Non-informative priors in hydrology

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Abstract

Bayesian methods play a prominent role in parameter estimation and uncertainty quantification. In a typical application of Bayes theorem, a prior distribution over the parameters is updated through a likelihood function to obtain the posterior distribution. In the absence of any prior knowledge, a non-informative prior is chosen to express lack of any preference by assigning a uniform distribution over the possible ranges of parameters. However, the validity of uniform priors as being truly non-informative is seldom questioned. The objective of this study is to test this assumption while estimating soil saturated hydraulic conductivity using data from infiltration experiments. The concept of a non-informative prior using an information theoretic approach is pursued for this application, and the results compared to those obtained from assignment of a uniform prior. Non-informative priors obtained by the information theoretic approach are different from a uniform prior, and estimates of the posterior distribution are influenced by the choice of the prior, especially when data are limited. Examples from both hypothetical and real data are utilized to highlight the importance of selecting truly non-informative priors.

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Noninformative priors in hydrological models: is uniform prior truly a noninformative prior?

1. Background and Objectives

In order to use Bayes theorem in hydrological models, one needs to specify a likelihood function and a prior distribution. Many studies have addressed the problem of choosing an appropriate likelihood function to model the information content in the data. However, relatively fewer studies have addressed the problem of prior specification. Non-informative priors do not seem to have been addressed in the hydrologic modeling literature.

Generally, uniform prior are assumed to be non-informative priors; but the validity of this assumption is never questioned. This study has the following two objectives:

- (1) To find out if the uniform priors over model-parameters are appropriate in hydrologic applications, and
- (2) to explore the principle of maximum gain to determine noninformative priors.



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4. Conclusions

Uniform prior may not always be the non-

Bernardo priors may be used to derive non-

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Example 3

- Again, the uniform prior is not the best non-informative prior
- The non-informative prior seems to be biased towards a Gaussian distribution
- If one uses Bernardo prior to infer the value of β , a large amount of data would be required to infer a Laplacian distribution ($\beta = 0.5$), in line with the fact that the large amount of data are required to accurately compute highorder moments, i.e., characterize Laplacian distribution.