration depth relative to the ice shell thickness in panel a) is shown for d) no porous layer, e) exponential-global and f) exponential-hemispheric distribution of the porous layer. Panels g), h) and i) show the high-loss cases.

231 In Fig. 4, we calculate the two-way attenuation at the eutectic interfaces of am-  
 232 monium chloride and ammonia following Souček et al. (2023) for the exponential-hemispheric  
 233 distribution of the porous layer (i.e., exponential decrease from 255 m at 85°S to 0 m at  
 234 equator) and assuming a thermal conductivity of the porous layer of  $0.025 \text{ Wm}^{-1}\text{K}^{-1}$ .

235 The eutectic interface of ammonium chloride ( $\text{NH}_4\text{Cl}$ ) is defined by the 257.79 K  
 236 isotherm, while the one for ammonia ( $\text{NH}_3$ ) by the 175.45 K isotherm (Marion et al., 2012).  
 237 Panels a and b of Fig. 4 show the depths at which the eutectic of  $\text{NH}_3$  and  $\text{NH}_4\text{Cl}$ , re-  
 238 spective, are reached. Fig. 4 c and d show the two-way attenuation for the low-loss at-  
 239 tenuation models, while the values obtained for the high-loss cases are shown in Fig. 4  
 240 e and f. Additional maps including different ice shell thicknesses and porous layer dis-  
 241 tribution are available in the SI (Section S4).



**Figure 4.** Maps showing the depth of: a) ammonia ( $\text{NH}_3$ ) and b) ammonium chloride ( $\text{NH}_4\text{Cl}$ ) eutectic interface for the exponential-hemispheric distribution of the porous layer. Panels c) and d) indicate the corresponding two-way attenuation values for the low-loss case at the eutectic interface of  $\text{NH}_3$  and  $\text{NH}_4\text{Cl}$ , respectively. Panels e) and f) are similar to c) and d), but for the high-loss scenarios.

242 The difference between the average depth of the ice-ocean interface and the aver-  
 243 age depth of the  $\text{NH}_4\text{Cl}$  eutectic interface is only 700 m. This is due to the fact that the  
 244 temperature of the  $\text{NH}_4\text{Cl}$  eutectic interface is only 20 K lower than the melting tem-  
 245 perature of water-ice at the base of the ice shell shown in Fig. 4 a. In contrast, the dif-  
 246 ference between the average depth of the ammonia eutectic interface and that of the ice-  
 247 ocean interface is 5 km, as  $\text{NH}_3$  has a much lower eutectic temperature of only 175.45 K.  
 248 Given the low eutectic temperature of  $\text{NH}_3$ , the two-way attenuation for the low-loss case  
 249 (Fig. 4 c) does not exceed 0.1 dB. For the eutectic interface of  $\text{NH}_4\text{Cl}$ , the two-way at-  
 250 tenuation shows an average value 13.7 dB in the low-loss scenario (Fig. 4 d). In the high-  
 251 loss attenuation case, the two-way attenuation at the eutectic interface of  $\text{NH}_3$  is only  
 252  $\sim 5$  dB (Fig. 4 e), while at the eutectic interface of  $\text{NH}_4\text{Cl}$  the average two-way at-  
 253 tenuation is about 400 dB (Fig. 4 f).

## 254 4 Discussion

255 Similar to other studies (Kalousová et al., 2017; Souček et al., 2023), we assume  
 256 a threshold of 100 dB for the two-way radar attenuation, above which the radar instru-  
 257 ment would no longer be able to detect subsurface interfaces. However, we note that this  
 258 threshold is only an estimate, that might change in a mission scenario depending on the  
 259 instrument design, operation scenarios, as well as surface and subsurface characteristics  
 260 (see e.g., Kalousová et al., 2017; Benedikter et al., 2024)[ for a detailed discussion]. Our  
 261 tests show that varying the two-way attenuation limit between 70 and 130 dB would not  
 262 significantly impact the results presented in Fig. 2. In these cases we observe a differ-

263 ence to the relative penetration depth shown in Fig. 2 of up to only 10% (see Fig. S1.1–  
264 S1.2 in the SI).

265 On Enceladus, the surface temperature lies between 60 and 85 K, the latter values  
266 being representative for the south polar region (Spencer et al., 2006). We tested the ef-  
267 fects of a higher surface temperature (i.e., 85 K) on our calculated radar attenuation val-  
268 ues (Fig. S2.1). A higher surface temperature shifts the ice shell temperature to higher  
269 values and leads to a smaller relative penetration depth. However the differences between  
270 using a surface temperature of 85 K compared to 60 K are only of the order of 2 – 4%.

271 We note that our study assumes simple distributions of a porous layer on Ence-  
272 ladus to give a first order overview of the potential detection of the ice-ocean interface  
273 via radar sounding. While our results show that the ice-ocean interface will be challeng-  
274 ing to detect in particular in regions covered by thick and highly thermal insulating porous  
275 layers, we note that large uncertainties exist for the global spatial distribution of such  
276 a porous layer on Enceladus. While models of the distribution of a porous layer on Ence-  
277 ladus exist (Kempf et al., 2010; Southworth et al., 2019), they typically investigate only  
278 the generation of such a layer through plume deposition. Such models indicate that tec-  
279 tonized regions on the leading and trailing hemispheres receive the least amount of mater-  
280 ial deposition, but that the plume eruption style (i.e., curtain-like vs. jet-like) affects  
281 the amount of snow deposits in the northern hemisphere (Southworth et al., 2019). The  
282 predicted distribution of a material deposition from models of jet-style eruptions seem  
283 to be consistent with the distribution of pit chains on the surface of Enceladus. The lat-  
284 ter, however, can only give a lower bound for the thickness of the porous layer, as the  
285 pits do not necessarily need to reach the base of the layer (Martin et al., 2023).

286 Another important factor that will affect the thermal state of the ice shell and hence  
287 the two-way attenuation is the thermal conductivity of the porous layer. A recent study  
288 by Jabaud et al. (2024) investigated the mechanical properties of powder-like materials  
289 similar to the expected snow deposits on Enceladus that are also suggested to exist to  
290 some extent on Europa. This study concluded that on Enceladus, the lower gravity leads  
291 to higher cohesion and the formation of loose, highly porous material. A high porosity  
292 is directly linked to a low thermal conductivity and thus highly insulating behavior. As  
293 shown in this study, an insulating porous layer would increase the ice shell temperature  
294 such that the resulting temperature contrast between the base of the porous layer and  
295 the ocean may be only 10s of degrees K. Such high average temperatures could result  
296 in the formation of shallow brines that could provide a radar-detectable source (Souček  
297 et al., 2023). Our models show that even in the presence of thick porous layers, the two-  
298 way radar attenuation remains below 25 dB for eutectic interfaces of  $\text{NH}_3$  and  $\text{NH}_4\text{Cl}$   
299 in the low-loss scenario. In the high-loss cases, only the  $\text{NH}_4\text{Cl}$  interface lies above the  
300 100 dB threshold for most of the ice shell apart from within about  $5^\circ$  of the south pole.  
301 As these eutectic interfaces are defined by isotherms, their detection would provide valu-  
302 able information about the thermal state of the ice shell and may help reconstructing  
303 not only the ice shell thickness (see discussion in Souček et al., 2023) but also the thick-  
304 ness of the porous layer that strongly affects the temperature in the ice shell and hence  
305 the depth of these interfaces.

306 This study has focused on the effect of a porous layer on two-way attenuation in  
307 a conductive ice shell. Future studies will test how such a porous layer, its thickness and  
308 spatial distribution, affects the ice shell dynamics and in particular the two-way radar  
309 attenuation for hot upwellings and cold downwellings. Depending on the ice shell tem-  
310 perature, cold downwellings could represent locations where the radar attenuation is low  
311 enough such that the ice-ocean interface may be reached, as previously discussed for Eu-  
312 ropa (Kalousová et al., 2017).

## 5 Conclusions

In this study we showed that a porous layer built up by the deposition of material from Enceladus's south pole plume or generated by impacts has a first order effect on the two-way radar attenuation. This porous layer acts as an insulation layer leading to high sub-surface temperatures and thus two-way attenuation. Through systematic parameter variations, we provide an extensive overview of the effects of a porous layer on the ability to reach the ice-ocean as well as other interfaces within the ice shell that are thought to exist based on the inferred ice shell chemistry.

Our investigations show that radar sounder instruments may penetrate anywhere from a few hundred meters to the entire ice shell of Enceladus. Nevertheless, those scenarios that prevent radar signals from reaching the ice ocean interface can provide valuable information about the ice shell. Identifying aspects of the Enceladus system that could prevent ocean detection may prove fundamental in further characterizing icy worlds. Valuable insights may be gained, such as the existence of near-surface liquid reservoirs, which are very likely for cases with high salt content and a porous layer on top that keeps the interior comparatively warm. Such brine reservoirs are considered niches for life, and their potential to be directly accessible by future missions is much greater compared to that of the subsurface oceans.

## 6 Open Research

Additional calculations including different ice shell thicknesses are available in the Supplementary Information. All data used in the figures and the code necessary to reproduce the calculations are available on Zenodo (Byrne et al., 2024)

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# Radar Attenuation for Subsurface Sounding on Enceladus: Effects of a Porous Ice Layer

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## Key Points:

- We calculate the two-way radar attenuation on Enceladus considering a porous thermally insulating surface layer.
- For regions covered by a thick, insulating porous layer the detection of the ice-ocean interface is unlikely.
- For the same regions the high subsurface temperatures increase the likelihood that shallow brines are present and can be detected by radar.

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## 17 **Abstract**

18 The presence of a global ocean, the water-rock interface at the base of the ocean, and  
 19 the inferred ocean composition derived from sampling the active plume at the south pole  
 20 of Enceladus, make Saturn’s moon a promising location for habitable conditions in the  
 21 Solar System. Due to its thin (<35 km) and cold ice shell, Enceladus is expected to ex-  
 22 hibit favourable conditions for direct detection of the ice-ocean interface using low-frequency  
 23 radar sounder instruments. Here we investigate the two-way radar attenuation in the Ence-  
 24 lадus ice shell, focusing on the effect of a porous icy layer generated by Enceladus’ jet  
 25 activity. Our results show that as little as 2% of the ice shell can be penetrated in re-  
 26 gions covered by thick and strongly insulating porous layers. However, the high subsur-  
 27 face temperatures in these regions could promote the formation of brines at shallow depth  
 28 that can be detected by future radar measurements.

## 29 **Plain Language Summary**

30 Saturn’s moon Enceladus is a prime target for planetary exploration and for the  
 31 search of habitable conditions beyond Earth. Beneath its icy surface, this small moon  
 32 is thought to harbor a global ocean, presumably sampled by active water jets which have  
 33 been observed at Enceladus’ south pole. Moreover, shallow brines may exist within the  
 34 ice shell. The detection of subsurface water reservoirs (either the ocean or shallow brines)  
 35 that can be achieved by radar is fundamental in characterizing Enceladus’ subsurface  
 36 environment and its habitability potential. In this study we calculate the attenuation  
 37 of radar signals through the ice shell in the presence of snow deposits that are believed  
 38 to exist on the surface of Enceladus due to its water jets activity. We find that the ice-  
 39 ocean interface may not be reached in regions covered by thick snow deposits that act  
 40 as a blanket and keep the subsurface warm. However, in these regions, due to the high  
 41 subsurface temperatures, shallow water bodies are likely to exist and could be detected  
 42 by future radar observations.

## 43 **1 Introduction**

44 Saturn’s moon, Enceladus is considered a priority target for future planetary mis-  
 45 sions due to its high astrobiological potential (Choblet et al., 2021; Cable et al., 2021).  
 46 Water jets presumably originating from a subsurface ocean have been observed at the  
 47 south pole of Enceladus by NASA’s Cassini mission (e.g., Porco et al., 2006; Hansen et  
 48 al., 2006), and their analysis provides a direct window into the ocean composition (Postberg  
 49 et al., 2009) that, in turn, can help to understand the nature and amount of impurities  
 50 that may exist within the ice shell. The most direct access to the ice shell structure could  
 51 be provided by future radar measurements. Radar instruments are widely used to char-  
 52 acterize polar ice sheets on the Earth (e.g., Schroeder et al., 2020) and Mars (Plaut et  
 53 al., 2007; Phillips et al., 2008), and are part of the instrument suites of JUICE and Eu-  
 54 ropa Clipper to investigate the ice shells of icy moons in the Jupiter system (Bruzzone  
 55 et al., 2013; Blankenship et al., 2009).

56 The ice shell thickness of Enceladus is thought to vary gradually depending on lat-  
 57 itude and longitude (Čadek et al., 2019; Hemingway & Mittal, 2019). It is expected to  
 58 be thinnest at the south-polar region and thickest at the equatorial sub- and anti-Saturn  
 59 points. Depending on the chosen shape model (Nimmo et al., 2011; Tajeddine et al., 2017)  
 60 and assumed density contrast between the ice shell and the ocean, ice shell thickness mod-  
 61 els suggest strong variations, with values as low as 5 km at the south pole and as high  
 62 as 35 km in equatorial regions, or a more homogeneous ice shell thickness distribution  
 63 with less than 15 km differences (Hemingway & Mittal, 2019).

64 Enceladus’ jet activity likely leads to the formation of a highly porous layer at the  
 65 top of the ice shell due to the material fall-back from the plume eruptions at the south

66 pole (Kempf et al., 2010). If present, such a porous layer could be stable on most of Ence-  
 67 ladius’s surface due to the low temperatures (Gundlach et al., 2018). The thickness of  
 68 this porous layer and its distribution are poorly constrained, but local thicknesses of up  
 69 to 700 m have been reported from the analysis of pit chains on the surface of Enceladus  
 70 (Martin et al., 2023). Such a thick porous layer may strongly affect the thermal state  
 71 of the ice shell, leading to higher signal attenuation (Souček et al., 2023), but its effects  
 72 have not been investigated so far.

73 Another aspect that can affect the subsurface temperature and hence the two-way  
 74 attenuation is the way heat is currently transported through Enceladus’s ice shell. Heat  
 75 transport through the ice shell could occur either by conduction or by convection and  
 76 can affect the thermal state of the ice shell with typically lower temperatures for a con-  
 77 ductive scenario. Here we focus on conductive cases. This scenario is very likely given  
 78 the thin ice shell (<35 km) and high viscosity at the conditions relevant for Enceladus’s  
 79 ice shell (Barr & McKinnon, 2007). High viscosities are expected based on the grain sizes  
 80 observed in polar ice sheets on the Earth (between 1 and 5 mm, (Montagnat & Duval,  
 81 2000)) that are considered to be good analogues for the icy shells in the outer Solar Sys-  
 82 tem.

## 83 2 Methods

### 84 2.1 Thermal State of Enceladus’s Ice Shell

85 To study how ice shell properties impact radar attenuation, we use 1-D steady-state,  
 86 conductive thermal models of Enceladus’s interior. The model is solved numerically us-  
 87 ing the stationary heat-conduction equation for a spherical shell with an outer radius  $R_{\text{top}}$   
 88 of 252 km and an inner radius  $R_{\text{bot}}$ , which is varied to account for surface fluctuations  
 89 on Enceladus. The steady-state heat conduction equation reads:

$$\frac{1}{r^2} \frac{\partial}{\partial r} \left( kr^2 \frac{\partial T}{\partial r} \right) = 0, \quad (1)$$

90 where  $r$  is the radius,  $k$  the thermal conductivity of ice, and  $T$  the temperature. The ther-  
 91 mal conductivity of ice is temperature-dependent and follows the parametrization of Petrenko  
 92 and Whitworth (1999):

$$k(T) = \frac{651}{T}. \quad (2)$$

93 We solve Eq. 1 numerically and use as boundary conditions the surface temperature of  
 94 Enceladus at the top and the melting temperature of water-ice at the ice-ocean inter-  
 95 face. For the surface temperature we use a value of 60 K, but additional tests with val-  
 96 ues of 70 and 85 K are shown in the Supplementary Information (Fig. S2.1)

97 In contrast to previous studies that calculated the two-way radar attenuation in  
 98 icy shells, we consider the effects of a porous ice layer. On Enceladus, the main process  
 99 responsible for the formation of such a layer is the deposition of material from the ac-  
 100 tive plume at the south pole (Kempf et al., 2010; Southworth et al., 2019). This porous  
 101 ice layer may considerably affect the thermal state of the ice shell due to its low ther-  
 102 mal conductivity. Thermal conductivity values have been measured for porous icy lay-  
 103 ers in laboratory experiments (Seiferlin et al., 1996) and derived from thermophysical  
 104 modeling (Ferrari et al., 2021). Such measurements have provided wide ranges in results  
 105 (between  $0.001$  and  $0.025 \text{ Wm}^{-1}\text{K}^{-1}$ ). Therefore, in order to cover a wide parameter space,  
 106 we vary the thermal conductivity of this porous layer between  $0.1$  and  $0.001 \text{ Wm}^{-1}\text{K}^{-1}$ .

107 The thickness and spatial distribution of a porous icy layer on Enceladus is poorly  
 108 constrained. A recent study by Martin et al. (2023) proposed porous layer thicknesses  
 109 of up to 700 m (mean of 250 m) based on the analysis of tectonic pit chains. We test a  
 110 variety of porous layer thicknesses up to 700 m and employ different spatial distributions  
 111 to account for uncertainties related to the porous layer on Enceladus.

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## 2.2 Radar Attenuation

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Radar attenuation in ice is caused by dielectric absorption losses as well as scattering losses. A common assumption in low-frequency radar sounding is that scattering losses are negligible due to the long wavelengths with respect to the scattering structures (e.g., ice grains) within the ice. Hence, attenuation purely driven by absorption losses is assumed here. Following the work of Kalousová et al. (2017) and Souček et al. (2023), we calculate the two-way attenuation along the propagation path at depth  $d$ , which was subdivided into  $N$  layers, as:

$$A_2(d) = \sum_{i=0}^N 2A_1(d_i)\Delta d \quad (3)$$

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where  $d_0$  represents the surface layer,  $d_N$  is the final layer,  $A_1(d_i)$  is the one-way attenuation at depth  $d_i$ , and  $\Delta d$  the thickness of each layer used in calculating  $A_1$ .

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The one-way attenuation  $A_1$  (in dB/km) of a radar signal is proportional to the electrical conductivity of ice ( $\sigma$ ) within the range of High Frequency (HF) and Very High Frequency (VHF) (Matsuoka et al., 2012), and can be approximated as follows:

$$A_1 \approx 0.914\sigma. \quad (4)$$

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The electrical conductivity of ice in terrestrial sounding experiments depends on the ice temperature along with the presence of chemical impurities within the ice, and can be written as follows (Corr et al., 1993):

$$\sigma = \sum_{i=0}^1 \sigma_i^0 C_i \exp \left[ -\frac{E_i}{k_B} \left( \frac{1}{T} - \frac{1}{T_r} \right) \right], \quad (5)$$

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with each contribution representing one component that affects the electrical conductivity. Each summand requires the material molar electrical conductivity  $\sigma_i$  at reference temperature  $T_r = 251$  K, molar concentration  $C_i$ , activation energy  $E_i$ , local ice temperature  $T$ , and the Boltzmann constant  $k_B$ . In this study we use the same values as in Table 1 of Souček et al. (2023). The index 0 indicates a scenario of a pure water-ice shell, while  $i = 1$  adds the effects of the maximum theoretical chloride concentration in pure water-ice (Souček et al., 2023).

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Similar to Kalousová et al. (2017) and Souček et al. (2023), we calculate the plausible attenuation ranges within Enceladus's ice shell. We use "low-loss" to indicate that the attenuation model considers only pure water ice, while the "high-loss" model is characterized by a homogeneous mixture of pure water ice and  $300 \mu\text{M}$  of chloride. The chloride concentration has been chosen based on plume material sampled during NASA's Cassini mission. Although carbonate salts, chloride, silica, and ammonia/ammonium have been detected, only chloride is expected to exist within the ice shell with significant concentrations (of up to  $300 \mu\text{M}$ ) to impact an orbital radar sounder (Souček et al., 2023).

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## 3 Results

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First, we investigate the difference between the "high" and "low" loss attenuation models in multiple 1-dimensional scenarios of Enceladus's internal structure. To this end, we calculate temperature profiles and corresponding two-way attenuation for various ice shell thicknesses, thicknesses of the porous layer, and porous layer thermal conductivities (Fig. 1).

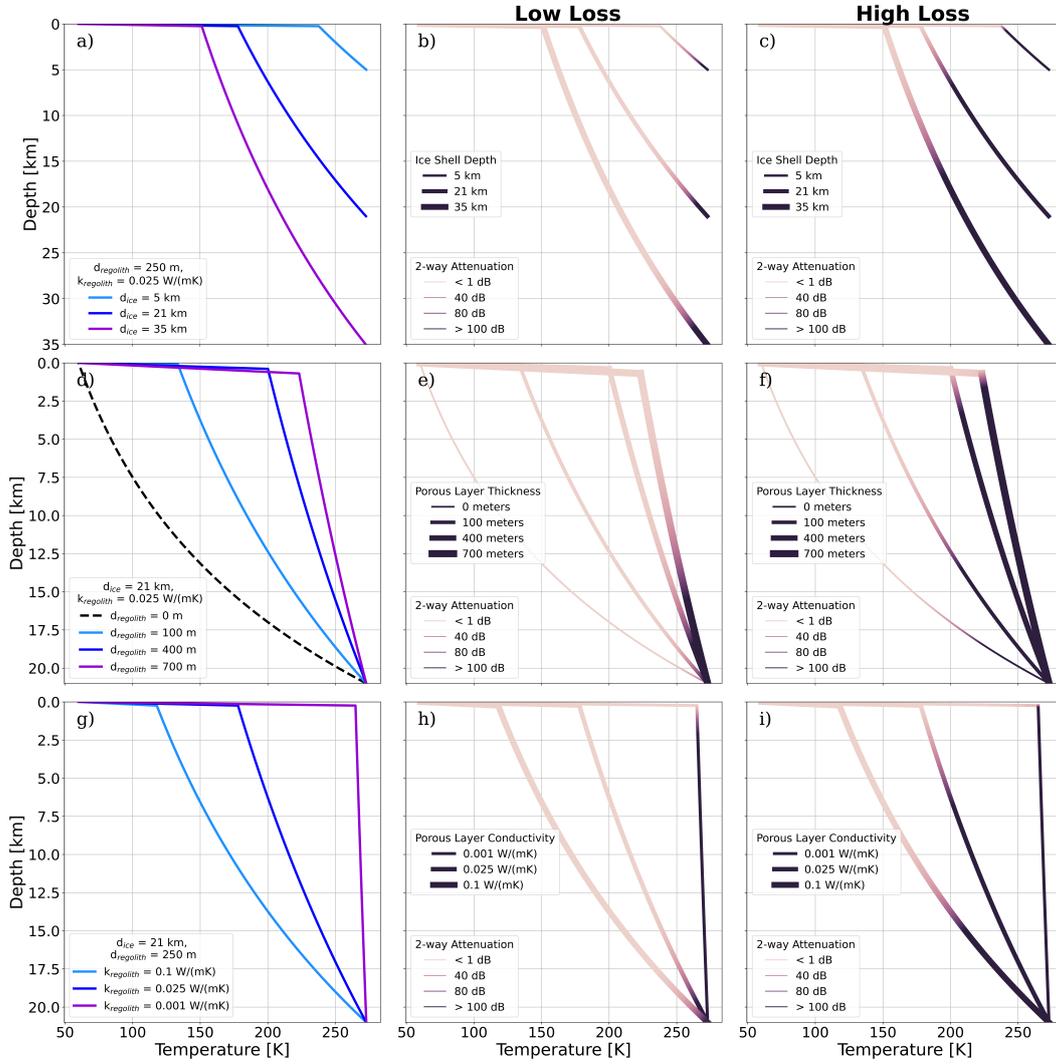
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We define a penetration depth, which is the depth at which the two-way attenuation reaches a 100 dB. The relative penetration depth is the penetration depth divided by the total ice shell thickness of the respective scenario. The relative penetration depth strongly depends on temperature, as the latter affects the electrical conductivity. For a



**Figure 1.** The two-way attenuation ( $A_2$ ) for various: a) ice shell depths (5 – 35 km), b) porous layer thicknesses (0 – 700 m), and c) porous layer thermal conductivities (0.1 – 0.001  $\text{Wm}^{-1}\text{K}^{-1}$ ). Panels d-f) show the low-loss scenarios, while panels g-i) show the high-loss cases.

153 conductive ice shell, the temperature itself depends on the thickness of the ice shell, and  
 154 to a first order on the presence of a porous layer. The porous layer leads to a high thermal  
 155 gradient near the surface due to its insulating effect caused by its low thermal conductivity.  
 156 The relative penetration depth in a low-loss scenario is 91%, 94%, and 95%,  
 157 for ice shell thicknesses of 5 km, 21 km, and 35 km, respectively. The penetration depths  
 158 relative to the total depth in the high-loss case are 16%, 33%, and 48%, for the same  
 159 ice shell thicknesses of 5 km, 21 km, and 35 km, respectively.

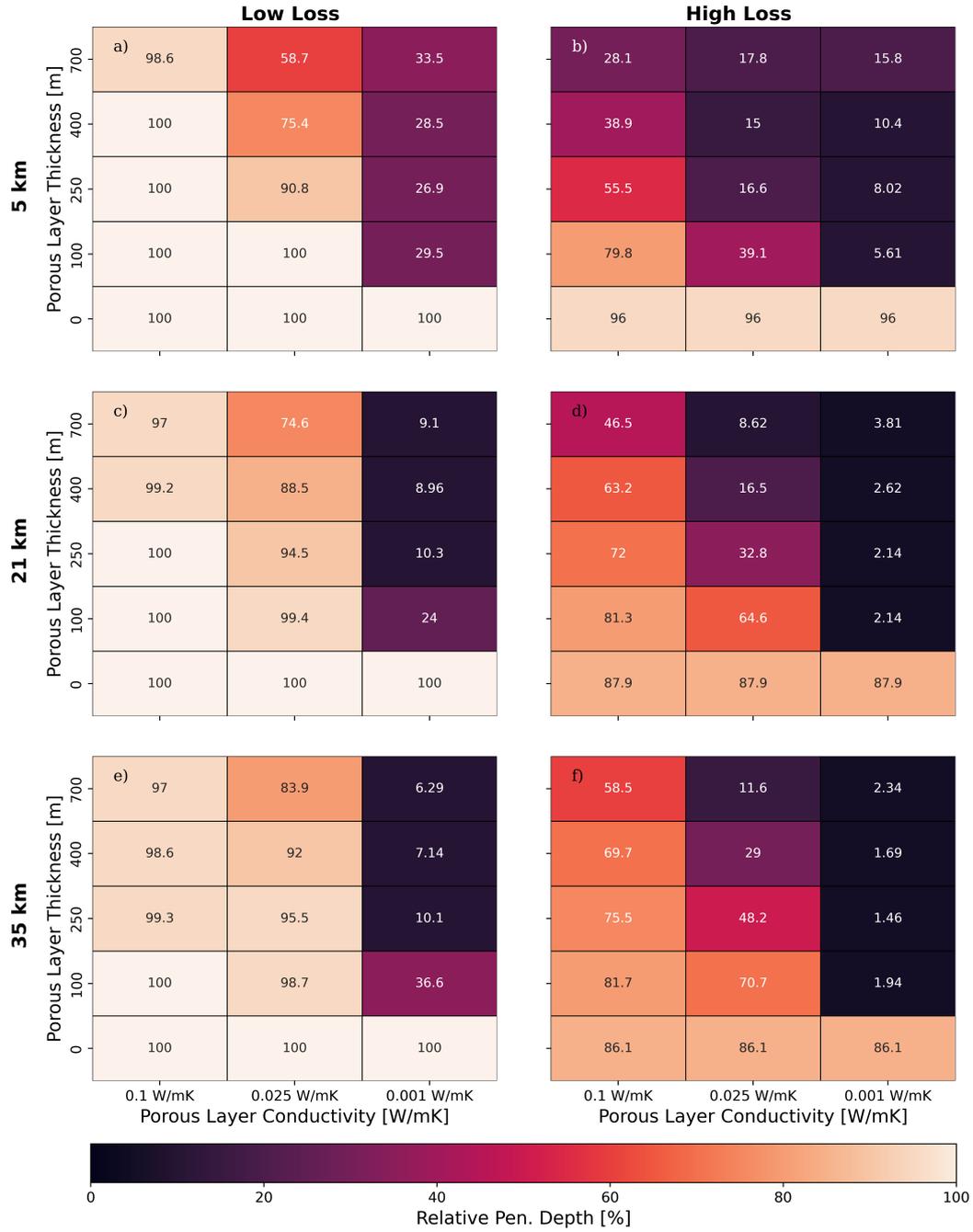
160 We can clearly observe in Fig. 1 that the attenuation dramatically increases with  
 161 increasing porous layer thickness. This can be again attributed to the insulating effect  
 162 of the porous layer, an effect that becomes more pronounced with increasing porous layer  
 163 thickness. As observed on Fig. 1d, the difference between the temperature profiles with  
 164 and without a porous layer of 700 m is as large as 150 K at shallow depth. The low-loss  
 165 scenario with no porous layer only reaches 53.4 dB at the ice-ocean interface, which was  
 166 set here to 21 km. In the low-loss scenario, the presence of a 100 m porous layer increases  
 167 the 2-way attenuation to 100 dB or higher at 99% of the ice shell depth. The relative pen-  
 168 etration depth associated with the 100 dB limit is 88% for a 400 m and 74% for a 700 m  
 169 porous layer. For the high-loss scenario, the radar attenuation increases to more than  
 170 100 dB before reaching the ice-ocean interface even when no porous layer is considered.  
 171 Thus, the relative penetration depth is 88% of the total ice shell for the no porous layer  
 172 case, 64% for the 100 m porous layer case, 16% for the 400 m case, and 8% for the 700 m  
 173 porous layer.

174 The thermal conductivity of the porous layer can significantly impact the thermal  
 175 profile within the ice shell. A highly insulating porous layer (i.e., thermal conductivity  
 176 of  $0.001 \text{ Wm}^{-1}\text{K}^{-1}$ ) with a thickness of 250 m, leads to a warm ice shell, only a few de-  
 177 grees colder than the ice-ocean interface. In the low-loss scenario, the 2-way attenuation  
 178 for the case with the highest thermal conductivity of the porous layer (i.e.,  $0.1 \text{ Wm}^{-1}\text{K}^{-1}$ )  
 179 reaches 95 dB at the ice-ocean interface. For a thermal conductivity of  $0.025 \text{ Wm}^{-1}\text{K}^{-1}$   
 180 of the porous layer, the 2-way attenuation reaches the 100 dB limit at about  $\sim 80\%$  of  
 181 the ice shell in both high- and low-loss scenarios. In the case with the most insulating  
 182 porous layer (i.e., regolith thermal conductivity of  $0.001 \text{ Wm}^{-1}\text{K}^{-1}$ ), the 2-way atten-  
 183 uation reaches 100 dB before 10% of the ice shell is penetrated in both the high and low-  
 184 loss scenarios.

185 In Fig. 2 we explore a large set of parameter combinations. Each cell represents  
 186 a single simulation (equivalent to one line graph in Fig. 1). The value inside each cell  
 187 represents the relative penetration depth. The simulations cover ice shell thicknesses of  
 188 5 km, 21 km, and 35 km, as well as the low-loss and high-loss attenuation models.

189 None of the high-loss models reach 100% relative depth penetration, even with a  
 190 5 km ice shell with no porous layer. Most simulations using a highly insulating porous  
 191 layer with a thermal conductivity of  $0.001 \text{ Wm}^{-1}\text{K}^{-1}$  reach less than 10% relative pen-  
 192 etration depth. Of the total of 90 simulations, 16 models penetrate the whole ice shell,  
 193 with those models generally having porous layers with small thicknesses and high ther-  
 194 mal conductivities.

195 As expected, every combination of parameters has a lower relative penetration depth  
 196 in the high-loss attenuation model compared to low-loss. Secondly, the relative penetra-  
 197 tion depth decreases with increasing porous layer thickness and decreasing thermal con-  
 198 ductivity. However, a trend reversal occurs (i.e., penetration depth increases) in highly  
 199 insulating porous layers (apart from the the 35 km low-loss scenarios). Such a reversal  
 200 only occurs in scenarios with both a highly conductive and very deep porous layer. This  
 201 behavior can be explained by the fact that with increasing porous layer thickness, the  
 202 thermal state of the ice shell starts to approach that of a conductive ice shell character-  
 203 ized by a single thermal conductivity. If the porous layer makes up the entire ice shell,



**Figure 2.** The relative penetration depth of a radar signal for ice shell thicknesses of 5 km (a, d), 21 km (b, e), and 35 km (c, f) and various porous layer thicknesses and thermal conductivities for low-loss (left column) and high-loss (right column) scenarios.

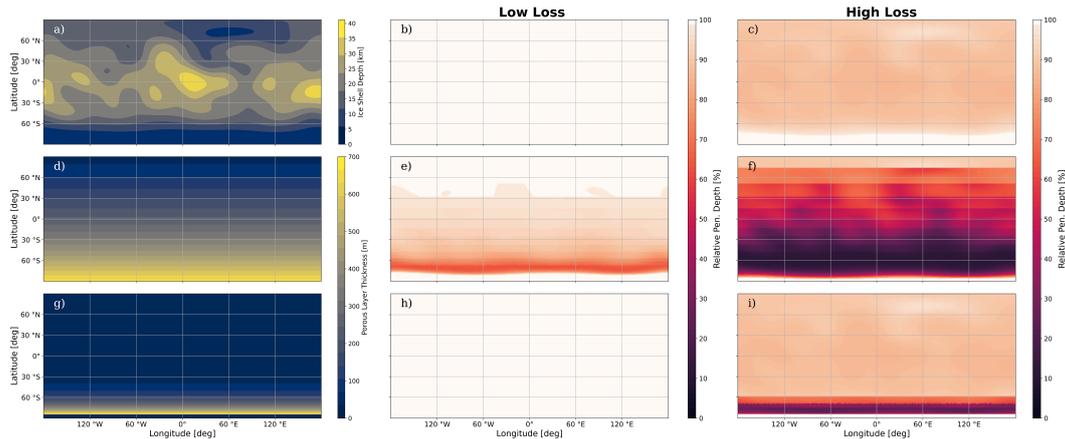
204 the steady-state thermal state will be similar to that of a homogeneous ice shell with a  
 205 thermal conductivity of pure water-ice.

206 Beyond 1-D analysis, we generate attenuation maps (Fig. 3 a)) using a global ice  
 207 shell thickness map from Hemingway and Mittal (2019), based on a shape model of Nimmo  
 208 et al. (2011), gravitational data, and assuming a density contrast between the ice shell  
 209 and the subsurface ocean of  $95 \text{ kg m}^{-3}$  similar to some of the models of (Hemingway &  
 210 Mittal, 2019). Additional attenuation maps using a different ice shell thickness, shape  
 211 model and ice-ocean density contrast are available in the Supporting Information (SI),  
 212 Section S3.

213 The attenuation was calculated by treating each data point as a single tempera-  
 214 ture profile using the corresponding ice shell thickness at the respective location. We con-  
 215 structed two distribution models for the porous layer under the assumption that the thick-  
 216 ness of the porous layer varies only with latitude and: 1) exponentially decreases from  
 217 a 700-m-thick layer at the south pole to 10-m-thick layer at the north pole of Enceladus,  
 218 which we denote as the "exponential-global distribution" (Fig. 3 b) while 2) the porous  
 219 layer is absent within the  $5^\circ$  of the south pole and then exponentially decreases from 255 m  
 220 to 0 m at equator (Fig. 3 c), which we will call "exponential-hemispheric distribution".  
 221 In all cases the conductivity of the porous layer is  $0.025 \text{ W m}^{-1} \text{ K}^{-1}$ .

222 In the low-loss attenuation maps (Fig. 3 d, e, and f), a majority of the surface has  
 223 more than 90% relative penetration depth, with both the no-porous-layer and the exponential-  
 224 hemispheric distribution cases having 100% global radar penetration down to the ice-  
 225 ocean interface. In all three high-loss scenarios, we observe a small band of 100% rela-  
 226 tive penetration depth roughly  $5^\circ$  in latitude away from the south pole. The thin ice shell  
 227 at the south pole allows for the signal to reach the ice-ocean interface even in the pres-  
 228 ence of a thick porous layer (i.e., 700 m in the exponential-global distribution case).

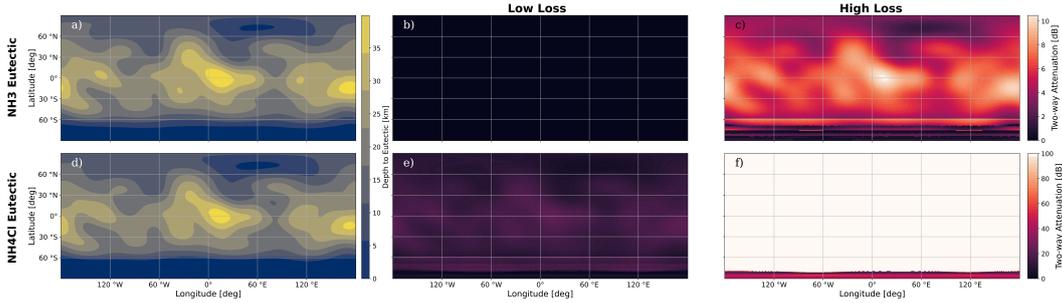
229 We note that in all cases besides the high-loss exponential-global distribution case,  
 230 the penetration depth reaches more than 80% of the ice shell for most locations.



**Figure 3.** Maps of the: a) ice shell thickness (Hemingway & Mittal, 2019) and porous layer distribution for b) the "exponential-global scenario" and c) the "exponential-hemispheric scenario" (see text). The radar penetration depth relative to the ice shell thickness in panel a) is shown for d) no porous layer, e) exponential-global and f) exponential-hemispheric distribution of the porous layer. Panels g), h) and i) show the high-loss cases.

231 In Fig. 4, we calculate the two-way attenuation at the eutectic interfaces of am-  
 232 monium chloride and ammonia following Souček et al. (2023) for the exponential-hemispheric  
 233 distribution of the porous layer (i.e., exponential decrease from 255 m at 85°S to 0 m at  
 234 equator) and assuming a thermal conductivity of the porous layer of  $0.025 \text{ Wm}^{-1}\text{K}^{-1}$ .

235 The eutectic interface of ammonium chloride ( $\text{NH}_4\text{Cl}$ ) is defined by the 257.79 K  
 236 isotherm, while the one for ammonia ( $\text{NH}_3$ ) by the 175.45 K isotherm (Marion et al., 2012).  
 237 Panels a and b of Fig. 4 show the depths at which the eutectic of  $\text{NH}_3$  and  $\text{NH}_4\text{Cl}$ , re-  
 238 spective, are reached. Fig. 4 c and d show the two-way attenuation for the low-loss at-  
 239 tenuation models, while the values obtained for the high-loss cases are shown in Fig. 4  
 240 e and f. Additional maps including different ice shell thicknesses and porous layer dis-  
 241 tribution are available in the SI (Section S4).



**Figure 4.** Maps showing the depth of: a) ammonia ( $\text{NH}_3$ ) and b) ammonium chloride ( $\text{NH}_4\text{Cl}$ ) eutectic interface for the exponential-hemispheric distribution of the porous layer. Panels c) and d) indicate the corresponding two-way attenuation values for the low-loss case at the eutectic interface of  $\text{NH}_3$  and  $\text{NH}_4\text{Cl}$ , respectively. Panels e) and f) are similar to c) and d), but for the high-loss scenarios.

242 The difference between the average depth of the ice-ocean interface and the aver-  
 243 age depth of the  $\text{NH}_4\text{Cl}$  eutectic interface is only 700 m. This is due to the fact that the  
 244 temperature of the  $\text{NH}_4\text{Cl}$  eutectic interface is only 20 K lower than the melting tem-  
 245 perature of water-ice at the base of the ice shell shown in Fig. 4 a. In contrast, the dif-  
 246 ference between the average depth of the ammonia eutectic interface and that of the ice-  
 247 ocean interface is 5 km, as  $\text{NH}_3$  has a much lower eutectic temperature of only 175.45 K.  
 248 Given the low eutectic temperature of  $\text{NH}_3$ , the two-way attenuation for the low-loss case  
 249 (Fig. 4 c) does not exceed 0.1 dB. For the eutectic interface of  $\text{NH}_4\text{Cl}$ , the two-way at-  
 250 tenuation shows an average value 13.7 dB in the low-loss scenario (Fig. 4 d). In the high-  
 251 loss attenuation case, the two-way attenuation at the eutectic interface of  $\text{NH}_3$  is only  
 252  $\sim 5$  dB (Fig. 4 e), while at the eutectic interface of  $\text{NH}_4\text{Cl}$  the average two-way at-  
 253 tenuation is about 400 dB (Fig. 4 f).

## 254 4 Discussion

255 Similar to other studies (Kalousová et al., 2017; Souček et al., 2023), we assume  
 256 a threshold of 100 dB for the two-way radar attenuation, above which the radar instru-  
 257 ment would no longer be able to detect subsurface interfaces. However, we note that this  
 258 threshold is only an estimate, that might change in a mission scenario depending on the  
 259 instrument design, operation scenarios, as well as surface and subsurface characteristics  
 260 (see e.g., Kalousová et al., 2017; Benedikter et al., 2024)[ for a detailed discussion]. Our  
 261 tests show that varying the two-way attenuation limit between 70 and 130 dB would not  
 262 significantly impact the results presented in Fig. 2. In these cases we observe a differ-

263 ence to the relative penetration depth shown in Fig. 2 of up to only 10% (see Fig. S1.1–  
264 S1.2 in the SI).

265 On Enceladus, the surface temperature lies between 60 and 85 K, the latter values  
266 being representative for the south polar region (Spencer et al., 2006). We tested the ef-  
267 fects of a higher surface temperature (i.e., 85 K) on our calculated radar attenuation val-  
268 ues (Fig. S2.1). A higher surface temperature shifts the ice shell temperature to higher  
269 values and leads to a smaller relative penetration depth. However the differences between  
270 using a surface temperature of 85 K compared to 60 K are only of the order of 2 – 4%.

271 We note that our study assumes simple distributions of a porous layer on Ence-  
272 ladus to give a first order overview of the potential detection of the ice-ocean interface  
273 via radar sounding. While our results show that the ice-ocean interface will be challeng-  
274 ing to detect in particular in regions covered by thick and highly thermal insulating porous  
275 layers, we note that large uncertainties exist for the global spatial distribution of such  
276 a porous layer on Enceladus. While models of the distribution of a porous layer on Ence-  
277 ladus exist (Kempf et al., 2010; Southworth et al., 2019), they typically investigate only  
278 the generation of such a layer through plume deposition. Such models indicate that tec-  
279 tonized regions on the leading and trailing hemispheres receive the least amount of mater-  
280 ial deposition, but that the plume eruption style (i.e., curtain-like vs. jet-like) affects  
281 the amount of snow deposits in the northern hemisphere (Southworth et al., 2019). The  
282 predicted distribution of a material deposition from models of jet-style eruptions seem  
283 to be consistent with the distribution of pit chains on the surface of Enceladus. The lat-  
284 ter, however, can only give a lower bound for the thickness of the porous layer, as the  
285 pits do not necessarily need to reach the base of the layer (Martin et al., 2023).

286 Another important factor that will affect the thermal state of the ice shell and hence  
287 the two-way attenuation is the thermal conductivity of the porous layer. A recent study  
288 by Jabaud et al. (2024) investigated the mechanical properties of powder-like materials  
289 similar to the expected snow deposits on Enceladus that are also suggested to exist to  
290 some extent on Europa. This study concluded that on Enceladus, the lower gravity leads  
291 to higher cohesion and the formation of loose, highly porous material. A high porosity  
292 is directly linked to a low thermal conductivity and thus highly insulating behavior. As  
293 shown in this study, an insulating porous layer would increase the ice shell temperature  
294 such that the resulting temperature contrast between the base of the porous layer and  
295 the ocean may be only 10s of degrees K. Such high average temperatures could result  
296 in the formation of shallow brines that could provide a radar-detectable source (Souček  
297 et al., 2023). Our models show that even in the presence of thick porous layers, the two-  
298 way radar attenuation remains below 25 dB for eutectic interfaces of  $\text{NH}_3$  and  $\text{NH}_4\text{Cl}$   
299 in the low-loss scenario. In the high-loss cases, only the  $\text{NH}_4\text{Cl}$  interface lies above the  
300 100 dB threshold for most of the ice shell apart from within about  $5^\circ$  of the south pole.  
301 As these eutectic interfaces are defined by isotherms, their detection would provide valu-  
302 able information about the thermal state of the ice shell and may help reconstructing  
303 not only the ice shell thickness (see discussion in Souček et al., 2023) but also the thick-  
304 ness of the porous layer that strongly affects the temperature in the ice shell and hence  
305 the depth of these interfaces.

306 This study has focused on the effect of a porous layer on two-way attenuation in  
307 a conductive ice shell. Future studies will test how such a porous layer, its thickness and  
308 spatial distribution, affects the ice shell dynamics and in particular the two-way radar  
309 attenuation for hot upwellings and cold downwellings. Depending on the ice shell tem-  
310 perature, cold downwellings could represent locations where the radar attenuation is low  
311 enough such that the ice-ocean interface may be reached, as previously discussed for Eu-  
312 ropa (Kalousová et al., 2017).

## 5 Conclusions

In this study we showed that a porous layer built up by the deposition of material from Enceladus's south pole plume or generated by impacts has a first order effect on the two-way radar attenuation. This porous layer acts as an insulation layer leading to high sub-surface temperatures and thus two-way attenuation. Through systematic parameter variations, we provide an extensive overview of the effects of a porous layer on the ability to reach the ice-ocean as well as other interfaces within the ice shell that are thought to exist based on the inferred ice shell chemistry.

Our investigations show that radar sounder instruments may penetrate anywhere from a few hundred meters to the entire ice shell of Enceladus. Nevertheless, those scenarios that prevent radar signals from reaching the ice ocean interface can provide valuable information about the ice shell. Identifying aspects of the Enceladus system that could prevent ocean detection may prove fundamental in further characterizing icy worlds. Valuable insights may be gained, such as the existence of near-surface liquid reservoirs, which are very likely for cases with high salt content and a porous layer on top that keeps the interior comparatively warm. Such brine reservoirs are considered niches for life, and their potential to be directly accessible by future missions is much greater compared to that of the subsurface oceans.

## 6 Open Research

Additional calculations including different ice shell thicknesses are available in the Supplementary Information. All data used in the figures and the code necessary to reproduce the calculations are available on Zenodo (Byrne et al., 2024)

## Acknowledgments

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*Geophysical Research Letters*

Supporting Information for

**Radar Attenuation for Subsurface Sounding on Enceladus:  
Effects of a Porous Ice Layer**

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**Contents of this file**

1. Two-way attenuation threshold
2. Surface temperature effects
3. Map of relative penetration depth
4. Depth to eutectic interfaces

**Additional Supporting Information (Files uploaded separately)**

1. Additional data sets and python scripts available on Zenodo repository

## Introduction

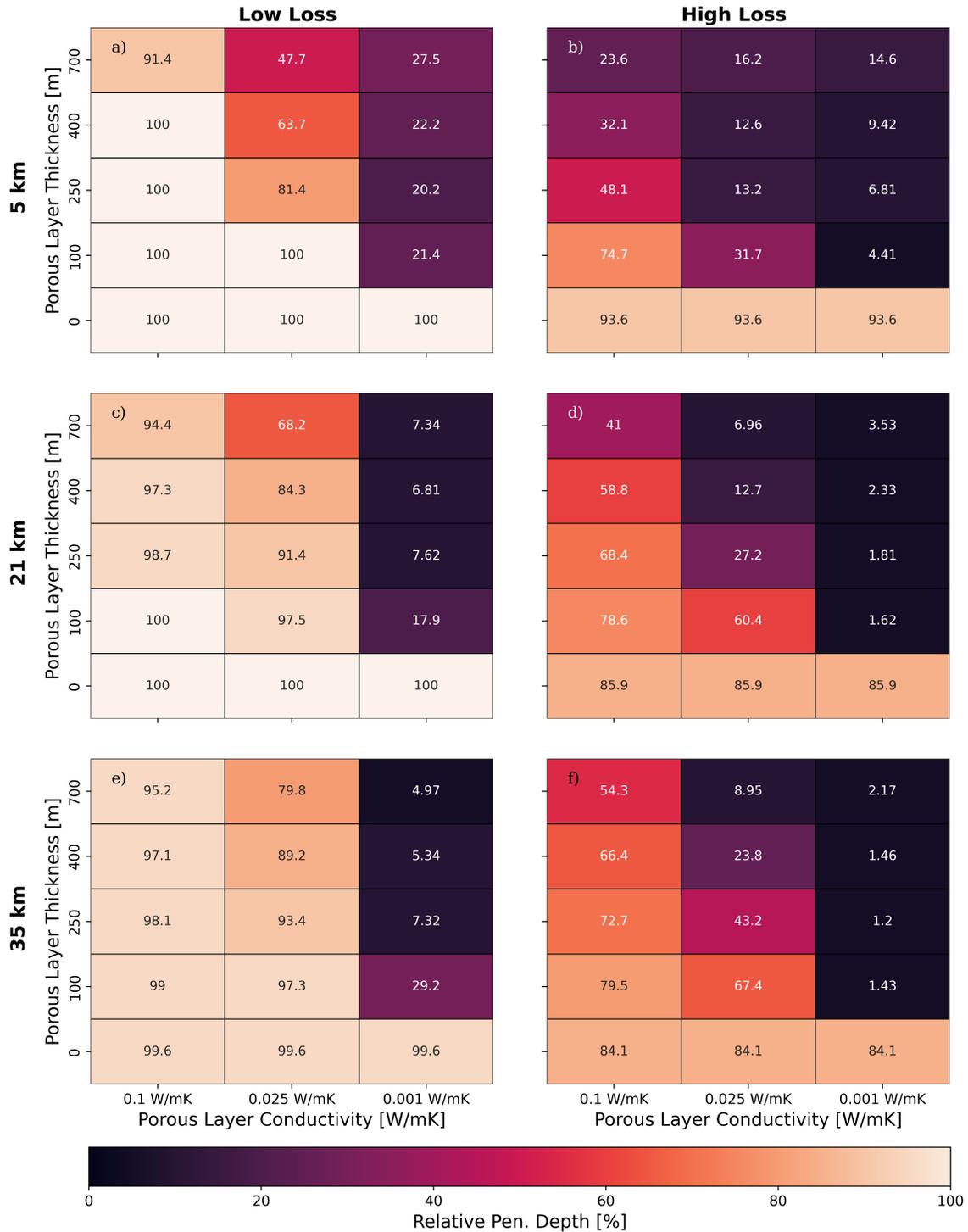
In this supplementary information we present additional calculations to those discussed in the main manuscript of "Radar Attenuation for Subsurface Sounding on Enceladus: Effects of a Porous Ice Layer". In section S1 we show the effects of using a threshold of 70 dB and 130 dB for the two-way radar attenuation, above which the radar signal will not be able to detect subsurface interfaces. As a comparison, Fig. 2 in the main manuscript uses a threshold of 100 dB (*Kalousová et al., 2017; Souček et al., 2023*). In section S3 we calculate the relative penetration depth of the two-way radar attenuation for a different ice shell thickness model that uses the shape model of *Tajeddine et al. (2017)*, an ice density of  $900 \text{ kg m}^{-3}$ , and an ocean density of  $1100 \text{ kg m}^{-3}$  that lead to more subtle ice shell thickness variations compared to the map in Fig. 3 of the main manuscript. Section S4 shows the depth of the ammonia and ammonium chloride eutectic interfaces similar the Fig. 4 of the main manuscript, but using an "exponential-global distribution" of the porous ice layer.

### S1 Two-way attenuation threshold

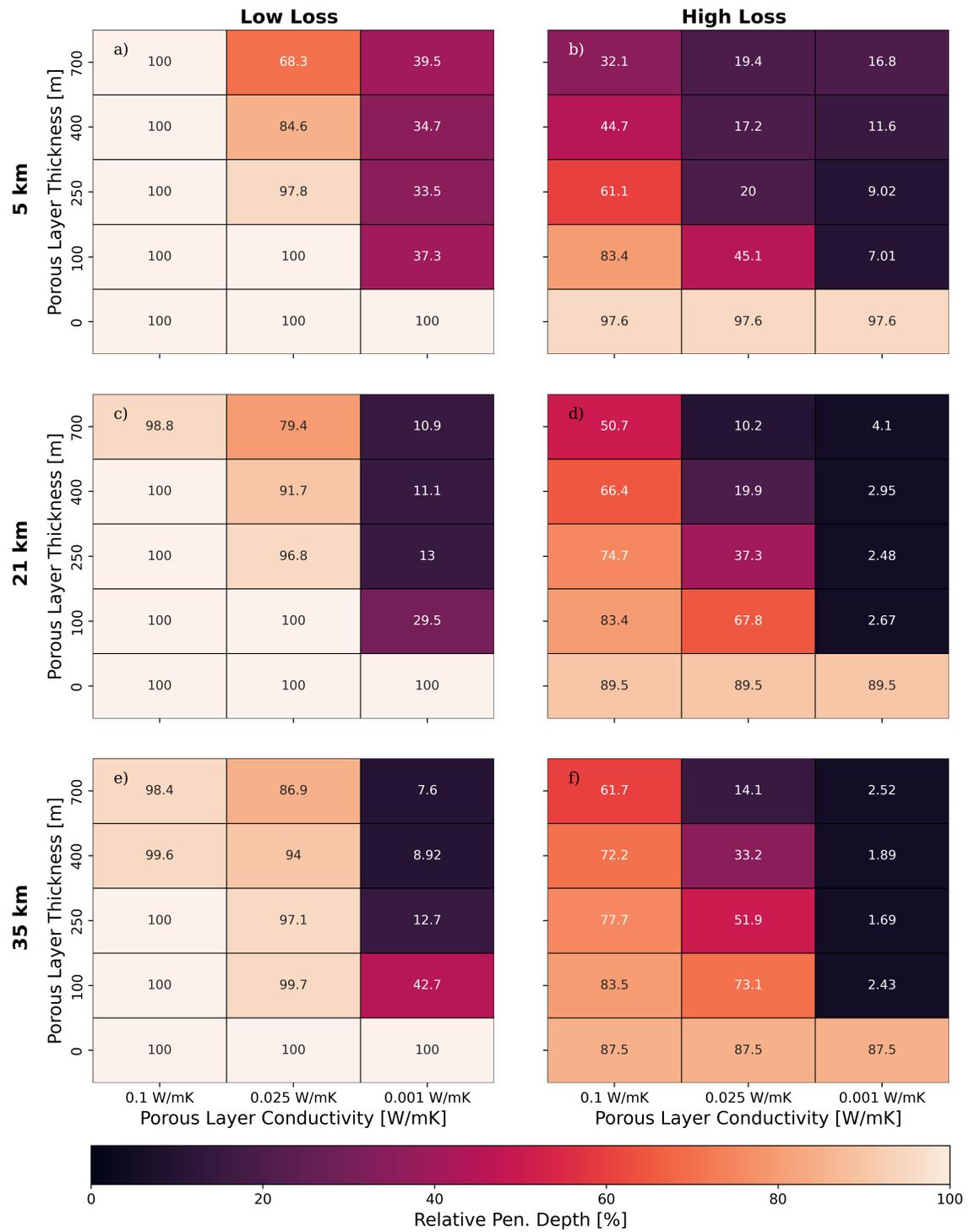
Here we performed sensitivity tests for the relative penetration depth of the two-way radar attenuation. Using the same set of models as discussed in Fig. 2 of the main manuscript, we computed the relative penetration depth of the two-way radar attenuation by assuming a 30% lower and higher threshold than the 100 dB value typically used in literature (*Kalousová et al., 2017; Souček et al., 2023*). Our models show that a threshold of 70 dB (Fig. 1.1) or 130 dB (Fig. 1.2) would only change the relative penetration depth by at most 10% compared to the results obtained when using a threshold value of 100 dB.

### S2 Surface temperature effects

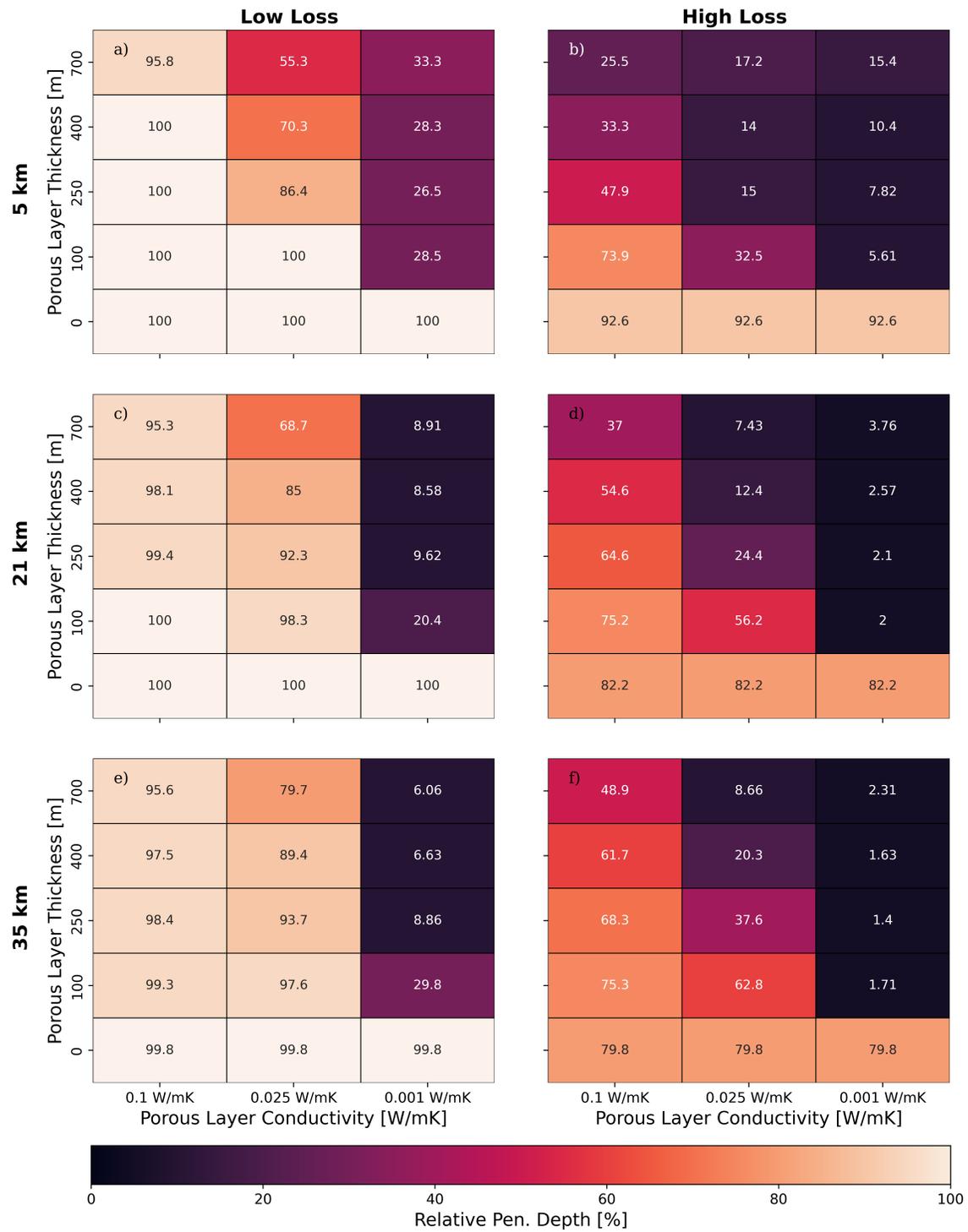
In this section, we test the effects of a higher surface temperature on the two-way radar attenuation, since on Enceladus the surface temperature varies between 60 and 85 K according to the data collected by the Cassini Composite Infrared Spectrometer (CIRS) (*Spencer et al., 2006*). To this end, we used a surface temperature of 85 K (Fig. 2.1). When compared to Fig. 2 of the main manuscript, our results show that a higher surface temperature (85 K instead of 60 K) leads to at most 2 – 4 % decrease in the relative penetration depth.



**Figure 1.1:** Systematic investigation of the relative penetration depth of a radar signal for ice shell thicknesses of 5 km (a, d), 21 km (b, e), and 35 km (c, f) and various porous thicknesses and thermal conductivities for low loss (left column) and high loss (right column) scenarios using a threshold for the two-way radar attenuation of 70 dB.



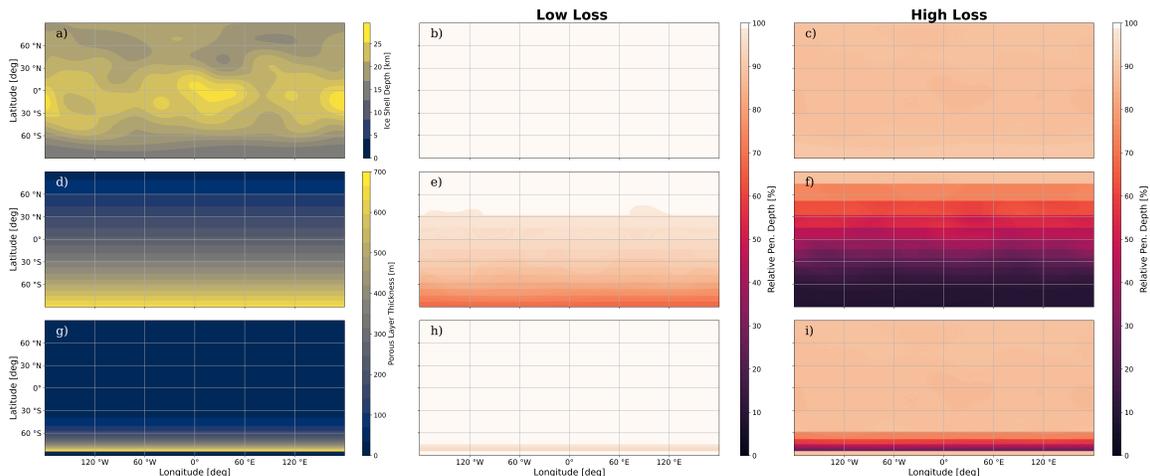
**Figure 1.2:** Similar as Fig. 1.1, but using a threshold for the two-way radar attenuation of 130 dB.



**Figure 2.1:** Similar as Fig. 2 in the main manuscript, but using a surface temperature of 85 K.

### S3 Map of relative penetration depth

Here we repeat the analysis of the relative penetration depth presented in the main manuscript with and without the presence of a porous ice layer of various thickness for a more homogeneous ice shell thickness (Fig. 3.1). To this end, we chose the ice shell thickness model of *Hemingway and Mittal (2019)* that uses the shape model of *Tajeddine et al. (2017)*, an ice density of  $900 \text{ kg m}^{-3}$ , and an ocean density of  $1100 \text{ kg m}^{-3}$ .

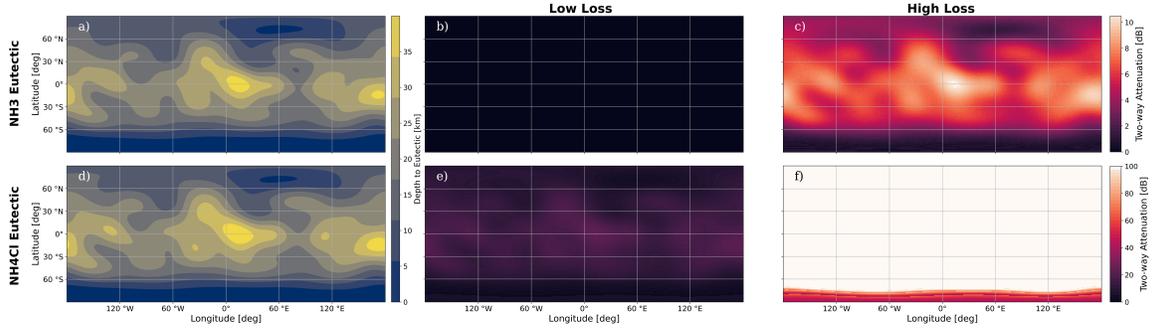


**Figure 3.1:** Maps of the: a) ice shell thickness *Hemingway and Mittal (2019)*, b) porous layer distribution for b) the "exponential-global distribution" (i.e., exponential decay from 700 m at the south pole to 20 m at the north pole), c) the "exponential-hemispheric distribution" (i.e., exponential decay from 255 m at  $85^\circ\text{S}$  to 0 m at the equator). The radar penetration depth relative to the ice shell thickness in panel a) is shown for d) no porous layer, e) exponential-global and f) exponential-hemispheric distribution of the porous layer. Panels g), h) and i) are similar to d), e), and f), but show the high-loss cases.

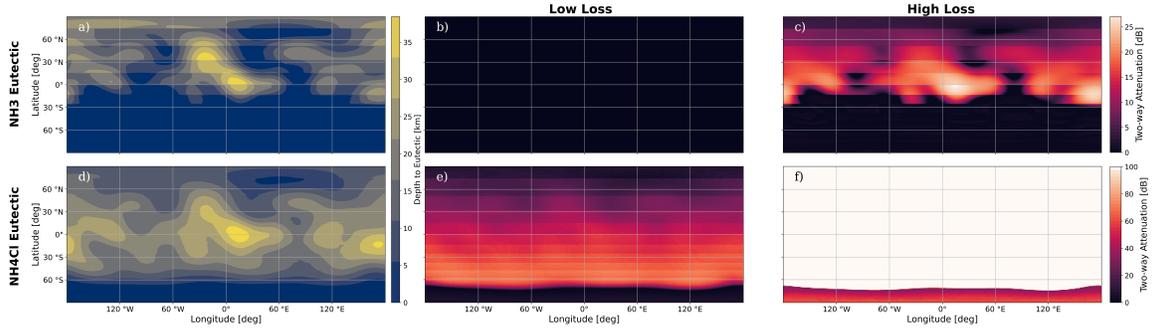
Given the thicker ice shell at the south pole in this scenario compared to the map shown in Fig. 3 of the main manuscript, in none of the high-loss scenarios, with or without the presence of a porous ice layer, 100% relative penetration depth is reached. In the low-loss scenarios, the relative penetration depth reaches 100% almost everywhere for the "no regolith" and the "exponential-hemispheric distribution" cases. For the "exponential-global distribution" scenario the relative penetration depth reaches 100% only for latitudes higher than  $30^\circ\text{N}$ .

### S4 Depth to eutectic interfaces

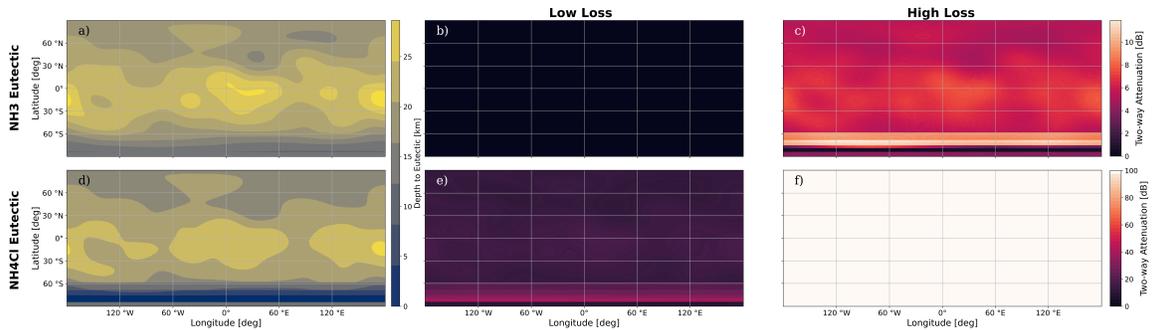
In the following plots, we show maps containing the depth to the ammonia and ammonium chloride eutectic interfaces similar as in Fig. 4 of the main manuscript, but now using different ice shell thicknesses and distributions of the porous ice layer. The results show that in the low-loss scenario, the eutectic interfaces can be reached before the two-way attenuation increases to 100 dB, independently of the ice shell thickness or porous layer distribution. In the high-loss scenario, the eutectic interface of ammonium chloride is difficult to detect, unless the ice shell is thin (i.e., around 5 km, cf. Fig. 4.2).



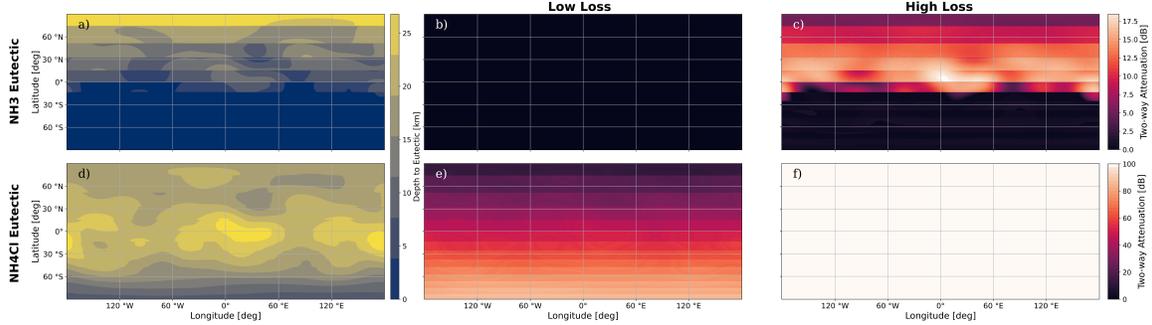
**Figure 4.1:** Maps showing the depth of: a) ammonia ( $\text{NH}_3$ ) and b) ammonium chloride ( $\text{NH}_4\text{Cl}$ ) eutectic interface for the same ice shell thickness used in Fig. 4 of the main manuscript but now without a porous ice layer. Panels c) and d) indicate the corresponding two-way attenuation values for the low-loss case at the eutectic interface of  $\text{NH}_3$  and  $\text{NH}_4\text{Cl}$ , respectively. Panels e) and f) are similar to c) and d), but for the high-loss scenarios.



**Figure 4.2:** Same as Fig. 4.1 but using the "exponential-global distribution" of the porous ice layer. Panels c) and d) indicate the corresponding two-way attenuation values for the low-loss case at the eutectic interface of  $\text{NH}_3$  and  $\text{NH}_4\text{Cl}$ , respectively. Panels e) and f) are similar to c) and d), but for the high-loss scenarios.



**Figure 4.3:** Same as Fig. 4.2 for the "exponential-hemispheric distribution" of the porous ice layer and a more homogeneous ice shell thickness that uses the shape model of *Tajeddine et al. (2017)* and assumes a density difference between the ice and ocean of  $200 \text{ kg m}^{-3}$  (*Hemingway and Mittal, 2019*).



**Figure 4.4:** Same as Fig. 4.4 using an "exponential-global distribution" of the porous ice layer.

## S5 Datasets

Additional datasets and the python scripts to reproduce the results presented in the main manuscript and supplementary material are available on Zenodo *Byrne et al. (2024)*.

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