

# Neimark-Sacker, flip and transcritical bifurcation in a symmetric system of difference equations with exponential terms

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## Abstract

In this paper, we study the conditions under which the following symmetric system of difference equations with exponential terms: 
$$\begin{cases} x_{n+1} = a_1 \frac{y_n}{b_1 + y_n} + c_1 \frac{x_n e^{k_1 - d_1 x_n}}{1 + e^{k_1 - d_1 x_n}}, \\ y_{n+1} = a_2 \frac{x_n}{b_2 + x_n} + c_2 \frac{y_n e^{k_2 - d_2 y_n}}{1 + e^{k_2 - d_2 y_n}} \end{cases}$$
 where  $a_i, b_i, c_i, d_i, k_i$ , for  $i=1,2$ , are real constants and the initial values  $x_0, y_0$  are real numbers, undergoes Neimark-Sacker, flip and transcritical bifurcation. The analysis is conducted applying center manifold theory and the normal form bifurcation analysis.

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