The 2021 Antarctic Total Eclipse: Ground Magnetometer and GNSS Wave Observations from the 40 Degree Magnetic Meridian

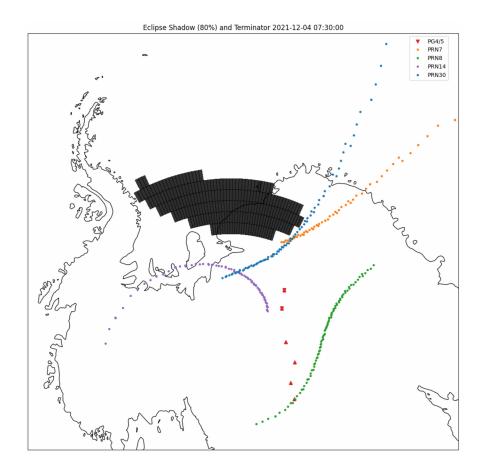
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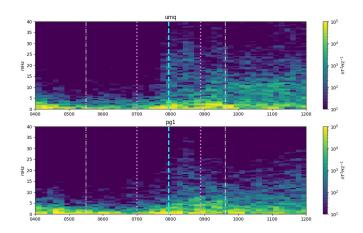
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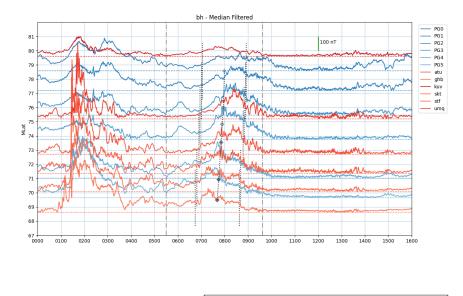
December 7, 2022

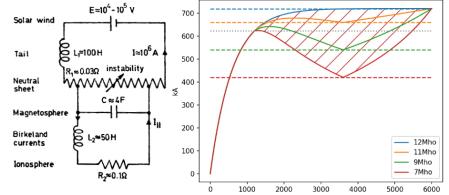
Abstract

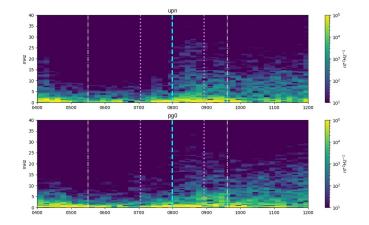
On December 04, 2021, a total solar eclipse occurred over west Antarctica. Nearly an hour beforehand, a geomagnetic substorm onset was observed in the northern hemisphere. Eclipses are suggested to influence magnetosphere-ionosphere (MI) coupling dynamics by altering the conductivity structure of the ionosphere by reducing photoionization. This sudden and dramatic change in conductivity is not only likely to alter global MI coupling, but it may also introduce a variety of localized instabilities that appear in both hemispheres. Global navigation satellite system (GNSS) based observations of the total electron content (TEC) in the southern high latitude ionosphere during the December 2021 eclipse show signs of wave activity coincident with the eclipse peak totality. Ground magnetic observations in the same region show similar activity, and our analysis suggest that these observations are due to an "eclipse effect" rather than the prior substorm. We present the first multi-point interhemispheric study of a total south polar eclipse with local TEC observational context in support of this conclusion.











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2	Magnetometer and GNSS Wave Observations from the
3	40 Degree Magnetic Meridian
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11	Key Points:

12	•	A total solar eclipse occurred over Antarctica on December 4, 2021 alongside a ge-
13		omagnetic substorm
14	•	Variations in total electron content (TEC) are spatiotemporally correlated with
15		eclipse shadow peak
16	•	Similar ground magnetic variations are observed in both hemispheres, suggesting
17		eclipse driven waves

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18 Abstract

On December 04, 2021, a total solar eclipse occurred over west Antarctica. Nearly an 19 hour beforehand, a geomagnetic substorm onset was observed in the northern hemisphere. 20 Eclipses are suggested to influence magnetosphere-ionosphere (MI) coupling dynamics 21 by altering the conductivity structure of the ionosphere by reducing photoionization. This 22 sudden and dramatic change in conductivity is not only likely to alter global MI cou-23 pling, but it may also introduce a variety of localized instabilities that appear in both 24 hemispheres. Global navigation satellite system (GNSS) based observations of the to-25 tal electron content (TEC) in the southern high latitude ionosphere during the Decem-26 ber 2021 eclipse show signs of wave activity coincident with the eclipse peak totality. Ground 27 magnetic observations in the same region show similar activity, and our analysis suggest 28 that these observations are due to an "eclipse effect" rather than the prior substorm. We 20 present the first multi-point interhemispheric study of a total south polar eclipse with 30

³¹ local TEC observational context in support of this conclusion.

32 Plain Language Summary

Solar eclipses occur when the Moon intersects the line between the Earth and the 33 Sun. This configuration of Sun and Moon presents a unique opportunity to investigate 34 the effects of the upper atmosphere's electrical conductivity on plasma waves that is in-35 dependent of season or geomagnetic field orientation. We present observations of plasma 36 waves in the high latitude region of Earth's upper atmosphere during the eclipse on De-37 cember 04, 2021. These waves are similar to those else-wise observed near dawn in re-38 gions where the magnetic field lines connect to dark skies in one hemisphere and sun-39 lit skies in the other. We suggest that the waves observed during the December 2021 eclipse 40 have a similar generation mechanism to those that occur near dawn, a result of the dif-41 ference in conductivities between magnetic field-line footprints. 42

43 1 Introduction

Solar eclipses provide an opportunity to study ionospheric dynamics in a way un-44 like any other. The majority of the sun's direct energy link into Earth's atmosphere is 45 rapidly turned off and on again, and the impact of such a modulation is profound. Any-46 one who has experienced an eclipse from under the track of totality in person can attest 47 to the dramatic temperature swings that occur from the momentary absence of sunlight. 48 From the perspective of the global atmospheric system, the effects are equally notewor-49 thy. Not only does an eclipse directly affect the thermosphere (McInerney et al., 2018; 50 Li et al., 2021), but the obscuration related reduction in photoionization undoubtedly 51 impacts the ionospheric composition (and therefore dynamics) as well (X. Chen et al., 52 2021; Dang et al., 2018). As a result of changes to the ionosphere's local total electron 53 content (TEC), currents flowing within the ionosphere should also be modified by an eclipse. 54 However, the exact physical description of how these currents are modified is an unset-55 tled question, particularly in polar regions where data coverage is sparse and eclipses are 56 relatively rare. It is therefore necessary for multi-point observations supported by mod-57 elling efforts to advance our understanding of eclipse related effects. 58

Several studies have suggested that ionosphere-thermosphere (IT) dynamics will 59 be altered during an eclipse. One of the main drivers of these modified dynamics (at least 60 at mid to low latitudes) is expected to be changes in the neutral wind structure that cre-61 ate counteracting flows in opposition to the regular wind dynamo (Aa et al., 2020; Choud-62 hary et al., 2011; St.-Maurice et al., 2011). Because of coupling between the ionosphere 63 and thermosphere, the normal evolution of the ionospheric electrojets are likely to be impacted as well by deviations in neutral winds. Couple this again with the well known 65 reduction in photoionization that results from the lunar umbra, and a significant change 66 in local ionospheric currents is the inevitable result. 67

An important facet of this modification of ionospheric currents is how this seem-68 ingly localized process can affect the global current systems. Because both ionospheres 69 in the northern and southern hemispheres are magnetically coupled via the geomagnetic 70 field, it follows that a changing current system in one may affect the other. Indeed, mod-71 elling efforts by Le et al. (2020) and X. Chen et al. (2021) as well as work by Zhang et 72 al. (2020) show that variations in electron density and temperature at a particular point 73 in one hemisphere can also impact the conjugate point in the other hemisphere. Regard-74 less of hemisphere, these eclipse-induced changes in ionospheric electron density are known 75 to have measurable impacts on human technology by affecting radio wave propagation 76 (Moses et al., 2021; Frissell et al., 2018), and are therefore worth further investigation. 77

Despite having a long history of study (Stening et al., 1971), ground based mag-78 netic observations from previous eclipses have presented an inconclusive picture of the 79 expected response to the moon's passing. Momani et al. (2011) reported on the previ-80 ous Antarctic total solar eclipse in 2003, showing a variation in the north-south compo-81 nent coincident with the eclipse signifying a change in the auroral electrojet overhead. 82 Ladynin et al. (2011) presented a change in the north-south component from an eclipse 83 in 2008. However, neither they nor Korte et al. (2001) could present an clearly identi-84 fiable response to the August 1999 eclipse. One reason for this discrepancy may have been 85 the creation of hemispherically asymmetric current systems (Korte et al., 2001). Indeed, 86 there are likely many factors at play that determine how much and in what ways an eclipse 87 will impact ionospheric dynamics (and the corresponding magnetic signature), as sug-88 gested by Stankov et al. (2017) and Verhulst and Stankov (2020). 89

One of the unique features of this study is the investigation of wave-like structures 90 91 that are apparently associated with the eclipse totality. These waves, as observed by groundbased magnetometers, fall into the ultra-low frequency (ULF) classification as in Jacobs 92 et al. (1964). Many studies have been conducted on the properties of ULF waves at high 93 latitudes (Simms et al., 2006; Martines-Bedenko et al., 2018; V. Pilipenko et al., 2015; 94 V. A. Pilipenko et al., 2019; Constantinescu et al., 2009) in order to characterize their 95 behavior. Furthermore, much has been published on the mechanisms that drive ULF waves 96 in the magnetosphere (Anderson, 1993; Turc et al., 2022; Takahashi et al., 2021). How-97 ever, because the eclipse's most notable feature is an absence of ionospheric photoion-98 ization, eclipses provide a unique opportunity to study less well documented ULF wave 99 driving conditions. 100

The particular eclipse occurring on December 4, 2021 is rare in that it occurred at 101 the high southern latitudes where total eclipses are often separated by nearly 20 years. 102 While this is not the first time observations were made of an eclipse occurring over Antarc-103 tica, previous studies relied on a limited number of observing stations. This study is the 104 first to utilize a large meridional array of magnetically conjugate instrument platforms 105 in both hemispheres to provide magnetic observations in unprecedented detail. It is also 106 the first to provide local TEC observations from the East Antarctic plateau as context 107 for the magnetic variations. 108

¹⁰⁹ 2 Methodology

The focus of this study is to present observations of phenomena associated with 110 the eclipse and coincident substorm from the vantage point of an array of instruments 111 located along the 40 degree magnetic meridian in both Antarctica and Greenland. A com-112 parison of models with and without an eclipse is conducted to give context on the ex-113 pected response in TEC. This is then qualitatively compared to the raw line-of-sight (some-114 times called "slant") TEC observations from Antarctica to confirm expected modifica-115 tion of ionospheric conductivity. Trends in TEC before and after the local eclipse total-116 ity are identified on a satellite by satellite basis. The most dramatic impacts are expected 117 to occur at low elevations looking in the direction of the totality, thereby sensing the largest 118

portion of the ionosphere covered by the shadow. Raw slant TEC data is shown with
 model TEC integrated along the ray path from ground to space. Additionally, spectro grams are also generated from the raw TEC measurements.

The other unique facet of this observational campaign stems from magnetometer measurements in both hemispheres. Short-time Fourier transform (STFT) spectrograms are created for each of the magnetically conjugate station pairs and an analysis of activity during the local eclipse window is conducted. Additionally, search-coil magnetometer measurements from the southern hemisphere stations are reviewed to provide additional context. These observations are then compared to nearby TEC measurements to draw conclusions about the source of any activity therein.

2.1 Ionosphere Modeling

The effects of the solar eclipse were simulated with the Thermosphere-Ionosphere-130 Electrodynamics General Circulation Model (TIE-GCM) version 2.0 (Richmond et al., 131 1992; Qian et al., 2014). Simulations were performed with a 2.5 degree horizontal grid 132 spacing and a vertical resolution of 1/4 scale height, with vertical levels ranging from about 133 97 to 500 km altitude. Observed solar wind and interplanetary magnetic field data were 134 used to drive the auroral parameterization and the Weimer (2005b) high-latitude elec-135 tric field model. Instantaneous and 81-day average F10.7 data were used to character-136 ize the solar extreme ultraviolet (EUV) radiative forcing. Output data were stored ev-137 ery 15 minutes from 0 UT on 4 December 2021 until 0 UT on 6 December 2021, although 138 we just use hourly outputs from 0530 UT until 0830 UT here. For the purposes of ex-139 ploring the eclipse effect, the baseline model run was compared to an "eclipse" run with 140 an imposed shadow. For the "eclipse" simulation, location-dependent solar obscuration 141 factors were calculated with the Python package provided by Verhulst and Stankov (2020). 142 Separate obscuration factors were calculated for the visible and EUV parts of the spec-143 trum, taking into account that EUV emissions from the solar corona are not fully blocked, 144 as recommended by Verhulst and Stankov (2020). Both simulations were initialized from 145 a 30-day spin-up simulation to allow the model to reach a quasi-steady state. 146

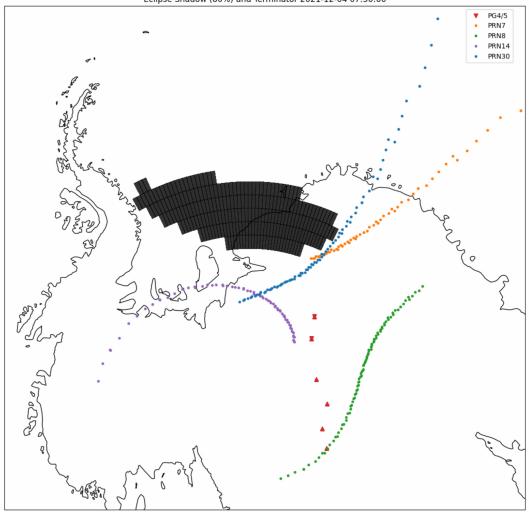
In an attempt to better understand the connection between the substorm related 147 effects and eclipse effects, we utilize a well-established empirical model for solar wind-148 magnetosphere coupling. While sensing the interplanetary magnetic field (IMF) directly 149 (as in via the OMNI database) is certainly useful in this effort, the relationship between 150 the IMF and ionospheric currents is complex. A useful model to estimate ionospheric 151 driving from solar wind data was developed by Weimer in the mid 90s and has since then 152 been refined (Weimer, 1995, 2005a, 2005b). This model provides an estimate of the cross 153 polar cap potential (CPCP), which maps to the ionosphere the electric potential imposed 154 on the magnetotail by the solar wind convection. We use this model to both provide con-155 text for the state of the electric field throughout the ionosphere, as well as to provide 156 an estimate of the energy contained in the disruption created by the eclipse. 157

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2.2 GPS TEC Observations

Thanks to a coordinated effort to observe the 2021 Antarctic eclipse in unprece-159 dented detail, high cadence (10s) TEC observations are available during a several day 160 window around the eclipse. Contributions from glaciology researchers and global nav-161 igation satellite system (GNSS) receivers as part of the The Polar Earth Observing Net-162 work (POLENET), Antarctic Network (A-NET), and United Kingdom Antarctic Net-163 work (UKANET) were leveraged to make up for an otherwise sparsely sampled region 164 of West Antarctica. On the East Antarctic plateau, the Autonomous Adaptive Low-Power 165 Instrument Platforms (AAL-PIPs, Figure 1) provide both critical GNSS-derived TEC 166 measurements as well as ground magnetic observations. Due to hardware limitations at 167 the AAL-PIP sites, only a single site could collect TEC observations at any one time (ex-168



Eclipse Shadow (80%) and Terminator 2021-12-04 07:30:00

Figure 1. Map of Antarctica showing the location of the eclipse shadow defined by an obscuration of 80% around the time of peak totality (0730 UT). The shaded region moves nominally from top to bottom over the course of the eclipse period (roughly 4hr). AAL-PIP sites are plotted as red triangles, with PG4/5 overplotted with downward triangles. Ray paths for select GNSS satellites are traced to an altitude of 600km for the duration of their respective measurements and organized by color. The sun is to the right of the figure, the solar terminator is to the left.

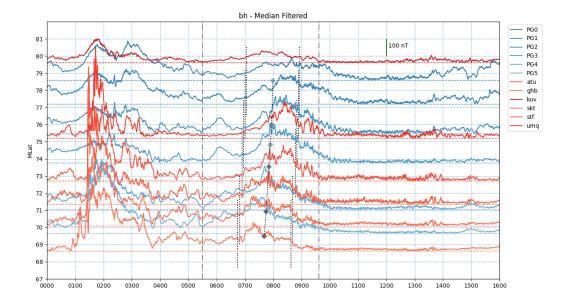


Figure 2. Horizontal component of the magnetic field variations organized by magnetic latitude, with 1 degree scaled to represent 100 nT. The six southern (northern) hemisphere stations are in blue (red). Dot-dashed lines represent the entire eclipse interval, while short dashed lines represent the local shadow interval. Diamonds represent the progression of the peak obscuration point across the array. An earlier substorm occurs between 1-2 UT, with a much smaller substorm occurring between 6-7 UT.

cepting a few minutes of overlap). Thus, we treat the entire array as a single mesoscale observation platform for the purpose of TEC measurements. To provide as great a temporal resolution as possible the cadence of these measurements was set to every 10s. Observations are unique to each satellite, and are uniquely identified by a pseudo-random number (PRN) code. These measurements are then compared to TEC integrated along similar rays traced through the TIE-GCM model ionosphere.

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2.3 Magnetometer Observations

The AAL-PIPs are a series of 6 ground-based observation platforms located along 176 the 40° magnetic meridian between 69 and 79 degrees latitude (Clauer et al., 2014). Each 177 station has an approximately magnetically conjugate counterpart on the west coast of 178 Greenland operated by the Danish Technical University. Combining observations from 179 both arrays provides a unique perspective on the global magnetospheric system and any 180 interhemispheric asymmetries that may occur. Both arrays operate fluxgate magnetome-181 ters at each site, while the AAL-PIP array also operates search-coil magnetometers and 182 the previously mentioned GNSS receivers at 4 of 6 sites. 183

In order to identify substorm occurrence, we utilize the auroral electrojet (AE) in-184 dex provided by the World Data Center hosted by Kyoto University (Iyemori et al., 1992). 185 The AE index is a composite of the horizontal deviation of the magnetic field at a dozen 186 locations in the auroral region, which give a sense of the strength of the ionospheric cur-187 rents flowing overhead. These currents are enhanced during periods of increased geomag-188 netic activity, such as during substorms. It is also possible to identify substorm signa-189 tures in ground magnetometer observations directly as shown in the AAL-PIP and DTU 190 time-series (Figure 2). 191

¹⁹² 3 Analysis and Results

3.1 TEC

Figure 3 shows slant TEC traced from the ground to select satellites in the con-194 trol model (orange), eclipse model (green), and observation (blue). The local totality win-195 dow (0648-0841 UT), the local totality peak (0744 UT), and the global totality peak 196 (0733 UT) are all marked by vertical dashed and dotted lines. Figure 4 shows the spec-197 trogram representation of the TEC observations, also with vertical lines representing the 198 local totality window and peak. The largest difference observed between the model ob-199 servations is approximately 4 TECU at the time of the local peak totality. Similar re-200 ductions in the Hall and Pedersen in the height integrated conductivities are apparent 201 in the eclipse model runs compared to the control. Observations of slant TEC from AAL-202 PIP are moderately in agreement with the models, with a few exceptions. A sharp in-203 crease in the TEC observations appears in PRNs 8 and 30 around the time of the global 204 totality peak. TEC along the path to PRN 14 does appear to have any clear eclipse re-205 lated signature, while after the peak obscuration PRNs 8, 30, and 7 begin to increase 206 at varying rates. This is in contrast to the expectations put forth by the model, which 207 suggest a much slower recovery from the eclipse. Moreover, the TEC observed by PG4/5208 has a step-function-like increase after the global eclipse peak, indicating that TEC has 209 increased beyond pre-eclipse levels. There also appears to be a general increase in ULF 210 wave activity coincident with the local time of the global peak obscuration, preceded by 211 some higher frequency activity in the 40-50 mHz range. This is most apparent in the spec-212 trogram of PRNs 8 and 30 in Figure 4. 213

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3.2 Magnetic Variations

The horizontal magnetic variation shown in Figure 2 is defined as the magnitude of the sum of the median filtered data to eliminate any bias from the DC magnetic field:

$$B_h = \sqrt{(B_x - \tilde{B}_x)^2 + (B_y - \tilde{B}_y)^2}$$
(1)

where B_x, B_y are the north/south and east/west aligned components of the magnetic 218 field measurement, and B_x, B_y are the median values of those components. The hori-219 zontal variation plot shows an easily identifiable substorm occurring just prior to 02 UT. 220 Additionally, there is activity occurring in both hemispheres near 0630. This small in-221 crease in magnetic activity occurs first in the southern hemisphere, and then in the north-222 ern hemisphere. Shortly after 0640, another disturbance occurs nearly simultaneously 223 in both hemispheres, first at low latitudes and then at higher latitudes (7-9 UT). This 224 activity is well correlated to the time period when the eclipse shadow is present at each 225 of the stations in the southern array. After the eclipse period is over, the remainder of 226 the day is comparatively uneventful from the perspective of the magnetometer data. Anal-227 ysis of the spectral composition of the fluxgate magnetometer (Figure 5, Supplemental 228 Figure S1-S4) data shows an increase in ultra-low frequency (ULF) waves in the 20 229 40mHz band that is tightly bounded by the occurrence of the local peak obscuration 230 at each station. These waves fall into the pulsation continuous 3 (PC3) band based on 231 the common ULF wave schema (Jacobs et al., 1964). A similar signature is observed in 232 the search-coil spectrograms (Figure 6, Supplemental Figure S5-S7) at each station where 233 they're available. There is a slight enhancement in wave activity around 0640 UT that 234 is more apparent in the search-coil data because of its higher sampling rate. This activ-235 ity may be indicative of the substorm observed in the AE index and subsides just prior 236 to the local eclipse interval. It is also worth noting that the wave power increase observed 237 in the magnetometer measurements is in a similar frequency band to that observed in 238 the TEC data. Additionally, Figure 6 shows an apparent suppression of wave activity 239 above 0.2 Hz. 240

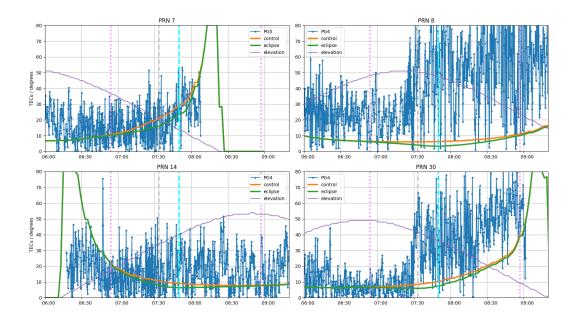


Figure 3. Line of sight TEC as measured from PG4/PG5. Elevation angle is plotted in magneta. TEC integrated along the ray path through TIE-GCM model ionosphere are plotted in orange (control) and green (eclipse). Blue lines are 10s TEC samples for each of the selected GNSS satellites (identified by their respective PRN). Vertical lines at 0654, 0733, 0750, and 0857 UT indicate the local eclipse start, global peak, local peak, and local eclipse end. PRN 7 shows fairly good agreement between model and observations as the elevation angle decreases. PRNs 8 & 30 show a significant increase in TEC occurring shortly after the global totality peak. PRN 14 shows very little activity associated with the eclipse, which may be due to the geometry of the ray path to that particular satellite.

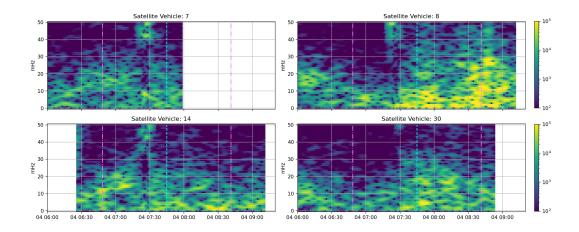


Figure 4. Spectral components of TEC measurements in Figure 3. Note the sharp increase in wave power near the local peak in obscuration in PRNs 8 & 30. All PRNs show an increase in wave power around 50 mHz just prior to the global totality peak.

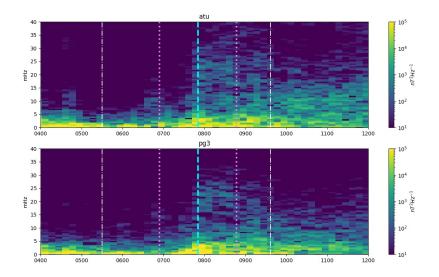


Figure 5. Spectrogram of fluxgate magnetometer data from ATU in Greenland and the conjugate station PG3 in Antarctica. White dot-dashed lines indicate the time interval of the entire eclipse (eclipse contact points P1 & P4), while the magenta dotted lines indicate the local eclipse interval at PG3. The cyan dashed line in the middle indicates the time of localized peak obscuration, which coincides with an increase in activity near 20 mHz.

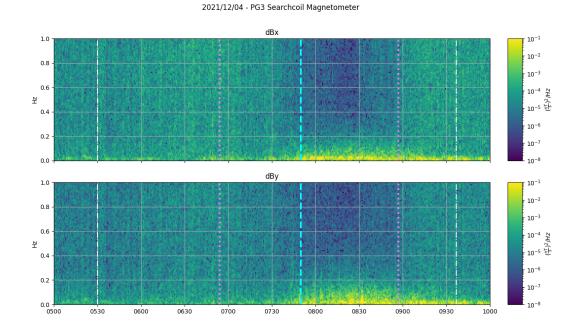


Figure 6. Search-coil magnetometer spectrogram, also from PG3. Similar temporal coincidence of waves and local obscuration peak is observed, though with a higher dynamic range of frequencies. A possible signature of the 0640 UT substorm is observed and subsides prior to the local onset of PC3 waves.

241 4 Discussion

It is expected that during an eclipse, one would experience a localized reduction 242 in TEC leading up to the peak obscuration followed by an increase in TEC as the so-243 lar disk re-emerges. This is well illustrated in the difference between control and eclipse 244 event model TEC outputs show in Figure 3. It is noted that while deviations of on the 245 order of 40 TEC units may seem quite large, line of sight measurements at low eleva-246 tion angles are sensing a much larger portion of the ionospheric layers than the more com-247 mon vertical TEC measurements. Idosa and Rikitu (2022) show similar modification of 248 TEC upwards of 14 TEC units under the region of shadow for the same event. One ques-249 tion about the observations from PG4/5 remains outstanding: Why is there a step-function-250 like increase in TEC immediately after the global peak obscuration, specifically in PRN 251 8 and 30 but not otherwise? This is not the first time such an observation has been made 252 during an eclipse (G. Chen et al., 2013; Cherniak & Zakharenkova, 2018; Wu et al., 2018). 253 A simple explanation for why the observations differ at all can be attributed to the ge-254 ometry of the ray paths and specifically the azimuth of the satellites from the ground. 255 If these differences are indeed indicative of a localized increase in TEC, one possible ex-256 planation may be auroral precipitation. This mechanism would explain both the spa-257 tial dependence as well as the apparent increase in TEC beyond "pre-eclipse" levels. While 258 it is well known that auroral activity increases during geomagnetic substorms, further 259 investigation by way of satellite observation and modeling may help determine the fea-260 sibility of a direct eclipse effect on precipitation. Another possible explanation for the 261 post-eclipse enhancement was suggested in Cnossen et al. (2019) which relies on strong 262 vertical drifts storing plasma at high altitudes and reversing after the eclipse. Again, di-263 rect observation of the plasma motion either by ground or space based instrumentation would aid in our understanding of this phenomenon. 265

Determining if and how the eclipse impact on the ionosphere modifies the currents 266 flowing within is a non-trivial task. It is therefore potentially useful to represent the cou-267 pled solar wind-magnetosphere-ionosphere (SWMI) using a circuit model as in Boström 268 (1974). The ionosphere in this model is typically represented as a load on the magne-269 tosphere coupled by field aligned currents. It is reasonable to expect that by modifying 270 the ionospheric resistance, the resultant currents are similarly modified. If one holds the 271 magnetospheric potential to be constant, the ionospheric portion of the circuit can be 272 reduced to a series inductor-resistor (LR) configuration with some ionospheric potential 273 like that from Weimer (1995). An example current profile generated by varying the re-274 sistance of the ionosphere is shown in Figure 7. Interestingly, a simple integration of the 275 energy "diverted" from the ionosphere in this manner over the period of an eclipse is of 276 similar magnitude to what has been suggested is sufficient to drive the magnetotail to 277 instability (Akasofu, 2021). For a CPCP at 60kV, $L_{FAC} = 50H$, and $t_{eclipse} \approx 4hrs$: 278

$$E_{diverted} = CPCP \cdot \int I_{iono} - I_{eclipse} \, dt \approx 2 \times 10^{14} J \tag{2}$$

It is possible that a reduction in current passing through the ionosphere contributes to currents flowing elsewhere in the magnetosphere, but it is also possible (and perhaps more likely) that the magnetospheric potential driving these currents is not constant. Clearly any conclusions about energy flux must necessarily provide more sophisticated modelling support than what is provided here.

Previous studies have shown a propensity for substorm activity to occur preferen-285 tially in dark hemispheres (lower conductivity) compared to sunlit (Laundal et al., 2017; 286 Liou et al., 2018; Singh et al., 2011; Wang et al., 2005; Wang & Lühr, 2007). It is dif-287 ficult, however, to separate out other seasonal effects like the Russell-McPheron effect 288 (Russell & McPherron, 1973) or thermospheric effects. Eclipses provide a unique oppor-289 tunity to study how substorm characteristics can be altered by changes in conductivity 290 independent of season. Interestingly, this is not the first time enhanced geomagnetic ac-291 tivity has been observed concurrently with a solar eclipse (Cherniakov, 2017; Rashid et 292

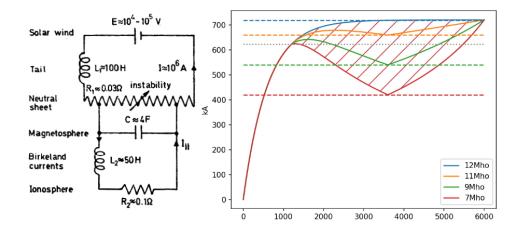


Figure 7. Circuit schematic of the SWMI system as in Boström (1974). During an eclipse, the ionospheric load changes rapidly and acts more like a variable resistance. An example current profile of the series LR circuit representing magnetosphere-ionosphere currents is given for $V_{PC} = 60kV$ (from Weimer), $L_{FAC} = 50H$ and $R_{iono} = 12^{-1}\Omega$. The resistance value is varied linearly from $12^{-1}\Omega$ to $7^{-1}\Omega$ for a time to simulate an eclipse. The area between the curves represents a difference in energy dissipation through the ionosphere because of the reduced conductivity.

al., 2006). It is therefore suggested that a followup study be conducted in order to identify any particular linkages between eclipses, substorms, and/or ionospheric current systems in general, with the overarching goal to better understand the impact of conductivity on the magnetosphere-ionosphere coupling system.

The eclipse is associated with large spatiotemporal variations in TEC, and subse-297 quently in both Hall and Pedersen conductivities. Newton et al. (1978) illustrates how 298 conductivity is related to ULF wave dissipation. Likewise, Allan and Knox (1979); Al-299 lan (1982) discuss the impact of interhemispheric asymmetries in conductivity on mag-300 netospheric waves. It is therefore well within reason to suggest that rapid variation of 301 conductivity in one hemisphere (like during an eclipse) is likely to alter wave properties 302 along the magnetic field line linking the hemispheres. It is suggested in Allan (1983) that 303 "quarter-wave" pulsations occur in regions where the ionospheric conductivity at the magnetic foot-points is highly asymmetric, and Obana et al. (2015) presents observations of 305 such waves, as well as a phase transition from "quarter-wave" mode to "half-wave" mode 306 associated with the dawnside terminator. Similar interhemispheric conductivity ratios 307 to Figure 15 of Obana et al. (2015) are predicted by the TIE-GCM eclipse model for this event, suggesting these waves may have a similar generation mechanism. 309

Recent work investigating the occurrence of PC3 waves at the dawnside termina-310 tor has shown evidence of what is termed the "sunrise effect" (Saka & Alperovich, 1993; 311 Somsikov, 2011; Tanaka et al., 2004; Yagova et al., 2017; Silva et al., 2020). While the 312 physical processes underlying the generation of these waves remains poorly understood, 313 it is noteworthy that PC3 waves occur frequently at the dawn side terminator. It is then 314 perhaps no coincidence that PC3 waves are observed by the AAL-PIP and DTU mag-315 netometers during the December 2021 eclipse, as this is liken to a "second sunrise" where 316 photoionization is suddenly reintroduced into a darkened ionosphere. However, most ob-317 servations of the "sunrise effect" have been at mid to low latitudes, where ionospheric 318 currents behave quite differently than at the high latitudes studied herein. One of the 319 proposed generation mechanisms for these waves involves the motion of neutral winds 320

across a thermal conductivity gradient (Silva et al., 2020). It is therefore suggested that further observational study of eclipse related ULF waves include a thermospheric wind measurement in conjunction with ionospheric sounding.

It may be tempting to associate the occurrence of ULF waves with well known mag-324 netospheric drivers like upstream pressure variations from the solar wind or ion foreshock 325 (Anderson, 1993; Turc et al., 2022; Takahashi et al., 2021). Indeed, this may explain why 326 longer period PC5 waves are being driven as well (Hartinger et al., 2013). There are two 327 reasons why these observations do not support such a mechanism. First, the difference 328 in wave onset times between the most pole-ward and equator-ward stations is nearly 20 329 minutes, much longer than would be expected. Secondly, the waves occur first at the more 330 equatorial station before moving pole-ward. The wave activity is also inconsistent with 331 internally driven waves which tend to have wave power concentrated in a much narrower 332 range of latitudes than that shown in Figure 2 (Shi et al., 2018). Though internal or ex-333 ternal drivers may be supplying some energy to sustain the waves, the eclipse-related IT 334 system changes are the primary factors controlling wave activity during this period. 335

This study is not the first time ground magnetic observations of waves in proxim-336 ity to an eclipse have been reported. Kim and Chang (2018) utilize wavelet analysis to 337 identify the frequency specific response to several total solar eclipses in comparison to 338 a similar time period 24 hrs later. They describe an eclipse related suppression of wave 339 activity at frequencies well above the PC3 range. Indeed, the search-coil spectrum of Fig-340 ure 6 does show an apparent damping of wave activity in the upper portion of the fig-341 ure after the totality peak. This suggests there is a frequency dependence on the impact 342 of the eclipse on ionospheric dynamics. 343

344

4.1 Summary and Conclusions

345	We have presented observations of a total solar eclipse occurring over Antarctica
346	on 04 December, 2021. In summary:
347	• Just prior to peak totality (0730 UT), a substorm (0640 UT) was observed in the
348	AE index as well as in the combined 40 degree array magnetograms
349 350	• TIE-GCM model runs predict peak reduction in slant total electron content of around 4 TECU during an eclipse
351 352	• Line-of-sight TEC observations near the path of totality show an increase in TEC after the peak totality for some regions of the ionosphere
353	• Magnetic oscillations in the PC3 band occur coincident with the local peak ob-
354	scuration at several ground magnetometer stations in both north and south hemi-
355	spheres.
356 357	• TEC oscillations are observed to be of similar frequency to those observed in mag- netometer data
358	• It appears that these oscillations occur independent of the substorm occurring dur-
359	ing the eclipse, but more investigation is required to explain the physical processes
360	involved
361	• Subsequent studies of eclipses would greatly benefit from advanced diagnostics of
362	the neutral atmosphere and ionospheric dynamics
363	• Coordinated, multi-point observations are required to "close the loop" on the iono-
364	spheric eclipse effect

365 V

³⁶⁶ 5 Open Research

GNSS data used in this study is available at mist.nianet.org, via MADRIGAL 367 (http://cedar.openmadrigal.org/) or by request. Magnetometer data from DTU can 368 be obtained via the Tromsø Geophysical Observatory (https://flux.phys.uit.no/ 369 geomag.html). Southern hemisphere magnetometer data is available via mist.nianet 370 .org. The AE index is available at https://wdc.kugi.kyoto-u.ac.jp/ae_realtime/ 371 202112/index_20211204.html. GNSS satellite position data can be obtained via https:// 372 in-the-sky.org/satmap_globe.php?year=2021&month=12&day=4. Eclipse details are 373 available via https://eclipse.gsfc.nasa.gov/. The TIE-GCM model is available at 374 https://www.hao.ucar.edu/modeling/tgcm/tie.php. 375

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Figure 1.

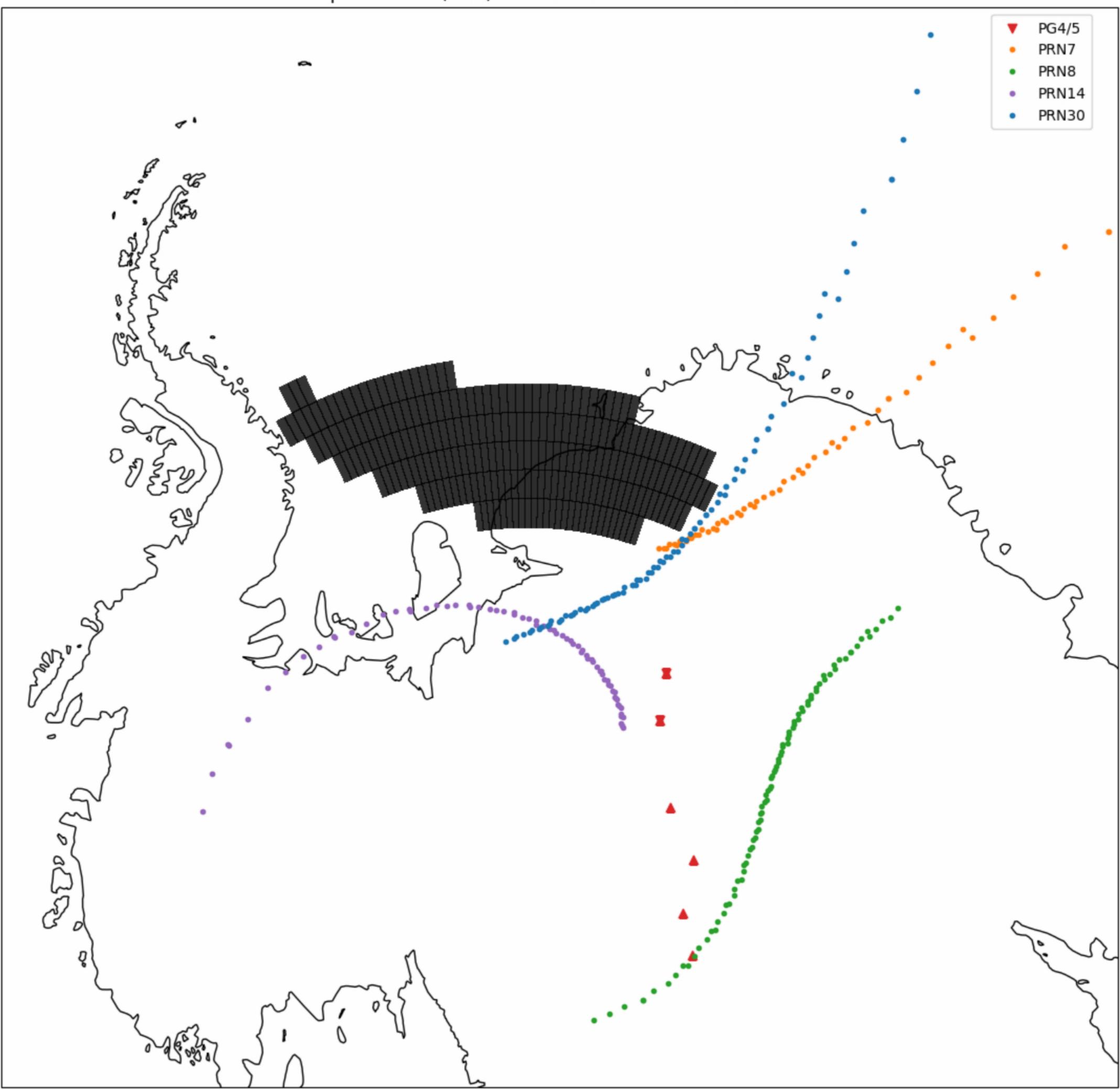


Figure 2.

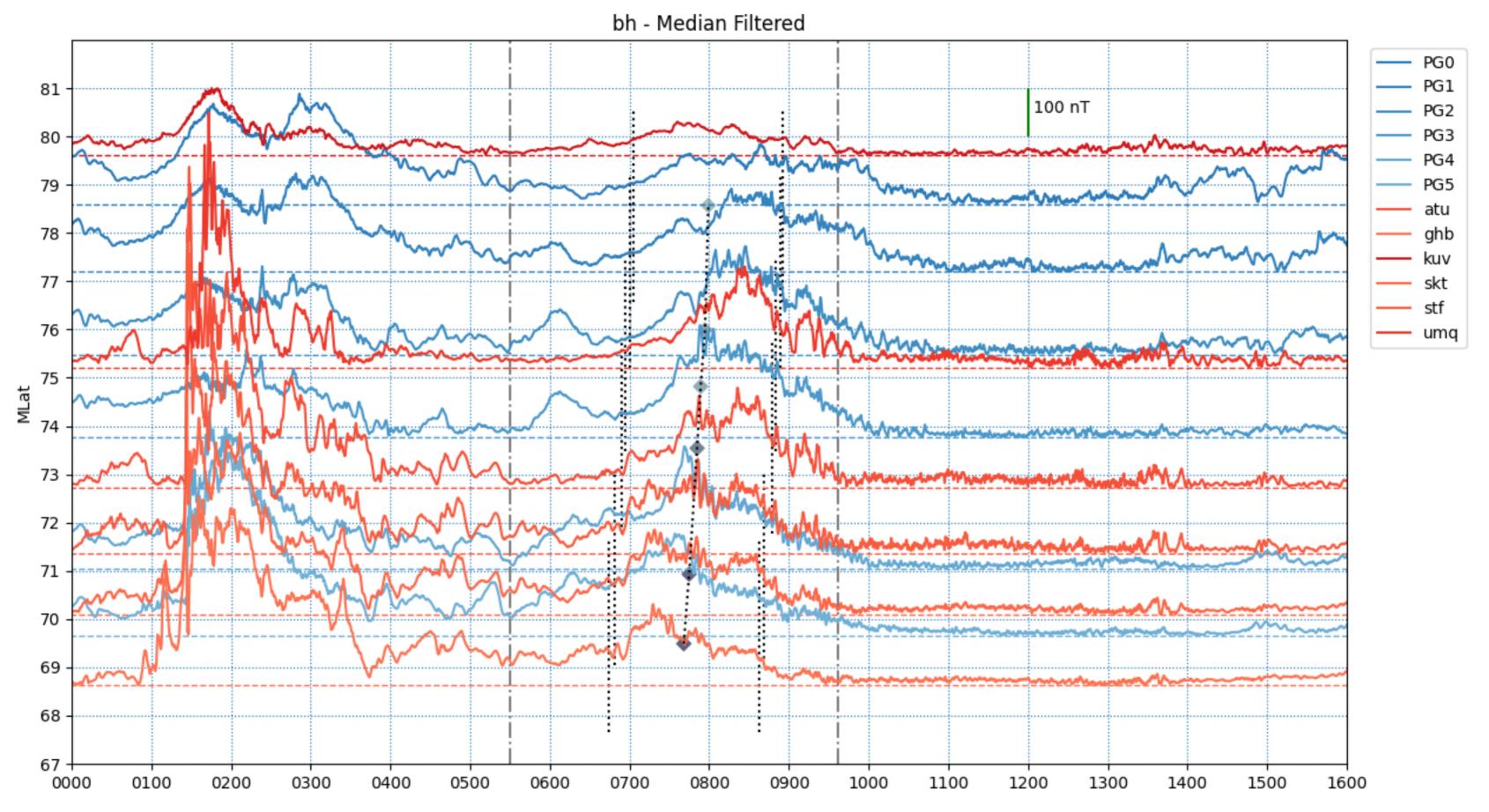


Figure 3.

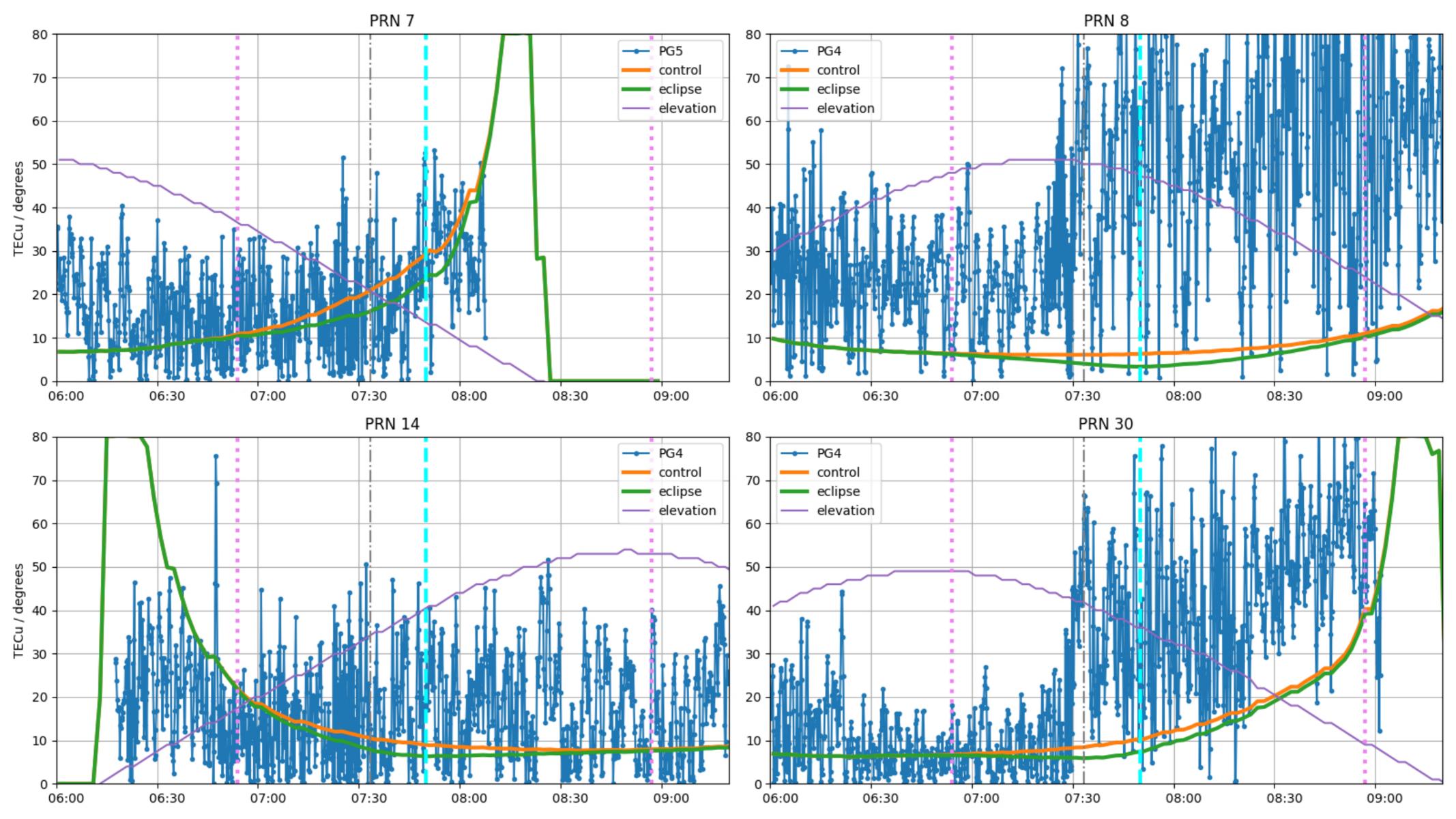
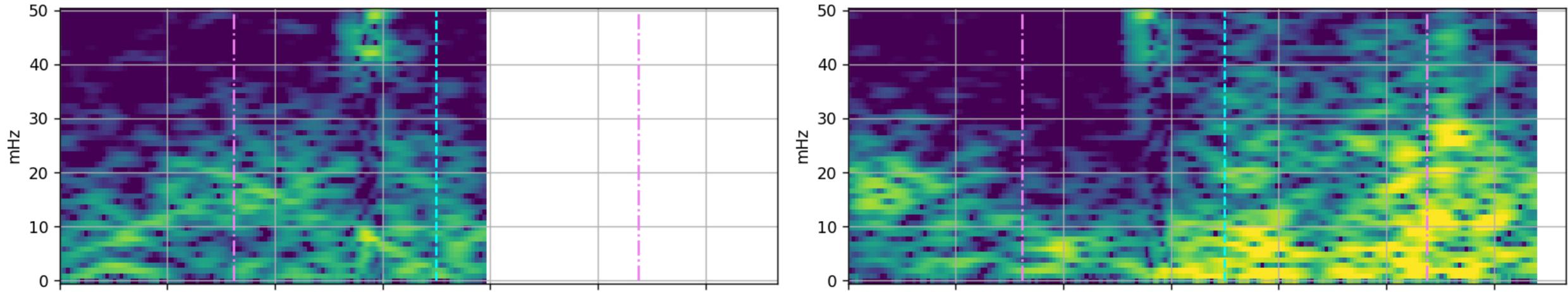
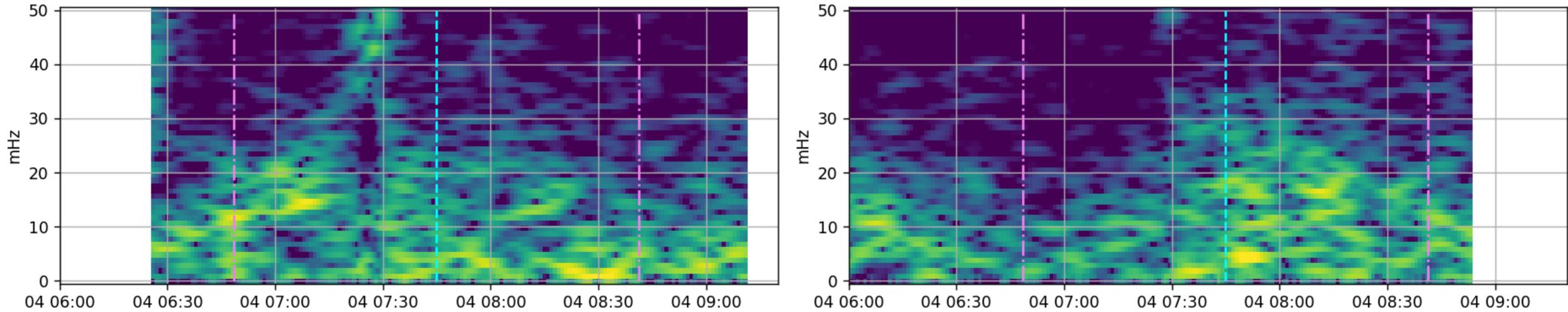


Figure 4.

Satellite Vehicle: 7

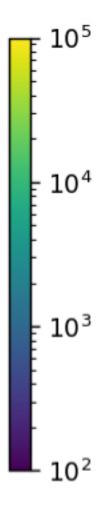


Satellite Vehicle: 14



Satellite Vehicle: 8

Satellite Vehicle: 30



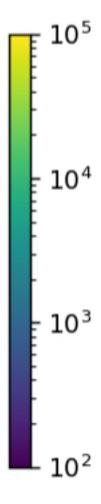
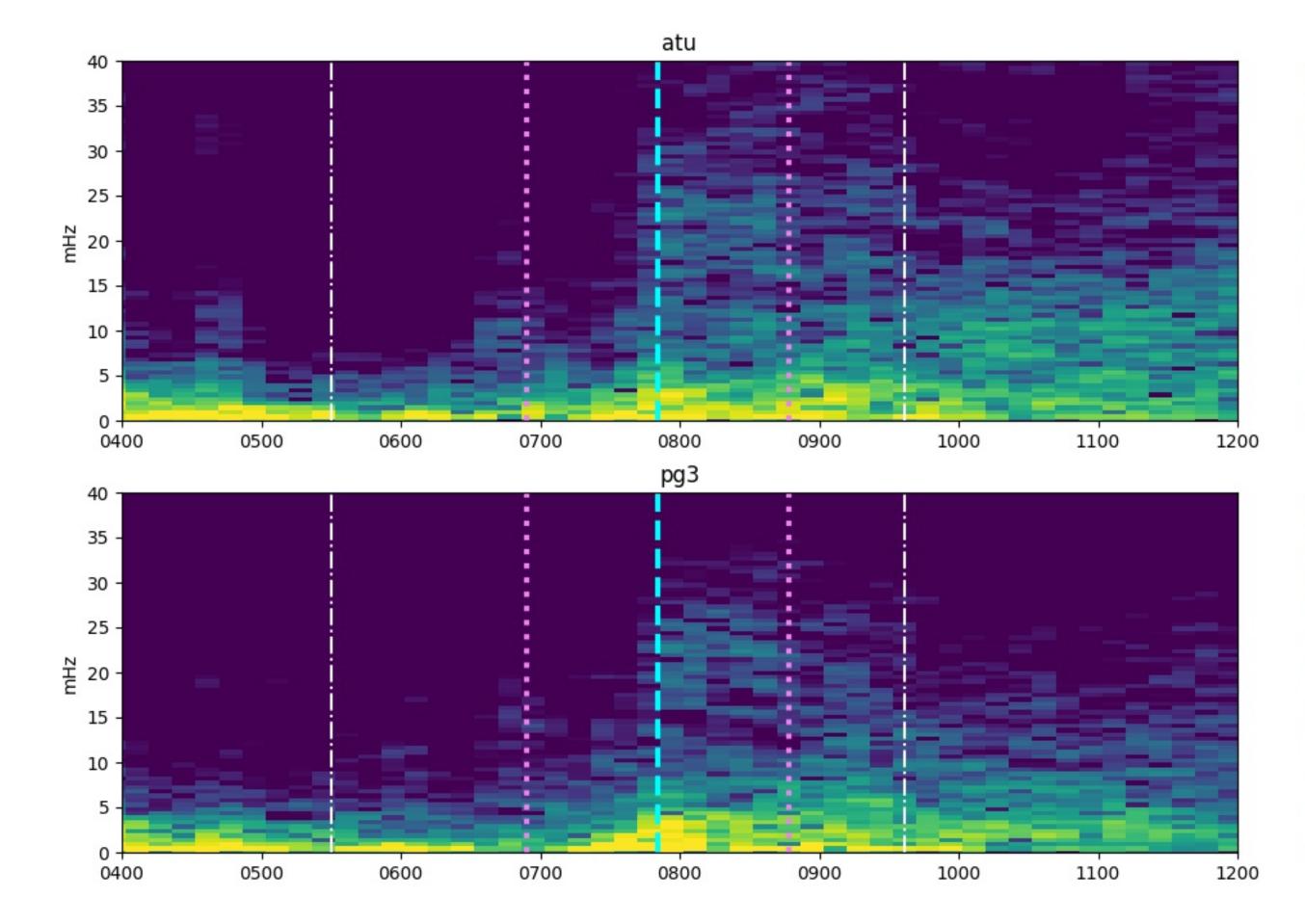
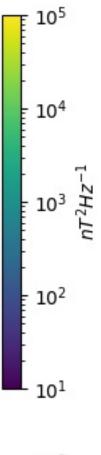


Figure 6.





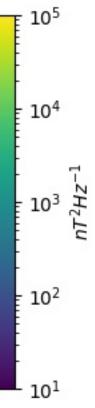
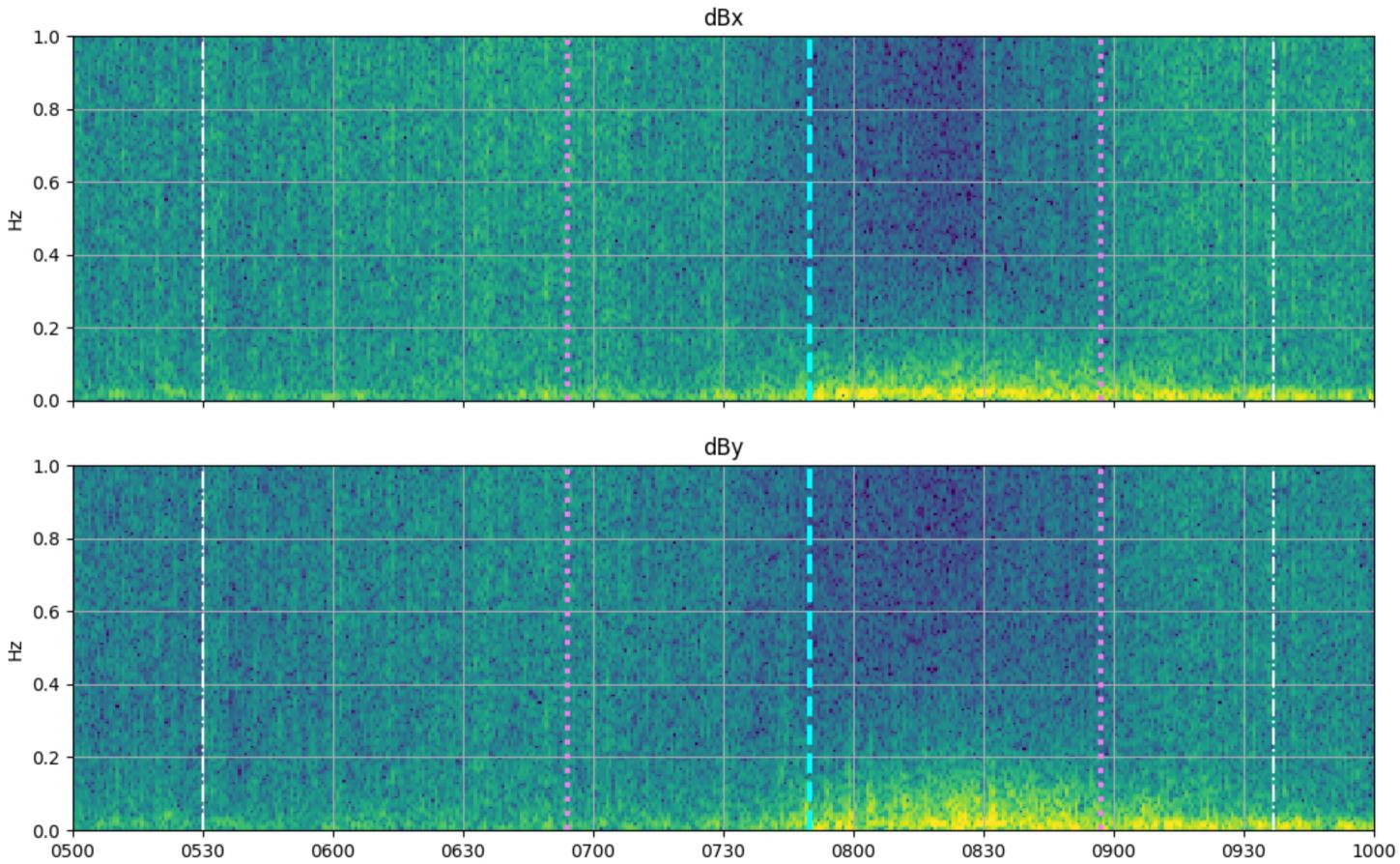


Figure 6.

2021/12/04 - PG3 Searchcoil Magnetometer



$$10^{-1}$$

 10^{-2}
 10^{-3}
 10^{-4} $H_{z}(\frac{1}{10})$
 10^{-5}
 10^{-6}
 10^{-7}
 10^{-8}

$$10^{-1}$$

 10^{-2}
 10^{-3}
 10^{-4} $H_{c}(\frac{h}{L_{U}})$
 10^{-5}
 10^{-6}
 10^{-7}
 10^{-8}

Figure 7.

